```
Help
/* Optimal Quantization Algorithm */
#include <stdlib.h>
#include <stdio.h>
#include <math.h>
#include <float.h>
#include "bsnd stdnd.h"
#include "math/linsys.h"
#include "pnl/pnl_basis.h"
#include "black.h"
#include "optype.h"
#include "enums.h"
#include "var.h"
#include "pnl/pnl_random.h"
#include "premia_obj.h"
#include "pnl/pnl matrix.h"
/* epsilon to detect if continuation value is reached */
#define EPS CONT 0.0000001
static const double LandMarkNorm=30;
static double *Q=NULL, *BSQ=NULL, *Weights=NULL, *Trans=NUL
    L, *Price=NULL, *Tesselation=NULL;
static double *Aux B=NULL, *Aux BN=NULL, *Brownian Bridge=
    NULL, *Cells To LandMark Up=NULL, *Cells To LandMark Do=NUL
static double *Radius=NULL, *Dist To LandMark=NULL, *Sqrt
    Inv_Time=NULL;
static int *Number Cell=NULL;
static int (*Search Method)(double *S,int Time, int AL T Si
    ze, long OP_EmBS_Di, int BS_Dimension);
static int QOpt Allocation(int AL T Size, int BS Dimension,
                           int OP_Exercice_Dates, long AL_
    MonteCarlo_Iterations)
{
  if (Tesselation==NULL) Tesselation=(double*)malloc(AL_T_
    Size*BS_Dimension*sizeof(double));
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if (Tesselation==NULL) return MEMORY ALLOCATION FAILURE;
if (Radius==NULL) Radius=(double*)malloc(AL T Size*sizeof
  (double));
if (Radius==NULL) return MEMORY ALLOCATION FAILURE;
if (Dist To LandMark==NULL) Dist_To_LandMark=(double*)mal
 loc(AL T Size*sizeof(double));
if (Dist_To_LandMark==NULL) return MEMORY_ALLOCATION_FAI
 LURE:
if (Cells To LandMark Up==NULL)
 Cells_To_LandMark_Up=(double*)malloc(BS_Dimension*AL_T_
 Size*sizeof(double));
if (Cells To LandMark Up==NULL) return MEMORY ALLOCATION
 FAILURE;
if (Cells To LandMark Do==NULL)
 Cells_To_LandMark_Do=(double*)malloc(BS_Dimension*AL_T_
 Size*sizeof(double));
if (Cells To LandMark Do==NULL) return MEMORY ALLOCATION
 FAILURE;
if (Q==NULL)
 Q=(double*)malloc(AL T Size*OP Exercice Dates*BS Dimens
 ion*sizeof(double));
if (Q==NULL) return MEMORY_ALLOCATION_FAILURE;
if (BSQ==NULL)
 BSQ=(double*)malloc(AL T Size*OP Exercice Dates*BS Dim
 ension*sizeof(double));
if (BSQ==NULL) return MEMORY ALLOCATION FAILURE;
if (Brownian Bridge==NULL)
 Brownian Bridge=(double*)malloc(AL MonteCarlo Iteratio
 ns*BS Dimension*sizeof(double));
if (Brownian_Bridge==NULL) return MEMORY_ALLOCATION_FAILU
 RE:
if (Number Cell==NULL)
 Number Cell=(int*)malloc(AL_MonteCarlo_Iterations*size
 of(int));
if (Number Cell==NULL) return MEMORY ALLOCATION FAILURE;
if (Trans==NULL)
 Trans=(double*)malloc(AL_T_Size*AL_T_Size*sizeof(
 double));
if (Trans==NULL) return MEMORY ALLOCATION FAILURE;
if (Weights==NULL)
 Weights=(double*)malloc(AL_T_Size*sizeof(double));
```

```
if (Weights==NULL) return MEMORY ALLOCATION FAILURE;
  if (Price==NULL)
   Price=(double*)malloc(OP_Exercice_Dates*AL_T_Size*size
    of(double));
  if (Price==NULL) return MEMORY ALLOCATION FAILURE;
  if (Aux B==NULL)
    Aux B=(double*)malloc(BS Dimension*sizeof(double));
  if (Aux B==NULL) return MEMORY ALLOCATION FAILURE;
  if (Aux BN==NULL)
   Aux_BN=(double*)malloc(BS_Dimension*sizeof(double));
