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    Help
#include <stdlib.h>
#include "dup1d_std.h"

#if 0 /* Unused */
static double
Call_OrnsteinUhlenbeck(double s,double k,double t,double r,
    double divid,
    double sigma)

{
    double v,y1,y2,val;

    v=sigma*sqrt((exp(-2*divid*t)-(exp(-2*r*t)))/(2.*(r-divid
    )));
    y1=(s*exp(-divid*t)-k*exp(-r*t))/v;
    y2=(-s*exp(-divid*t)-k*exp(-r*t))/v;

    /*Price*/
    val=(s*exp(-divid*t)-k*exp(-r*t))*cdf_nor(y1)+
        (s*exp(-divid*t)+exp(-r*t)*k)*cdf_nor(y2)+
        v*(pn1_normal_density(y1)-pn1_normal_density(y2));

    /* printf("%f\n", (exp(-divid*t))*N(y2)); */

    return val;
}
#endif

/*tridiagonal matrices*/
struct tridiag{
    int size;
    double *subdiag; /*size-1*/
    double *diag;    /*size*/
    double *updiag;  /*size-1*/
};

/*bidiagonal matrices*/
struct bidiag{
    int size;
    double *subdiag; /*size-1*/

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    double *diag;    /*size*/
};

/*tridiagonal system Tx=b */
struct tridiagSystem{
    int size;
    struct tridiag *T;
    double *b;
};

/*bidiagonal system Tx=b */
struct bidiagSystem{
    int size;
    struct bidiag *T;
    double *b;
};

/*equals the tridiag matrix B to the tridiag matrix A when
they already have the same size*/
static void affectOperator(struct tridiag *A, struct tridia
g *B){

    int i;

    for (i=0;i<=B->size-2;i++){
        B->subdiag[i] = A->subdiag[i];
        B->diag[i] = A->diag[i];
        B->updiag[i] = A->updiag[i];
    }
    B->diag[B->size-1] = A->diag[B->size-1];

}

static int find_index(double x, double *grid, int size,
    int start){
    /* OUTPUT
    - returns the index i such that grid[i]<=x<grid[i+1]
    INPUT
    - x (x = y or T)
    - grid = grid of discretized values of x, grid = x_0,..

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    ..,x_n (x = y or T)
    - size = size of grid - 1 (M for T_grid, N for y_grid)
    - start = index at which we start the search of i */

int k;

if (grid[size] <= x)
    return size-1;
else{
    k=start;
    while (k<size && grid[k]<=x)
        k++;
    return k-1;
}
}

/*changes the tridiagonal system to a triangular system*/
static void tridiagToBidiagSyst(struct bidiagSystem *U,
    struct tridiagSystem *S){

    int size,i;

    size = S->size;
    U->T->diag[size-1] = S->T->diag[size-1];
    U->b[size-1] = S->b[size-1];

    for (i=size-2;i>=0;i--){
        U->T->diag[i] = S->T->diag[i] - S->T->updiag[i]*S->T->
            subdiag[i]/(U->T->diag[i+1]);
        U->b[i] = S->b[i] - S->T->updiag[i]*U->b[i+1]/(U->T->
            diag[i+1]);
        U->T->subdiag[i] = S->T->subdiag[i];
    }

}

/*changes a tridiagonal matrix to a bidiagonal one*/
#if 0
static void tridiagToBidiagMat(struct bidiag *B, struct tri

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        diag *T)
{
    int size,i;
    size = T->size;
    B->diag[size-1] = T->diag[size-1];

    for (i=size-2;i>=0;i--){
        B->diag[i] = T->diag[i] - T->updiag[i]*T->subdiag[i]/(
            B->diag[i+1]);
        B->subdiag[i] = T->subdiag[i];
    }
}
#endif

/*solves the bidiagonal system at each time step*/
static void solveSyst(double *sol, struct bidiagSystem *S){

    int size,i;

    size = S->size;
    sol[0] = (S->b)[0]/(S->T->diag[0]);

    for (i=1;i<=size-1;i++){
        sol[i] = (S->b[i] - S->T->subdiag[i-1]*sol[i-1])/(S->T->diag[i]);
    }

