```
Help
#include <stdlib.h>
#define WITH_boundary 1
#include "bs1d lim.h"
#include "error msg.h"
#define PRECISION 1.0e-7 /*Precision for the localization
    of FD methods*/
static int Gauss_UpIn(int am,double s,NumFunc_1 *p,double
    1, double rebate, double t, double r, double divid, double sigma
    ,int N,int M,double theta,double *ptprice,double *ptdelta)
    {
  int
           Index,PriceIndex,TimeIndex;
           k,vv,loc,h,z,alpha,beta,gamma,y,alpha1,beta1,gam
  double
    ma1,up,price1=0.,price2,upwind_alphacoef;
  double *Obst,*A,*B,*C,*P,*S,pricenh,pricep2h,priceph;
  /*Memory Allocation*/
  Obst= malloc((N+2)*sizeof(double));
  if (Obst==NULL)
    return MEMORY ALLOCATION FAILURE;
  A= malloc((N+2)*sizeof(double));
  if (A==NULL)
    return MEMORY ALLOCATION FAILURE;
  B= malloc((N+2)*sizeof(double));
  if (B==NULL)
    return MEMORY ALLOCATION FAILURE;
  C= malloc((N+2)*sizeof(double));
  if (C==NULL)
    return MEMORY_ALLOCATION_FAILURE;
 P= malloc((N+2)*sizeof(double));
  if (P==NULL)
    return MEMORY_ALLOCATION_FAILURE;
  S= malloc((N+2)*sizeof(double));
  if (S==NULL)
    return MEMORY ALLOCATION FAILURE;
  /*Time Step*/
  k=t/(double)M;
  /*Space Localisation*/
```

```
vv=0.5*sigma*sigma;
z=(r-divid)-vv;
loc=sigma*sqrt(t)*sqrt(log(1.0/PRECISION))+fabs(z)*t;
/*Space Step*/
y=log(s);
up=log(1);
h=(up-(y-loc))/(double)(N+1);
/*Coefficient of diffusion augmented */
if ((h*fabs(z)) \leq vv)
  upwind alphacoef=0.5;
else {
  if (z>0.) upwind alphacoef=0.0;
  else upwind_alphacoef=1.0;
vv-=z*h*(upwind alphacoef-0.5);
/*Lhs Factor of theta-schema*/
alpha=theta*k*(-vv/(h*h)+z/(2.0*h));
beta=1.0+k*theta*(r+2.*vv/(h*h));
gamma=k*theta*(-vv/(h*h)-z/(2.0*h));
for(PriceIndex=1;PriceIndex<=N;PriceIndex++)</pre>
    A[PriceIndex] = alpha;
    B[PriceIndex] = beta;
    C[PriceIndex] = gamma;
  }
/*Rhs Factor of theta-schema*/
alpha1=k*(1.0-theta)*(vv/(h*h)-z/(2.0*h));
beta1=1.0-k*(1.0-theta)*(r+2.*vv/(h*h));
gamma1=k*(1.0-theta)*(vv/(h*h)+z/(2.0*h));
/*Set Gauss*/
for(PriceIndex=N-1;PriceIndex>=1;PriceIndex--)
  B[PriceIndex] = B[PriceIndex] - C[PriceIndex] * A[PriceIndex+
  1]/B[PriceIndex+1];
for(PriceIndex=1;PriceIndex<=N;PriceIndex++)</pre>
  A[PriceIndex] = A[PriceIndex] / B[PriceIndex];
for(PriceIndex=1;PriceIndex<N;PriceIndex++)</pre>
```

```
C[PriceIndex] = C[PriceIndex] / B[PriceIndex + 1];
/*Terminal Values*/
for(PriceIndex=0;PriceIndex<=N;PriceIndex++) {</pre>
  Obst[PriceIndex] = (p->Compute) (p->Par, exp(y-loc+(double)
  PriceIndex*h));
 P[PriceIndex] = rebate;
price2=(p->Compute)(p->Par,1);
/*Finite Difference Cycle*/
for(TimeIndex=1;TimeIndex<=M;TimeIndex++)</pre>
  {
    /*Set Rhs*/
    S[1]=beta1*P[1]+gamma1*P[2]+alpha1*P[0]-alpha*P[0];
    for(PriceIndex=2;PriceIndex<=N;PriceIndex++)</pre>
S[PriceIndex] = alpha1*P[PriceIndex-1]+beta1*P[PriceInd
  ex]+
  gamma1*P[PriceIndex+1];
    price1=Boundary(l,p,(double)TimeIndex*k,r,divid,sigma
  );
    S[N]=beta1*P[N]+alpha1*P[N-1]+gamma1*price2-gamma*
  price1;
    price2=price1;
    /*Solve the system*/
    for(PriceIndex=N-1;PriceIndex>=1;PriceIndex--)
S[PriceIndex] = S[PriceIndex] - C[PriceIndex] * S[PriceIndex+1
  ];
    P[1] = S[1]/B[1];
    for(PriceIndex=2;PriceIndex<=N;PriceIndex++)</pre>
P[PriceIndex] = S[PriceIndex] / B[PriceIndex] - A[PriceIndex] *
  P[PriceIndex-1];
    /*Splitting for the american case*/
    if (am)
for(PriceIndex=1;PriceIndex<=N;PriceIndex++)</pre>
```

```
P[PriceIndex] = MAX(Obst[PriceIndex], P[PriceIndex]);
 Index=(int)floor(loc/h);
 P[N+1]=price1;
 /*Price*/
 *ptprice=P[Index]+(P[Index+1]-P[Index])*(exp(y)-exp(y-
   loc+Index*h))/(exp(y-loc+(Index+1)*h)-exp(y-loc+Index*h));
 /*Delta*/
 priceph=P[Index-1]+(P[Index]-P[Index-1])*(exp(y-h)-exp(y-
   loc+(Index-1)*h))/(exp(y-loc+(Index)*h)-exp(y-loc+(Index-1)*
   h));
 if (y!=up) {
   pricenh=P[Index+1]+(P[Index+2]-P[Index+1])*(exp(y+h)-
   \exp(y-loc+(Index+1)*h))/(\exp(y-loc+(Index+2)*h)-\exp(y-loc+(Index+2)*h))
   Index+1)*h));
   *ptdelta=(pricenh-priceph)/(2*s*h);
 } else {
   pricep2h=P[Index-2]+(P[Index-3]-P[Index-2])*(exp(y-2*h)
   loc+(Index-2)*h));
   *ptdelta=(-4*priceph+pricep2h+3*(*ptprice))/(2*s*h);
 /*Memory Desallocation*/
 free(Obst);
 free(A);
 free(B);
 free(C);
 free(P);
 free(S);
 return OK;
int CALC(FD_Gauss_UpIn)(void *Opt,void *Mod,PricingMethod *
   Met)
 TYPEOPT* ptOpt=(TYPEOPT*)Opt;
 TYPEMOD* ptMod=(TYPEMOD*)Mod;
```

