.*VSTU.*

Team Reference Document

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1. Code Templates

```
1.1. Basic Configuration.
1.1.1. .vimrc.
set cin nu ts=2 sw=2 sts=2 mouse=a
syn on
function! Compile()
    :!q++ -std=qnu++11 -q % -o %<.exe
endfunction
function! Run()
    :!time ./%<.exe
endfunction
map <F4> :call Compile()<cr>
map <F5> :call Run()<cr>
map <C-A> qqVG"+y
1.1.2. stress and template.
// g++ -std=c++11 main.cpp -o main -D"_DEBUG_TEMICH_"
#pragma GCC optimize("03")
#pragma GCC target(
    "sse, sse2, sse3, ssse3, sse4, popcnt, abm, mmx")
#include <algorithm>
#include <cmath>
#include <functional>
#include <iostream>
#include <map>
#include <queue>
#include <set>
#include <sstream>
#include <string>
#include <vector>
using namespace std;
using LL = long long;
using pii = pair<int, int>;
#define X first
#define Y second
template<typename T>
ostream& operator<<(ostream& out, const vector<T>& v);
template<typename U, typename V>
ostream& operator<<(ostream& out, const map<U, V>& v);
template<typename U, typename V>
ostream& operator<<(ostream& out, const pair<U, V>& v);
template<typename U, typename V>
ostream& operator<<(ostream& out, const pair<U, V>& v) {
 return out << "(" << v.first << ", " << v.second << ")";</pre>
```

```
}
                                                                   struct SolutionStr {
                                                                     string solve(string input) {
template<typename U, typename V>
                                                                       istringstream is(input);
ostream& operator<<(ostream& out, const map<U, V>& v) {
                                                                       ostringstream os;
  out << "{";
                                                                       Solution().solve(is, os);
  bool f = false:
                                                                       return os.str();
  for (const auto& p : v) {
    out << (!f ? "" : ", ") << p;
                                                                  };
    f = true:
                                                                   string gen_input(int it) {
                                                                     (void)it;
  return out << "}";</pre>
                                                                     return "10 20";
template<typename T>
ostream& operator<<(ostream& out, const vector<T>& v) {
                                                                   void stress() {
  out << "{";
                                                                     for (int it = 0; it < 1000; ++it) {
  for (int i = 0; i < int(v.size()); ++i)</pre>
                                                                       auto input = gen_input(it);
    out << (i == 0 ? "" : ", ") << v[i];
                                                                       auto brute_out = SolutionStr<Solver>().solve(input);
  return out << "}";</pre>
                                                                       auto sol_out = SolutionStr<Brute>().solve(input);
                                                                       if (sol_out != brute_out) {
}
                                                                         cerr << "WA #" << it << endl;
void cerr_printer(bool start) {}
                                                                         cerr << "input: " << endl;</pre>
template<typename T, typename ... Args>
                                                                         cerr << input << endl;</pre>
void cerr_printer(bool start, const T& x, const Args& ... args) {
                                                                         cerr << "expected: " << brute_out << endl;</pre>
  if (!start) cerr << ", ";
                                                                         cerr << "got: " << sol_out << endl;</pre>
  cerr << x;
                                                                         exit(1);
  cerr_printer(false, args...);
                                                                     cerr << "OK" << endl;</pre>
template<typename ... Args>
void dbg(const char * name, int line, const Args& ... args) {
  cerr << "[" << line << "] (" << name << ") = (";
  cerr_printer(true, args...);
                                                                   int main() {
  cerr << ")" << endl;</pre>
                                                                     #ifdef _DEBUG_TEMICH_
}
                                                                     stress();
                                                                     #endif
#define DBG(...) { dbg(#__VA_ARGS__, __LINE__, __VA_ARGS__); }
                                                                     Solver().solve(cin, cout);
