DATA SCIENCE WITH R

DECISION TREES

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- 1 Introduction
- 2 Decision Trees
 - Basics
 - Example
 - Algorithm
- 3 Building Decision Trees
 - In Rattle
 - In R



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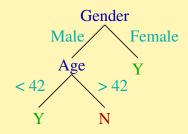
PREDICTIVE MODELLING: CLASSIFICATION

- Goal of classification is to build models (sentences) in a knowledge representation (language) from examples of past decisions.
- The model is to be used on unseen cases to make decisions.
- Often referred to as supervised learning.
- Common approaches: decision trees; neural networks; logistic regression; support vector machines.



LANGUAGE: DECISION TREES

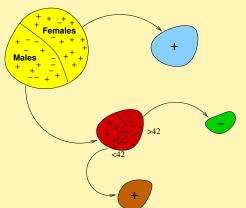
- Knowledge representation: A flow-chart-like tree structure
- Internal nodes denotes a test on a variable
- Branch represents an outcome of the test
- Leaf nodes represent class labels or class distribution





TREE CONSTRUCTION: DIVIDE AND CONQUER

- Decision tree induction is an example of a recursive partitioning algorithm: divide and conquer.
- At start, all the training examples are at the root
- Partition examples recursively based on selected variables





TRAINING DATASET: BUYS COMPUTER?

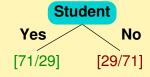
What rule would you "learn" to identify who buys a computer?

Age	Income	Student	Credit	Buys
< 30	High	No	Poor	No
< 30	High	No	Good	Yes
30 - 40	High	No	Poor	Yes
> 40	Medium	No	Poor	Yes
> 40	Low	Yes	Poor	Yes
> 40	Low	Yes	Good	No
30 - 40	Low	Yes	Good	Yes
< 30	Medium	No	Poor	No
< 30	Low	Yes	Poor	No
> 40	Medium	Yes	Poor	Yes
< 30	Medium	Yes	Good	Yes
30 - 40	Medium	No	Good	Yes
30 - 40	High	Yes	Poor	Yes
> 40	Medium	No	Good	No



One possible tree:

Top

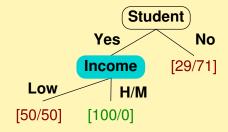


Гор



One possible tree:

Top

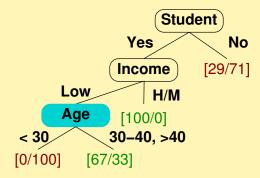


Гор



One possible tree:

Top



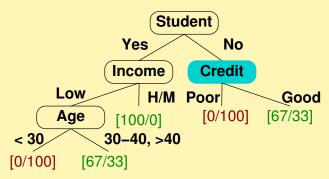
Тор





One possible tree:

Top

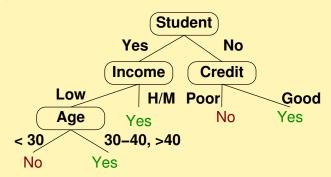


Тор



One possible tree:

Top



Тор



ALGORITHM FOR DECISION TREE INDUCTION

- A greedy algorithm: takes the best immediate (local) decision while building the overall model
- Tree constructed top-down, recursive, divide-and-conquer
- Begin with all training examples at the root
- Data is partitioned recursively based on selected variables
- Select variables on basis of a measure
- Stop partitioning when?
 - All samples for a given node belong to the same class
 - There are no remaining variables for further partitioning majority voting is employed for classifying the leaf
 - There are no samples left



- A random data set may have high entropy:
 - Y is from a uniform distribution
 - a frequency distribution would be flat!
 - a sample will include uniformly random values of Y
- A data set with low entropy:
 - Y's distribution will be very skewed
 - a frequency distribution will have a single peak
 - a sample will predominately contain just Yes or just No
- Work towards reducing the amount of entropy in the data!



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We are trying to predict output Y from input X.

