#### Pixel Recurrent Neural Networks

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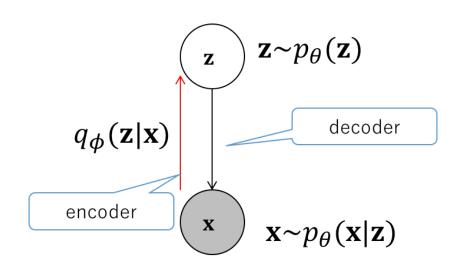
ФКН ВШЭ, 2017

## Генерация естественных изображений

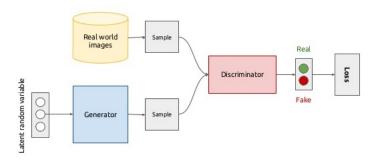
**Цель:** обучить генеративную модель естественных изображений

- ▶ Модели со скрытыми переменными (например, вариационный автокодировщик)
- Adversarial (GAN)
- ightharpoonup Autoregressive (Pixel RNN) моделирование распредедения  $p(X) = \prod_{i=1}^{n^2} p(x_i|x_{i-1},\ldots,x_1)$

## Вариационный автокодировщик

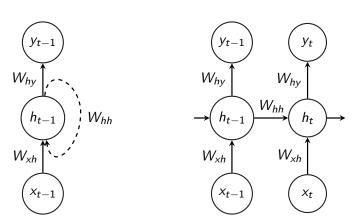


### Generative Adversarial Networks

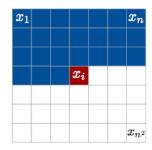


### Recurrent Neural Network

$$h_t = f(W_{hh}h_{t-1} + W_{xh}x_t + b)$$



### Pixel RNN



$$p(X) = \prod_{i=1}^{n^2} p(x_i|x_{i-1}, \dots x_1)$$

$$p(x_{i,R}|\mathbf{x}_{< i})p(x_{i,G}|\mathbf{x}_{< i}, x_{i,R})p(x_{i,B}|\mathbf{x}_{< i}, x_{i,R}, x_{i,G})$$

- ▶ Похоже на language modelling
- Дискретное преставление пискелей (softmax на последнем слое)

## Softmax sampling

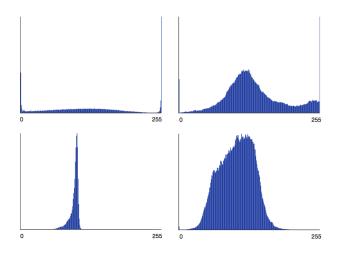


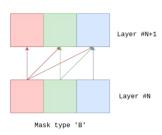
Рис.: Примеры активаций softmax слоя в модели: в модели нет априорных предположений о форме распределения.

## Модели

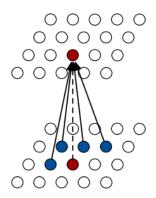
- ► Pixel CNN
  - ▶ Fully convolutional
- ► Pixel RNN
  - Row LSTM
  - ▶ Diagonal Bi-LSTM

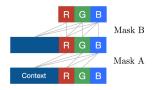
### Masked Convolution

1	1	1	1	1
1	1	1	1	1
1	1	0	0	0
0	0	0	0	0
0	0	0	0	0



### Pixel CNN

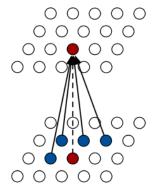




**PixelCNN** 

No pooling layers!

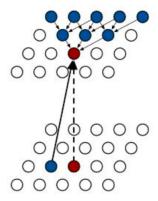
### Pixel CNN



**PixelCNN** 

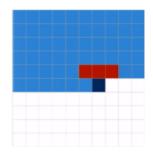
- Предсказание и backbrop через все пиксели одновременно
- Распараллеливание из-за сверток, самая быстрая архитектура из трех
- Фиксированный receptive field :(

### Row LSTM

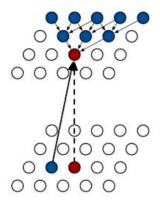


Row LSTM

- ► Recurrent connections
- State is a whole vector
- Convolutional state-to-state mapping