}

#if 0 /* Unused */
static void tridiagMatrixInv(double **inv, struct tridiag *
    T){

    struct bidiagSystem *U;
    struct tridiagSystem *V;
    double *x_j;
    int i,j,size;

    size = T->size;

    /*memory allocation */

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/* memory allocation for the tridiagonal system V*/
V = malloc(sizeof(struct tridiagSystem));
V->T = malloc(sizeof(struct tridiag));
V->T->size = size;
V->T->subdiag = malloc((size-1)*sizeof(double));
V->T->diag = malloc(size*sizeof(double));
V->T->updiag = malloc((size-1)*sizeof(double));
V->b = malloc(size*sizeof(double));
V->size = size;

/* memory allocation for the bidiagonal system U*/
U = malloc(sizeof(struct bidiagSystem));
U->T = malloc(sizeof(struct bidiag));
U->T->subdiag = malloc((size-1)*sizeof(double));
U->T->diag = malloc(size*sizeof(double));
U->T->size = size;
U->b = malloc(size*sizeof(double));
U->size = size;

/*memory alloc for x_j*/
x_j = malloc(size*sizeof(double));

/*initialization of V->T*/
affectOperator(T,V->T);

for (j=0;j<size;j++){
    /*initialisation of V->b */
    for(i=0;i<j;i++)
        V->b[i] = 0;
    V->b[j] = 1;
    for(i=j+1;i<size;i++)
        V->b[i] = 0;
    /*computation of the jth column of the inverse */
    tridiagToBidiagSyst(U,V);
    solveSyst(x_j,U);
    for (i=0;i<size;i++){
        inv[i][j] = x_j[i];
    }
}

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/* memory desallocation */
free(V->T->subdiag);
V->T->subdiag = NULL;
free(V->T->diag);
V->T->diag = NULL;
free(V->T->updiag);
V->T->subdiag = NULL;
free(V->T);
V->T = NULL;
free(V->b);
V->b = NULL;
free(V);
V = NULL;

free(U->T->subdiag);
U->T->subdiag = NULL;
free(U->T->diag);
U->T->diag = NULL;
free(U->T);
U->T = NULL;
free(U->b);
U->b = NULL;
free(U);
U = NULL;

free(x_j);
x_j = NULL;
}
#endif

#if 0 /* Unused */
static void tridiagMatMult(double **res, struct tridiag *A,
    double **B){
    /* res = B*A */
    int i,j,size;

    size = A->size;
    for (i=0;i<size;i++){
        res[i][0] = A->diag[0]*B[i][0] + A->subdiag[0]*B[i][1];

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    for (j=1;j<size-1;j++)
        res[i][j] = A->updiag[j-1]*B[i][j-1] + A->diag[j]*B[
i][j] + A->subdiag[j]*B[i][j+1];
    res[i][size-1] = A->updiag[size-2]*B[i][size-2] + A->
diag[size-1]*B[i][size-1];
}
}
#endif

static void discretizeSigma(double (*volatility)(double,
double,int), double **sigmaCoarseGrid, int n, int m, double *y_
coarseGrid, double *T_coarseGrid,int sigma_type){
/* OUTPUT
- sigmaCoarseGrid = coarse grid of discretized values
of sigma
INPUTS
- volatility = function defining the volatility
- n,m = size of the coarse grid
- y_coarseGrid = array of dicretized values y (for th
e coarse grid)
- T_coarseGrid = array of dicretized values T (for th
e coarse grid) */

int i,j;

for (i=0;i<=n;i++)
    for(j=0;j<=m;j++)
        sigmaCoarseGrid[i][j] = volatility(T_coarseGrid[j],
exp(y_coarseGrid[i]),sigma_type);

}

static double invtanh(double x, double a, double b){
/*fonction invtanh (inverse de a*tanh(y-b)) */
/* returns y so that a*tanh(y-b) = x          */
return b+.5*log((a+x)/(a-x));
}

static void buildFineGrid(double *y_fineGrid, double *T_
fineGrid, int N, int M, double t_0, double T_max, double y_mi

