

# Package ‘abcrlda’

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**Type** Package

**Title** Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis

**Version** 0.1.1

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**Description** This package offers methods to perform  
asymptotically bias-corrected regularized linear discriminant analysis  
for cost-sensitive binary classification.

**Imports** stats

**License** GPL-3

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**LazyData** true

**RoxygenNote** 6.1.1

## R topics documented:

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abcrlda	<i>Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis for Cost-Sensitive Binary Classification</i>
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## Description

Performs Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis

## Usage

```
abcrlda(x, y, gamma = 1, cost = c(0.5, 0.5))
```

## Arguments

x	Input matrix or data.frame , of dimension nobs x nvars; each row is an observation vector.
y	Class labels. Should be a factor with two levels, or a vector with two distinct values. If y is presented as a vector, it will be coerced into a factor. Length of y has to correspond to number of samples in x.
gamma	Regularization parameter in the following equation

$$W_{ABC}^{RLDA} = \gamma(x - \frac{\bar{x}_0 + \bar{x}_1}{2})^T H(\bar{x}_0 - \bar{x}_1) - \log(\frac{C_{01}}{C_{10}}) + \omega_{opt}$$

cost	parameter that controls prioritization of classes. This is a vector of length 1 or 2 where first value is $C_{10}$ (represents prioritization of class 0) and second value if provided is $C_{01}$ (represents prioritization of class 1). Default value is c(0.5, 0.5), so both classes have equal priority and risk essentially becomes equivalent to error rate.  If single value is provided it should be normalized to be between 0 and 1 (but not including 0 or 1). This value will be assigned to $C_{10}$ and $C_{01}$ will be equal to $(1 - C_{10})$ In a vector of length 1, values bigger than 0.5 prioritizes correct classification of 0 class while values less than 0.5 prioritizes 1 class.
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## Value

An object of class "rrlda" is returned which can be used for class prediction (see predict())

a	Slope of a discriminant hyperplane. $W(x) = a'x + m$ .
m	Bias term. $W(x) = a'x + m$ .
cost	Normalized cost such that $C_{10} + C_{01} == 1$ .
gamma	Regularization parameter value provided during fitting.
lev	Levels. Corresponds to the labels in y.

## Reference

A. Zollanvari, M. Abdirash, A. Dadlani and B. Abibullaev, "Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis for Cost-Sensitive Binary Classification," in IEEE Signal Processing Letters, vol. 26, no. 9, pp. 1300-1304, Sept. 2019. doi: 10.1109/LSP.2019.2918485 URL: <http://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=8720003&isnumber=8770167>

## See Also

Other Other functions in the package: [cross\\_validation](#), [da\\_risk\\_estimator](#), [grid\\_search](#), [predict.abcrlda](#)

## Examples

```
data(iris)
train_data <- iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 1:4]
train_label <- factor(iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 5])
model <- abcrlda(train_data, train_label, gamma = 0.5, cost = 0.75)
predict(model, train_data)
```

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cross_validation	<i>Cross Validation</i>
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**Description**

Cross Validation

**Usage**

```
cross_validation(x, grouping, gamma = 1, cost = c(0.5, 0.5),
  kfolds = 10)
```

**Arguments**

x	Input matrix or data.frame , of dimension nobs x nvars; each row is an observation vector.
gamma	regularization parameter
cost	parameter that controls prioritization of classes. It's value should be between 0 and 1 (0 < cost_10 < 1) Values bigger than 0.5 prioritizes correct classification of 0 class while values less than 0.5 prioritizes 1 class
kfolds	Number of for cross validation algorithm

**Value**

Returns average error of cross validation

**See Also**

Other Other functions in the package: [abcrllda](#), [da\\_risk\\_estimator](#), [grid\\_search](#), [predict.abcrllda](#)

**Examples**

```
data(iris)
train_data <- iris[which(iris[, ncol(iris)] == "virginica" |
  iris[, ncol(iris)] == "versicolor"), 1:4]
train_label <- factor(iris[which(iris[, ncol(iris)] == "virginica" |
  iris[, ncol(iris)] == "versicolor"), 5])
model <- abcrllda(train_data, train_label, gamma = 0.5, cost = 0.75)
risk_estimate_20(model)
```

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da_risk_estimator	<i>Double Asymptotic Risk Estimator</i>
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**Description**

Calculates weighted error based on normalized cost values

**Usage**

```
da_risk_estimator(object)
```

**Arguments**

object                      An object of class "abcrlda".

