Shell sort

Performing shell sort on a sorted array

Shell sort being executed for array: 1 2 3 4 5 6 7 8 9 10

Current 'gap' is: 5

Since 6 at position 5 is bigger or equal than 1 at position 0 we will not perform the swapping Since 7 at position 6 is bigger or equal than 2 at position 1 we will not perform the swapping Since 8 at position 7 is bigger or equal than 3 at position 2 we will not perform the swapping Since 9 at position 8 is bigger or equal than 4 at position 3 we will not perform the swapping Since 10 at position 9 is bigger or equal than 5 at position 4 we will not perform the swapping

Current 'gap' is: 2

Since 3 at position 2 is bigger or equal than 1 at position 0 we will not perform the swapping Since 4 at position 3 is bigger or equal than 2 at position 1 we will not perform the swapping Since 5 at position 4 is bigger or equal than 3 at position 2 we will not perform the swapping Since 6 at position 5 is bigger or equal than 4 at position 3 we will not perform the swapping Since 7 at position 6 is bigger or equal than 5 at position 4 we will not perform the swapping Since 8 at position 7 is bigger or equal than 6 at position 5 we will not perform the swapping Since 9 at position 8 is bigger or equal than 7 at position 6 we will not perform the swapping Since 10 at position 9 is bigger or equal than 8 at position 7 we will not perform the swapping Current 'gap' is: 1

Since 2 at position 1 is bigger or equal than 1 at position 0 we will not perform the swapping Since 3 at position 2 is bigger or equal than 2 at position 1 we will not perform the swapping Since 4 at position 3 is bigger or equal than 3 at position 2 we will not perform the swapping Since 5 at position 4 is bigger or equal than 4 at position 3 we will not perform the swapping Since 6 at position 5 is bigger or equal than 5 at position 4 we will not perform the swapping Since 7 at position 6 is bigger or equal than 6 at position 5 we will not perform the swapping Since 8 at position 7 is bigger or equal than 7 at position 6 we will not perform the swapping Since 9 at position 8 is bigger or equal than 8 at position 7 we will not perform the swapping Since 10 at position 9 is bigger or equal than 9 at position 8 we will not perform the swapping

Gap will be reduced again and will be less than 1 so the sorting will be finished

In the end total number of comparisons was: 22

Total number of displacements was: 0

Final array is:

12345678910

Performing shell sort on a reversely sorted array

Shell sort being executed for array: 10 9 8 7 6 5 4 3 2 1

Current 'gap' is: 5

Since 5 at position 5 is smaller than 10 at position 0 we will swap them

Our array is now

59876104321

Total number of displacements: 1

Total number of comparisons: 1

Since 4 at position 6 is smaller than 9 at position 1 we will swap them

Our array is now

54876109321

Total number of displacements: 2

Total number of comparisons: 2

Since 3 at position 7 is smaller than 8 at position 2 we will swap them

Our array is now

54376109821

Total number of displacements: 3

Total number of comparisons: 3

Since 2 at position 8 is smaller than 7 at position 3 we will swap them

Our array is now

54326109871

Total number of displacements: 4

Total number of comparisons: 4

Since 1 at position 9 is smaller than 6 at position 4 we will swap them

Our array is now

54321109876

Total number of displacements: 5

Total number of comparisons: 5

Current 'gap' is: 2

Since 3 at position 2 is smaller than 5 at position 0 we will swap them

Our array is now

34521109876

Total number of displacements: 6

Total number of comparisons: 6

Since 2 at position 3 is smaller than 4 at position 1 we will swap them

Our array is now

32541109876

Total number of displacements: 7

Total number of comparisons: 7

Since 1 at position 4 is smaller than 5 at position 2 we will swap them

Our array is now

32145109876

Total number of displacements: 8

Total number of comparisons: 8

Since 1 at position 2 is smaller than 3 at position 0 we will swap them

Our array is now

12345109876

Total number of displacements: 9

Total number of comparisons: 9

Since 10 at position 5 is bigger or equal than 4 at position 3 we will not perform the swapping

Since 9 at position 6 is bigger or equal than 5 at position 4 we will not perform the swapping

Since 8 at position 7 is smaller than 10 at position 5 we will swap them

Our array is now

12345891076

Total number of displacements: 10

Total number of comparisons: 12

Since 8 at position 5 is bigger or equal than 4 at position 3 we will not perform the swapping

Since 7 at position 8 is smaller than 9 at position 6 we will swap them

Our array is now

12345871096

Total number of displacements: 11

Total number of comparisons: 14

Since 7 at position 6 is bigger or equal than 5 at position 4 we will not perform the swapping

Since 6 at position 9 is smaller than 10 at position 7 we will swap them

Our array is now

12345876910

Total number of displacements: 12

Total number of comparisons: 16

Since 6 at position 7 is smaller than 8 at position 5 we will swap them

Our array is now

12345678910

Total number of displacements: 13

Total number of comparisons: 17

Since 6 at position 5 is bigger or equal than 4 at position 3 we will not perform the swapping

Current 'gap' is: 1

Since 2 at position 1 is bigger or equal than 1 at position 0 we will not perform the swapping

Since 3 at position 2 is bigger or equal than 2 at position 1 we will not perform the swapping

Since 4 at position 3 is bigger or equal than 3 at position 2 we will not perform the swapping

Since 5 at position 4 is bigger or equal than 4 at position 3 we will not perform the swapping

Since 6 at position 5 is bigger or equal than 5 at position 4 we will not perform the swapping

Since 7 at position 6 is bigger or equal than 6 at position 5 we will not perform the swapping

Since 8 at position 7 is bigger or equal than 7 at position 6 we will not perform the swapping

Since 9 at position 8 is bigger or equal than 8 at position 7 we will not perform the swapping

Since 10 at position 9 is bigger or equal than 9 at position 8 we will not perform the swapping