struct Solver {
  void solve(istream& cin, ostream& cout) {
                                                                   1.2. Vector.
    int a, b;
                                                                   struct Vec {
    cin >> a >> b;
    cout << a + b << endl;
                                                                     explicit Vec(LL x = 0, LL y = 0) : x(x), y(y) {}
                                                                     Vec operator+(const Vec& o) const {
};
                                                                       return Vec(x + o.x, y + o.y); }
                                                                     Vec operator-(const Vec& o) const {
struct Brute {
                                                                       return Vec(x - o.x, y - o.y); }
  void solve(istream& cin. ostream& cout) {
                                                                     Vec operator*(const LL p) const {
    int a, b;
                                                                       return Vec(x * p, y * p); }
    cin >> a >> b;
                                                                     double len() const { return sqrt(x * x + y * y); }
    while (b--) ++a:
                                                                     LL cross(const Vec& o) const { return x * o.y - y * o.x; }
    cout << a << endl:
                                                                     LL dot(const Vec& o) const { return x * o.x + y * o.y; }
                                                                     static Vec read(istream& cin) {
};
                                                                       LL x, y;
                                                                       cin >> x >> y;
template <typename Solution>
                                                                       return Vec(x, y);
```

```
const double Pi = acos(-1);
};
                                                                   Complex roots[MAX_N / 2];
bool cmp(Vec a. Vec b) {
  return a.x < b.x \mid | (a.x == b.x \&\& a.y < b.y);
                                                                   int bit_reverse[MAX_N];
bool cw(Vec a, Vec b, Vec c) {
                                                                   void prep() {
  return (b - a).cross(c - b) < 0:
                                                                    bit_reverse[0] = 0:
                                                                     for (int i = 1; i < MAX_N; ++i)
bool ccw(Vec a. Vec b. Vec c) {
                                                                       bit_reverse[i] = (bit_reverse[i >> 1]
  return (b - a).cross(c - b) > 0;
                                                                           | ((i & 1) << MAX_SHIFT)) >> 1;
void convex_hull(vector<Vec> & a) {
                                                                     for (int i = 0; i + i < MAX_N; ++i) {
  if (a.size() == 1) return:
                                                                       double angle = 2 * i * Pi / MAX_N:
  sort(a.begin(), a.end(), &cmp);
                                                                       roots[i] = Complex(cos(angle), sin(angle));
  Vec p1 = a[0], p2 = a.back();
                                                                    }
  vector<Vec> up, down;
                                                                  }
  up.push_back(p1);
  down.push_back(p1);
                                                                   Complex arr[MAX_N];
  for (size_t i=1; i<a.size(); ++i) {</pre>
                                                                   void fft(int k) {
    if (i==a.size()-1 || cw(p1, a[i], p2)) {
                                                                     assert(k <= MAX_SHIFT);</pre>
      while (up.size()>=2
          && !cw(up[up.size()-2], up[up.size()-1], a[i]))
                                                                     const int n = 1 \ll k;
        up.pop_back();
                                                                     for (int i = 0; i < n; ++i) {
      up.push_back (a[i]);
                                                                      int rv = bit_reverse[i] >> (MAX_SHIFT - k);
                                                                       if (rv < i) swap(arr[i], arr[rv]);</pre>
    if (i == a.size()-1 \mid | ccw(p1, a[i], p2)) {
      while (down.size()>=2
          && !ccw(down[down.size()-2],
                                                                     for (int bs = 2; bs \leq n; bs *= 2) {
            down[down.size()-1], a[i]))
                                                                       const int hbs = bs / 2;
        down.pop_back();
                                                                       const int factor = (MAX_N / 2) / hbs;
      down.push_back(a[i]);
                                                                       for (int i = 0; i < n; i += bs) {
    }
                                                                         for (int j = 0; j < hbs; ++j) {
  }
                                                                           auto a = arr[i + j];
                                                                           auto b = arr[i + j + hbs] * roots[factor * j];
  a.clear();
  for (size_t i=0; i<up.size(); ++i)</pre>
                                                                           arr[i + j] = a + b;
    a.push_back(up[i]);
                                                                           arr[i + j + hbs] = a - b;
  for (size_t i=down.size()-2; i>0; --i)
    a.push_back(down[i]);
                                                                      }
}
                                                                    }
                                                                  }
1.3. FFT.
                                                                   const int Base = 100;
struct Complex {
  long double re, im;
                                                                   void square(vector<int>& number) {
  explicit Complex(long double re = 0,
                                                                     int sz = number.size() * 2;
      long double im = 0) : re(re), im(im) {}
                                                                     int k = 1;
  Complex operator+(const Complex& o) const {
    return Complex(re + o.re, im + o.im); }
                                                                       int rsz = 2:
  Complex operator-(const Complex& o) const {
                                                                       while (rsz < sz) {</pre>
    return Complex(re - o.re, im - o.im); }
                                                                        rsz *= 2;
  Complex operator*(const Complex& o) const {
                                                                         ++k:
    return Complex(re * o.re - im * o.im, re * o.im + im * o.re); }
};
                                                                       sz = rsz;
const int MAX_SHIFT = 22:
const int MAX_N
                    = 1 << MAX_SHIFT:
```

```
assert(sz <= MAX_N);
 for (int i = 0: i < sz: ++i)
   arr[i] = Complex(i < number.size() ? number[i] : 0);</pre>
 fft(k):
  for (int i = 0: i < sz: ++i)
   arr[i] = arr[i] * arr[i];
 fft(k):
  reverse(arr + 1, arr + sz);
 number.resize(sz);
 int cr = 0:
 for (int i = 0; i < sz; ++i) {
   number[i] = cr + int(arr[i].re / sz + 0.5);
   cr = number[i] / Base;
   number[i] %= Base;
 while (number.back() == 0) number.pop_back();
