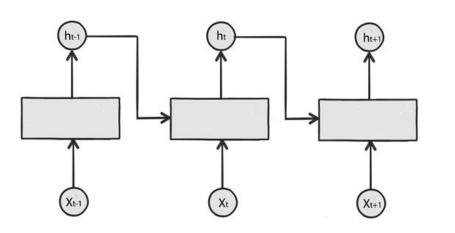
### Вывод алгоритмических закономерностей с помощью Stack RNN

### Рекуррентные нейронные сети (RNN) Basics

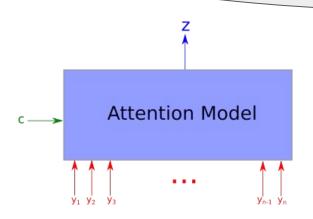


Elman model

$$h_t = \sigma(Ux_t + R_h h_{t-1})$$
  
$$y_t = softmax(Vh_t)$$

# HUNGRY FOR McDonalds Attention

### Рекуррентные нейронные сети (RNN) Attention

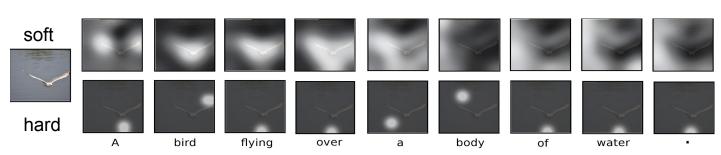


next word = f(image, last word)

$$h_t = f(x, h_{t-1})$$

$$\text{next word} = g(h_t)$$

$$h_t = f(attention(x, h_{t-1}), h_{t-1})$$

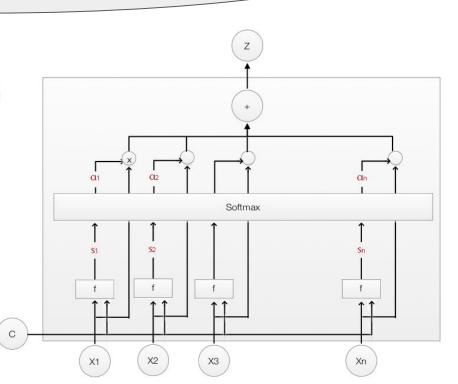


### Рекуррентные нейронные сети (RNN) Soft Attention

$$s_i = anh(W_cC + W_xX_i) = anh(W_ch_{t-1} + W_xx_i)$$

$$lpha_i = softmax(s_1, s_2, \ldots, s_i, \ldots)$$

$$Z = \sum_i lpha_i x_i$$

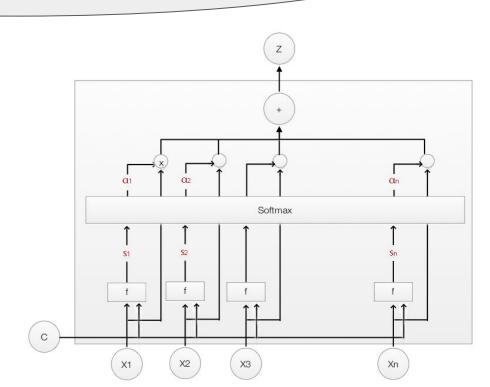


### Рекуррентные нейронные сети (RNN) Soft Attention

Attention as differentiable layer

No sampling

Training with backprop



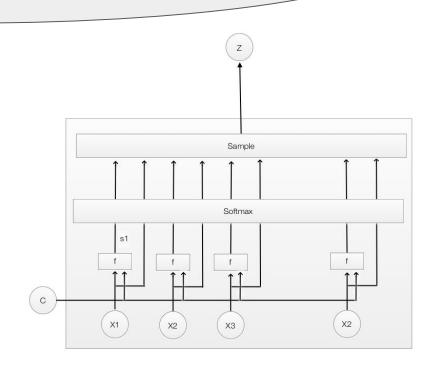
### Рекуррентные нейронные сети (RNN) Hard Attention

Attention as stochastic process; sampling

Supports discrete decisions (number of steps)

Training with REINFORCE

 $Z\sim x_i, lpha_i$ 



### Рекуррентные нейронные сети (RNN) Attention

#### Hard attention

Better results (sometimes?)

