

# 1.2 Perceptron

## Delta learning perceptron algorithm:

Step 1: Choose  $\eta$ , let  $E = 0$ , Initialize random weights ( $w$ ).

Step 2: Calculate the output of the neural network.

$$y = \text{step}(w(k)^T x(k))$$

Step 3: Update weights using delta law.

$$w_i(k+1) = w_i(k) + \eta(d_i - y_i).x(k)$$

Step 4: Calculate error.

$$E = E + \frac{1}{2} \|d(k) - y(k)\|^2$$

Step 5: if  $k < \text{data\_length}$  then  $k = k+1$ , go to Step 2; If  $k == \text{data\_length}$ , go to Step 6.

Step 6: If  $E == 0$ , end of training; If  $E > 0$ , let  $k=0$ ,  $E=0$  then go to Step 2.

## Delta learning Adaline algorithm:

Step 1: Choose  $\eta$ , let  $E = 0$ , Initialize random weights ( $w$ ).

Step 2: Calculate the output of the neural network.

$$y = w(k)^T x(k)$$

Step 3: Update weights using delta law.

$$w_i(k+1) = w_i(k) + \eta (d_i - y_i) \cdot x(k)$$

Step 4: Calculate error.

$$E = E + \frac{1}{2} \|d(k) - y(k)\|^2$$

Step 5: if  $k < data\_length$  then  $k = k+1$ , go to Step 2; If  $k == data\_length$ , go to Step 6.

Step 6: If  $E < \varepsilon$ , end of training; If  $E \geq \varepsilon$ , let  $k=0$ ,  $E=0$  then go to Step 2.

# 1.3 Multi-Layer Perceptron

## The learning algorithm : Back propagation

Step 1: Choose  $\eta$  , let  $E = 0$ , Initialize random weights ( $w, v$ ).

Step 2: Calculate the output of the neural network.

$$\text{Hidden layer: } net_h(k) = v^T x(k)$$

$$y_h(k) = a_h(net_h(k))$$

$$\text{Output layer: } net_o(k) = w^T y_h(k)$$

$$y(k) = a_o(net_o(k))$$

Step 3: Calculate error.

$$E = E + \frac{1}{2} \|d(k) - y(k)\|^2$$

# 1.3 Multi-Layer Perceptron

## The learning algorithm : Back propagation

Step 4: Update weights of output layer.

$$w_{(:,i)}(k+1) = w_{(:,i)}(k) + \eta \frac{-\partial E}{\partial w_{(:,i)}}, i : 0 \rightarrow output\_number - 1$$

Step 5. Update weights of hidden layer

$$v_{(:,j)}(k+1) = v_{(:,j)}(k) + \eta \frac{-\partial E}{\partial v_{(:,j)}}, j : 0 \rightarrow hidden\_number - 1$$

Step 5: if  $k < data\_length$  then  $k = k+1$ , go to Step 2; If  $k == data\_length$ , go to Step 6.

Step 6: If  $E < \varepsilon$ , end of training cycle; If  $E \geq \varepsilon$ , let  $k=0$ ,  $E=0$  then go to Step 2.

# Learning Algorithm 2: the output of RBF

**Step 1:** - Choose  $\eta$ ,  $E_{\max}$  ;

- Initialize random weights  $w_{iq}$  ( $i = \overline{1, n}; q = \overline{1, l}$ )  
;  $E=0$ .

**Step 2:** Calculate the output of the neural network

$$y_i = \sum_{q=1}^l w_{iq} \varphi_q(x) = \sum_{q=1}^l w_{iq} \exp\left(-\frac{\|x - \mu_q\|^2}{2\sigma_q^2}\right)$$

**Step 3:** Update weights of the output layer

$$w_{iq}(k+1) = w_{iq}(k) + \eta(d_i(k) - y_i(k)) \cdot z_q(k); \quad i = \overline{1, n}; \quad q = \overline{1, l};$$
$$z_q(k) = \exp\left(-\frac{\|x(k) - \mu_q\|^2}{2\sigma_q^2}\right)$$

**Step 4:** Calculate error:

$$E = E + \frac{1}{2} \sum_{i=1}^n (d_i(k) - y_i(k))^2$$

**Step 5:** If  $k < \text{data\_length}$  then  $k = k + 1$ , go to step 2. If  $k = \text{data\_length}$  then go to step 6.

**Step 6:** If  $E < E_{\max}$  then end of training cycle. If  $E \geq E_{\max}$  then lets  $E = 0$ ,  $k = 0$  and go to Step 2.