X = Course

Y = Purchase Neo1973

Х	Y
Math	Yes
History	No
CS	Yes
Math	No
Math	No
CS	Yes
History	No
Math	Yes

$$P(Yes) = 0.5$$

 $P(Math) = 0.5$
 $P(Math \& Yes) = 0.25$
 $P(History \& Yes) = 0$



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CS	Yes
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Math	No
CS	Yes
History	No
Math	Yes

Assuming this represents true probabilities:

$$P(Yes) = 0.5$$

 $P(Math) = 0.5$
 $P(Math \& Yes) = 0.25$
 $P(History \& Yes) = 0$



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Math	No
Math	No
CS	Yes
History	No
Math	Yes

Focus on Y

$$P(Yes) = 0.5$$

 $P(No) = 0.5$

$$E(p, n) = -\frac{p}{p+n} \log_2 \frac{p}{p+r} - \frac{n}{p+n} \log_2 \frac{p}{p+r}$$



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Uniform distribution of *Y* Entropy of *Y* is 1

$$E(p,n) = -\frac{p}{p+n} \log_2 \frac{p}{p+n} - \frac{n}{p+n} \log_2 \frac{n}{p+n}$$

 $log_2(0.5) = -1$



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Focus on Y

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History	No
CS	Yes
Math	No
Math	No
CS	Yes
History	No
Math	Yes

Focus on just students of History

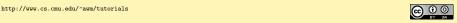
$$P(Yes) = 0$$

 $P(No) = 1$

Skewed distribution of *Y* Entropy of *Y* is 0

$$E(p, n) = -\frac{0}{0+2} \log_2 \frac{0}{0+2} \\ -\frac{2}{0+2} \log_2 \frac{2}{0+2}$$

 $\log_2(0) = -\ln \log_2(1) = 0$



We are trying to predict output Y from input X.

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Math	No
Math	No
CS	Yes
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$$P(Yes) = 0$$

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Skewed distribution of Y Entropy of Y is 0

$$E(p, n) = -\frac{0}{0+2} \log_2 \frac{0}{0+2} \\ -\frac{2}{0+2} \log_2 \frac{2}{0+2}$$

 $log_2(0) = -Inf log_2(1) = 0$



Variable Selection Measure: Entropy

- Information gain (ID3/C4.5)
- Select the variable with the highest information gain
- Assume there are two classes: P and N
- Let the data S contain p elements of class P and n elements of class N
- The amount of information, needed to decide if an arbitrary example in S belongs to P or N is defined as

$$I_E(p,n) = -\frac{p}{p+n} \log_2 \frac{p}{p+n} - \frac{n}{p+n} \log_2 \frac{n}{p+n}$$



VARIABLE SELECTION MEASURE: GINI

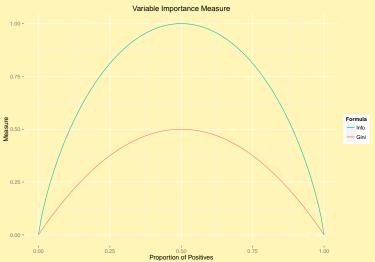
- Gini index of impurity traditional statistical measure CART
- Measure how often a randomly chosen observation is incorrectly classified if it were randomly classified in proportion to the actual classes.
- Calculated as the sum of the probability of each observation being chosen times the probability of incorrect classification, equivalently:

$$I_G(p, n) = 1 - (p^2 + (1 - p)^2)$$

• As with Entropy, the Gini measure is maximal when the classes are equally distributed and minimal when all observations are in one class or the other.



VARIABLE SELECTION MEASURE





Information Gain

- Now use variable A to partition S into v cells: $\{S_1, S_2, \dots, S_v\}$
- If S_i contains p_i examples of P and n_i examples of N, the information now needed to classify objects in all subtrees S_i is:

$$E(A) = \sum_{i=1}^{V} \frac{p_i + n_i}{p + n} I(p_i, n_i)$$

• So, the information gained by branching on A is:

$$Gain(A) = I(p, n) - E(A)$$

So choose the variable A which results in the greatest gain in information.

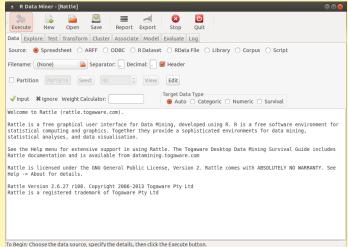


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STARTUP RATTLE

library(rattle) rattle()





LOAD EXAMPLE WEATHER DATASET

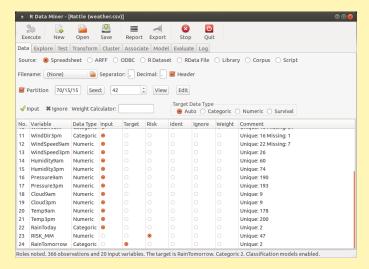
- Click on the Execute button and an example dataset is offered.
- Click on Yes to load the weather dataset.





