

Linear equations, inequalities, sets and functions, quadratics

Simplify expressions

Simplify the following expressions as much as possible:¹

a. $(-x^4y^2)^2$

b. $9(3^0)$

c. $(2a^2)(4a^4)$

d. $\frac{x^4}{x^3}$

e. $(-2)^{4-7}$

f. $\left(\frac{1}{27b^3}\right)^{1/3}$

g. $y^7y^6y^5y^4$

h. $\frac{2a/7b}{11b/5a}$

i. $(z^2)^4$

Simplify a (more complex) expression

Simplify the following expression:²

$$(a+b)^2 + (a-b)^2 + 2(a+b)(a-b) - 3a^2$$

Graph sketching

Let the functions $f(x)$ and $g(x)$ be defined for all $x \in \mathbb{R}$ by

$$f(x) = \begin{cases} |x| & \text{if } x < 1 \\ 1 & \text{if } x \geq 1 \end{cases}, \quad g(x) = \begin{cases} x^2 & \text{if } x < 2 \\ 4 & \text{if } x \geq 2 \end{cases}$$

Sketch the graphs of:³

1. $y = f(x)$

2. $y = g(x)$

3. $y = f(g(x))$

4. $y = g(f(x))$

¹Gill 1.1

²Gill 1.2

³Pemberton and Rau problem 3-1

Root finding

Find the roots (solutions) to the following quadratic equations.⁴

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

a. $9x^2 - 3x - 12 = 0$

b. $x^2 - 2x - 16 = 0$

c. $6x^2 - 6x - 6 = 0$

Systems of linear equations

Solve the following systems of equations for their unknown values. If there is no solution, indicate as such.

a. Two unknowns⁵

$$3x - 2y = 18$$

$$5x + 10y = -10$$

b. Three unknowns⁶

$$5x - 2y + 3z = 20$$

$$2x - 4y - 3z = -9$$

$$x + 6y - 8z = 21$$

c. An animal shelter has a total of 350 animals comprised of cats, dogs, and rabbits. If the number of rabbits is 5 less than one-half the number of cats, and there are 20 more cats than dogs, how many of each animal are at the shelter?⁷

Work with sets

Using the sets

$$A = \{2, 3, 7, 9, 13, 16\}$$

$$B = \{x : 4 \leq x \leq 8 \text{ and } x \text{ is an integer}\}$$

$$C = \{x : 2 < x < 25 \text{ and } x \text{ is prime}\}$$

$$D = \{1, 4, 9, 16, 25, \dots\}$$

identify the following:⁸

1. $A \cup B$

2. $(A \cup B) \cap C$

3. $C \cap D$

⁴Gill 1.25

⁵OpenStax Algebra ex 7.1.12

⁶OpenStax Algebra ex 7.2.12

⁷OpenStax Algebra 7.2.54

⁸Grimmer HW1.1