```
Help
#include <stdlib.h>
#include "bs1d_pad.h"
#include "error_msg.h"
static double y(double y min, double i, double h)
  return ((y_min)+(i)*(h));
static double coth(double x)
  return (1/tanh(x));
static int Fixed_RodgerShi(double pseudo_stock,double pseu
    do strike, NumFunc 2 *p, double t, double r, double divid,
    double sigma,int N,int M,double *ptprice,double *ptdelta)
  int i,j,j0,PriceIndex;
  double y0,y_min,y_max,k,h,boundary;
  double fact1,fact2,fact3,gammaj,alphaj;
  double *a,*b,*P,*S,*alpha,*beta,*gamma;
  double *A, *B, *C;
  /*Memory Allocation*/
  A= malloc((N+2)*sizeof(double));
  if (A==NULL)
    return MEMORY ALLOCATION FAILURE;
  B= malloc((N+2)*sizeof(double));
  if (B==NULL)
    return MEMORY ALLOCATION FAILURE;
  C= malloc((N+2)*sizeof(double));
  if (C==NULL)
    return MEMORY ALLOCATION FAILURE;
  a= malloc((N+1)*sizeof(double));
  if (a==NULL)
    return MEMORY_ALLOCATION_FAILURE;
  b= malloc((N+1)*sizeof(double));
  if (b==NULL)
    return MEMORY_ALLOCATION_FAILURE;
```

```
alpha= malloc((N+1)*sizeof(double));
if (alpha == NULL)
  return MEMORY_ALLOCATION_FAILURE;
beta= malloc((N+1)*sizeof(double));
if (beta==NULL)
  return MEMORY ALLOCATION FAILURE;
gamma= malloc((N+1)*sizeof(double));
if (gamma==NULL)
  return MEMORY ALLOCATION FAILURE;
P= malloc((N+1)*sizeof(double));
if (P==NULL)
  return MEMORY ALLOCATION FAILURE;
S= malloc((N+1)*sizeof(double));
if (S==NULL)
  return MEMORY_ALLOCATION_FAILURE;
/*Space Localisation*/
y0=pseudo_strike/pseudo_stock;
y_min=0.;
y max=6.;
/*Time Step*/
k=t/(double)M;
/*Space Step*/
h=(y max-y min)/(double)N;
/*Lhs Factor*/
fact1=sigma*sigma/(double)(2*h*h);
fact2=-((r-divid)+sigma*sigma)/(double)(2*h);
fact3=-1/(t*h);
for(j=1;j<N;j++){
  /* Operator L1 Diffusion */
  alpha[j] = fact1*(y(y_min, j-0.5,h)*y(y_min, j-0.5,h));
  beta[j]=-fact1*(y(y min, j-0.5,h)*y(y min, j-0.5,h)+y(y
  \min, j+0.5, h)*y(y \min, j+0.5, h));
  gamma[j] = fact1*(y(y_min, j+0.5,h)*y(y_min, j+0.5,h));
  /* Operator L1 Drift */
  alpha[j] += -fact2*(y(y_min, j-0.5,h));
  beta[j]+=fact2*(-y(y_min, j+0.5,h)+y(y_min, j-0.5,h));
```

```
gamma[j]+=fact2*(y(y min,j+0.5,h));
  /* Operator L2 */
  gammaj=2*h/(double)(t*sigma*sigma*y(y min,j,h)*y(y min,
  alphaj=0.5*(1+coth(gammaj/(double)2))-1/(double)gammaj;
  /* 1/2 < alphaj < 1 : 1/2 = centered ; 1 = decentered *
  alphaj=0.5;
  alpha[j]+=-fact3*alphaj;
  beta[j]+=fact3*(2*alphaj-1);
  gamma[j]+=fact3*(1-alphaj);
  alpha[j]/=2.;
  beta[j]/=2.;
  gamma[j]/=2.;
  /* + Time term */
 beta[j]+=-1.0/k;
/* To prepare the inversion */
for(PriceIndex=1;PriceIndex<N;PriceIndex++){</pre>
  A[PriceIndex] = alpha[PriceIndex];
  B[PriceIndex] = beta[PriceIndex];
  C[PriceIndex] = gamma[PriceIndex];
}
for(PriceIndex=N-2;PriceIndex>=1;PriceIndex--)
  B[PriceIndex] = B[PriceIndex] - C[PriceIndex] * A[PriceIndex+
  1]/B[PriceIndex+1];
for(PriceIndex=1;PriceIndex<N;PriceIndex++)</pre>
  A[PriceIndex] = A[PriceIndex] / B[PriceIndex];
for(PriceIndex=1;PriceIndex<N-1;PriceIndex++)</pre>
  C[PriceIndex] = C[PriceIndex] / B[PriceIndex + 1];
/*Final Condition*/
if ((p->Compute) == &Call_OverSpot2)
```

```
for(j=0;j<=N;j++) /* CALL */