  if (Aux BN==NULL) return MEMORY ALLOCATION FAILURE;
  if (Sqrt Inv Time==NULL)
    Sqrt Inv Time=(double*)malloc(OP Exercice Dates*sizeof(
    double));
  if (Sqrt_Inv_Time==NULL) return MEMORY_ALLOCATION FAILU
    RE:
 return OK;
}
static void QOpt Liberation()
  if (Brownian_Bridge!=NULL) { free(Brownian_Bridge);
    nian Bridge=NULL; }
  if (Tesselation!=NULL) { free(Tesselation); Tesselation=
   NULL; }
  if (Q!=NULL) { free(Q); Q=NULL; }
  if (BSQ!=NULL) { free(BSQ);BSQ=NULL;}
  if (Trans!=NULL) {free(Trans);Trans=NULL; }
  if (Weights!=NULL) {free(Weights); Weights=NULL; }
  if (Price!=NULL) { free(Price); Price=NULL;}
  if (Aux_B!=NULL) { free(Aux_B); Aux_B=NULL;}
  if (Aux BN!=NULL) { free(Aux BN); Aux BN=NULL; }
  if (Radius!=NULL) { free(Radius); Radius=NULL;}
  if (Sqrt_Inv_Time!=NULL) { free(Sqrt_Inv_Time); Sqrt_Inv_
    Time=NULL;}
  if (Cells To LandMark Up!=NULL) {free(Cells To LandMark
    Up);Cells_To_LandMark_Up=NULL; }
  if (Cells_To_LandMark_Do!=NULL) {free(Cells_To_LandMark_
    Do);Cells To LandMark Do=NULL; }
  if (Dist_To_LandMark!=NULL) {free(Dist_To_LandMark);Dist_
    To LandMark=NULL;}
```

```
if (Number Cell!=NULL) {free(Number Cell); Number Cell=NUL
    L;}
}
static int NearestCellD1(double *S,int Time, int AL T Size,
     long OP_EmBS_Di, int BS_Dimension)
  int j,l=0;
  long ind;
  double min=DBL_MAX,aux;
  /*one dimensional nearest cell search*/
  ind=0;
  for (j=0;j<AL_T_Size;j++)</pre>
      aux=fabs(*S-Tesselation[ind]);
      ind+=BS_Dimension;
      if (min>aux) { min=aux; l=j;}
    }
  return 1;
}
static int NearestCell(double *S,int Time, int AL_T_Size,
    long OP_EmBS_Di, int BS_Dimension)
  /*the Brownian Motion S must be normalised. */
  /*used if the fast nearest cell search fails; this event
    is of very small probability*/
  int j,k,l=0;
  double min=DBL_MAX,aux,auxnorm;
  for (j=0;j<AL_T_Size;j++)</pre>
    {
      aux=0;
      k=0;
      while ((aux<min)&&(k<BS_Dimension))</pre>
          auxnorm=S[k]-Tesselation[j*BS_Dimension+k];
          aux+=auxnorm*auxnorm;
```

```
k++;
      if (aux<min){ min=aux; l=j;}</pre>
  return 1;
}
static int FastNearestCell(double *S,int Time, int AL_T_Si
    ze, long OP_EmBS_Di, int BS_Dimension)
{
  /* The Brownian Motion S must be normalised. */
  /* see the documentation for the explanation of the fast
    nearest cell search*/
  int j,k,l=-1,m;
  int InegTrue;
  long jmBS_Dim,mmAL_T_Sizepj;
  double min=DBL_MAX,aux,auxnorm;
  for (m=0;m<BS Dimension;m++){</pre>
    Dist To LandMark[m]=0;
    for (k=0; k< m; k++){
      Dist_To_LandMark[m]+=S[k]*S[k];
    Dist_To_LandMark[m]+=(S[m]-LandMarkNorm)*(S[m]-LandMar
    kNorm);
    for (k=m+1;k<BS_Dimension;k++){</pre>
      Dist_To_LandMark[m]+=S[k]*S[k];
    }
  }
  jmBS_Dim=0;
  for (j=0; j<AL \ T \ Size; j++){}
    aux=0;
    k=0;
    m=0;
    InegTrue=1;
    mmAL_T_Sizepj=j;
    do {
```

```
InegTrue=(InegTrue)&&(Dist To LandMark[m] <= Cells To</pre>
    LandMark_Up[mmAL_T_Sizepj])&&(Dist_To_LandMark[m]>=Cells_To_
    LandMark_Do[mmAL_T_Sizepj]);
      m++;
      mmAL T Sizepj+=AL T Size;
    } while ((InegTrue)&&(m<BS_Dimension));</pre>
    if (InegTrue){