Gap will be reduced again and will be less than 1 so the sorting will be finished

In the end total number of comparisons was: 27

Total number of displacements was: 13

Final array is:

12345678910

Performing shell sort on a given array {5, 2, 13, 9, 1, 7, 6, 8, 1, 15, 4, 11}

Shell sort being executed for array: 5 2 13 9 1 7 6 8 1 15 4 11

Current 'gap' is: 6

Since 6 at position 6 is bigger or equal than 5 at position 0 we will not perform the swapping

Since 8 at position 7 is bigger or equal than 2 at position 1 we will not perform the swapping

Since 1 at position 8 is smaller than 13 at position 2 we will swap them

Our array is now

521917681315411

Total number of displacements: 1

Total number of comparisons: 3

Since 15 at position 9 is bigger or equal than 9 at position 3 we will not perform the swapping

Since 4 at position 10 is bigger or equal than 1 at position 4 we will not perform the swapping

Since 11 at position 11 is bigger or equal than 7 at position 5 we will not perform the swapping

Current 'gap' is: 3

Since 9 at position 3 is bigger or equal than 5 at position 0 we will not perform the swapping

Since 1 at position 4 is smaller than 2 at position 1 we will swap them

Our array is now

511927681315411

Total number of displacements: 2

Total number of comparisons: 8

Since 7 at position 5 is bigger or equal than 1 at position 2 we will not perform the swapping

Since 6 at position 6 is smaller than 9 at position 3 we will swap them

Our array is now

511627981315411

Total number of displacements: 3

Total number of comparisons: 10

Since 6 at position 3 is bigger or equal than 5 at position 0 we will not perform the swapping

Since 8 at position 7 is bigger or equal than 2 at position 4 we will not perform the swapping

Since 13 at position 8 is bigger or equal than 7 at position 5 we will not perform the swapping

Since 15 at position 9 is bigger or equal than 9 at position 6 we will not perform the swapping

Since 4 at position 10 is smaller than 8 at position 7 we will swap them

Our array is now

511627941315811

Total number of displacements: 4

Total number of comparisons: 15

Since 4 at position 7 is bigger or equal than 2 at position 4 we will not perform the swapping

Since 11 at position 11 is smaller than 13 at position 8 we will swap them

Our array is now

511627941115813

Total number of displacements: 5

Total number of comparisons: 17

Since 11 at position 8 is bigger or equal than 7 at position 5 we will not perform the swapping

Current 'gap' is: 1

Since 1 at position 1 is smaller than 5 at position 0 we will swap them

Our array is now

151627941115813

Total number of displacements: 6

Total number of comparisons: 19

Since 1 at position 2 is smaller than 5 at position 1 we will swap them

Our array is now

115627941115813

Total number of displacements: 7

Total number of comparisons: 20

Since 1 at position 1 is bigger or equal than 1 at position 0 we will not perform the swapping

Since 6 at position 3 is bigger or equal than 5 at position 2 we will not perform the swapping

Since 2 at position 4 is smaller than 6 at position 3 we will swap them

Our array is now

115267941115813

Total number of displacements: 8

Total number of comparisons: 23

Since 2 at position 3 is smaller than 5 at position 2 we will swap them

Our array is now

112567941115813

Total number of displacements: 9

Total number of comparisons: 24

Since 2 at position 2 is bigger or equal than 1 at position 1 we will not perform the swapping

Since 7 at position 5 is bigger or equal than 6 at position 4 we will not perform the swapping

Since 9 at position 6 is bigger or equal than 7 at position 5 we will not perform the swapping

Since 4 at position 7 is smaller than 9 at position 6 we will swap them

Our array is now

112567491115813

Total number of displacements: 10

Total number of comparisons: 28

Since 4 at position 6 is smaller than 7 at position 5 we will swap them

Our array is now

 $1\ 1\ 2\ 5\ 6\ 4\ 7\ 9\ 11\ 15\ 8\ 13$

Total number of displacements: 11

Total number of comparisons: 29

Since 4 at position 5 is smaller than 6 at position 4 we will swap them

Our array is now

 $1\ 1\ 2\ 5\ 4\ 6\ 7\ 9\ 11\ 15\ 8\ 13$

Total number of displacements: 12

Total number of comparisons: 30

Since 4 at position 4 is smaller than 5 at position 3 we will swap them

Our array is now

112456791115813

Total number of displacements: 13

Total number of comparisons: 31

Since 4 at position 3 is bigger or equal than 2 at position 2 we will not perform the swapping

Since 11 at position 8 is bigger or equal than 9 at position 7 we will not perform the swapping

Since 15 at position 9 is bigger or equal than 11 at position 8 we will not perform the swapping

Since 8 at position 10 is smaller than 15 at position 9 we will swap them

Our array is now

112456791181513

Total number of displacements: 14

Total number of comparisons: 35

Since 8 at position 9 is smaller than 11 at position 8 we will swap them

Our array is now

112456798111513

Total number of displacements: 15

Total number of comparisons: 36

Since 8 at position 8 is smaller than 9 at position 7 we will swap them

Our array is now

112456789111513

Total number of displacements: 16

Total number of comparisons: 37

Since 8 at position 7 is bigger or equal than 7 at position 6 we will not perform the swapping

Since 13 at position 11 is smaller than 15 at position 10 we will swap them

Our array is now

112456789111315

Total number of displacements: 17

Total number of comparisons: 39

Since 13 at position 10 is bigger or equal than 11 at position 9 we will not perform the swapping

Gap will be reduced again and will be less than 1 so the sorting will be finished

In the end total number of comparisons was: 40

Total number of displacements was: 17

Final array is:

112456789111315

Performing shell sort on a given array of characters {'S', 'B', 'I', 'M', 'H', 'Q', 'C', 'L', 'R', 'E', 'P', 'K'}