SUMMARY OF THE WEATHER DATASET

A summary of the weather dataset is displayed.







Model Tab — Decision Tree

• Click on the Model tab to display the modelling options.

● R Data Miner - [Rattle (weather.csv)]			
Execute New Open Save Report Export Stop Quit			
Data Explore Test Transform Cluster Associate Model Evaluate Log			
Type: Forest O Boost O SVM O Linear O Neural Net O Survival O All			
Farget: RainTomorrow Algorithm: Traditional Conditional Model Builder: rpart			
Min Split: 20 \$\dagger\$ Max Depth: 30 \$\dagger\$ Priors:			
Min Bucket: 7 Complexity: 0.0100 Complexity:			
ecision Tree Model			
Decision Tree Model A decision tree model is one of the most common data mining models. It is popular because the resulting model is easy to understand. The algorithms use a recursive partitioning approach. The traditional algorithm is implemented in the rpart package. It is comparable to CART and ID3/C4. The conditional tree algorithm is implemented in the party package. It builds trees in a conditional inference framework. Note that the ensemble approaches (boosting and random forests) tend to produce models that exhibit less bias and variance than a single decision tree.			



BUILD TREE TO PREDICT RAINTOMORROW

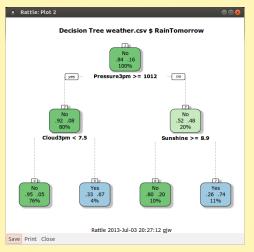
• Decision Tree is the default model type—simply click Execute.

R Data Miner - [Rattle (weather.csv)]	⊜ ⊕ ⊗		
Execute New Open Save Report Export Stop Quit			
Data Explore Test Transform Cluster Associate Model Evaluate Log			
Type: ● Tree ○ Forest ○ Boost ○ SVM ○ Linear ○ Neural Net ◎ Survival ○ All			
Target: RainTomorrow Algorithm: Traditional Conditional	Model Builder: rpart		
Min Split: 20	☐ Include Missing		
Min Bucket: 7 Complexity: 0.0100 \$\times\$ Loss Matrix:	Rules Draw		
Summary of the Decision Tree model for Classification (built using 'rpart'):			
n= 256			
node), split, n, loss, yval, (yprob) * denotes terminal node			
1) root 256 41 No (0.83984375 0.16015625) 2) Pressure3pm=1811.9 264 16 No (0.92156863 0.07843137) 4) Cloud3pm=7.3 159 16 No (0.93817395 0.65128285) * 5) Cloud3pm=7.5 9 3 Yes (0.3333333 0.66666667) * 3) Pressure3pm=1811.9 22 25 No (0.13129377 0.46876923) 6) Sunshinc>8.5 25 5 No (0.88608608 0.28608608) * 7) Sunshinc>8.5 27 7 Yes (0.25925250 6.74674874) *			
<pre>Classification tree: rpart(formula = RainTomorrow ~ ., data = crs\$dataset[crs\$train,</pre>			
Variables actually used in tree construction: [1] Cloud3pm Pressure3pm Sunshine			
Root node error: 41/256 = 0.16016			
The Decision Tree model has been built. Time taken: 0.09 secs			



DECISION TREE PREDICTING RAINTOMORROW

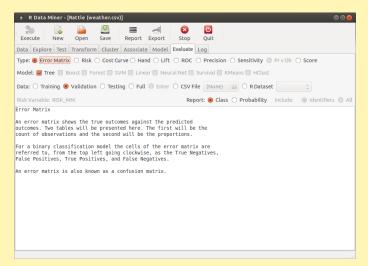
 Click the Draw button to display a tree (Settings → Advanced Graphics).





EVALUATE DECISION TREE

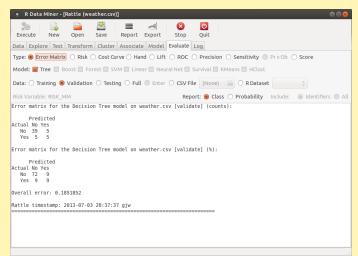
Click Evaluate tab—options to evaluate model performance.