      while ((aux<min)&&(k<BS_Dimension)){</pre>
        auxnorm=S[k]-Tesselation[jmBS_Dim+k];
        aux+=auxnorm*auxnorm;
        k++;
      }
      if (aux<min){</pre>
        min=aux;
        1=j;
      }
    jmBS_Dim+=BS_Dimension;
  if (1==-1){
    1=NearestCell(S,Time,AL_T_Size,OP_EmBS_Di,BS_Dimension)
   return 1;
  }
  return 1;
}
static int InitTesselation(char *path, char *name, int BS_
    Dimension, int AL_T_Size)
{
  int i,j,nvl;
  char NameDef[MAX_PATH_LEN];
  FILE *filtes;
  /*load of a file containing an optimal tesselation*/
 NameDef[0]='{0';
  if (*name=='d'){
    sprintf(NameDef,"%sd%dn%d.tes",path,BS Dimension,AL T
    Size);
    filtes=fopen(NameDef, "r");
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```
if (filtes==NULL) return UNABLE TO OPEN FILE;
    sprintf(NameDef, "%s%s", path, name);
    filtes=fopen(NameDef, "r");
    if (filtes==NULL) return UNABLE TO OPEN FILE;
  if (BS_Dimension!=1){
    nvl=fscanf(filtes,"%s{n",NameDef);
    nvl=fscanf(filtes,"%s{n",NameDef);
    nvl=fscanf(filtes,"%s{n",NameDef);
    nvl=fscanf(filtes,"%s{n",NameDef);
  } else {
    nvl=fscanf(filtes,"%s{n",NameDef);
    nvl=fscanf(filtes,"%s{n",NameDef);
    nvl=fscanf(filtes,"%s{n",NameDef);
  for (i=0;i<AL T Size;i++){</pre>
    for(j=0;j<BS Dimension;j++){</pre>
      nvl=fscanf(filtes,"%lf ",Tesselation+i*BS_Dimension+
    j);
      if (nvl!=1) return BAD TESSELATION FORMAT;
    }
    if (BS_Dimension!=1){
      nvl=fscanf(filtes,"%lf ",Radius+i);
      if (nvl!=1) return BAD TESSELATION FORMAT;
    }
  }
  fclose(filtes);
  return OK;
static void InitLandMark(int BS Dimension, int AL T Size)
  int i,j,k;
  double AuxD;
  /*initialization of the distances (landmarks, quantization
    s points)+/-(cell radius) used in the fast nearest cell se
    arch*/
  for (i=0;i<BS_Dimension;i++){</pre>
    for (j=0;j<AL_T_Size;j++){</pre>
```

```
AuxD=0.;
      for (k=0; k<i; k++){
        AuxD+=Tesselation[j*BS_Dimension+k]*Tesselation[j*
    BS Dimension+k];
      }
      AuxD+=(Tesselation[j*BS Dimension+i]-LandMarkNorm)*(
    Tesselation[j*BS_Dimension+i]-LandMarkNorm);
      for (k=i+1;k<BS Dimension;k++){</pre>
        AuxD+=Tesselation[j*BS Dimension+k]*Tesselation[j*
    BS_Dimension+k];
      }
      AuxD=sqrt(AuxD);
      Cells_To_LandMark_Up[i*AL_T_Size+j]=(AuxD+Radius[j])*
    (AuxD+Radius[j]);
      Cells_To_LandMark_Do[i*AL_T_Size+j]=(AuxD-Radius[j])*
    (AuxD-Radius[j]);
    }
 }
static void Tesselations_Scale(int AL_T_Size, int OP_Exerc
    ice_Dates, int BS_Dimension,
                                double Step, double *BS_Spo
    t)
{
  int i,j,k;
  double SqrtTime;
  /*scalings of the initial N(0,Id) optimal tesselation*/
  for (j=1;j<OP_Exercice_Dates;j++){</pre>
    SqrtTime=sqrt((double)j*Step);
    for (i=0;i<AL T Size;i++){</pre>
      for (k=0;k<BS Dimension;k++){</pre>
        Q[i*OP Exercice Dates*BS Dimension+j*BS Dimension+
    k]=SqrtTime*Tesselation[i*BS_Dimension+k];
      }
      BlackScholes Transformation((double) j*Step, BSQ+i*OP
    Exercice_Dates*BS_Dimension+j*BS_Dimension,Q+i*OP_Exercice_
    Dates*BS_Dimension+j*BS_Dimension,BS_Dimension,BS_Spot);
    }
  }
}
```

```