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    n, double y_max, double S_0, int gridType){
/* builds the arrays of discretized values of y and T for the fine grid
   OUTPUTS:
   - y_fineGrid = array of discretized values of y for the fine grid
   - T_fineGrid = array of discretized values of y for the fine grid
   - (N,M) = size of the fine grid
   - t_0 = time origin
   - T_max = time horizon
   - y_min = log(S_min)
   - y_max = log(S_max)
   - gridType = type of the y_fineGrid (0 for regular, 1 for tanh)
*/

double K,H, valInvTanh;
int i,l;

K = (T_max-t_0)/M; /* size of time step*/
for (i=0;i<M+1;i++)
    T_fineGrid[i] = t_0+K*i;

/* steps for the fine grid : */
H = (y_max-y_min)/N;

for (i=0;i<N+1;i++)
    y_fineGrid[i] = y_min+H*i;

if (gridType){ /* tanh grid */
    i=1;
    valInvTanh = invtanh(y_min+H,y_max,log(S_0));
    while (i<N && valInvTanh <= y_min){
        i = i+1;
        valInvTanh = invtanh(y_min+i*H,y_max,log(S_0));
    }
}

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/* the i first values (from 0 to i-1) of invtanh(y_min+
i*H,y_max,log(S_0)) */
/* are below y_min so for the i first values of y_tanh
Grid[.], we do a uniform */
/* discretization so that y_coarseGrid[0] = y_min
*/
for (l=i-1;l>=0;l--)
    y_fineGrid[l] = valInvtanh - (i-l)*(valInvtanh - y_min)/i;

while (i<N && valInvtanh < y_max){
    y_fineGrid[i] = valInvtanh;
    i = i+1;
    valInvtanh = invtanh(y_min+i*H,y_max,log(S_0));
}
/* once the image of y_min+i*H is greater than y_max,
we do a uniform */
/* discretization until N, so that y_coarseGrid[N] =
y_max */
for (l=i;l<=N;l++)
    y_fineGrid[l] = y_fineGrid[i-1] + (l-i+1)*(y_max -
y_fineGrid[i-1])/(N-i+1);

}

}

static double f(int optionType, double y, double S_0){
    /* condition for T=t_0
    OUTPUT :
    - returns f(y,S_0) (condition for T=t_0
    INPUTS :
    - optionType = 1 for a call, 0 for a put
    - y : log of the price of the asset
    - S_0 : price of the asset at t_0 */

    if (optionType==1)
        return (S_0-exp(y)>=0) ? S_0-exp(y) : 0;
    else

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    return (exp(y)-S_0>=0) ? exp(y)-S_0 : 0;
}

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static void buildOperator(struct tridiag *A, double r,
    double q, double S_0, int j, int N, double **sigmaFineGrid,
    double *y_fineGrid){
/*  builds the discretized operator A
    OUTPUT:
    - A : discretized operator (tridiagonal matrix) of size N-1
    INPUTS:
    - r : RF rate
    - q : dividends
    - S_0 : price of the asset at t_0
    - j : index of time step
    - N : number of space (price) steps for the fine grid
    - sigmaFineGrid : fine grid of the values of sigma
    - y_fineGrid : discretized values of y (for the fine grid) */

double x,h_i,h_i_1;
int i;

i=1;
h_i = y_fineGrid[i+1]- y_fineGrid[i];
h_i_1 = y_fineGrid[i] - y_fineGrid[i-1];
x = .5*(r-q+pow(sigmaFineGrid[i][j],2)/2);
A->diag[i-1] = pow(sigmaFineGrid[i][j],2)/(h_i+h_i_1)*(1/
    h_i + 1/h_i_1) + x*(1/h_i_1 - 1/h_i) + q;
A->updiag[i-1] = x/h_i - pow(sigmaFineGrid[i][j],2)/((h_i+h_i_1)*h_i);
for (i=2;i<=N-2;i++){
    h_i = y_fineGrid[i+1]- y_fineGrid[i];
    h_i_1 = y_fineGrid[i] - y_fineGrid[i-1];
    x = .5*(r-q+pow(sigmaFineGrid[i][j],2)/2);
    A->subdiag[i-2] = -x/h_i_1 - pow(sigmaFineGrid[i][j],2)/((h_i+h_i_1)*h_i_1);
    A->diag[i-1] = pow(sigmaFineGrid[i][j],2)/(h_i+h_i_1)*(
        1/h_i + 1/h_i_1) + x*(1/h_i_1 - 1/h_i) + q;
}