EVALUATE DECISION TREE—ERROR MATRIX

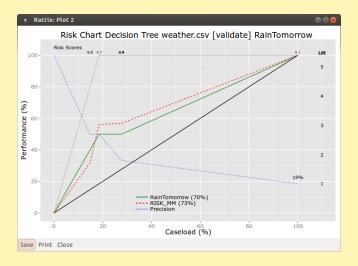
- Click Execute to display simple error matrix.
- Identify the True/False Positives/Negatives.





DECISION TREE RISK CHART

Click the Risk type and then Execute.

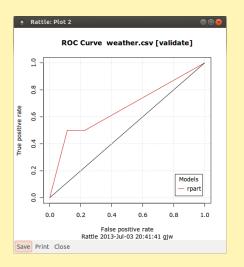






DECISION TREE ROC CURVE

• Click the ROC type and then Execute.

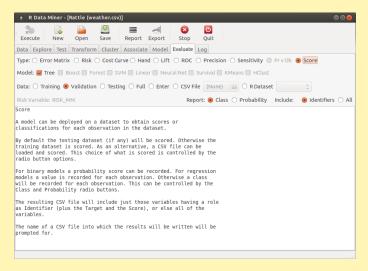






Score a Dataset

Click the Score type to score a new dataset using model.

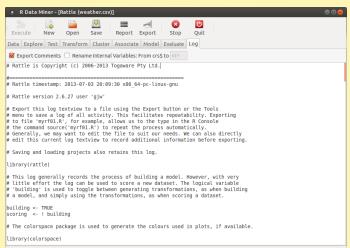






Log of R. Commands

- Click the Log tab for a history of all your interactions.
- Save the log contents as a script to repeat what we did.

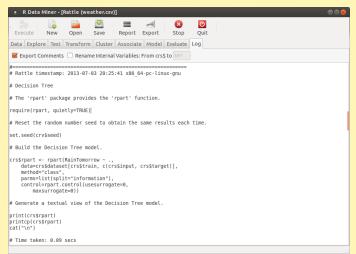






Log of R Commands—rpart()

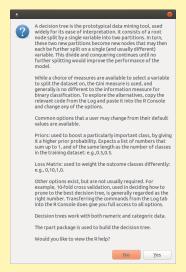
- Here we see the call to rpart() to build the model.
- Click on the Export button to save the script to file.





$\text{Help} \rightarrow \text{Model} \rightarrow \text{Tree}$

Rattle provides some basic help—click Yes for R help.





OVERVIEW

- - Basics
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Weather Dataset - Inputs

```
ds <- weather
head(ds, 4)
```

```
##
        Date Location MinTemp MaxTemp Rainfall Evaporation Sunshine
## 1 2007-11-01 Canberra
                      8.0
                            24.3
                                    0.0
                                              3.4
                                                     6.3
## 2 2007-11-02 Canberra 14.0 26.9 3.6
                                              4.4 9.7
## 3 2007-11-03 Canberra 13.7 23.4 3.6
                                           5.8 3.3
## 4 2007-11-04 Canberra 13.3 15.5 39.8
                                              7.2
                                                     9.1
```

summary(ds[3:5])

```
MinTemp
                  MaxTemp Rainfall
##
##
   Min. :-5.30
                Min. : 7.6 Min. : 0.00
   1st Qu.: 2.30 1st Qu.:15.0 1st Qu.: 0.00
##
##
   Median: 7.45 Median: 19.6 Median: 0.00
   Mean : 7.27 Mean : 20.6 Mean : 1.43
##
```



Weather Dataset - Target

```
target <- "RainTomorrow"</pre>
summary(ds[target])
   RainTomorrow
   No :300
##
## Yes: 66
(form <- formula(paste(target, "~ .")))</pre>
## RainTomorrow ~ .
(vars \leftarrow names(ds)[-c(1, 2, 23)])
    [1] "MinTemp"
                         "MaxTemp"
                                          "Rainfall"
                                                           "Evaporation"
    [5] "Sunshine"
                                          "WindGustSpeed" "WindDir9am"
##
                         "WindGustDir"
    [9] "WindDir3pm"
                         "WindSpeed9am"
                                          "WindSpeed3pm"
                                                           "Humidity9am"
   [13] "Humidity3pm"
                                          "Pressure3pm"
                         "Pressure9am"
                                                           "Cloud9am"
   [17] "Cloud3pm"
                         "Temp9am"
                                          "Temp3pm"
                                                           "RainToday"
   [21] "RainTomorrow"
```