static void
Compute_Transition(long AL_MonteCarlo_Iterations, int AL_T_
    Size, int BS Dimension,
                    int OP EmBS Di, int OP Exercice Dates,
    int Time, double Sqrt Inv Time)
{
  int i,j,k,AuxNumCell;
  long 1;
  for (i=0;i<AL_T_Size;i++){
    Weights[i]=0.;
    for (j=0; j<AL T Size; j++){
      Trans[i*AL_T_Size+j]=0.;
    }
  /*computation of the brownian bridge transition probabil
    ities from the quantizations cells at time "Time" to the qu
    antization cells at time "Time+1" (see the documantation fo
    r more informations)*/
  for (l=0;l<AL MonteCarlo Iterations;l++){</pre>
    for (k=0;k<BS_Dimension;k++){</pre>
      Aux_B[k]=Sqrt_Inv_Time*Brownian_Bridge[1*BS_Dimensio
    n+k];
    }
    AuxNumCell=Search Method(Aux B, Time, AL T Size, OP EmBS
    Di,BS Dimension);
    Trans[AuxNumCell*AL T Size+Number Cell[1]]+=1.;
    Weights[AuxNumCell]+=1.;
    Number Cell[1] = AuxNumCell;
  }
  /*normalization*/
  for (i=0;i<AL T Size;i++){</pre>
    for (j=0;j<AL T Size;j++){</pre>
      if (Weights[i]>0.)
        Trans[i*AL_T_Size+j]/=Weights[i];
    }
  }
}
```

```
static void Close()
  /*memory liberation*/
  QOpt Liberation();
  End BS();
}
/*see the documentation for the parameters meaning*/
static int QOpt(PnlVect *BS_Spot,
                NumFunc_nd *p,
                double OP_Maturity,
                double BS Interest Rate,
                PnlVect *BS Dividend Rate,
                PnlVect *BS Volatility,
                double *BS_Correlation,
                long AL_MonteCarlo_Iterations,
                int generator,
                int OP_Exercice_Dates,
                int AL_T_Size,
                char *AL Tesselation Path,
                char *AL Tesselation Name,
                double *AL_FPrice,
                double *AL_BPrice)
{
  int i,j,k,AuxNumCell, init_mc, init;
  long 1;
  int BS Dimension = BS Spot->size;
  long OP_ExmBS_Di=(long)OP_Exercice_Dates*BS_Dimension;
  double Step,Sqrt_Step,DiscountStep,aux;
  PnlVect VStock;
  VStock.size=BS Dimension;
  /* MC sampling */
  init_mc= pnl_rand_init(generator, BS_Dimension, AL_
    MonteCarlo Iterations);
  /* Test after initialization for the generator */
  if(init_mc != OK) return init_mc;
  /*time step*/
  Step=OP_Maturity/(double)(OP_Exercice_Dates-1);
```

```
Sqrt Step=sqrt(Step);
/*discounting factor for a time step*/
DiscountStep=exp(-BS_Interest_Rate*Step);
/*memory allocation of the BlackScholes variables*/
init=Init BS(BS Dimension, BS Volatility->array,
             BS_Correlation, BS_Interest_Rate, BS_Dividend_
  Rate->array);
if (init!=OK) return init;
/*memory allocation of the algorithm's variables*/
init=QOpt_Allocation(AL_T_Size,BS_Dimension,OP_Exercice_
  Dates,AL MonteCarlo Iterations);
if (init!=OK) return init;
if (BS_Dimension==1) Search_Method=NearestCellD1;
else Search Method=FastNearestCell;
for (j=1;j<OP_Exercice_Dates;j++)</pre>
  Sqrt_Inv_Time[j]=1./sqrt((double)j*Step);
/*initialization of the optimal quantizers*/
init=InitTesselation(AL_Tesselation_Path,AL_Tesselation_
  Name,BS_Dimension,AL_T_Size);
if (init!=OK) return init;
/*landmarks initialization for the fast nearest cell sear