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    A->updiag[i-1] = x/h_i - pow(sigmaFineGrid[i][j],2)/((
    h_i+h_i_1)*h_i);
}

/* i=N-1 */
h_i = y_fineGrid[N]- y_fineGrid[N-1];
h_i_1 = y_fineGrid[N-1] - y_fineGrid[N-2];
x = .5*(r-q+pow(sigmaFineGrid[N-1][j],2)/2);
A->subdiag[N-3] = -x/h_i_1 - pow(sigmaFineGrid[N-1][j],2)
/((h_i+h_i_1)*h_i_1);
A->diag[N-2] = pow(sigmaFineGrid[N-1][j],2)/(h_i+h_i_1)*
(1/h_i + 1/h_i_1) + x*(1/h_i_1 - 1/h_i) + q;
}

static void buildTridiagSystem(int optionType, struct tri
diagSystem *S, struct tridiag *A, struct tridiag *A_prev,
double *u_prev, double k, double theta, double condLim){
/* builds the data of the tridiagonal system S (Mat*X =
b, with Mat tridiagonal matrix, b right hand side vector)

    OUTPUT:
    - S : tridiagonal system
    INPUTS:
    - optionType: type of the option (1 for call, 0 for
put)
    - A : current discretized operator

    - A_prev : previous discretized operator

    - u_prev : vector of prices computed in the previous
iteration
    - k : size of time step

    - theta : parameter of the finite difference scheme

    - condLim : limit condition (depending on the time of
the option) */

int size,i;

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size = A->size;

S->b[0] = (1-theta*k*A_prev->diag[0])*u_prev[0] - theta*
    k*A_prev->updiag[0]*u_prev[1];

if (optionType == 1) /* call option */
    S->b[0] = S->b[0] + condLim;

S->T->subdiag[0] = (1-theta)*k*A->subdiag[0];
S->T->diag[0] = 1+(1-theta)*k*A->diag[0];
S->T->updiag[0] = (1-theta)*k*A->updiag[0];

for (i=1;i<size-1;i++){
    S->b[i] = (-theta*k*A_prev->subdiag[i-1])*u_prev[i-1] +
        (1-theta*k*A_prev->diag[i])*u_prev[i] - theta*k*(A_prev->
        updiag[i])*u_prev[i+1];
    S->T->subdiag[i] = (1-theta)*k*A->subdiag[i];
    S->T->diag[i] = 1+(1-theta)*k*A->diag[i];
    S->T->updiag[i] = (1-theta)*k*A->updiag[i];
}

S->T->diag[size-1] = 1+(1-theta)*k*A->diag[size-1];
S->b[size-1] = -theta*k*A_prev->subdiag[size-2]*u_prev[si
    ze-2] + (1-theta*k*A_prev->diag[size-1])*u_prev[size-1];
if (optionType == 0) /*put option*/
    S->b[size-1] = S->b[size-1] + condLim;
}

static void solve(int optionType, double **res, double S_0,
    int N, int M, double r, double q, double theta, double (*
    f)(int,double,double), double **sigmaFineGrid, double *y_
    fineGrid, double *T_fineGrid){
/* solves the EDP using the finite difference method
    OUTPUT :
    - res : fine grid of prices to be computed (size N*M)
    INPUTS :
    - optionType : type of the option (1 for call, 0 for
    put)
    - S_0 : price of the asset at t_0

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- N : number of space steps of the fine grid

