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Help
#include <stdlib.h>
#include "bs1d_std.h"
#include "enums.h"
#include "error_msg.h"
#define PRECISION 1.0e-7 /*Precision for the localization
    of FD methods*/

static int boundary(int bound, NumFunc_1 *p, double y, double
    l, double h, double *ptbound1, double *ptbound2)
{
    /*Natural Dirichlet Boundary Conditions*/
    if (bound==0) {
        *ptbound1=(p->Compute)(p->Par,exp(y-l));
        *ptbound2=(p->Compute)(p->Par,exp(y+l));
    }

    /*Natural Neumann Boundary Conditions*/
    else
    {
        if (( (p->Compute) == &Call))
        {
            *ptbound1=0.;
            *ptbound2=exp(y+l)*h;
        }
        else
        if (( (p->Compute) == &Put))
        {
            *ptbound1=-exp(y-l)*h;
            *ptbound2=0.;
        }
        else
        /*if (( (p->Compute) == &CallSpread )||((p->Compute) ==
            &Digit))*/
        {
            *ptbound1=0.;
            *ptbound2=0.;
        }
    }

    return OK;
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}

static int GaussThetaSchema(int am,double s,NumFunc_1 *p,
    double t,double r,double divid,double sigma,int N,int M,double
    theta,int bound,double *ptprice,double *ptdelta)
{
    int Index,PriceIndex,TimeIndex;
    double k,vv,l,h,z,alpha,beta,gamma,y,alpha1,beta1,gamma1,
        bound1,bound2,upwind_alphacoef;
    double *Obst,*A,*B,*C,*A1,*B1,*C1,*P,*S;

    /*Memory Allocation*/
    if (N%2==1) N++;
    Obst= malloc((N+1)*sizeof(double));
    if (Obst==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    A= malloc((N+1)*sizeof(double));
    if (A==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    B= malloc((N+1)*sizeof(double));
    if (B==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    C= malloc((N+1)*sizeof(double));
    if (C==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    A1= malloc((N+1)*sizeof(double));
    if (A1==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    B1= malloc((N+1)*sizeof(double));
    if (B1==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    C1= malloc((N+1)*sizeof(double));
    if (C1==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    P= malloc((N+1)*sizeof(double));
    if (P==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    S= malloc((N+1)*sizeof(double));
    if (S==NULL)
        return MEMORY_ALLOCATION_FAILURE;

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/*Time Step*/
k=t/(double)M;

/*Space Localisation*/
vv=0.5*SQR(sigma);
z=(r-divid)-vv;
l=sigma*sqrt(t)*sqrt(log(1.0/PRECISION))+fabs(z*t);

/*Space Step*/
h=2.0*l/(double)N;

/*Peclet Condition-Coefficient of diffusion augmented */
if ((h*fabs(z))<=vv)
    upwind_alphacoef=0.5;
else {
    if (z>0.) upwind_alphacoef=0.0;
    else upwind_alphacoef=1.0;
}
vv-=z*h*(upwind_alphacoef-0.5);

/*Lhs Factor of theta-schema*/
alpha=theta*k*(-vv/(h*h)+z/(2.0*h));
beta=1.0+k*theta*(r+2.*vv/(h*h));
gamma=k*theta*(-vv/(h*h)-z/(2.0*h));

for(PriceIndex=1;PriceIndex<=N-1;PriceIndex++)
{
    A[PriceIndex]=alpha;
    B[PriceIndex]=beta;
    C[PriceIndex]=gamma;
}

/*Neumann Boundary Condition*/
if (bound==1) {
    B[1]=beta+alpha;
    B[N-1]=beta+gamma;
}

/*Rhs Factor of theta-schema*/
alpha1=k*(1.0-theta)*(vv/(h*h)-z/(2.0*h));
beta1=1.0-k*(1.0-theta)*(r+2.*vv/(h*h));

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gamma1=k*(1.0-theta)*(vv/(h*h)+z/(2.0*h));

for(PriceIndex=1;PriceIndex<=N-1;PriceIndex++)
{
    A1[PriceIndex]=alpha1;
    B1[PriceIndex]=beta1;
    C1[PriceIndex]=gamma1;
}

/*Neumann Boundary Condition*/
if (bound==1) {
    B1[1]=beta1+alpha1;
    B1[N-1]=beta1+gamma1;
}

/*Set Gauss*/
for(PriceIndex=N-2;PriceIndex>=1;PriceIndex--)
    B[PriceIndex]=B[PriceIndex]-C[PriceIndex]*A[PriceIndex+1]/B[PriceIndex+1];
for(PriceIndex=1;PriceIndex<N;PriceIndex++)
    A[PriceIndex]=A[PriceIndex]/B[PriceIndex];
for(PriceIndex=1;PriceIndex<N-1;PriceIndex++)
    C[PriceIndex]=C[PriceIndex]/B[PriceIndex+1];