1.4. Matrix.
struct Matrix {
 ULL vals[N][N];
 Matrix() {
   for (int i = 0; i < N; ++i)
      fill(vals[i], vals[i] + N, 0);
 ULL* operator[](const int idx) {
    return vals[idx];
 const ULL* operator[](const int idx) const {
    return vals[idx];
 static Matrix Ident() {
   Matrix res:
   for (int i = 0; i < N; ++i)
      res[i][i] = 1;
    return res:
 Matrix operator*(const Matrix& o) const {
   Matrix res:
   for (int i = 0; i < N; ++i) {
      for (int j = 0; j < N; ++j) {
       for (int k = 0; k < N; ++k) {
          res[i][i] += vals[i][k] * o[k][i];
         if (k == 7)
            res[i][j] %= MOD;
```

```
res[i][j] %= MOD;
      }
    }
    return res;
};
1.5. SegmTree.
class SegmTreeSum {
  vector<int> tree;
  int n;
  int get(int v, int l, int r, int L, int R) const {
    if (L > R) return 0;
    if (l == L \&\& r == R) return tree[v];
    int mid = (l + r) / 2;
    int a = get(2 * v + 1, l, mid, L, min(R, mid));
    int b = get(2 * v + 2, mid + 1, r, max(L, mid + 1), R);
    return a + b;
  }
  void set(int v, int l, int r, int pos, int val) {
    if (l == r) {
      tree[pos] = val;
      return;
    }
    int mid = (l + r) / 2;
    if (pos \leftarrow mid) set(2 * v + 1, l, mid, pos, val);
    else set(2 * v + 2, mid + 1, r, pos, val);
    tree[v] = tree[2 * v + 1] + tree[2 * v + 2];
  }
public:
  void init(int n_) {
    n = n_{-};
    tree.assign(4 * n, 0);
  int get(int l, int r) const {
    return get(0, 0, n - 1, l, r);
  void set(int pos, int val) {
    set(0, 0, n - 1, pos, val);
};
class SegmTreeMax {
  vector<Pair> tree:
```

```
vector<int> psh;
int n;
void build(int v, int l, int r, const vector<int>& dp) {
 if (l == r) {
   tree[v] = Pair(dp[l], l);
   return:
 int mid = (l + r) / 2;
 build(2 * v + 1, l, mid, dp);
 build(2 * v + 2, mid + 1, r, dp);
 tree[v] = max(tree[2 * v + 1], tree[2 * v + 2]);
void push(int v, int l, int r) {
 if (l != r) {
   psh[2 * v + 1] += psh[v];
   psh[2 * v + 2] += psh[v];
 tree[v].X += psh[v];
 psh[v] = 0;
Pair getMax(int v, int l, int r, int L, int R) {
 push(v, l, r);
 if (L > R) return Pair(-INF, -INF);
 if (l == L \&\& r == R)
   return tree[v];
 int mid = (l + r) / 2;
 Pair a = getMax(2 * v + 1, l, mid, L, min(R, mid));
 Pair b = getMax(2 * v + 2, mid + 1, r, max(L, mid + 1), R);
 return max(a, b);
void add(int v, int l, int r, int L, int R, int val) {
 push(v, l, r);
 if (L > R) return:
 if (l == L \&\& r == R)  {
   psh[v] += val;
   push(v, l, r);
   return;
 int mid = (l + r) / 2:
 add(2 * v + 1, l, mid, L, min(R, mid), val);
 add(2 * v + 2, mid + 1, r, max(L, mid + 1), R, val);
```

```
tree[v] = max(tree[2 * v + 1], tree[2 * v + 2]);
public:
  void init(const vector<int>& dp) {
    n = dp.size();
    tree.resize(4 * n);
    psh.assign(4 * n, 0);
    build(0, 0, n - 1, dp);
  Pair getMax(int l. int r) {
    return getMax(0, 0, n - 1, l, r);
  }
  void add(int l, int r, int val) {
    add(0, 0, n - 1, l, r, val);
 }
};
1.6. Aho.
struct Matcher {
  static const int LETTERS_COUNT = 'z' - 'a' + 1;
  struct Next {
    int nxt[LETTERS_COUNT];
    Next() { fill(nxt, nxt + LETTERS_COUNT, -1); }
    int& operator[](char c) { return nxt[c - 'a']; }
  };
  vector<Next> next:
  vector<int> link;
  vector<char> p_char;
  vector<int> p;
  vector<int> id;
  void build(const set<string>& strings) {
    int total_size = 0;
    for (const auto& s : strings)
      total_size += s.size();
    next.reserve(total_size);
    link.reserve(total_size);
    p_char.reserve(total_size);
    p.reserve(total_size);
    push();
    int _id = 0:
    for (const auto& s : strings) {
      add(s, _id);
      ++_id;
  }
  void push() {
    next.push_back(Next());
```

```
link.push_back(-1);
                                                                 int get_id(int state) { return id[state]; }
                                                                                                                                 const int MAXN = 500;
 p_char.push_back('#');
                                                               };
                                                                                                                                 int n, g[MAXN][MAXN];
 p.push_back(-1);
                                                                                                                                 int best_cost = 10000000000;
 id.push_back(-1);