- M : number of time steps of the fine grid

- r : RF rate

- q : dividends

- theta : parameter of the finite difference scheme

- sigma : fine grid of values of sigma

- y_fineGrid : discretized values of y (for the fine
grid)
- T_fineGrid : discretized values of t (for the fine
grid)      */

/* declarations */
double *u_prev,*u_next;
int i,j;
struct tridiag *op, *op_prev;
struct tridiagSystem *S1;
struct bidiagSystem *S2;
double x,h_0,h_1,alpha,alpha2,gamma,gamma2,condLim,k;
double t_0,y_min,y_max;

y_min = y_fineGrid[0];
y_max = y_fineGrid[N];
t_0 = T_fineGrid[0];

/* memory allocation for the operator (of type struct tri
diag *) */
op = malloc(sizeof(struct tridiag));
op->subdiag = malloc((N-2)*sizeof(double));
op->diag = malloc((N-1)*sizeof(double));
op->updiag = malloc((N-2)*sizeof(double));
op->size = N-1;

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/* memory allocation for the operator (of type struct tri
   diag *) */
op_prev = malloc(sizeof(struct tridiag));
op_prev->subdiag = malloc((N-2)*sizeof(double));
op_prev->diag = malloc((N-1)*sizeof(double));
op_prev->updiag = malloc((N-2)*sizeof(double));
op_prev->size = N-1;

/* memory allocation for the tridiagonal system S1*/
S1 = malloc(sizeof(struct tridiagSystem));
S1->T = malloc(sizeof(struct tridiag));
S1->T->subdiag = malloc((N-2)*sizeof(double));
S1->T->diag = malloc((N-1)*sizeof(double));
S1->T->updiag = malloc((N-2)*sizeof(double));
S1->T->size = N-1;
S1->b = malloc((N-1)*sizeof(double));
S1->size = N-1;

/* memory allocation for the bidiagonal system S2*/
S2 = malloc(sizeof(struct bidiagSystem));
S2->T = malloc(sizeof(struct bidiag));
S2->T->subdiag = malloc((N-2)*sizeof(double));
S2->T->diag = malloc((N-1)*sizeof(double));
S2->T->size = N-1;
S2->b = malloc((N-1)*sizeof(double));
S2->size = N-1;

/* memory allocation for u_prev and u_next */
u_prev = malloc((N-1)*sizeof(double));
u_next = malloc((N-1)*sizeof(double));

/* initialization of u */

if (optionType == 1)
    res[0][0] = S_0;
else
    res[0][0] = 0;

for (i=1;i<N;i++){

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    u_prev[i-1] = f(optionType,y_fineGrid[i],S_0);
    res[i][0] = u_prev[i-1];
}
res[N][0] = f(optionType,y_max,S_0);

/*builds the initial discretized operator*/
buildOperator(op_prev,r,q,S_0,0,N,sigmaFineGrid,y_fine
Grid);
for (j=1;j<=M;j++){
    buildOperator(op,r,q,S_0,j,N,sigmaFineGrid,y_fineGrid);
    /*builds the discretized operator*/
    /* initial condition for y=y_min*/
    h_0 = y_fineGrid[1]-y_fineGrid[0];
    h_1 = y_fineGrid[2]-y_fineGrid[1];
    k = T_fineGrid[j]-T_fineGrid[j-1];
    x = .5*(r-q+pow(sigmaFineGrid[1][j-1],2)/2);
    alpha = -x/h_0 - pow(sigmaFineGrid[1][j-1],2)/((h_1+h_0)
)*h_0);
    gamma = x/h_0 - pow(sigmaFineGrid[1][j-1],2)/((h_1+h_0)
)*h_0);
    x = .5*(r-q+pow(sigmaFineGrid[1][j],2)/2);
    alpha2 = -x/h_0 - pow(sigmaFineGrid[1][j],2)/((h_1+h_0)
)*h_0);
    gamma2 = x/h_0 - pow(sigmaFineGrid[1][j],2)/((h_1+h_0)
)*h_0);
    if (optionType==1) /*call*/
        condLim = - S_0*k*(theta*alpha*exp(-q*(T_fineGrid[j-1]
]-t_0)) + (1-theta)*alpha2*exp(-q*(T_fineGrid[j]-t_0)))+
exp(y_min)*k*(theta*alpha*exp(-r*(T_fineGrid[j-1]-t_0)) + (1
-theta)*alpha2*exp(-r*(T_fineGrid[j]-t_0)));
    else /*put*/
        condLim = - k*theta*gamma*(-S_0*exp(-q*(T_fineGrid[j-1]
]-t_0))+exp(y_max)*exp(-r*(T_fineGrid[j-1]-t_0))) + k*(1-
theta)*gamma2*(-S_0*exp(-q*(T_fineGrid[j]-t_0))+exp(y_max)*
exp(-r*(T_fineGrid[j]-t_0)));

