

Homework 1

1.

A)

$$\text{Wafer-X-area} = r^2 \pi = \left(\frac{0,16\text{m}}{2}\right)^2 \pi = (0,08\text{m})^2 \pi = 0,022\text{m}^2 = \boxed{201\text{cm}^2}$$

$$\text{I) Die X-area} = \frac{\text{wafer-X-area}}{\text{dies-per-wafer}} = \frac{201\text{cm}^2}{64} = \boxed{3,14\text{cm}^2}$$

$$\text{Wafer-Y-area} = r^2 \pi = \left(\frac{0,2\text{m}}{2}\right)^2 \pi = (0,1\text{m})^2 \pi = 0,01\text{m}^2 \cdot \pi = 0,0314\text{m}^2 = \boxed{314\text{cm}^2}$$

$$\text{II) Die -Y-area} = \frac{\text{wafer-Y-area}}{\text{dies-per-wafer}} = \frac{314\text{cm}^2}{100} = \boxed{3,14\text{cm}^2}$$

B

Yield-X = ?

1)

$$\text{Defected-dies-X} = 201 \text{ wafer} \cdot 0.02 \frac{\text{defects}}{\text{wafer}} = \underline{4.02} \text{ defected dies}$$

$$\Rightarrow \text{Yield-X} = \frac{64 - 4.02}{64} = \boxed{0.934}$$

$$\text{Cost-per-die-X} = \frac{\text{cost-per-wafer-X}}{\text{dies-per-wafer-X} - \text{defected-dies-X}} = \frac{15}{64 - 4.02} = \boxed{0.25} \text{ per die}$$

11)

$$\text{defected-dies-Y} = 314 \text{ wafer} \cdot 0.03 \frac{\text{defects}}{\text{wafer}} = \underline{9.42}$$

$$\text{Yield-Y} = \frac{100 - 9.42}{100} = \frac{90.58}{100} = \boxed{0.9}$$

$$\text{cost-per-die-Y} = \frac{\text{cost-per-wafer-Y}}{\text{dies-per-wafer-Y} - \text{defected-dies-Y}} = \frac{24}{100 - 9.42} = \frac{24}{90.58} = \boxed{0.266} \text{ per die}$$

C

	cost	# dies	defect / cm ²
X	$15 \cdot 0.8 = 12$	$64 \cdot 1.1 = 70.4$	$0.02 \cdot 1.15 = 0.023$
Y	$24 \cdot 0.8 = 19.2$	$100 \cdot 1.1 = 110$	$0.03 \cdot 1.15 = 0.0345$

A) 1) Wafer's area stays the same!

$$\text{die-X-area} = \frac{201 \text{ cm}^2}{70.4} = \boxed{2.85 \text{ cm}^2}$$

$$\text{die-Y-area} = \frac{314 \text{ cm}^2}{110} = \boxed{2.85 \text{ cm}^2}$$

$$\text{B) 1) defect-X} = 201 \text{ cm}^2 \cdot 0.023 \frac{\text{def}}{\text{cm}^2} = \underline{4.623}$$

$$\text{yield-X} = \frac{70.4 - 4.623}{70.4} = \underline{0.93}$$

$$\text{cost-die-X} = \frac{12}{70.4 - 4.623} = \frac{12}{65.77} = \underline{0.18}$$

$$\text{II) defect-Y} = 314 \text{ cm}^2 \cdot 0.0345 \frac{\text{def}}{\text{cm}^2} = 10.8 \text{ def}$$

$$\text{yield-Y} = \frac{110 - 10.8}{110} = \frac{99.2}{110} = \underline{0.9}$$

$$\text{cost-die-Y} = \frac{19.2}{110 - 10.8} = \frac{19.2}{99.2} = \underline{0.19}$$

2.

$$F_1 = 3 \text{ GHz}, F_2 = 1.5 \text{ GHz}$$

$$A) T_1 = \frac{1}{F_1} = \frac{1}{3 \cdot 10^9} = 0.3 \cdot 10^{-9} \text{ s}; T_2 = \frac{1}{1.5 \cdot 10^9} = 0.6 \cdot 10^{-9} \text{ s}$$

clock cycle \rightarrow seconds per cycle

T_1 and T_2 are the solutions to this part
if by clock cycles you mean clock cycle
of P_1 and clock cycle of P_2

$$P_{c1} = 2.05 + 4.05 + 3.02 = \boxed{32 \cdot 10^3}$$

$$P_{c2} = 3.05 + 3.05 + 3.02 = \boxed{30 \cdot 10^3}$$

P_{c1} and P_{c2} is the solution if by clock cycles you meant total clock cycles of P_1 and total clock cycles of P_2

0.3 0.5 0.2
R T J

R

50%
5
4
3

J

20% \rightarrow in billions
2
3
3

8)

$$\begin{aligned}
 P_{C1-R} &= 1.0.3 = 0.6 \text{ billion cycles} \\
 P_{C1-I} &= 4.0.5 = 2 \text{ billion cycles} \\
 P_{C1-J} &= 3.0.2 = 0.6 \text{ billion cycles}
 \end{aligned}$$

$$\begin{aligned}
 P_{C2-R} &= 3.0.3 = 0.9 \cdot 10^9 \\
 P_{C2-I} &= 8.0.5 = 1.5 \cdot 10^9 \\
 P_{C2-D} &= 3.0.2 = 0.6 \cdot 10^9
 \end{aligned}$$

$$CPl_1 = P_{C1-avg} = \frac{3.2 \cdot 10^9 \text{ cycles}}{2+4+3} = \frac{3.2 \cdot 10^9 \text{ cycle}}{9} = 0.35 \cdot 10^9 \frac{\text{cycle}}{\text{instruction}}$$

$$CPl_2 = P_{C2-avg} = \frac{3.0 \cdot 10^9 \text{ cycles}}{3+3+3} = 0.3 \cdot 10^9 \frac{\text{cycle}}{\text{instr}}$$

c)

$$ET_1 = P_{C1} \cdot T_1 = 3.2 \cdot 10^9 \cdot 0.3 \cdot 10^{-9} \text{ s} = \boxed{1.06 \text{ s}}$$

$$ET_2 = P_{C2} \cdot T_2 = 3.1 \cdot 10^9 \text{ cycle} \cdot 0.6 \cdot 10^{-9} \frac{1}{\text{cycle}} = \boxed{1.99 \text{ s}}$$

d)

$$\frac{ET_2}{ET_1} = \frac{1.99 \text{ s}}{1.06 \text{ s}} = 1.875 \Rightarrow \underline{P_1 \text{ is 1.875 times faster.}}$$