

source/linear_least_squares.hpp

```
1  #pragma once
2
3  #include "qr_factorization.hpp"
4  #include "slae.hpp"
5
6
7
8  // Linear Least Squares problem.  $O(N^3)$  complexity.
9  //
10 // LLS has a following solution:
11 //    $x = A^+ b$ 
12 //   where  $A^+ = R^{-1} * Q^T$ 
13 //
14 // We can rewrite it as a SLAE:
15 //    $R x = Q^T b$ 
16 //
17 // since 'R' is upper-triangular, we only need to do the backwards gaussian
18 // elimination, which is  $O(N^2)$ .
19 //
20 Vector linear_least_squares(const Matrix& A, const Matrix& b) {
21     // Computing QR the usual way
22     // const auto [Q, R] = qr_factorize(A);
23     // const auto x      = backwards_gaussian_elimination(R, Q.transpose() * b);
24
25     // Computing QR with  $(Q^T * b)$  directly
26     const auto [QTb, R] = qr_factorize_lls(A, b);
27     const auto x        = backwards_gaussian_elimination(R, QTb);
28
29     return x;
30 }
```