}

{

```
double r, divid, limit, rebate;
  r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
  limit=((ptOpt->Limit.Val.V NUMFUNC 1)->Compute)((ptOpt->
                                                               Limit.Val.V NUMFUN
  rebate=((ptOpt->Rebate.Val.V NUMFUNC 1)->Compute)((ptOpt-
    >Rebate.Val.V_NUMFUNC_1)->Par,ptMod->T.Val.V_DATE);
  return Gauss_UpIn(ptOpt->EuOrAm.Val.V_BOOL,
        ptMod->SO.Val.V_PDOUBLE,ptOpt->PayOff.Val.V_
    NUMFUNC 1,
        limit,rebate,ptOpt->Maturity.Val.V DATE-ptMod->T.
    Val.V DATE,
        r,divid,ptMod->Sigma.Val.V_PDOUBLE,
        Met->Par[0].Val.V_INT2,Met->Par[1].Val.V_INT2,
    Met->Par[2].Val.V_RGDOUBLE051,
        &(Met->Res[0].Val.V_DOUBLE),&(Met->Res[1].Val.V_
    DOUBLE));
}
static int CHK OPT(FD Gauss UpIn)(void *Opt, void *Mod)
  Option* ptOpt=(Option*)Opt;
  TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
  if ((opt->OutOrIn).Val.V BOOL==IN)
    if ((opt->DownOrUp).Val.V BOOL==UP)
      if ((opt->Parisian).Val.V_BOOL==WRONG)
  return OK;
 return WRONG;
}
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if (Met->init == 0)
    {
      Met->init=1;
      Met->Par[0].Val.V_INT2=100;
      Met->Par[1].Val.V_INT2=100;
```

```
Met->Par[2].Val.V RGDOUBLE=1.0;
    }
 return OK;
}
PricingMethod MET(FD_Gauss_UpIn)=
  "FD_Gauss_UpIn",
  {{"SpaceStepNumber",INT2,{100},ALLOW },{"TimeStepNumber"
    ,INT2,{100},ALLOW},
   {"Theta", RGDOUBLE051, {100}, ALLOW}, {" ", PREMIA_NULLTYPE, {
    0},FORBID}},
  CALC(FD_Gauss_UpIn),
  {{"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORB
    ID} ,{" ",PREMIA_NULLTYPE,{0},FORBID}},
  CHK_OPT(FD_Gauss_UpIn),
  CHK split,
  MET(Init)
};
```

References