  ch procedure*/
if (BS Dimension>1)
  InitLandMark(BS Dimension, AL T Size);
/*optimal tesselation scalings*/
Tesselations_Scale(AL_T_Size,OP_Exercice_Dates,BS_Dimens
  ion,Step,BS Spot->array);
/*initialization of the brownian bridge at the maturity*/
Init_Brownian_Bridge(Brownian_Bridge,AL_MonteCarlo_Itera
  tions, BS Dimension, OP Maturity, generator);
/*initialisation of the dynamical programming prices at
  the maturity*/
for (i=0;i<AL_T_Size;i++)</pre>
    VStock.array=BSQ+i*OP_Exercice_Dates*BS_Dimension+(
  OP_Exercice_Dates-1)*BS_Dimension;
```

```
Price[(OP Exercice Dates-1)*AL T Size+i]=p->Compute(
  p->Par, &VStock);
/*quantization of the brownian bridge*/
for (i=0;i<AL_MonteCarlo_Iterations;i++){</pre>
  /*normalisation for the nearest cell search procedure*/
  for (k=0;k<BS Dimension;k++){</pre>
    Aux B[k]=Sqrt Inv Time[OP Exercice Dates-1]*Brownian
  Bridge[i*BS Dimension+k];
  /*nearest cell search*/
  Number Cell[i] = Search Method(Aux B, OP Exercice Dates-1,
  AL T Size, OP ExmBS Di, BS Dimension);
}
/*dynamical programming algorithm*/
for (i=OP Exercice Dates-2;i>=1;i--){
  /*computation of the brownian bridge at time i*/
  Compute Brownian Bridge(Brownian Bridge, i*Step, Step, BS
  Dimension, AL_MonteCarlo_Iterations, generator);
  /*computation of the quantized transition kernel of th
  e brownian bridge between times i and i+1*/
  Compute_Transition(AL_MonteCarlo_Iterations,AL_T_Size,
  BS_Dimension,OP_ExmBS_Di,OP_Exercice_Dates,i,Sqrt_Inv_Time[
  il):
  /*approximation of the conditionnal expectations*/
  for (j=0;j<AL_T_Size;j++){</pre>
    aux=0;
    for (k=0; k<AL \ T \ Size; k++){}
      aux+=Price[(i+1)*AL T Size+k]*Trans[j*AL T Size+k];
    /*discounting for a time step*/
    aux*=DiscountStep;
    /*aux contains the continuation value at quantization
   point j and time i*/
    /*exercise decision*/
    VStock.array=BSQ+j*OP Exercice Dates*BS Dimension+i*
  BS Dimension;
    Price[i*AL_T_Size+j]=MAX(p->Compute(p->Par,&VStock),
  aux);
}
```

```
aux=0;
for (k=0; k<AL_T_Size; k++){
  aux+=Price[AL_T_Size+k]*Weights[k];
}
aux/=(double)AL MonteCarlo Iterations;
aux*=DiscountStep;
/*output backward price*/
*AL BPrice=MAX(p->Compute(p->Par,BS Spot),aux);
/* Forward price */
*AL FPrice = 0.;
if (*AL BPrice==p->Compute(p->Par,BS Spot)){
  *AL FPrice=*AL BPrice;
}
else {
  double payoff;
  for (l=0;l<AL_MonteCarlo_Iterations;l++){</pre>
    /*spot of the brownian motion*/
    for (k=0;k<BS Dimension;k++) Aux B[k]=0.;</pre>
    /*optimal stopping for a quantized path*/
    do
      {
        i++;
        for (k=0;k<BS Dimension;k++)</pre>
          {
            Aux B[k]+=Sqrt Step*pnl rand normal(
                                                     generator);
            /*normalization of Aux B*/
            Aux_BN[k]=Sqrt_Inv_Time[i]*Aux_B[k];
          }
        /*search of the Aux BN number cell*/
        AuxNumCell=Search_Method(Aux_BN,i,AL_T_Size,OP_
  Exercice_Dates*BS_Dimension,BS_Dimension);
        VStock.array = BSQ+AuxNumCell*OP Exercice Dates*
  BS Dimension+i*BS Dimension;
        payoff = p->Compute(p->Par, &VStock);
