

1

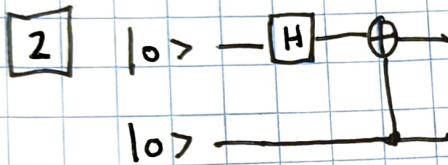
 $H \otimes I$ $\frac{1}{\sqrt{2}}$

$$H: \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \end{bmatrix}$$

$$CNOT: \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

// control
on 2ndNeed Target
on Second

$$|0\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle)$$



WHK

6. Let $f : \{0, 1\}^2 \rightarrow \{0, 1\}$ be a Deutsch-Jozsa oracle function (so f is assumed to be either constant or balanced) with the property that $f(00) = 1$ and $f(11) = 0$. Also suppose a quantum circuit implements f with three wires (as done in class). So the first two wires will accept a bit string s of length two converted to two kets (left to right becomes top to bottom on the wires) and last (bottom wire) is always given input $|0\rangle$. The last wire produces the output ket $|y\rangle$ so that the function takes value $f(s) = y$. Also, suppose that the circuit consists of blocks with combinations of X and CCNOT gates (as done in class) and contains the following block: a single X on the first wire, followed by a CCNOT, followed by an X again on the first wire. This information implies which of the following?

i) f is balanced

ii) $f(01) = 1$

iii) $f(10) = 0$

a) TTF

b) TFT

c) TFF

d) TTT

e) FTT



MAT 399

Quiz 2

Fall 2025

Quiz ID: WHK

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Answers:

1. ☐ b
2. ☐ a
3. ☐ b
4. ☐ c
5. ☐ b
6. ☐ c

Submit electronic answers at

<http://azrael.digipen.edu/cgi-bin/MAT399quiz.pl>