buildTridiagSystem(optionType,S1,op,op_prev,u_prev,k,th
eta,condLim); /*builds the tridiagonal system*/

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tridiagToBidiagSyst(S2,S1); /* changes the tridiag sy
stem to a bidiagonal one */
solveSyst(u_next,S2); /* solves the bidiagonal system*/

/*we update u_prev and stock the results in the matrix
res */
if (optionType == 1){ /*call*/
    res[0][j] = S_0*exp(-q*(T_fineGrid[j]-t_0)); /* = limit condition for
    res[N][j] = 0; /* = limit condition for y = y_max fo
    r a call option*/
}else{
    res[0][j] = 0; /* = limit condition for y = y_min for
    a put option*/
    res[N][j] = -S_0*exp(-q*(T_fineGrid[j]-t_0))+exp(y_
    max)*exp(-r*(T_fineGrid[j]-t_0)); /* = limit condition for
    y = y_max for a put option*/
}

for (i=1;i<N;i++){
    res[i][j] = u_next[i-1];
    u_prev[i-1] = u_next[i-1];
}

/* update of op_prev */
affectOperator(op,op_prev);

}

/*free memory space*/
free(S1->T->subdiag);
free(S1->T->diag);
free(S1->T->updiag);
free(S1->T);
free(S1->b);
free(S1);

free(S2->T->subdiag);
free(S2->T->diag);

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    free(S2->T);
    free(S2->b);
    free(S2);

    free(op->subdiag);
    free(op->diag);
    free(op->updiag);
    free(op);

    free(op_prev->subdiag);
    free(op_prev->diag);
    free(op_prev->updiag);
    free(op_prev);

    free(u_prev);
    free(u_next);

}

/* Main Procedure */
static int Implicit(NumFunc_1 *p,double S_0,double T,
    double r,double q,int sigma_type,int n,int m,double *ptprice,
    double *ptdelta)
{
    /*declarations*/
    int i,optionType,gridType;
    double y_max,y_min,T_max,t_0,theta,K,temp;
    double **res; /* res contains the values of the option
        today */
    /*for different strikes and maturities */
    double **grid; /* discretized values of sigma */
    double *y_grid, *T_grid; /* grids of the uniformly discr
        etized values of y and t used for the small grid of sigma*/

    double priceph,pricenh,inc=0.00001;

    /* Resolution of DUPIRE EDP */
    if((p->Compute) == &Call)
        optionType=1;
    else /*if((p->Compute) == &Put)*/

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    optionType=0;

    /* gridType = type of the y_fineGrid (0 for regular, 1
       for tanh) */
    gridType=1;
    K=p->Par[0].Val.V_DOUBLE;

    /*Transformation to BLACK-SCHOLES EDP*/
    temp=S_0;
    S_0=K;
    K=temp;

    temp=r;
    r=q;
    q=temp;

    if(optionType==1)
        optionType=0;
    else optionType=1;

    /*Cranck-Nicholson*/
    theta = .5;
    y_max = log(10.*S_0); /*S_max=exp(y_max)*/
    y_min = -y_max; /*S_max=exp(y_min)*/
    T_max = T;
    t_0 = 0; /* time origin */

    /*memory allocation for y_grid and t_grid*/
    y_grid = malloc((n+1)*sizeof(double));
    T_grid = malloc((m+1)*sizeof(double));