Shell sort being executed for array: S B I M H Q C L R E P K

Current 'gap' is: 6

Since C at position 6 is smaller than S at position 0 we will swap them

Our array is now

CBIMHQSLREPK

Total number of displacements: 1

Total number of comparisons: 1

Since L at position 7 is bigger or equal than B at position 1 we will not perform the swapping

Since R at position 8 is bigger or equal than I at position 2 we will not perform the swapping

Since E at position 9 is smaller than M at position 3 we will swap them

Our array is now

CBIEHQSLRMPK

Total number of displacements: 2

Total number of comparisons: 4

Since P at position 10 is bigger or equal than H at position 4 we will not perform the swapping

Since K at position 11 is smaller than Q at position 5 we will swap them

Our array is now

CBIEHKSLRMPQ

Total number of displacements: 3

Total number of comparisons: 6

Current 'gap' is: 3

Since E at position 3 is bigger or equal than C at position 0 we will not perform the swapping

Since H at position 4 is bigger or equal than B at position 1 we will not perform the swapping

Since K at position 5 is bigger or equal than I at position 2 we will not perform the swapping

Since S at position 6 is bigger or equal than E at position 3 we will not perform the swapping

Since L at position 7 is bigger or equal than H at position 4 we will not perform the swapping

Since R at position 8 is bigger or equal than K at position 5 we will not perform the swapping

Since M at position 9 is smaller than S at position 6 we will swap them

Our array is now

CBIEHKMLRSPQ

Total number of displacements: 4

Total number of comparisons: 13

Since M at position 6 is bigger or equal than E at position 3 we will not perform the swapping

Since P at position 10 is bigger or equal than L at position 7 we will not perform the swapping

Since Q at position 11 is smaller than R at position 8 we will swap them

Our array is now

CBIEHKMLQSPR

Total number of displacements: 5

Total number of comparisons: 16

Since Q at position 8 is bigger or equal than K at position 5 we will not perform the swapping

Current 'gap' is: 1

Since B at position 1 is smaller than C at position 0 we will swap them

Our array is now

BCIEHKMLQSPR

Total number of displacements: 6

Total number of comparisons: 18

Since I at position 2 is bigger or equal than C at position 1 we will not perform the swapping

Since E at position 3 is smaller than I at position 2 we will swap them

Our array is now

BCEIHKMLQSPR

Total number of displacements: 7

Total number of comparisons: 20

Since E at position 2 is bigger or equal than C at position 1 we will not perform the swapping

Since H at position 4 is smaller than I at position 3 we will swap them

Our array is now

BCEHIKMLQSPR

Total number of displacements: 8

Total number of comparisons: 22

Since H at position 3 is bigger or equal than E at position 2 we will not perform the swapping

Since K at position 5 is bigger or equal than I at position 4 we will not perform the swapping

Since M at position 6 is bigger or equal than K at position 5 we will not perform the swapping

Since L at position 7 is smaller than M at position 6 we will swap them

Our array is now

BCEHIKLMQSPR

Total number of displacements: 9

Total number of comparisons: 26

Since L at position 6 is bigger or equal than K at position 5 we will not perform the swapping

Since Q at position 8 is bigger or equal than M at position 7 we will not perform the swapping

Since S at position 9 is bigger or equal than Q at position 8 we will not perform the swapping

Since P at position 10 is smaller than S at position 9 we will swap them

Our array is now

BCEHIKLMQPSR

Total number of displacements: 10

Total number of comparisons: 30

Since P at position 9 is smaller than Q at position 8 we will swap them

Our array is now

BCEHIKLMPQSR

Total number of displacements: 11

Total number of comparisons: 31

Since P at position 8 is bigger or equal than M at position 7 we will not perform the swapping

Since R at position 11 is smaller than S at position 10 we will swap them

Our array is now

BCEHIKLMPQRS

Total number of displacements: 12

Total number of comparisons: 33

Since R at position 10 is bigger or equal than Q at position 9 we will not perform the swapping

Gap will be reduced again and will be less than 1 so the sorting will be finished

In the end total number of comparisons was: 34

Total number of displacements was: 12

Final array is:

BCEHIKLMPQRS

Merge sort

Merge sort

NOTE: Since merge sort is not in place algorithm i won't talk about the number of 'displacements' . Also I just performed merge sort and didn't talk about the number of displacements for each merge of two arrays(separate linear funciton that merges two sorted arrays in one sorted array) instead I just calculated the number of comparisons during those merges and gave a final answer. If I did also write for merge it would just be way to long. Also I was executing it the same way the program would (recursively).

Merge sorting {1,2,3,4,5,6,7,8,9,10}

Our current array that will be separated in left and right array is: 1 2 3 4 5 6 7 8 9 10 $\,$

Left array: 12345

Right array: 6 7 8 9 10

Our current array that will be separated in left and right array is: 1 2 3 4 5

Left array: 12

Right array: 3 4 5

Our current array that will be separated in left and right array is: 12

Left array: 1

Right array: 2

Left array (merged): 1

Right array (merged): 2

After this we will merge and the merged array will be: 12

Our current array that will be separated in left and right array is: 3 4 5

Left array: 3

Right array: 45

Our current array that will be separated in left and right array is: 45

Left array: 4

Right array: 5

Left array (merged): 4

Right array (merged): 5

After this we will merge and the merged array will be: 45

Left array (merged): 3

Right array (merged): 45

After this we will merge and the merged array will be: 3 4 5

Left array (merged): 12

Right array (merged): 3 4 5

After this we will merge and the merged array will be: 1 2 3 4 5

Our current array that will be separated in left and right array is: 6 7 8 9 10

Left array: 67

Right array: 8 9 10

Our current array that will be separated in left and right array is: 67

Left array: 6

Right array: 7

Left array (merged): 6

Right array (merged): 7

After this we will merge and the merged array will be: 67

Our current array that will be separated in left and right array is: 8 9 10

Left array: 8

Right array: 9 10

Our current array that will be separated in left and right array is: 9 10

Left array: 9

Right array: 10

Left array (merged): 9

Right array (merged): 10

After this we will merge and the merged array will be: 9 10

Left array (merged): 8

Right array (merged): 9 10

After this we will merge and the merged array will be: 8 9 10

Left array (merged): 67

Right array (merged): 8 9 10

After this we will merge and the merged array will be: 6 7 8 9 10

Left array (merged): 1 2 3 4 5

Right array (merged): 6 7 8 9 10

After this we will merge and the merged array will be: 1 2 3 4 5 6 7 8 9 10

Numer of comparisons is: 15

So in the end after sorting array is:

12345678910

Merge sorting {10,9,8,7,6,5,4,3,2,1}

Our current array that will be separated in left and right array is: 10 9 8 7 6 5 4 3 2 1

Left array: 10 9 8 7 6

Right array: 5 4 3 2 1

Our current array that will be separated in left and right array is: 10 9 8 7 6

Left array: 109

Right array: 8 7 6

Our current array that will be separated in left and right array is: 109 Left array: 10 Right array: 9 Left array (merged): 10 Right array (merged): 9 After this we will merge and the merged array will be: 9 10 Our current array that will be separated in left and right array is: 8 7 6 Left array: 8 Right array: 76 Our current array that will be separated in left and right array is: 7 6 Left array: 7 Right array: 6 Left array (merged): 7 Right array (merged): 6 After this we will merge and the merged array will be: 67 Left array (merged): 8 Right array (merged): 67 After this we will merge and the merged array will be: 6 7 8 Left array (merged): 9 10 Right array (merged): 678 After this we will merge and the merged array will be: 6 7 8 9 10 Our current array that will be separated in left and right array is: 5 4 3 2 1 Left array: 5 4 Right array: 3 2 1 Our current array that will be separated in left and right array is: 5 4 Left array: 5 Right array: 4 Left array (merged): 5 Right array (merged): 4

After this we will merge and the merged array will be: 45

Our current array that will be separated in left and right array is: 3 2 1

Left array: 3

Right array: 21

Our current array that will be separated in left and right array is: 21

Left array: 2

Right array: 1

Left array (merged): 2

Right array (merged): 1

After this we will merge and the merged array will be: 12

Left array (merged): 3

Right array (merged): 12

After this we will merge and the merged array will be: 1 2 3

Left array (merged): 45

Right array (merged): 123

After this we will merge and the merged array will be: 1 2 3 4 5

Left array (merged): 6 7 8 9 10

Right array (merged): 1 2 3 4 5

After this we will merge and the merged array will be: 1 2 3 4 5 6 7 8 9 10

Numer of comparisons is: 19

So in the end after sorting array is:

12345678910

Merge sorting {5, 2, 13, 9, 1, 7, 6, 8, 1, 15, 4, 11}

Our current array that will be separated in left and right array is: 5 2 13 9 1 7 6 8 1 15 4 11

Left array: 5 2 13 9 1 7

Right array: 6 8 1 15 4 11

Our current array that will be separated in left and right array is: 5 2 13 9 1 7

Left array: 5 2 13

Right array: 917

Our current array that will be separated in left and right array is: 5 2 13

Left array: 5 Right array: 2 13 Our current array that will be separated in left and right array is: 2 13 Left array: 2 Right array: 13 Left array (merged): 2 Right array (merged): 13 After this we will merge and the merged array will be: 2 13 Left array (merged): 5 Right array (merged): 2 13 After this we will merge and the merged array will be: 2 5 13 Our current array that will be separated in left and right array is: 9 1 7 Left array: 9 Right array: 17 Our current array that will be separated in left and right array is: 17 Left array: 1 Right array: 7 Left array (merged): 1 Right array (merged): 7 After this we will merge and the merged array will be: 17 Left array (merged): 9 Right array (merged): 17 After this we will merge and the merged array will be: 179 Left array (merged): 2 5 13 Right array (merged): 179 After this we will merge and the merged array will be: 1 2 5 7 9 13 Our current array that will be separated in left and right array is: 6 8 1 15 4 11

Our current array that will be separated in left and right array is: 6 8 1

Left array: 6

Left array: 681

Right array: 15 4 11

Right array: 8 1

Our current array that will be separated in left and right array is: 8 1

Left array: 8

Right array: 1

Left array (merged): 8

Right array (merged): 1

After this we will merge and the merged array will be: 18

Left array (merged): 6

Right array (merged): 18

After this we will merge and the merged array will be: 168

Our current array that will be separated in left and right array is: 15 4 11

Left array: 15

Right array: 4 11

Our current array that will be separated in left and right array is: 4 11

Left array: 4

Right array: 11

Left array (merged): 4

Right array (merged): 11

After this we will merge and the merged array will be: 4 11

Left array (merged): 15

Right array (merged): 4 11

After this we will merge and the merged array will be: 4 11 15

Left array (merged): 168

Right array (merged): 4 11 15

After this we will merge and the merged array will be: 1 4 6 8 11 15

Left array (merged): 1 2 5 7 9 13

Right array (merged): 1 4 6 8 11 15

After this we will merge and the merged array will be: 1 1 2 4 5 6 7 8 9 11 13 15

Numer of comparisons is: 32

So in the end after sorting array is:

 $1\ 1\ 2\ 4\ 5\ 6\ 7\ 8\ 9\ 11\ 13\ 15$

Merge sorting {'S', 'B', 'I', 'M', 'H', 'Q', 'C', 'L', 'R', 'E', 'P', 'K'}

Our current array that will be separated in left and right array is: S B I M H Q C L R E P K