                                  P[i]=0.0;
else
                 for(j=0;j<=N;j++) /* PUT */
                                  P[j]=y(y min, j,h);
/*Finite Difference Cycle Implicite Schema : back in
                 time*/
for(i=M-1;i>=0;i--)
                 {
                                  /*Boundary Value*/
                                   if ((p->Compute) == &Call_OverSpot2) {
if ((r-divid)==0.){
                 boundary=(t-k*(double)i)/t;
}
else
                 boundary=(1.0/((r-divid)*t))*(1.0-exp(-(r-divid)*(t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-divid)*t-k*))*(1.0-exp(-(r-div
                 (double)i)));}
                                  else{
boundary=exp(-(r-divid)*(t-k*(double)i))*y_max;
if ((r-divid)==0.){
                 boundary-=(t-k*(double)i)/t;
}
else
                 boundary=(1.0/((r-divid)*t))*(1.0-exp(-(r-divid)*(t-divid))*(1.0-exp(-(r-divid))*(t-divid))*(1.0-exp(-(r-divid))*(t-divid))*(1.0-exp(-(r-divid))*(t-divid))*(1.0-exp(-(r-divid))*(t-divid))*(t-divid)*(t-divid))*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-divid)*(t-di
                 k*(double)i)));}
                                  /*set Rhs */
                                  for(j=1;j<N;j++)</pre>
S[j]=-P[j]/k;
                                  /* Dirichlet */
                                   if ((p->Compute) == &Call OverSpot2) /* CALL */
S[1] -= alpha[1] *boundary;
                                   else /* PUT */
S[N-1] = gamma[N-1] *boundary;
                                   for(j=1;j<N;j++)
S[j] = alpha[j] *P[j-1] + (beta[j] + 1.0/k) *P[j] + gamma[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j] *P[j+1.0/k] *P[j+1
```

```
1];
    /*Solve the system*/
    for(PriceIndex=N-2;PriceIndex>=1;PriceIndex--)
S[PriceIndex] = S[PriceIndex] - C[PriceIndex] * S[PriceIndex+1
  ];
    P[1] = S[1]/B[1];
    for(PriceIndex=2;PriceIndex<=N-1;PriceIndex++)</pre>
P[PriceIndex] = S[PriceIndex] / B[PriceIndex] - A[PriceIndex] *
  P[PriceIndex-1];
    if ((p->Compute) == &Call_OverSpot2){ /* CALL */
P[0]=boundary; /* et P[N]=0 */}
    else{ /* PUT */
P[N-1]=boundary; /* et P[0]=0 */}
  }
j0=(int)floor((y0-y min)/h);
/*Price*/
*ptprice=exp(-divid*t)*pseudo_stock*(P[j0]+(P[j0+1]-P[j0]
  *(y0-y(y min, j0,h))/h);
/*Delta */
*ptdelta=exp(-divid*t)*(P[j0]-y0*(P[j0+1]-P[j0-1])/(2.*h)
  );
/*Memory Desallocation*/
free(a);
free(b);
free(alpha);
free(beta);
free(gamma);
free(A);
free(B);
free(C);
free(P);
free(S);
/* free(Obst);*/
```

```
return OK;
}
int CALC(FD FixedAsian RodgerShi)(void *Opt,void *Mod,Prici
    ngMethod *Met)
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
 TYPEMOD* ptMod=(TYPEMOD*)Mod;
  int return value;
  double r, divid, time spent, pseudo spot, pseudo strike;
  double t_0, T_0;
  r=log(1.+ptMod->R.Val.V DOUBLE/100.);
 divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
  T 0 = ptMod->T.Val.V_DATE;
  t_0= (ptOpt->PathDep.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUB
   LE;
  if(T_0 < t_0)
    {
      Fprintf(TOSCREEN, "T_0 < t_0, untreated case{n\{n\{n"\}\};
      return_value = WRONG;
  /* Case t 0 <= T 0 */
  else
    {
      time_spent=(ptMod->T.Val.V_DATE-(ptOpt->PathDep.Val.