                                                               1.7. Suffix Automaton.
                                                                                                                                 vector<int> best_cut;
                                                               struct State {
                                                                                                                                 void mincut() {
                                                                 map<char, int> nxt;
void add(const string& s, int _id) {
                                                                                                                                   vector<int> v[MAXN];
                                                                 int link;
 int state = 0;
                                                                                                                                   for (int i=0; i<n; ++i)
                                                                 int len;
                                                                                                                                     v[i].assign(1, i);
                                                                 bool added:
 for (char c : s) {
                                                                                                                                   int w[MAXN];
                                                                 int cnt;
   int next_state = next[state][c];
                                                                                                                                   bool exist[MAXN], in_a[MAXN];
                                                               };
   if (next_state == -1) {
                                                                                                                                   memset (exist, true, sizeof exist);
      push();
                                                                                                                                   for (int ph=0; ph<n-1; ++ph) {
                                                               State st[N];
      p_char.back() = c;
                                                                                                                                     memset (in_a, false, sizeof in_a);
                                                               int lst;
                                                                                                                                     memset (w, 0, sizeof w);
      p.back() = state;
                                                               int sz;
      next_state = p.size() - 1;
                                                                                                                                     for (int it=0, prev; it<n-ph; ++it) {</pre>
      next[state][c] = next_state;
                                                                                                                                       int sel = -1:
                                                               void init() {
                                                                                                                                       for (int i=0; i<n; ++i)</pre>
                                                                 lst = 0;
                                                                                                                                         if (exist[i] && !in_a[i] && (sel == -1
                                                                 sz = 1:
   state = next_state;
                                                                                                                                               || w[i] > w[sel])
                                                                 st[0].link = -1;
 }
                                                                                                                                           sel = i:
                                                                 st[0].len = 1;
                                                                                                                                       if (it == n-ph-1) {
 id[state] = _id;
                                                                                                                                         if (w[sel] < best_cost)</pre>
                                                                                                                                           best_cost = w[sel], best_cut = v[sel];
                                                               void ext(char c) {
                                                                                                                                         v[prev].insert (v[prev].end(),
                                                                 // cerr << "ext : " << c << endl;
int get_next(int state, char c) {
                                                                                                                                             v[sel].begin(), v[sel].end());
                                                                 int cur = sz++:
 int x = _get_next(state, c);
                                                                                                                                         for (int i=0; i<n; ++i)</pre>
 // cerr << "get next " << state << " " << c << " = " << x << endl;
                                                                                                                                           g[prev][i] = g[i][prev] += g[sel][i];
 return x;
                                                                                                                                         exist[sel] = false;
                                                                                                                                       }
                                                                 for (p = lst; p != -1 \&\& !st[p].nxt.count(c); p = st[p].link)
                                                                                                                                       else {
                                                                   st[p].nxt[c] = cur;
int _get_next(int state, char c) {
                                                                                                                                         in_a[sel] = true;
 if (next[state][c] == -1 \&\& state == 0)
                                                                                                                                         for (int i=0; i<n; ++i)</pre>
                                                                 if (p == -1) {
   return 0;
                                                                                                                                           w[i] += q[sel][i];
                                                                   st[cur].link = 0;
 if (\text{next[state][c]} == -1)
                                                                                                                                         prev = sel;
                                                                 } else {
   next[state][c] = get_next(get_link(state), c);
                                                                   int q = st[p].nxt[c];
 return next[state][c];
                                                                   if (st[p].len + 1 == st[q].len) {
                                                                                                                                  }
                                                                     st[cur].link = q;
                                                                                                                                 }
                                                                   } else {
int get_link(int state) { int x = _get_link(state);
                                                                     int clone = sz++;
 // cerr << "get link " << state << " = " << x << endl;
                                                                                                                                 1.9. Flow.
                                                                     st[clone] = st[q];
 return x;
                                                                     st[clone].len = st[p].len + 1;
                                                                                                                                 struct Edge {
                                                                     st[clone].cnt = st[st[clone].link].cnt;
                                                                                                                                  int u, v, flow, cap;
                                                                                                                                   Edge(): u(0), v(0), flow(0), cap(0) {}
int _get_link(int state) {
                                                                     st[q].link = st[cur].link = clone;
                                                                                                                                   Edge(int u, int v, int c) : u(u), v(v), flow(0), cap(c) {}
 if (state == 0)
                                                                                                                                 };
   return 0;
                                                                     for (; p != -1 \&\& st[p].nxt[c] == q; p = st[p].link)
 if (p[state] == 0)
                                                                       st[p].nxt[c] = clone;
                                                                                                                                 const int N = 666:
   return 0;
                                                                                                                                 const int T = 1111;
                                                                 }
 int& l = link[state];
                                                                                                                                 const int MAXN = N + 2 * T + 100:
 if (l == -1)
   l = get_next(get_link(p[state]), p_char[state]);
                                                                 st[cur].cnt = st[st[cur].link].cnt;
 return l;
                                                                                                                                 vector<int> q[500000]:
                                                                                                                                 vector<Edge> edges;