Left array: SBIMHQ

Right array: CLREPK

Our current array that will be separated in left and right array is: S B I M H Q

Left array: S B I

Right array: MHQ

Our current array that will be separated in left and right array is: S B I

Left array: S

Right array: B I

Our current array that will be separated in left and right array is: B I

Left array: B

Right array: I

Left array (merged): B

Right array (merged): I

After this we will merge and the merged array will be: B I

Left array (merged): S

Right array (merged): B I

After this we will merge and the merged array will be: BIS

Our current array that will be separated in left and right array is: M H Q

Left array: M

Right array: H Q

Our current array that will be separated in left and right array is: H Q

Left array: H

Right array: Q

Left array (merged): H

Right array (merged): Q

After this we will merge and the merged array will be: H Q

Left array (merged): M Right array (merged): H Q After this we will merge and the merged array will be: H M Q Left array (merged): BIS Right array (merged): H M Q After this we will merge and the merged array will be: BHIMQS Our current array that will be separated in left and right array is: C L R E P K Left array: CLR Right array: E P K Our current array that will be separated in left and right array is: CLR Left array: C Right array: LR Our current array that will be separated in left and right array is: LR Left array: L Right array: R Left array (merged): L Right array (merged): R After this we will merge and the merged array will be: LR Left array (merged): C Right array (merged): LR After this we will merge and the merged array will be: CLR Our current array that will be separated in left and right array is: E P K Left array: E Right array: P K Our current array that will be separated in left and right array is: P K Left array: P Right array: K Left array (merged): P Right array (merged): K After this we will merge and the merged array will be: K P

Left array (merged): E

Right array (merged): K P

After this we will merge and the merged array will be: EKP

Left array (merged): CLR

Right array (merged): EKP

After this we will merge and the merged array will be: CEKLPR

Left array (merged): BHIMQS

Right array (merged): CEKLPR

After this we will merge and the merged array will be: B C E H I K L M P Q R S

Numer of comparisons is: 31

So in the end after sorting array is:

BCEHIKLMPQRS

Quick sort

Perfrming quick sort now

Note that I took the first element as a pivot for each subarray here

Performing quick sort on a sorted array

First element of 'subarray' with lower and upper bound of: 0, 9 of the original array will be taken as pivot or array[lower_bound]:1 is the pivot

Partitioning the array(pivot:1)1 2 3 4 5 6 7 8 9 10

Swapping the pivot element: 0 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 1 2 3 4 5 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 1, 9 of the original array will be taken as pivot or array[lower_bound]:2 is the pivot

Partitioning the array(pivot:2)2 3 4 5 6 7 8 9 10

Swapping the pivot element: 1 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 2 3 4 5 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 2, 9 of the original array will be taken as pivot or array[lower bound]:3 is the pivot

Partitioning the array(pivot:3)3 4 5 6 7 8 9 10

Swapping the pivot element: 2 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 3 4 5 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 3, 9 of the original array will be taken as pivot or array[lower bound]:4 is the pivot

Partitioning the array(pivot:4)4 5 6 7 8 9 10

Swapping the pivot element: 3 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 4 5 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 4, 9 of the original array will be taken as pivot or array[lower_bound]:5 is the pivot

Partitioning the array(pivot:5)5 6 7 8 9 10

Swapping the pivot element: 4 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 5 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 5, 9 of the original array will be taken as pivot or array[lower bound]:6 is the pivot

Partitioning the array(pivot:6)6 7 8 9 10

Swapping the pivot element: 5 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 6 7 8 9 10

First element of 'subarray' with lower and upper bound of: 6, 9 of the original array will be taken as pivot or array[lower_bound]:7 is the pivot

Partitioning the array(pivot:7)7 8 9 10

Swapping the pivot element: 6 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 7 8 9 10

First element of 'subarray' with lower and upper bound of: 7, 9 of the original array will be taken as pivot or array[lower_bound]:8 is the pivot

Partitioning the array(pivot:8)8 9 10

Swapping the pivot element: 7 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 8 9 10

First element of 'subarray' with lower and upper bound of: 8, 9 of the original array will be taken as pivot or array[lower_bound]:9 is the pivot

Partitioning the array(pivot:9)9 10

Swapping the pivot element: 8 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 9 10

After sorting the total number of comparisons is: 54

Total number of displacements: 0

Array after sorting is:

12345678910

Performing quick sort sort on a reversly sorted array

First element of 'subarray' with lower and upper bound of: 0, 9 of the original array will be taken as pivot or array[lower_bound]:10 is the pivot

Partitioning the array(pivot:10)10 9 8 7 6 5 4 3 2 1

Swapping the pivot element: 0 with the element at 'end': 9 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 19876543210

First element of 'subarray' with lower and upper bound of: 0, 8 of the original array will be taken as pivot or array[lower_bound]:1 is the pivot

Partitioning the array(pivot:1)198765432

Swapping the pivot element: 0 with the element at 'end': 8 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 198765432

First element of 'subarray' with lower and upper bound of: 1, 8 of the original array will be taken as pivot or array[lower_bound]:9 is the pivot

Partitioning the array(pivot:9)9 8 7 6 5 4 3 2

Swapping the pivot element: 1 with the element at 'end': 8 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 28765439

First element of 'subarray' with lower and upper bound of: 1, 7 of the original array will be taken as pivot or array[lower_bound]:2 is the pivot

Partitioning the array(pivot:2)2 8 7 6 5 4 3

Swapping the pivot element: 1 with the element at 'end': 7 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 2876543

First element of 'subarray' with lower and upper bound of: 2, 7 of the original array will be taken as pivot or array[lower_bound]:8 is the pivot

Partitioning the array(pivot:8)8 7 6 5 4 3

Swapping the pivot element: 2 with the element at 'end': 7 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 3 7 6 5 4 8

First element of 'subarray' with lower and upper bound of: 2, 6 of the original array will be taken as pivot or array[lower bound]:3 is the pivot

Partitioning the array(pivot:3)3 7 6 5 4

Swapping the pivot element: 2 with the element at 'end': 6 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 3 7 6 5 4