More principled

Hard to train



#### Soft attention

Not always applicable

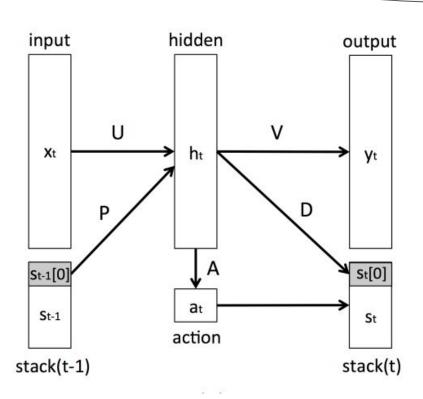
Easy to train

Model	BLEU-1	BLEU-2	BLEU-3	BLEU-4	METEOR
Log Bilinear°	70.8	48.9	34.4	24.3	20.03
Soft-Attention	70.7	49.2	34.4	24.3	23.90
Hard-Attention	71.8	50.4	35.7	25.0	23.04

## Задача

Sequence generator	Example
$\{a^n b^n \mid n > 0\}$	aab <b>ba</b> aab <b>bba</b> baaaaab <b>bbbb</b>
$\{a^nb^nc^n \mid n>0\}$	aaab <b>bbccca</b> b <b>ca</b> aaaab <b>bbbbccccc</b>
$\{a^n b^n c^n d^n \mid n > 0\}$	aab <b>bccdda</b> aab <b>bbcccddda</b> b <b>cd</b>
$\left\{a^n b^{2n} \mid n > 0\right\}$	aab <b>bbba</b> aab <b>bbbbbba</b> b <b>b</b>
$\{a^n b^m c^{n+m} \mid n, m > 0\}$	aabc <b>cca</b> aabbc <b>cccca</b> bc <b>c</b>
$n \in [1, k], X \to nXn, X \to =$	(k=2) 12= <b>21</b> 2122= <b>2212</b> 11121= <b>12111</b>

#### Stack RNN: Концепция



Добавим стек, в котором будем сохранять какие-то сведения о данных и через который будем обновлять скрытые состояния

3 Операции: PUSH, POP и NO-OP

PUSH - добавляет новый элемент на верх стека

РОР - удаляет верхний элемент стека

NO-OP - ничего не делает

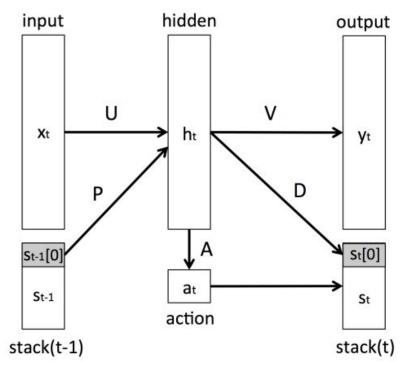
### Stack RNN: Формулы

$$s_t[0] = a_t[\mathrm{PUSH}]\sigma(Dh_t) + a_t[\mathrm{POP}]s_{t-1}[1]$$
 
$$s_t[i] = a_t[\mathrm{PUSH}]s_{t-1}[i-1] + a_t[\mathrm{POP}]s_{t-1}[i+1]$$

$$s_t[0] = a_t[{\tt PUSH}] \sigma(Dh_t) + a_t[{\tt POP}] s_{t-1}[1] + a_t[{\tt NO-OP}] s_{t-1}[0]$$

#### Stack RNN: Формулы

$$a_t = softmax(Ah_t)$$
 
$$h_t = \sigma \left( Ux_t + Rh_{t-1} + Ps_{t-1}^k \right)$$
 
$$s_t[0] = a_t[\text{PUSH}]\sigma(Dh_t) + a_t[\text{POP}]s_{t-1}[1]$$
 
$$y_t = softmax(Vh_t)$$



#### n-Stack RNN

Один стек это не очень круто так как можем делать только одно действие в один момент времени.

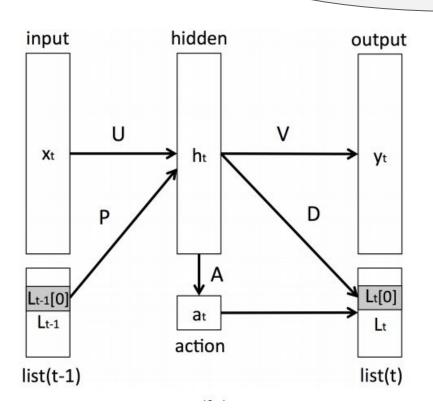
Сделаем несколько

??????

