

Assessment Evaluation - POST Math Prefresher - 9/2021 33 possible points

We've just spent a magical week together. This is to see how much stuck from the course and to help you identify areas that could use more attention and development. Do your best. **Note: THERE ARE TWO PAGES!**

Background questions:

Name, discipline and subfield?

Questions

1. Basics

(a) Explain the significance or use of the following symbols:

i. Σ

(b) Solve: (no need to simplify but show steps/work if possible)

i. $5 \leq x - 3$

ii. $-9x - 2 > 3$

iii. $|x - 2| \leq 3$

iv. $2e^{6x} = 18$

v. $e^{x^4} = 1$

vi. $\ln(x^2) = 5$

vii. $\sum_{n=1}^{10} 2 + 5n$

viii. $5!$

ix. $\left(\frac{x^6 y^{-3}}{x^2 y^3}\right)^3$

(c) Factor

i. $m^2 + 3m - 4$

ii. $x^2 + 6x + 9$

iii. $2x^4 - 4x^2$

2. Set Theory

(a) Explain the meaning of the following symbols:

i. \in

ii. \forall

(b) Suppose $A = \{3, 6, 12\}$, $B = \{\text{hat, bulldozer, forklift}\}$ and $C = \{x | x \text{ is a natural number} | x > 3 \text{ and } x < 11\}$

i. What is $A \cup B$?

ii. Write the elements of C

iii. What is $A \cap C$?

iv. What is $A \setminus C$?

3. Functions & Pre-Calculus

- (a) What is a continuous function?
- (b) Draw an increasing function.

(c) What is a tangent line? What does it do?

(d) What is a derivative?

4. Matrix Algebra

- (a) Give an example of a 3×4 matrix
- (b) Consider the following matrices:

$$\mathbf{A} = \begin{bmatrix} 3 & 4 & 1 \\ 0 & 2 & 1 \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} 0 & 1 & 1 \\ 1 & 2 & 4 \end{bmatrix} \quad \mathbf{C} = \begin{bmatrix} 1 & 4 & 1 \\ 0 & 2 & 1 \\ 6 & 2 & 9 \end{bmatrix}$$

- i. Which matrices can be added together? Why?
- ii. Add the matrices from the above response.
- iii. Which matrices can be multiplied together? Why?
- iv. Multiply the matrices from the above response.

5. Calculus

- (a) what is the derivative of 4?
- (b) what is the derivative of $2x$?
- (c) find the derivative of $7m^2 - m + 2$
- (d) calculate the integral $\int_0^5 (x^3 + 0.5x^2 + 5x) dx$
- (e) calculate the integral $\int e^x dx$