First element of 'subarray' with lower and upper bound of: 3, 6 of the original array will be taken as pivot or array[lower_bound]:7 is the pivot

Partitioning the array(pivot:7)7 6 5 4

Swapping the pivot element: 3 with the element at 'end': 6 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 4 6 5 7

First element of 'subarray' with lower and upper bound of: 3, 5 of the original array will be taken as pivot or array[lower bound]:4 is the pivot

Partitioning the array(pivot:4)4 6 5

Swapping the pivot element: 3 with the element at 'end': 5 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 4 6 5

First element of 'subarray' with lower and upper bound of: 4, 5 of the original array will be taken as pivot or array[lower_bound]:6 is the pivot

Partitioning the array(pivot:6)6 5

Swapping the pivot element: 4 with the element at 'end': 5 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 5 6

After sorting the total number of comparisons is: 54

Total number of displacements: 5

Array after sorting is:

12345678910

Performing quick sort on a given array {5, 2, 13, 9, 1, 7, 6, 8, 1, 15, 4, 11}

First element of 'subarray' with lower and upper bound of: 0, 11 of the original array will be taken as pivot or array[lower_bound]:5 is the pivot

Partitioning the array(pivot:5)5 2 13 9 1 7 6 8 1 15 4 11

Now swapping element in this subbaray at: 2 with the element at: 10

Now swapping element in this subbaray at: 3 with the element at: 8

Swapping the pivot element: 0 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 1 2 4 1 5 7 6 8 9 15 13 11

First element of 'subarray' with lower and upper bound of: 0, 3 of the original array will be taken as pivot or array[lower bound]:1 is the pivot

Partitioning the array(pivot:1)1 2 4 1

Now swapping element in this subbaray at: 1 with the element at: 3

Swapping the pivot element: 0 with the element at 'end': 3 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 1142

First element of 'subarray' with lower and upper bound of: 2, 3 of the original array will be taken as pivot or array[lower_bound]:4 is the pivot

Partitioning the array(pivot:4)4 2

Swapping the pivot element: 2 with the element at 'end': 3 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 24

First element of 'subarray' with lower and upper bound of: 5, 11 of the original array will be taken as pivot or array[lower_bound]:7 is the pivot

Partitioning the array(pivot:7)7 6 8 9 15 13 11

Swapping the pivot element: 5 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 6 7 8 9 15 13 11

First element of 'subarray' with lower and upper bound of: 7, 11 of the original array will be taken as pivot or array[lower_bound]:8 is the pivot

Partitioning the array(pivot:8)8 9 15 13 11

Swapping the pivot element: 7 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 8 9 15 13 11

First element of 'subarray' with lower and upper bound of: 8, 11 of the original array will be taken as pivot or array[lower_bound]:9 is the pivot

Partitioning the array(pivot:9)9 15 13 11

Swapping the pivot element: 8 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 9 15 13 11

First element of 'subarray' with lower and upper bound of: 9, 11 of the original array will be taken as pivot or array[lower bound]:15 is the pivot

Partitioning the array(pivot:15)15 13 11

Swapping the pivot element: 9 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 11 13 15

First element of 'subarray' with lower and upper bound of: 9, 10 of the original array will be taken as pivot or array[lower_bound]:11 is the pivot

Partitioning the array(pivot:11)11 13

Swapping the pivot element: 9 with the element at 'end': 10 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: 11 13

After sorting the total number of comparisons is: 39

Total number of displacements: 8

Array after sorting is:

112456789111315

Performing quick sort on a given array of characters {'S', 'B', 'I', 'M', 'H', 'Q', 'C', 'L', 'R', 'E', 'P', 'K'}

First element of 'subarray' with lower and upper bound of: 0, 11 of the original array will be taken as pivot or array[lower_bound]:S is the pivot

Partitioning the array(pivot:S)S B I M H Q C L R E P K

Swapping the pivot element: 0 with the element at 'end': 11 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: KBIMHQCLREPS

First element of 'subarray' with lower and upper bound of: 0, 10 of the original array will be taken as pivot or array[lower bound]:K is the pivot

Partitioning the array(pivot:K)K B I M H Q C L R E P

Now swapping element in this subbaray at: 3 with the element at: 9

Now swapping element in this subbaray at: 5 with the element at: 6

Swapping the pivot element: 0 with the element at 'end': 10 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: CBIEHKQLRMP

First element of 'subarray' with lower and upper bound of: 0, 4 of the original array will be taken as pivot or array[lower_bound]:C is the pivot

Partitioning the array(pivot:C)C B I E H

Swapping the pivot element: 0 with the element at 'end': 4 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: BCIEH

First element of 'subarray' with lower and upper bound of: 2, 4 of the original array will be taken as pivot or array[lower_bound]: I is the pivot

Partitioning the array(pivot:I)I E H

Swapping the pivot element: 2 with the element at 'end': 4 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: H E I

First element of 'subarray' with lower and upper bound of: 2, 3 of the original array will be taken as pivot or array[lower_bound]:H is the pivot

Partitioning the array(pivot:H)H E

Swapping the pivot element: 2 with the element at 'end': 3 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: E H

First element of 'subarray' with lower and upper bound of: 6, 10 of the original array will be taken as pivot or array[lower_bound]:Q is the pivot

Partitioning the array(pivot:Q)Q L R M P

Now swapping element in this subbaray at: 8 with the element at: 10

Swapping the pivot element: 6 with the element at 'end': 10 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: M L P Q R

First element of 'subarray' with lower and upper bound of: 6, 8 of the original array will be taken as pivot or array[lower_bound]:M is the pivot

Partitioning the array(pivot:M)M L P

Swapping the pivot element: 6 with the element at 'end': 8 index which is begining of elements bigger than pivot:

After 'partitioning' the subArray is: L M P

After sorting the total number of comparisons is: 41
Total number of displacements: 10
Array after sorting is:
BCEHIKLMPQRS
Heap sort
Perfomrming heap sort now
Performing heap sort on a sorted array
I will use heapfy method to sort this array and make it heap before performing the sorting algorithm
Array is:
12345678910
Array after heapify:
12345678910
Swaping place of 10 with 5
Array after heapify:
12341067895
Swaping place of 8 with 4
Array after heapify:
1 2 3 8 10 6 7 4 9 5

Swaping place of 10 with 3 Swaping place of 9 with 3 Array after heapify: $1\,2\,10\,8\,9\,6\,7\,4\,3\,5$ Swaping place of 10 with 2 Swaping place of 9 with 2 Swaping place of 5 with 2 Array after heapify: 11098567432 Swaping place of 10 with 1 Swaping place of 9 with 1 Swaping place of 6 with 1 Array after heapify: 10968517432 Our array now has a heap form: 10968517432 Now array 'shrinking' and removing element by element in our max heap will be performed 10968517432 Swapping 2 with 10 Swaping place of 9 with 2 Swaping place of 8 with 2 Swaping place of 7 with 2 After the swap and the heapify of subaray, array is 98675124310 98675124310 Swapping 3 with 9 Swaping place of 8 with 3 Swaping place of 7 with 3 Swaping place of 4 with 3

After the swap and the heapify of subaray, array is 87645123910 87645123910 Swapping 3 with 8 Swaping place of 7 with 3 Swaping place of 6 with 3 Swaping place of 5 with 3 After the swap and the heapify of subaray, array is 76543128910 76543128910 Swapping 2 with 7 Swaping place of 6 with 2 Swaping place of 5 with 2 Swaping place of 3 with 2 After the swap and the heapify of subaray, array is 65342178910 65342178910 Swapping 1 with 6 Swaping place of 5 with 1 Swaping place of 4 with 1 After the swap and the heapify of subaray, array is 54312678910 54312678910 Swapping 2 with 5 Swaping place of 4 with 2 Swaping place of 3 with 2 After the swap and the heapify of subaray, array is 43215678910 43215678910 Swapping 1 with 4 Swaping place of 3 with 1

Swaping place of 2 with 1
After the swap and the heapify of subaray, array is
3 2 1 4 5 6 7 8 9 10
3 2 1 4 5 6 7 8 9 10
Swapping 1 with 3
Swaping place of 2 with 1
After the swap and the heapify of subaray, array is
2 1 3 4 5 6 7 8 9 10
2 1 3 4 5 6 7 8 9 10
Swapping 1 with 2
After the swap and the heapify of subaray, array is
12345678910
12345678910
Swapping 1 with 1
After the swap and the heapify of subaray, array is
12345678910
Total number of displacements: 39
Total number of comparisons: 90
Final array is:
12345678910
Performing heap sort sort on a reversly sorted array
I will use heapfy method to sort this array and make it heap before performing the sorting algorithm
Array is:
10987654321
Array after heapify:

10 9 8 7 6 5 4 3 2 1
Array after heapify:
10 9 8 7 6 5 4 3 2 1
Array after heapify:
10 9 8 7 6 5 4 3 2 1
Array after heapify:
10 9 8 7 6 5 4 3 2 1
Array after heapify:
10 9 8 7 6 5 4 3 2 1
Array after heapify:
10 9 8 7 6 5 4 3 2 1
Our array now has a heap form:
10 9 8 7 6 5 4 3 2 1
Now array 'shrinking' and removing element by element in our max heap will be performed
10 9 8 7 6 5 4 3 2 1
Swapping 1 with 10
Swaping place of 9 with 1
Swaping place of 8 with 1
Swaping place of 6 with 1
Swaping place of 2 with 1
After the swap and the heapify of subaray, array is
98672543110
98672543110
Swapping 1 with 9
Swaping place of 8 with 1
Swaping place of 7 with 1
Swaping place of 4 with 1
After the swap and the heapify of subaray, array is
87642513910

87642513910 Swapping 3 with 8 Swaping place of 7 with 3 Swaping place of 6 with 3 Swaping place of 5 with 3 After the swap and the heapify of subaray, array is 76542318910 76542318910 Swapping 1 with 7 Swaping place of 6 with 1 Swaping place of 5 with 1 Swaping place of 3 with 1

After the swap and the heapify of subaray, array is

65342178910

65342178910

Swapping 1 with 6

Swaping place of 5 with 1

Swaping place of 4 with 1

After the swap and the heapify of subaray, array is

54312678910

54312678910

Swapping 2 with 5

Swaping place of 4 with 2

Swaping place of 3 with 2

After the swap and the heapify of subaray, array is

43215678910

43215678910

Swapping 1 with 4

Swaping place of 3 with 1

Swaping place of 2 with 1

After the swap and the heapify of subaray, array is

32145678910 Swapping 1 with 3 Swaping place of 2 with 1 After the swap and the heapify of subaray, array is 21345678910 21345678910 Swapping 1 with 2 After the swap and the heapify of subaray, array is 12345678910 12345678910 Swapping 1 with 1 After the swap and the heapify of subaray, array is 12345678910 Total number of displacements: 30 Total number of comparisons: 72 Final array is: 12345678910 Performing heap sort on a given array {5, 2, 13, 9, 1, 7, 6, 8, 1, 15, 4, 11} I will use heapfy method to sort this array and make it heap before performing the sorting algorithm Array is: 5 2 13 9 1 7 6 8 1 15 4 11

32145678910

Array after heapify:

521391768115411

Swaping place of 11 with 7

5 2 13 9 1 11 6 8 1 15 4 7 Swaping place of 15 with 1 Array after heapify: 5 2 13 9 15 11 6 8 1 1 4 7 Array after heapify: 5 2 13 9 15 11 6 8 1 1 4 7 Swaping place of 15 with 13 Array after heapify: 521591311681147 Swaping place of 15 with 2 Swaping place of 13 with 2 Array after heapify: 5 15 13 9 2 11 6 8 1 1 4 7 Swaping place of 15 with 5 Swaping place of 13 with 5 Swaping place of 11 with 5 Swaping place of 7 with 5 Array after heapify: 15 13 11 9 2 7 6 8 1 1 4 5 Our array now has a heap form: 15 13 11 9 2 7 6 8 1 1 4 5 Now array 'shrinking' and removing element by element in our max heap will be performed 15 13 11 9 2 7 6 8 1 1 4 5 Swapping 5 with 15 Swaping place of 13 with 5 Swaping place of 11 with 5 Swaping place of 7 with 5

After the swap and the heapify of subaray, array is

Array after heapify:

13 11 7 9 2 5 6 8 1 1 4 15

13 11 7 9 2 5 6 8 1 1 4 15

Swapping 4 with 13

Swaping place of 11 with 4

Swaping place of 9 with 4

Swaping place of 8 with 4

After the swap and the heapify of subaray, array is

11 9 7 8 2 5 6 4 1 1 13 15

119782564111315

Swapping 1 with 11

Swaping place of 9 with 1

Swaping place of 8 with 1

Swaping place of 6 with 1

After the swap and the heapify of subaray, array is

987625141111315

987625141111315

Swapping 1 with 9

Swaping place of 8 with 1

Swaping place of 7 with 1

Swaping place of 5 with 1

After the swap and the heapify of subaray, array is

875621149111315

875621149111315

Swapping 4 with 8

Swaping place of 7 with 4

Swaping place of 6 with 4

After the swap and the heapify of subaray, array is

765421189111315

765421189111315

Swapping 1 with 7

Swaping place of 6 with 1

Swaping place of 5 with 1

Swaping place of 2 with 1

After the swap and the heapify of subaray, array is

652411789111315

652411789111315

Swapping 1 with 6

Swaping place of 5 with 1

Swaping place of 4 with 1

After the swap and the heapify of subaray, array is

542116789111315

542116789111315

Swapping 1 with 5

Swaping place of 4 with 1

Swaping place of 2 with 1

After the swap and the heapify of subaray, array is

421156789111315

421156789111315

Swapping 1 with 4

Swaping place of 2 with 1

After the swap and the heapify of subaray, array is

211456789111315

211456789111315

Swapping 1 with 2

After the swap and the heapify of subaray, array is

112456789111315

 $1\ 1\ 2\ 4\ 5\ 6\ 7\ 8\ 9\ 11\ 13\ 15$

Swapping 1 with 1

After the swap and the heapify of subaray, array is

112456789111315

112456789111315

Swapping 1 with 1

After the swap and the heapify of subaray, array is
1 1 2 4 5 6 7 8 9 11 13 15
Total number of displacements: 43
Total number of comparisons: 100
Final array is:
1 1 2 4 5 6 7 8 9 11 13 15
Performing heap sort on a given array of characters {'S', 'B', 'I', 'M', 'H', 'Q', 'C', 'L', 'R', 'E', 'P', 'K'}
I will use heapfy method to sort this array and make it heap before performing the sorting algorithm
Array is:
SBIMHQCLREPK
Array after heapify:
SBIMHQCLREPK
Array after heapify:
SBIMHQCLREPK
Swaping place of R with H
Array after heapify:
SBIMRQCLHEPK
Array after heapify:
SBIMRQCLHEPK
Swaping place of R with I
Array after heapify:
SBRMIQCLHEPK
Swaping place of R with B
Swaping place of Q with B
Swaping place of P with B

Array after heapify: SRQMIPCLHEBK Array after heapify: SRQMIPCLHEBK Our array now has a heap form: SRQMIPCLHEBK Now array 'shrinking' and removing element by element in our max heap will be performed SRQMIPCLHEBK Swapping K with S Swaping place of R with K Swaping place of Q with K Swaping place of P with K After the swap and the heapify of subaray, array is RQPMIKCLHEBS RQPMIKCLHEBS Swapping B with R Swaping place of Q with B Swaping place of P with B Swaping place of K with B After the swap and the heapify of subaray, array is QPKMIBCLHERS QPKMIBCLHERS Swapping E with Q Swaping place of P with E Swaping place of M with E Swaping place of L with E After the swap and the heapify of subaray, array is **PMKLIBCEHQRS** P M K L I B C E H Q R S

Swapping H with P Swaping place of M with H Swaping place of L with H After the swap and the heapify of subaray, array is MLKHIBCEPQRS MLKHIBCEPQRS Swapping E with M Swaping place of L with E Swaping place of K with E Swaping place of I with E After the swap and the heapify of subaray, array is LKIHEBCMPQRS LKIHEBCMPQRS Swapping C with L Swaping place of K with C Swaping place of I with C Swaping place of E with C After the swap and the heapify of subaray, array is KIEHCBLMPQRS KIEHCBLMPQRS Swapping B with K Swaping place of I with B Swaping place of H with B After the swap and the heapify of subaray, array is IHEBCKLMPQRS IHEBCKLMPQRS Swapping C with I Swaping place of H with C Swaping place of E with C After the swap and the heapify of subaray, array is

HECBIKLMPQRS

HECBIKLMPQRS

Swapping B with H

Swaping place of E with B

Swaping place of C with B

After the swap and the heapify of subaray, array is

ECBHIKLMPQRS

ECBHIKLMPQRS

Swapping B with E

Swaping place of C with B

After the swap and the heapify of subaray, array is

CBEHIKLMPQRS

CBEHIKLMPQRS

Swapping B with C

After the swap and the heapify of subaray, array is

BCEHIKLMPQRS

BCEHIKLMPQRS

Swapping B with B

After the swap and the heapify of subaray, array is

BCEHIKLMPQRS

Total number of displacements: 41

Total number of comparisons: 96

Final array is:

BCEHIKLMPQRS