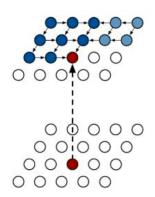


#### Row LSTM

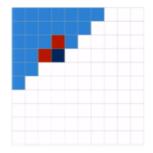


$$\begin{aligned} [\mathbf{o}_i, \mathbf{f}_i, \mathbf{i}_i, \mathbf{g}_i] &= \sigma(\mathbf{K}^{ss} \circledast \mathbf{h}_{i-1} + \mathbf{K}^{is} \circledast \mathbf{x}_i) \\ \mathbf{c}_i &= \mathbf{f}_i \odot \mathbf{c}_{i-1} + \mathbf{i}_i \odot \mathbf{g}_i \\ \mathbf{h}_i &= \mathbf{o}_i \odot \tanh(\mathbf{c}_i) \end{aligned}$$

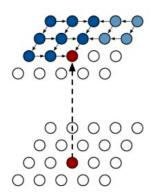
## Diagonal Bi-LSTM

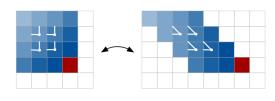


- State progresses diagonally
- Captures entire available context
- Bidirectional: 2 LSTMS (from top left and top right)



# Diagonal Bi-LSTM





$$egin{aligned} [\mathbf{o}_i, \mathbf{f}_i, \mathbf{i}_i, \mathbf{g}_i] &= \sigma(\mathbf{K}^{ss} \circledast \mathbf{h}_{i-1} + \mathbf{K}^{is} \circledast \mathbf{x}_i) \ \mathbf{c}_i &= \mathbf{f}_i \odot \mathbf{c}_{i-1} + \mathbf{i}_i \odot \mathbf{g}_i \ \mathbf{h}_i &= \mathbf{o}_i \odot anh(\mathbf{c}_i) \end{aligned}$$

## Архитекутры

<b>PixelCNN</b>	Row LSTM	Diagonal BiLSTM		
7 × 7 conv mask A				
Multiple residual blocks: (see fig 5)				
Conv $3 \times 3$ mask B	Row LSTM i-s: 3 × 1 mask B s-s: 3 × 1 no mask	Diagonal BiLSTM i-s: $1 \times 1$ mask B s-s: $1 \times 2$ no mask		
ReLU followed by 1 × 1 conv, mask B (2 layers)				
256-way Softmax for each RGB color (Natural images) or Sigmoid (MNIST)				

### Residual blocks

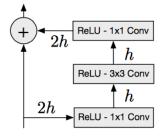


Рис.: Residual block for CNN

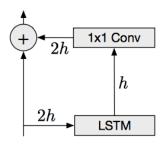


Рис.: Residual block for RNN

## Residuals blocks: experiments

# layers:	1	2	3	6	9	12
NLL:	3.30	3.20	3.17	3.09	3.08	3.06

Puc.: Negative log likelihood evaluated on the CIFAR-10 validation set

	No skip	Skip
No residual:	3.22	3.09
Residual:	3.07	3.06

Рис.: Negative log likelihood evaluated on the CIFAR-10 validation set, 12 layers

## CIFAR-10

Model	NLL Test
DBM 2hl [1]:	≈ 84.62
DBN 2hl [2]:	$\approx 84.55$
NADE [3]:	88.33
EoNADE 2hl (128 orderings) [3]:	85.10
EoNADE-5 2hl (128 orderings) [4]:	84.68
DLGM [5]:	$\approx 86.60$
DLGM 8 leapfrog steps [6]:	$\approx 85.51$
DARN 1hl [7]:	$\approx 84.13$
MADE 2hl (32 masks) [8]:	86.64
DRAW [9]:	$\le 80.97$
PixelCNN:	81.30
Row LSTM:	80.54
Diagonal BiLSTM (1 layer, $h = 32$ ):	80.75
Diagonal BiLSTM (7 layers, $h = 16$ ):	<b>79.20</b>

# Occluded images



## Результаты

- Autoregressive models for image generation
- Use 2D-LSTM (Pixel RNN) and convolutions (Pixel CNN) to model conditional distribution
- Softmax for pixel prediction
- Masked convolutions enforce ordering and model color dependecies
- ► State-of-the art (log-likelihood) for Binary MNIST, CIFAR-10 and realistic generated samples

### Reference

Статья: https://arxiv.org/abs/1601.06759