/*Terminal Values*/
y=log(s);
for(PriceIndex=1;PriceIndex<N;PriceIndex++) {
    Obst[PriceIndex]=(p->Compute)(p->Par,exp(y-1+(double)
    PriceIndex*h));
    P[PriceIndex]= Obst[PriceIndex];
}

boundary(bound,p,y,l,h,&bound1,&bound2);

/*Finite Difference Cycle*/
for(TimeIndex=1;TimeIndex<=M;TimeIndex++)
{
    /*Set Rhs*/
    S[1]=B1[1]*P[1]+C1[1]*P[2]+A1[1]*bound1-alpha*bound1;
    for(PriceIndex=2;PriceIndex<N-1;PriceIndex++)
        S[PriceIndex]=A1[PriceIndex]*P[PriceIndex-1]+

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        B1[PriceIndex]*P[PriceIndex]+
        C1[PriceIndex]*P[PriceIndex+1];
    S[N-1]=A1[N-1]*P[N-2]+B1[N-1]*P[N-1]+C1[N-1]*bound2-
    gamma*bound2;

    /*Solve the system*/
    for(PriceIndex=N-2;PriceIndex>=1;PriceIndex--)
        S[PriceIndex]=S[PriceIndex]-C[PriceIndex]*S[PriceI
ndex+1];

    P[1] =S[1]/B[1];
    for(PriceIndex=2;PriceIndex<N;PriceIndex++)
        P[PriceIndex]=S[PriceIndex]/B[PriceIndex]-A[PriceI
ndex]*P[PriceIndex-1];

    /*Splitting for the american case*/
    if (am)
        for(PriceIndex=1;PriceIndex<N;PriceIndex++)
            P[PriceIndex]=MAX(Obst[PriceIndex],P[PriceIndex])
;
    }

Index=(int) floor ((double)N/2.0);

/*Price*/
*ptprice=P[Index];

/*Delta*/
*ptdelta = (P[Index+1]-P[Index-1])/(2.0*s*h);

/*Memory Desallocation*/
free(Obst);
free(A);
free(B);
free(C);
free(A1);
free(B1);
free(C1);
free(P);
free(S);

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    return OK;
}

int CALC(FD_Gauss)(void *Opt,void *Mod,PricingMethod *Met)
{
    TYPEOPT* ptOpt=( TYPEOPT*)Opt;
    TYPEMOD* ptMod=( TYPEMOD*)Mod;
    double r,divid;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    return GaussThetaSchema(ptOpt->EuOrAm.Val.V_BOOL,ptMod->
        SO.Val.V_PDOUBLE,
                                ptOpt->PayOff.Val.V_NUMFUNC_1,pt
    Opt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,r,divid,ptMod->
    Sigma.Val.V_PDOUBLE,
                                Met->Par[0].Val.V_INT,Met->Par[1]
        .Val.V_INT,Met->Par[2].Val.V_RGDOUBLE051,Met->Par[3].Val.
        V_ENUM.value,
                                &(Met->Res[0].Val.V_DOUBLE),&(
        Met->Res[1].Val.V_DOUBLE));
}

static int CHK_OPT(FD_Gauss)(void *Opt, void *Mod)
{
    /*
        Option* ptOpt=(Option*)Opt;
        TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
    */
    return OK;
}

static PremiaEnumMember BoundaryCondMembers[] =
{
    { "Dirichlet", 0 },
    { "Neumann", 1 },
    { NULL, NULLINT }
};

DEFINE_ENUM(BoundaryCondition, BoundaryCondMembers);

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static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_INT2=100;
        Met->Par[1].Val.V_INT2=100;
        Met->Par[2].Val.V_RGDOUBLE=0.5;
        Met->Par[3].Val.V_ENUM.value=1;
        Met->Par[3].Val.V_ENUM.members=&BoundaryCondition;

    }

    return OK;
}

PricingMethod MET(FD_Gauss)=
{
    "FD_Gauss",
    {{ "SpaceStepNumber",INT2,{100},ALLOW },{"TimeStepNumber",INT2,{100},ALLOW},
      {"Theta",RGDOUBLE051,{100},ALLOW},
      {"Boundary Condition",ENUM,{1},ALLOW},
      {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(FD_Gauss),
    {{ "Price",DOUBLE,{100},FORBID},
      {"Delta",DOUBLE,{100},FORBID} ,
      {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(FD_Gauss),
    CHK_split,
    MET(Init)
};

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References