                                                               1.8. Stoer Wagner.
```

```
int flow, s, t;
                                                                    edges.emplace_back(v, u, 0);
                                                                                                                                      for (int i=1; i<p; ++i) {
int start[MAXN], used[MAXN], dist[MAXN];
                                                                                                                                        rem = (rem * 1ll * rem) % n:
                                                                                                                                        if (rem == n-1) return true:
bool bfs() {
                                                                  int calc(int ss, int tt) {
  memset(start, 0, sizeof(start));
                                                                    //cout << "calc (" << ss << ", " << tt << ")" << endl;
                                                                                                                                      return false;
  memset(dist, -1, sizeof(dist));
                                                                    flow = 0, s = ss, t = tt;
  dist[s] = 0:
                                                                    while (bfs()) {
                                                                      while (int add = dfs(ss)) {
                                                                                                                                    int jacobi (int a, int b)
  aueue<int> a:
                                                                        flow += add:
  q.push(s);
                                                                                                                                      if (a == 0) return 0;
                                                                    }
                                                                                                                                      if (a == 1) return 1;
  while (q.size()) {
                                                                    return flow;
                                                                                                                                      if (a < 0)
    int u = q.front();
                                                                                                                                        if ((b \& 2) == 0)
    q.pop();
                                                                                                                                           return jacobi (-a, b);
                                                                  1.10. Prefix function.
                                                                  vector<int> prefix_function (string s) {
    for (int id : q[u]) {
                                                                                                                                           return - jacobi (-a, b);
                                                                    int n = (int) s.length();
      Edge &e = edges[id];
                                                                                                                                      int a1=a. e=0:
                                                                    vector<int> pi (n);
                                                                                                                                      while ((a1 \& 1) == 0)
      int v = e.v;
                                                                    for (int i=1; i<n; ++i) {</pre>
                                                                                                                                        a1 >>= 1, ++e;
                                                                      int j = pi[i-1];
      if (dist[v] == -1 \&\& e.flow < e.cap) {
                                                                                                                                      int s:
                                                                      while (j > 0 \&\& s[i] != s[j])
        dist[v] = dist[u] + 1;
                                                                                                                                      if ((e \& 1) == 0 || (b \& 7) == 1 || (b \& 7) == 7)
                                                                        j = pi[j-1];
        q.push(v);
                                                                                                                                        s = 1:
                                                                      if (s[i] == s[j]) ++j;
      }
                                                                                                                                      else
                                                                      pi[i] = j;
    }
                                                                                                                                        s = -1:
  }
                                                                                                                                      if ((b \& 3) == 3 \& \& (a1 \& 3) == 3)
                                                                    return pi;
  return dist[t] != -1;
                                                                                                                                        s = -s;
}
                                                                                                                                      if (a1 == 1)
                                                                                                                                        return s;
                                                                  1.11. BPWS.
int dfs(int u, int fl = -1) {
                                                                                                                                      return s * jacobi (b % a1, a1);
                                                                  const int trivial_limit = 50;
  if (fl == -1) memset(used, false, sizeof(used));
                                                                  int p[1000];
  used[u] = true:
                                                                                                                                    bool bpsw (int n) {
                                                                  int gcd (int a, int b) {
  if (u == t) return fl;
                                                                                                                                      if ((int)sgrt(n+0.0) *
                                                                    return a ? qcd (b%a, a) : b;
                                                                                                                                                             (int)sqrt(n+0.0) == n) return false;
  for (int &i = start[u]; i < q[u].size(); ++i) {</pre>
                                                                                                                                      int dd=5;
    int id = g[u][i];
                                                                                                                                      for (;;) {
                                                                  int powmod (int a, int b, int m) {