**PROFIT** 



#### List RNN: Концепция



Все то же самое, только теперь вместо стека двусвязный список

3 Операции: LEFT, RIGHT и INSERT и пишущая головка (HEAD)

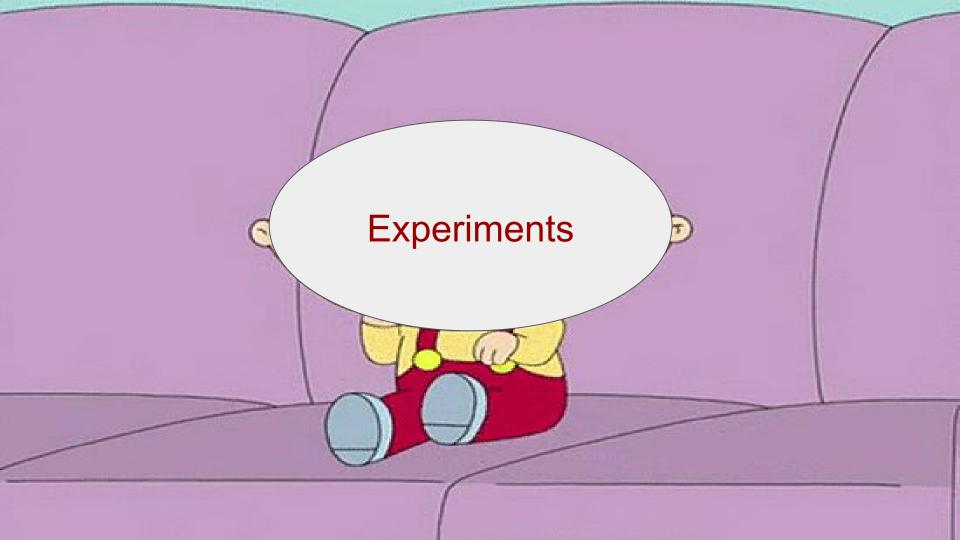
LEFT - сдвинуть HEAD влево

RIGHT - сдвинуть HEAD вправо

INSERT - вставить новый элемент на место HEAD

#### List RNN: Формулы

$$L_t[i] = \begin{cases} a_t[\mathtt{RIGHT}] L_{t-1}[i+1] + a_t[\mathtt{LEFT}] L_{t-1}[i-1] + a_t[\mathtt{INSERT}] \sigma(Dh_t) & \text{if } i = \mathtt{HEAD}, \\ a_t[\mathtt{RIGHT}] L_{t-1}[i+1] + a_t[\mathtt{LEFT}] L_{t-1}[i-1] + a_t[\mathtt{INSERT}] L_{t-1}[i+1] & \text{if } i < \mathtt{HEAD}, \\ a_t[\mathtt{RIGHT}] L_{t-1}[i+1] + a_t[\mathtt{LEFT}] L_{t-1}[i-1] + a_t[\mathtt{INSERT}] L_{t-1}[i] & \text{if } i > \mathtt{HEAD}. \end{cases}$$