**Value**

Weighted error based on "abcrlda" object

**Reference**

A. Zollanvari, M. Abdirash, A. Dadlani and B. Abibullaev, "Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis for Cost-Sensitive Binary Classification," in IEEE Signal Processing Letters, vol. 26, no. 9, pp. 1300-1304, Sept. 2019. doi: 10.1109/LSP.2019.2918485 URL: <http://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=8720003&isnumber=8770167>

**See Also**

Other Other functions in the package: [abcrlda](#), [cross\\_validation](#), [grid\\_search](#), [predict.abcrlda](#)

**Examples**

```
data(iris)
train_data <- iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 1:4]
train_label <- factor(iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 5])
model <- abcrlda(train_data, train_label, gamma = 0.5, cost = 0.75)
risk_estimate_20(model)
```

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grid\_search

*Grid Search*


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**Description**

Performs grid search based on cross validation or error estimation formula.

**Usage**

```
grid_search(x, y, range_gamma, range_cost, method = "estimator",
            nfold = 10)
```

**Arguments**

x	Input matrix or data.frame , of dimension nobx x nvax; each row is an observation vector.
y	Class labels. Should be a factor with two levels, or a vector with two distinct values. If y is presented as a vector, it will be coerced into a factor. Length of y has to correspond to number of samples in x.
range_gamma	vector of gamma values to check
range_cost	[1 x n] vector or [2 x n] matrix of cost values to check
method	selects method to evaluate error. "estimator" and "cross"
nfold	number of fold to use with cross-validation

**Value**

List of best founded parameters

**See Also**

Other functions in the package: [abcrlda](#), [cross\\_validation](#), [da\\_risk\\_estimator](#), [predict.abcrlda](#)

**Examples**

```
data(iris)
train_data <- iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 1:4]
train_label <- factor(iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 5])

cost_range <- seq(0.1, 0.9, by = 0.2)
gamma_range <- c(0.1, 1, 10, 100, 1000)

gs <- grid_search(train_data, train_label,
                  range_gamma = gamma_range,
                  range_cost = cost_range,
                  method = "estimator")
model <- abcrlda(train_data, train_label,
                 gamma = gs$gamma[1], cost = gs$cost[1])
predict(model, train_data)
```

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predict.abcrlda	<i>Class Prediction for abcrlda objects</i>
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**Description**

Computes class predictions for new data based on a given abcrlda object

**Usage**

```
## S3 method for class 'abcrlda'
predict(object, newx, out_type = "class", ...)
```

**Arguments**

object	An object of class "abcrlda".
newx	Matrix of new values for x at which predictions are to be made.
...	Argument used by generic function predict(object, x, ...).
type	Determines a type of output. Two type of input could be provided. If "class" value is provided this will return factor with levels corresponding to lev stored in object. If "raw" value is provided this will return numeric vector with values obtained from discriminant function.

**Value**

class Class prediction for each observation. raw Raw values.

## Reference

A. Zollanvari, M. Abdirash, A. Dadlani and B. Abibullaev, "Asymptotically Bias-Corrected Regularized Linear Discriminant Analysis for Cost-Sensitive Binary Classification," in IEEE Signal Processing Letters, vol. 26, no. 9, pp. 1300-1304, Sept. 2019. doi: 10.1109/LSP.2019.2918485 URL: <http://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=8720003&isnumber=8770167>

## See Also

Other Other functions in the package: [abcrlda](#), [cross\\_validation](#), [da\\_risk\\_estimator](#), [grid\\_search](#)

## Examples

```
data(iris)
train_data <- iris[which(iris[, ncol(iris)] == "virginica" |
                        iris[, ncol(iris)] == "versicolor"), 1:4]
train_label <- factor(iris[which(iris[, ncol(iris)] == "virginica" |
                              iris[, ncol(iris)] == "versicolor"), 5])
model <- abcrlda(train_data, train_label, gamma = 0.5, cost = 0.75)
predict(model, train_data)
```

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