    Edge &e = edges[id];
                                                                                                                                        int g = gcd (n, abs(dd));
                                                                    int res = 1:
                                                                                                                                        if (1<q && q<n) return false;
    int v = e.v:
                                                                    while (b)
    if (!used[v] \&\& dist[v] == dist[u] + 1 \&\& e.flow < e.cap) {
                                                                                                                                        if (jacobi (dd, n) == -1) break;
                                                                      if (b & 1)
      int can = e.cap - e.flow;
                                                                                                                                        dd = dd < 0 ? -dd + 2 : -dd - 2;
                                                                        res = (res * 1ll * a) % m, --b;
      int df = dfs(v, fl == -1 ? can : min(fl, can));
      if (df > 0) {
                                                                                                                                      int p=1, q=(p*p-dd)/4;
                                                                        a = (a * 111 * a) % m, b >>= 1;
        edges[id ^ 0].flow += df;
                                                                                                                                      int d=n+1, s=0;
                                                                    return res;
        edges[id ^ 1].flow -= df;
                                                                                                                                      while ((d \& 1) == 0)
        return df;
                                                                                                                                        ++s, d>>=1;
                                                                                                                                      long long u=1, v=p, u2m=1, v2m=p, qm=q, qm2=q*2, qkd=q;
      }
                                                                  bool miller_rabin (int n) {
    }
                                                                                                                                      for (int mask=2; mask<=d; mask<<=1) {</pre>
                                                                    int b = 2:
                                                                                                                                        u2m = (u2m * v2m) % n:
                                                                    for (int q; (q = qcd (n, b)) != 1; ++b)
                                                                                                                                        v2m = (v2m * v2m) % n;
  return 0;
                                                                      if (n > q)
                                                                                                                                        while (v2m < gm2) v2m += n;
}
                                                                        return false;
                                                                                                                                        v2m -= am2:
                                                                    int p=0, q=n-1;
void add_edge(int u. int v. int c) {
                                                                                                                                        am = (am * am) % n:
                                                                    while ((q \& 1) == 0)
  //cout << "add (" << u << " " << v << " " << c << ") " << endl;
                                                                                                                                        qm2 = qm * 2;
                                                                      ++p, q >>= 1;
  g[u].push_back(edges.size());
                                                                                                                                        if (d \& mask) {
                                                                    int rem = powmod (b, q, n);
  edges.emplace_back(u, v, c);
                                                                                                                                           long long t1 = (u2m * v) % n,
                                                                    if (rem == 1 | | rem == n-1)
  g[v].push_back(edges.size());
                                                                                                                                                                              t2 = (v2m * u) % n,
                                                                      return true;
```

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Volgograd State Technical University (Bulankin, Nosov, Penskoy)
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```
t3 = (v2m * v) % n,
                                 t4 = (((u2m * u) % n) * dd) % n;
      u = t1 + t2;
      if (u \& 1) u += n;
      u = (u >> 1) % n;
      v = t3 + t4;
      if (v \& 1) v += n;
      v = (v >> 1) % n;
      qkd = (qkd * qm) % n;
  if (u==0 \mid | v==0) return true;
  long long qkd2 = qkd*2;
  for (int r=1; r<s; ++r) {</pre>
    v = (v * v) % n - qkd2;
    if (v < 0) v += n;
    if (v < 0) v += n;
    if (v >= n) v -= n;
    if (v >= n) v -= n;
    if (v == 0) return true;
    if (r < s-1) {
      qkd = (qkd * 1ll * qkd) % n;
      qkd2 = qkd * 2;
  }
  return false;
}
bool prime (int n) {
        // Call for prime check
  for (int i=0; i<trivial_limit && p[i]<n; ++i)</pre>
    if (n % p[i] == 0)
      return false;
  if (p[trivial_limit-1]*p[trivial_limit-1] >= n)
    return true;
  if (!miller_rabin (n))
    return false;
  return bpsw (n);
}
void prime_init() {
        // Call before prime check
  for (int i=2, j=0; j<trivial_limit; ++i) {</pre>
    bool pr = true;
    for (int k=2; k*k<=i; ++k)</pre>
      if (i % k == 0)
        pr = false;
    if (pr)
      p[j++] = i;
```

2. Misc

2.1. Debugging Tips.

- Stack overflow? Recursive DFS on tree that is actually a long path?
- Floating-point numbers
 - Getting NaN? Make sure acos etc. are not getting values out of their range (perhaps 1+eps).
 - Rounding negative numbers?
 - Outputting in scientific notation?
- Wrong Answer?
 - Read the problem statement again!
 - Are multiple test cases being handled correctly? Try repeating the same test case many times.
 - Integer overflow?
 - Think very carefully about boundaries of all input parameters
 - Try out possible edge cases:
 - * $n = 0, n = -1, n = 1, n = 2^{31} 1$ or $n = -2^{31}$
 - * List is empty, or contains a single element
 - * n is even, n is odd
 - * Graph is empty, or contains a single vertex
 - * Graph is a multigraph (loops or multiple edges)
 - * Polygon is concave or non-simple
 - Is initial condition wrong for small cases?
 - Are you sure the algorithm is correct?
 - Explain your solution to someone.
 - Are you using any functions that you don't completely understand? Maybe STL functions?
 - Maybe you (or someone else) should rewrite the solution?
 - Can the input line be empty?
- Run-Time Error?
 - Is it actually Memory Limit Exceeded?