SIMPLE TRAIN/TEST PARADIGM

```
set.seed(1421)
train <- c(sample(1:nrow(ds), 0.70*nrow(ds))) # Training dataset
head(train)
## [1] 288 298 363 107 70 232
length(train)
## [1] 256
test <- setdiff(1:nrow(ds), train)
                                                # Testing dataset
length(test)
## [1] 110
```



DISPLAY THE MODEL

```
model <- rpart(form, ds[train, vars])</pre>
model
## n = 256
##
## node), split, n, loss, yval, (yprob)
         * denotes terminal node
##
##
##
    1) root 256 44 No (0.82812 0.17188)
      2) Humidity3pm< 59.5 214 21 No (0.90187 0.09813)
##
        4) WindGustSpeed< 64 204 14 No (0.93137 0.06863)
##
          8) Cloud3pm< 6.5 163 5 No (0.96933 0.03067) *
##
          9) Cloud3pm>=6.5 41 9 No (0.78049 0.21951)
##
           18) Temp3pm< 26.1 34 4 No (0.88235 0.11765) *
##
           19) Temp3pm>=26.1 7 2 Yes (0.28571 0.71429) *
##
```

• Notice the legend to help interpret the tree.



Performance on Test Dataset

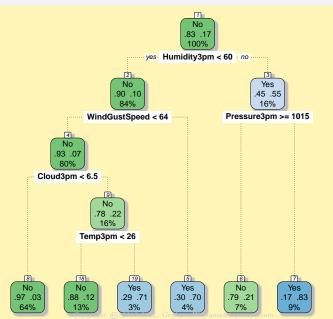
The predict() function is used to score new data.

```
head(predict(model, ds[test,], type="class"))
## 2 4 6 8 11 12
## No No No No No No
## Levels: No Yes

table(predict(model, ds[test,], type="class"), ds[test, target])
##
## No Yes
## No 77 14
## Yes 11 8
```



EXAMPLE DTREE PLOT USING RATTLE





AN R SCRIPTING HINT

- Notice the use of variables ds, target, vars.
- Change these variables, and the remaining script is unchanged.
- Simplifies script writing and reuse of scripts.

```
ds <- iris
target <- "Species"
vars <- names(ds)</pre>
```

• Then repeat the rest of the script, without change.



An R Scripting Hint — Unchanged Code

This code remains the same to build the decision tree.

```
form <- formula(paste(target, "~ ."))</pre>
train <- c(sample(1:nrow(ds), 0.70*nrow(ds)))</pre>
test <- setdiff(1:nrow(ds), train)</pre>
model <- rpart(form, ds[train, vars])</pre>
model
## n = 105
##
## node), split, n, loss, yval, (yprob)
         * denotes terminal node
##
##
   1) root 105 69 setosa (0.34286 0.32381 0.33333)
##
     2) Petal.Length< 2.6 36 0 setosa (1.00000 0.00000 0.00000) *
     3) Petal.Length>=2.6 69 34 virginica (0.00000 0.49275 0.50725)
##
       6) Petal.Length< 4.95 35 2 versicolor (0.00000 0.94286 0.05714) *
##
       7) Petal.Length>=4.95 34 1 virginica (0.00000 0.02941 0.97059) *
##
```





AN R SCRIPTING HINT — UNCHANGED CODE

Similarly for the predictions.

```
head(predict(model, ds[test,], type="class"))
##
                            10
## setosa setosa setosa setosa setosa setosa
## Levels: setosa versicolor virginica
table(predict(model, ds[test,], type="class"), ds[test, target])
##
##
                setosa versicolor virginica
##
                    14
     setosa
                                0
##
     versicolor
                               15
    virginica
##
```



Modelling Framework

Language Tree with single variable tests

Measure Entropy, Gini, . . .

Search Recursive partitioning



SUMMARY

- Decision Tree Induction.
- Most widely deployed machine learning algorithm.
- Simple idea, powerful learner.
- Available in R through the rpart package.



Chapter 11.

Reference Book



Data Mining with Rattle and R Graham Williams 2011, Springer, Use R! ISBN: 978-1-4419-9889-7.



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Chapter 11.

