

1 Exercise 1

Assumption:

$$P(A \cup D) = P(A) + P(D) - P(A \cap D) \quad (1)$$

Convert $D \rightarrow B \cup C$:

$$P(A \cup B \cup C) = P(A) + P(B \cup C) - P(A \cap (B \cup C)) \quad (2)$$

Evaluate $P(B \cup C)$ with (1):

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(B \cap C) - P(A \cap (B \cup C)) \quad (3)$$

Notice that $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ and evaluate $P(A \cap (B \cup C))$ with (1):

$$P((A \cap B) \cup (A \cap C)) = P(A \cap B) + P(A \cap C) - P(A \cap B \cap C) \quad (4)$$

Where I used $(A \cap B) \cap (A \cap C) = ((A \cap B) \cap A) \cap ((A \cap B) \cap C) = (A \cap B) \cap (A \cap B \cap C) = A \cap B \cap C$.

Plugging (4) into (3) results in:

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(B \cap C) - P(A \cap B) - P(A \cap C) + P(A \cap B \cap C) \quad (5)$$

2 Exercise 2

2.1

Law: Performance doubles every 18 months.

Data: 148,600.0 (Summit)

Equation: $148,600 \text{TFlop/s} * 2^{(x/18\text{months})} = 1,000,000 \text{TFlop/s}$

$\rightarrow x = 49.5\text{months}$ (Source: Wolframalpha)

2.2

Data:

11/2007: 478.2 TFlop/s (LLNL)

11/2011: 10500 TFlop/s (K Computer)

Equation: $478.2 \text{TFlop/s} * 2^{(48\text{mo}/x)} = 10500 \text{TFlop/s}$

$\rightarrow x = 10.8$ (Wolframalpha)

If we replace 18 months with 10.8 months, we get 1 ExaFlop/s in 29.7 months.

3 Exercise 3

3.1

$$t_{Old} = t_{Calc} + t_{IO}$$

$$t_{New} = t_{Calc}/10 + t_{IO}$$

$$t_{Calc} = 0.4 * t_{Old}$$

$$t_{IO} = 0.6 * t_{Old}$$

$$\rightarrow \text{Speedup} = t_{Old}/t_{New} = 1/(0.4 * 0.1 + 0.6) = 1/0.64 = 156.25\%$$

3.2

As above:

$$\rightarrow \text{Speedup}_{SQR} = t_{OldSQR}/t_{NewSQR} = 1/(0.2 * 0.1 + 0.8) = 1/0.82 = 122.95\%$$

$$\rightarrow \text{Speedup}_{FP} = t_{OldFP}/t_{NewFP} = 1/(0.5/1.6 + 0.5) = 1/0.8125 = 123.07\%$$

FP is faster, but not by much.

3.3

As above:

$$\text{Amdahl} : \text{Speedup} = 1/((1 - P) + P/N)$$

$$\rightarrow 100 = \text{Speedup} = 1/(S + (1 - S)/128)$$

$$\rightarrow 0.01 = (S + (1 - S)/128)$$

$$\rightarrow 1.28 = 128 * S + (1 - S)$$

$$\rightarrow 0.28 = 127 * S$$

$$\rightarrow S = 0.002205$$

The serial fraction can be up to 0.2205%.