2.2. Solution Ideas.

- Dynamic Programming
 - Parsing CFGs: CYK Algorithm
 - Drop a parameter, recover from others
 - Swap answer and a parameter
 - When grouping: try splitting in two
 - -2^k trick
 - When optimizing
 - * Convex hull optimization
 - $\cdot \operatorname{dp}[i] = \min_{i < i} \{\operatorname{dp}[j] + b[j] \times a[i]\}$
 - $b[j] \geq b[j+1]$
 - · optionally $a[i] \leq a[i+1]$
 - $O(n^2)$ to O(n)
 - * Divide and conquer optimization
 - $dp[i][j] = \min_{k < j} \{dp[i-1][k] + C[k][j]\}$
 - $A[i][j] \leq A[i][j+1]$
 - · $O(kn^2)$ to $O(kn\log n)$
 - · sufficient: $C[a][c] + C[b][d] \le C[a][d] + C[b][c]$, $a \le b \le c \le d$ (QI)
 - * Knuth optimization
 - $dp[i][j] = \min_{i < k < j} \{dp[i][k] + dp[k][j] + C[i][j]\}$
 - $A[i][j-1] \le A[i][j] \le A[i+1][j]$
 - · $O(n^3)$ to $O(n^2)$
 - · sufficient: QI and $C[b][c] \leq C[a][d]$, $a \leq b \leq c \leq d$

- Randomized
- Optimizations
 - Use bitset (/64)
 - Switch order of loops (cache locality)
- Process queries offline
 - Mo's algorithm
- Square-root decomposition
- Precomputation
- Efficient simulation
 - Mo's algorithm
 - Sqrt decomposition
 - Store 2^k jump pointers
- Data structure techniques
 - Sqrt buckets
 - Store 2^k jump pointers
 - -2^k merging trick
- Counting
 - Inclusion-exclusion principle
 - Generating functions
- Graphs
 - Can we model the problem as a graph?
 - Can we use any properties of the graph?
 - Strongly connected components
 - Cycles (or odd cycles)
 - Bipartite (no odd cycles)
 - * Bipartite matching
 - * Hall's marriage theorem
 - * Stable Marriage
 - Cut vertex/bridge
 - Biconnected components
 - Degrees of vertices (odd/even)
 - Trees
 - * Heavy-light decomposition
 - * Centroid decomposition
 - * Least common ancestor
 - * Centers of the tree
 - Eulerian path/circuit
 - Chinese postman problem
 - Topological sort
 - (Min-Cost) Max Flow
 - Min Cut
 - * Maximum Density Subgraph
 - Huffman Coding
 - Min-Cost Arborescence
 - Steiner Tree
 - Kirchoff's matrix tree theorem
 - Prüfer sequences
 - Lovász Toggle
 - Look at the DFS tree (which has no cross-edges)
 - Is the graph a DFA or NFA?
 - * Is it the Synchronizing word problem?
- Mathematics
 - Is the function multiplicative?
 - Look for a pattern
 - Permutations
 - * Consider the cycles of the permutation

- Functions
 - * Sum of piecewise-linear functions is a piecewise-linear function
 - * Sum of convex (concave) functions is convex (concave)
- Modular arithmetic
 - * Chinese Remainder Theorem
 - * Linear Congruence
- Sieve
- System of linear equations
- Values too big to represent?
 - * Compute using the logarithm
 - * Divide everything by some large value
- Linear programming
 - * Is the dual problem easier to solve?
- Can the problem be modeled as a different combinatorial problem? Does that simplify calculations?
- Logic
 - 2-SAT
 - XOR-SAT (Gauss elimination or Bipartite matching)
- Meet in the middle
- Only work with the smaller half $(\log(n))$
- Strings
 - Trie (maybe over something weird, like bits)
 - Suffix array
 - Suffix automaton (+DP?)
 - Aho-Corasick
 - eerTree
 - Work with S + S
- Hashing
- Euler tour, tree to array
- Segment trees
 - Lazy propagation
 - Persistent
 - Implicit
 - Segment tree of X
- Geometry
 - Minkowski sum (of convex sets)
 - Rotating calipers
 - Sweep line (horizontally or vertically?)
 - Sweep angle
 - Convex hull
- Fix a parameter (possibly the answer).
- Are there few distinct values?
- Binary search
- Sliding Window (+ Monotonic Queue)
- Computing a Convolution? Fast Fourier Transform
- Computing a Convolution? Fast Fourier Transform
 Computing a 2D Convolution? FFT on each row, and then on each column
- Exact Cover (+ Algorithm X)
- Cycle-Finding
- What is the smallest set of values that identify the solution? The cycle structure of the permutation? The powers of primes in the factorization?