    /* memory allocation for the matrix sigma = grid*/
    grid = malloc((n+1)*sizeof(double *));
    for (i=0;i<=n;i++)
        grid[i] = malloc((m+1)*sizeof(double));

    /* memory allocation for the matrix res*/
    res = malloc((n+1)*sizeof(double *));
    for (i=0;i<=n;i++)

```

```

    res[i] = malloc((m+1)*sizeof(double));

    /*initialization of y_grid and t_grid*/
    buildFineGrid(y_grid,T_grid,n,m,t_0,T_max,y_min,y_max,S_0
        ,gridType);

    /* discretization of the analytical function sigma_func *
    /
    discretizeSigma(volatility,grid,n,m,y_grid,T_grid,sigma_
        type);

    /* solves Dupire PDE */
    solve(optionType,res,S_0,n,m,r,q,theta,f,grid,y_grid,T_
        grid);

    /* gives the option price for K and T*/
    i = find_index(log(K),y_grid,n,0);

    /*for(i=0;i<=n;i++)
        printf("%f %f {n",exp(y_grid[i]),res[i][m]-Call_Ornstei
            nUhlenbeck(S_0,exp(y_grid[i]),T,r,q,15.));*/

    /* linear linterpolation */
    *ptprice= res[i+1][m]-(y_grid[i+1]-log(K))*(res[i+1][m]-
        res[i][m])/(y_grid[i+1]-y_grid[i]);

    /*printf("%f %f %f{n",exp(y_grid[i]),res[i][m],Call_Orns
        teinUhlenbeck(S_0,K,T,r,q,15.));*/

    /*Delta*/
    i= find_index(log(K)+inc,y_grid,n,0);
    priceph=res[i+1][m]-(y_grid[i+1]-(log(K)+inc))*(res[i+1][
        m]-res[i][m])/(y_grid[i+1]-y_grid[i]);

    i= find_index(log(K)-inc,y_grid,n,0);
    pricenh=res[i+1][m]-(y_grid[i+1]-(log(K)-inc))*(res[i+1][
        m]-res[i][m])/(y_grid[i+1]-y_grid[i]);

    *ptdelta=(priceph-pricenh)/(2.*inc*K);

```

```

/*****
*****/
/*                      memory deallocation
*/
/*****
*****/

for (i=0;i<=n;i++)
    free(grid[i]);
free(grid);

free(T_grid);
free(y_grid);

for (i=0;i<=n;i++)
    free(res[i]);
free(res);

return OK;
}

int CALC(FD_Implicit)(void *Opt,void *Mod,PricingMethod *
    Met)
{
    TYPEOPT* ptOpt=( TYPEOPT*)Opt;
    TYPEMOD* ptMod=( TYPEMOD*)Mod;
    double r,divid;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    return Implicit(ptOpt->PayOff.Val.V_NUMFUNC_1,ptMod->S0.
        Val.V_PDOUBLE,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,r,
        divid,ptMod->Sigma.Val.V_INT, Met->Par[0].Val.V_INT,Met->
        Par[1].Val.V_INT,
        &(Met->Res[0].Val.V_DOUBLE),&(Met->Res[1].Val.V_
        DOUBLE));
}

```

```

static int CHK_OPT(FD_Implicit)(void *Opt, void *Mod)
{
    /*
    Option* ptOpt=(Option*)Opt;
    TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
    */
    if ((strcmp( ((Option*)Opt)->Name,"CallEuro")==0)|| (strcmp( ((Option*)Opt)->Name,"PutEuro")==0))
        return OK;

    return WRONG;
}

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_INT2=1000;
        Met->Par[1].Val.V_INT2=100;

    }

    return OK;
}

PricingMethod MET(FD_Implicit)=
{
    "FD_Dupire",
    {"Space StepNumber",INT2,{100},ALLOW},{"Time StepNumber",
    INT2,{100},ALLOW}, {" " ,PREMIA_NULLTYPE,{0},FORBID}},
    CALC(FD_Implicit),
    {"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORBID},{" " ,PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(FD_Implicit),
    CHK_ok,
    MET(Init)
};

```

References