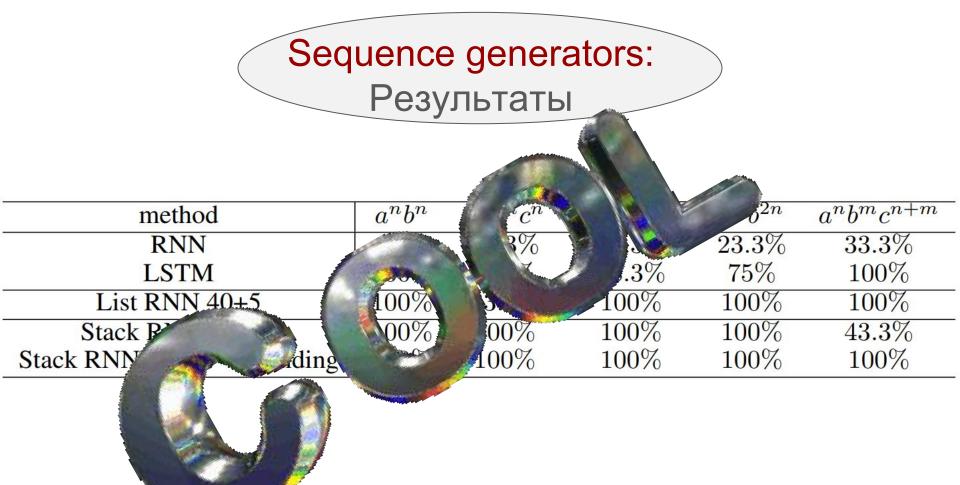


## Sequence generators: Пример

current	next	prediction	proba(next)	act	stack1[top]	stack2[to]	
b	a	a	0.99	POP	POP	-1	0.53
a	a	a	0.99	PUSH	POP	0.01	0.97
a	a	a	0.95	PUSH	PUSH	0.18	0.99
a	a	a	0.93	PUSH	PUSH	0.32	0.98
a	a	a	0.91	PUSH	PUSH	0.40	0.97
a	a	a	0.90	PUSH	PUSH	0.46	0.97
a	b	a	0.10	PUSH	PUSH	0.52	0.97
b	b	b	0.99	PUSH	PUSH	0.57	0.97
b	b	b	1.00	POP	PUSH	0.52	0.56
b	b	b	1.00	POP	PUSH	0.46	0.01
b	b	b	1.00	POP	PUSH	0.40	0.00
b	b	b	1.00	POP	PUSH	0.32	0.00
b	b	b	1.00	POP	PUSH	0.18	0.00
b	b	b	0.99	POP	PUSH	0.01	0.00
b	b	b	0.99	POP	POP	-1	0.00
b	b	b	0.99	POP	POP	-1	0.00
b	b	b	0.99	POP	POP	-1	0.00
b	b	b	0.99	POP	POP	-1	0.01
b	a	a	0.99	POP	POP	-1	0.56

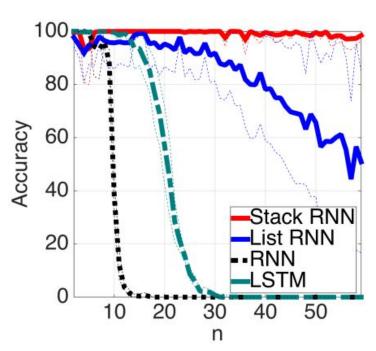
## Sequence generators: Результаты

method	$a^nb^n$	$a^nb^nc^n$	$a^n b^n c^n d^n$	$a^nb^{2n}$	$a^n b^m c^{n+m}$
RNN	25%	23.3%	13.3%	23.3%	33.3%
LSTM	100%	100%	68.3%	75%	100%
List RNN 40+5	100%	33.3%	100%	100%	100%
Stack RNN 40+10	100%	100%	100%	100%	43.3%
Stack RNN 40+10 + rounding	100%	100%	100%	100%	100%
List RNN 40+5 Stack RNN 40+10	100% 100%	33.3% 100%	100% 100%	100% 100%	100% 43.3%

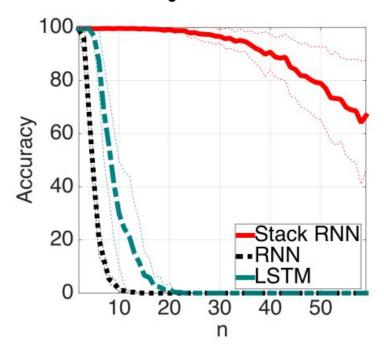


#### Больше Графиков

#### Memorization



### Binary addition



## Binary addition: Пример

Inputs:		1	0	0	0	1	1	+	1	1	1	0	=	1	0	0	0	1	1		
Predictions:	0	0		0	1	0	1	0	1	1	1	1	1	0	0	0	1	1		0	
Stack 1:	0							1					1							0	Counter
Stack 2:	1	-1											1			0				1	End of number 2
Stack 3:	0	0	1	1	1	0	0	0	0	0	0	1	0	0	0	0	0	0	1	0	Number 2
Stack 4:								1	0	0	0	0	0	0	0	1					Length of number 2
Stack 5:	0	1	0	0	0	1	1	0	0	0	0	0	1	0	0	0	0	1	1	0	Carry
Stack 6:			1	0	0	0	1	1					0	1	0	0	0	1	-1		Number 1
Stack 7:																					Junk
Stack 8:																					Junk
Stack 9:																					Junk
Stack 10:																					Junk