- Look at the complement problem
 - Minimize something instead of maximizing

 \bullet Greedy

- \bullet Immediately enforce necessary conditions. (All values greater than 0? Initialize them all to 1)
- Add large constant to negative numbers to make them positive
- Counting/Bucket sort

	$C_0 = 1, C_n = \frac{1}{n+1} {2n \choose n} = \sum_{i=0}^{n-1} C_i C_{n-i-1} = \frac{4n-2}{n+1} C_{n-1}$	
	$\begin{bmatrix} 0 \\ 0 \end{bmatrix} = 1, \begin{bmatrix} n \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ n \end{bmatrix} = 0, \begin{bmatrix} n \\ k \end{bmatrix} = (n-1) \begin{bmatrix} n-1 \\ k \end{bmatrix} + \begin{bmatrix} n-1 \\ k-1 \end{bmatrix}$	#perms of n objs with exactly k cycles
Stirling 2nd kind	$\begin{Bmatrix} {n \atop 1} \end{Bmatrix} = \begin{Bmatrix} {n \atop n} \end{Bmatrix} = 1, \begin{Bmatrix} {n \atop k} \end{Bmatrix} = k \begin{Bmatrix} {n-1 \atop k} \end{Bmatrix} + \begin{Bmatrix} {n-1 \atop k-1} \end{Bmatrix}$	#ways to partition n objs into k nonempty sets
Euler	$\left \left\langle {n \atop 0} \right\rangle = \left\langle {n \atop n-1} \right\rangle = 1, \left\langle {n \atop k} \right\rangle = (k+1) \left\langle {n-1 \atop k} \right\rangle + (n-k) \left\langle {n-1 \atop k-1} \right\rangle$	#perms of n objs with exactly k ascents
Euler 2nd Order	$\left \left\langle $	#perms of $1, 1, 2, 2,, n, n$ with exactly k ascents
Bell	$B_1 = 1, B_n = \sum_{k=0}^{n-1} {n \choose k} {n-1 \choose k} = \sum_{k=0}^{n} {n \choose k}$	#partitions of 1 n (Stirling 2nd, no limit on k)

//1-1-1-1-1	n^{n-1}
#labeled rooted trees	10
#labeled unrooted trees	n^{n-2}
#forests of k rooted trees	$\frac{k}{n} \binom{n}{k} n^{n-k}$
$\sum_{i=1}^{n} i^2 = n(n+1)(2n+1)/6$	$\sum_{i=1}^{n} i^3 = n^2(n+1)^2/4$
$!n = n \times !(n-1) + (-1)^n$!n = (n-1)(!(n-1)+!(n-2))
$\sum_{i=1}^{n} \binom{n}{i} F_i = F_{2n}$	$\sum_{i} \binom{n-i}{i} = F_{n+1}$
$\sum_{k=0}^{n} \binom{k}{m} = \binom{n+1}{m+1}$	$x^k = \sum_{i=0}^k i! \begin{Bmatrix} k \\ i \end{Bmatrix} \binom{x}{i} = \sum_{i=0}^k \begin{Bmatrix} k \\ i \end{Bmatrix} \binom{x+i}{k}$
$a \equiv b \pmod{x,y} \Rightarrow a \equiv b \pmod{\operatorname{lcm}(x,y)}$	$\sum_{d n} \phi(d) = n$
$ac \equiv bc \pmod{m} \Rightarrow a \equiv b \pmod{\frac{m}{\gcd(c,m)}}$	$(\sum_{d n} \sigma_0(d))^2 = \sum_{d n} \sigma_0(d)^3$
$p \text{ prime } \Leftrightarrow (p-1)! \equiv -1 \pmod{p}$	$\gcd(n^a - 1, n^b - 1) = n^{\gcd(a,b)} - 1$
$\sigma_x(n) = \prod_{i=0}^r \frac{p_i^{(a_i+1)x} - 1}{p_i^x - 1}$	$\sigma_0(n) = \prod_{i=0}^r (a_i + 1)$
$\sum_{k=0}^{m} (-1)^k \binom{n}{k} = (-1)^m \binom{n-1}{m}$	
$2^{\omega(n)} = O(\sqrt{n})$	$\sum_{i=1}^{n} 2^{\omega(i)} = O(n \log n)$
$d = v_i t + \frac{1}{2} a t^2$	$v_f^2 = v_i^2 + 2ad$
$v_f = v_i + at$	$d = \frac{v_i + v_f}{2}t$

2.3. The Twelvefold Way. Putting n balls into k boxes.

	Balls	same	distinct	same	distinct	
	Boxes	same	same	distinct	distinct	Remarks
	-	$p_k(n)$	$\sum_{i=0}^{k} {n \brace i}$	$\binom{n+k-1}{k-1}$	k^n	$p_k(n)$: #partitions of n into $\leq k$ positive parts
1	$size \ge 1$	p(n,k)	$\binom{n}{k}$	$\binom{n-1}{k-1}$	$k!\binom{n}{k}$	p(n,k): #partitions of n into k positive parts
	$size \leq 1$	$[n \le k]$	$[n \le k]$	$\binom{k}{n}$	$n!\binom{k}{n}$	[cond]: 1 if $cond = true$, else 0

PRACTICE CONTEST CHECKLIST

- How many operations per second? Compare to local machine.
- What is the stack size?
- How to use printf/scanf with long long/long double?
- Are __int128 and __float128 available?
- Does MLE give RTE or MLE as a verdict? What about stack overflow?
- What is RAND_MAX?
- How does the judge handle extra spaces (or missing newlines) in the output?
- Look at documentation for programming languages.
- Try different programming languages: C++, Java and Python.
- Try the submit script.
- Try local programs: i?python[23], factor.
- Try submitting with assert(false) and assert(true).
- Return-value from main.
- Look for directory with sample test cases.
- Make sure printing works.
- Remove this page from the notebook.