      } while (payoff<Price[i*AL_T_Size+AuxNumCell] - EP</pre>
  S CONT);
    /*MonteCarlo formulae for the forward price*/
    VStock.array=BSQ+AuxNumCell*OP_Exercice_Dates*BS_Dim
```

```
ension+i*BS Dimension;
      *AL FPrice+=Discount(i*Step,BS Interest Rate)*(p->
    Compute(p->Par, &VStock));
    /*output forward price*/
    *AL FPrice/=(double)AL MonteCarlo Iterations;
  }
 Close();
 return OK;
}
int CALC(MC_QuantizationND)(void *Opt, void *Mod, Pricing
   Method *Met)
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
 TYPEMOD* ptMod=(TYPEMOD*)Mod;
  double r;
  int i, res;
  double *BS cor;
 PnlVect *divid = pnl_vect_create(ptMod->Size.Val.V_PINT);
  char tes[MAX_PATH_LEN];
  char *file ="d";
 PnlVect *spot, *sig;
  spot = pnl vect compact to pnl vect (ptMod->S0.Val.V PNLV
    ECTCOMPACT);
  sig = pnl_vect_compact_to_pnl_vect (ptMod->Sigma.Val.V_PN
    LVECTCOMPACT);
  for(i=0; i<ptMod->Size.Val.V PINT; i++)
    pnl vect set (divid, i,
           log(1.+ pnl_vect_compact_get (ptMod->Divid.Val.
    V_PNLVECTCOMPACT, i)/100.));
 r= log(1.+ptMod->R.Val.V DOUBLE/100.);
  if ((BS_cor = malloc(ptMod->Size.Val.V_PINT*ptMod->Size.
    Val.V PINT*sizeof(double)))==NULL)
    return MEMORY ALLOCATION FAILURE;
  for(i=0; i<ptMod->Size.Val.V_PINT*ptMod->Size.Val.V_PINT;
```

```
BS_cor[i] = ptMod->Rho.Val.V_DOUBLE;
  for(i=0; i<ptMod->Size.Val.V_PINT; i++)
    BS_cor[i*ptMod->Size.Val.V_PINT+i]= 1.0;
  /* path name for the tesselation file*/
  strcpy(tes, premia_data_dir);
  strcat(tes, "/"); strcat(tes, "tes"); strcat(tes, "/");
  res=QOpt(spot,
           ptOpt->PayOff.Val.V NUMFUNC ND,
           ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,
           r, divid, sig,
           BS_cor,
           Met->Par[0].Val.V_LONG,
           Met->Par[1].Val.V ENUM.value,
           Met->Par[2].Val.V_INT,
           Met->Par[3].Val.V_INT,
           tes,
           file,
           &(Met->Res[0].Val.V_DOUBLE),
           &(Met->Res[1].Val.V_DOUBLE));
  pnl vect free(&divid);
  pnl_vect_free (&spot);
  pnl_vect_free (&sig);
  free(BS_cor);
  return res;
}
static int CHK_OPT(MC_QuantizationND)(void *Opt, void *Mod)
  Option* ptOpt=(Option*)Opt;
  TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
  if ((opt->EuOrAm).Val.V BOOL==AMER)
    return OK;
  else
```

```
return WRONG;
}
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if ( Met->init == 0)
    {
      Met->init=1;
      Met->Par[0].Val.V_LONG=10000;
      Met->Par[1].Val.V_ENUM.value=0;
      Met->Par[1].Val.V_ENUM.members=&PremiaEnumMCRNGs;
      Met->Par[2].Val.V INT=10;
      Met->Par[3].Val.V_INT=200;
    }
  return OK;
PricingMethod MET(MC_QuantizationND)=
  "MC Quantization nd",
  {{"N iterations",LONG,{100},ALLOW},
   {"RandomGenerator", ENUM, {100}, ALLOW},
   {"Number of Exercise Dates", INT, {100}, ALLOW},
   {"Tesselation Size", INT, {100}, ALLOW},
   {" ",PREMIA_NULLTYPE,{O},FORBID}},
  CALC(MC QuantizationND),
  {{"Forward Price", DOUBLE, {100}, FORBID}, {"Backward Price",
    DOUBLE, {100}, FORBID},
   {" ",PREMIA NULLTYPE, {0}, FORBID}},
  CHK_OPT(MC_QuantizationND),
  CHK mc,
  MET(Init)
};
#undef EPS CONT
```

## References