    V NUMFUNC 2)->Par[0].Val.V PDOUBLE)/
  (ptOpt->Maturity.Val.V DATE-(ptOpt->PathDep.Val.V
    NUMFUNC 2)->Par[0].Val.V PDOUBLE);
      pseudo_spot=(1.-time_spent)*ptMod->SO.Val.V_PDOUBLE;
      pseudo strike=(ptOpt->PayOff.Val.V NUMFUNC 2)->Par[0]
    .Val.V PDOUBLE-time spent*(ptOpt->PathDep.Val.V NUMFUNC 2)
    ->Par[4].Val.V_PDOUBLE;
      if (pseudo strike<=0.)
  {
    Fprintf(TOSCREEN, "ANALYTIC FORMULA{n{n{n");
```

```
return value=Analytic KemnaVorst(pseudo spot,pseudo
    strike, time spent, ptOpt->PayOff.Val.V NUMFUNC 2, ptOpt->Matu
    rity.Val.V_DATE-ptMod->T.Val.V_DATE,r,divid,&(Met->Res[0].
    Val.V DOUBLE),&(Met->Res[1].Val.V DOUBLE));
  }
      else
  return_value=Fixed_RodgerShi(pseudo_spot,pseudo_strike,
    ptOpt->PayOff.Val.V NUMFUNC 2,ptOpt->Maturity.Val.V DATE-pt
    Mod->T.Val.V DATE, r, divid, ptMod->Sigma.Val.V PDOUBLE, Met->
    Par[0].Val.V_INT2,Met->Par[1].Val.V_INT2,&(Met->Res[0].Val.V_
    DOUBLE),&(Met->Res[1].Val.V DOUBLE));
    }
  return return_value;
}
static int CHK_OPT(FD_FixedAsian_RodgerShi)(void *Opt, voi
    d *Mod)
  if ((strcmp(((Option*)Opt)->Name, "AsianCallFixedEuro")==
    0) || (strcmp( ((Option*)Opt)->Name, "AsianPutFixedEuro")==
    0))
    return OK;
  return WRONG;
}
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if (Met->init == 0)
    {
      Met->init=1;
      Met->Par[0].Val.V_INT2=1000;
      Met->Par[1].Val.V INT2=1000;
    }
  return OK;
}
PricingMethod MET(FD_FixedAsian_RodgerShi)=
{
```

```
"FD_FixedAsian_RodgerShi",
   {{"SpaceStepNumber",INT2,{2000},ALLOW },
    {"TimeStepNumber",INT2,{1000},ALLOW},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(FD_FixedAsian_RodgerShi),
    {{"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORB ID}, ,{" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(FD_FixedAsian_RodgerShi),
    CHK_ok,
    MET(Init)
};
```

References