```
   Help
#include "nig1d_std.h"
#include "pnl/pnl_integration.h"
#include "pnl/pnl_complex.h"
#include "pnl/pnl_specfun.h"
#include "pnl/pnl_mathtools.h"
#include "enums.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
     (2010+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(TR_MSS_NIG)(void *Opt, void *Mod)
{
  return NONACTIVE;
}
int CALC(TR_MSS_NIG)(void *Opt,void *Mod,PricingMethod *
    Met)
{
  return AVAILABLE_IN_FULL_PREMIA;
}
#else
static double sigma_g,theta_g,kappa_g,A,B,C,dt;

//-----------------------------------------------------------
    ----
//-----------------------------------------------------------
    ----
//-Density Function NIG
//-----------------------------------------------------------
    ----
static double probdensityx(double x, void * p)// Bonne
{
  double y,bes,Cp;
  double t;
  t=dt;
  bes=pnl_bessel_k(1,B*sqrt(SQR(x)+SQR(t*sigma_g)/kappa_g))
    ;
  Cp= t*exp(t/kappa_g)*sqrt(SQR(theta_g)/kappa_g/SQR(sigma_
    g)+1/SQR(kappa_g))/M_PI;
  y=Cp*exp(A*x)*bes/sqrt(SQR(x)+SQR(t*sigma_g)/kappa_g);
```

```
  return y;
}

static double pt(double x,double z)
{
  double abserr,results;
  int neval;
  PnlFunc func;
  func.function =probdensityx;
  func.params = NULL;
  neval=50;
  pnl_integration_GK(&func,x,z,0.0001,1,&results,&abserr,&
    neval);

  return results;

}

static double Ldensity(double t,void *p)
{
  double y,besss;

  besss=pnl_bessel_k(1,B*fabs(t));

  y=C*exp(A*t)*besss/fabs(t);

  return y;
}

static double Levy(double x,double z)
{
  double abserr,results;
  int neval;
  PnlFunc func;
  func.function =Ldensity;
  func.params = NULL;
  neval=500;
  pnl_integration_GK(&func,x,z,0.0001,1,&results,&abserr,&
    neval);

  return results;
```

```
}

static double omegadensity(double t,void *p)
{
  double y,b;

  b=pnl_bessel_k(1,B*fabs(t));

  if(fabs(t)<=1)
  y=(exp(t)-1-t)*C*exp(A*t)*b/fabs(t);
  else
  y=(exp(t)-1)*C*exp(A*t)*b/fabs(t);

  return y;
}


static double iomega(double x,double z)
{
  double abserr,results;
  int neval;
  PnlFunc func;
  func.function =omegadensity;
  func.params = NULL;
  neval=500;
  pnl_integration_GK(&func,x,z,0.0001,1,&results,&abserr,&
    neval);

  return results;

}

static double Ldensityx2(double t,void *p)
{
  double y,be;

  be=pnl_bessel_k(1,B*fabs(t));

  y=C*fabs(t)*exp(A*t)*be;
```

```
  return y;
}

static double sigmabar2(double x,double z)
{
  double abserr,results;
  int neval;
  PnlFunc func;
  func.function =Ldensityx2;
  func.params = NULL;
  neval=5000;
  pnl_integration_GK(&func,x,z,0.0001,1,&results,&abserr,&
    neval);

  return results;

}

static int TreeNIG(int am,double S0,NumFunc_1  *p,double T,
    double r,double divid,double sigma,double theta,double kappa,
    int N,int flag_scheme,double *ptprice,double *ptdelta)
{
 double *P,*stock,*proba,*x;
  double dx;
  int i,j,k,N2,N_plus,N_minus,M;
  double exp_drift,dis,emp_mean,sum,sig,omega;

  sigma_g=sigma;
  theta_g=theta;
  kappa_g=kappa;

   //Lévy measure
  A=theta/SQR(sigma);
  B=sqrt(SQR(theta)+SQR(sigma)/kappa)/SQR(sigma);
  C=sqrt(SQR(theta)+SQR(sigma)/kappa)/(M_PI*sigma*sqrt(kapp
    a));

  N_plus=N;
  N_minus=N;
  M=N_plus+N_minus;
  N2=N*M;
```

```
//Memory allocation
P=(double *)malloc((N2+1)*sizeof(double));
stock=(double *)malloc((N2+1)*sizeof(double));
proba=(double *)malloc((M+1)*sizeof(double));
x=(double *)malloc((M+1)*sizeof(double));

//Time step
dt=T/(double)N;

//Space step
sig=sqrt(sigmabar2(-0.1,-0.0000001)+sigmabar2(0.0000001,0
  .1));
if(flag_scheme==1)
  dx=sig*sqrt(dt);
else
  dx=(0.5/T)*sigma*sqrt(dt);

for (i=0;i<=M;i++)
  proba[i]=0.;

if(flag_scheme==1) //Compute true transition probaiblities
  {
    sum=0.;
    for (i=0;i<=M;i++)
      {
        x[i]=-(double)N_minus*dx+(double)i*dx;
        if (i!=M/2)
          proba[i]=pt(x[i]-dx/2.,x[i]+dx/2.);
        sum+=proba[i];
      }
     proba[M/2]=1.-sum;
  }
else //Paper MLS
  {

    sum=0.;
    for (i=0;i<=M;i++)
      {
        x[i]=-(double)N_minus*dx+(double)i*dx;
```

```
        if (i!=M/2)
          {
            proba[i]=Levy(x[i]-dx/2.,x[i]+dx/2.)*dt;
            sum+=proba[i];
          }
      }
    proba[M/2]=1.-sum;
  }

//Compute expectation
emp_mean=0.;
for(i=0;i<=M;i++)
 if (fabs(proba[i])<=1)
      emp_mean+=proba[i]*x[i];

//Discounted probabilities
for (i=0;i<=M;i++)
  proba[i]*=exp(-r*dt);

/*Maturity condition*/
//Drift changement for the risk-neutral measure = -iomeg
  a(-100,100)
omega=iomega(-1,-0.0001)+iomega(0.00001,1)+iomega(1,20)+
  iomega(-20,-1);
dis=exp(-(r-omega)*dt+emp_mean);
exp_drift=exp((r-omega)*T-(double)N*emp_mean);

for(i=0;i<=N2;i++)
  {
    stock[i]=S0*exp_drift*exp(-(double)N*N_minus*dx+(
  double)i*dx);
    P[i]=(p->Compute)(p->Par,stock[i]);
  }

/*******************/
/*Backward Resolution*/
/*******************/
for (i=1;i<=N;i++)
  {
    for (j=0;j<=N2-M*i;j++)
      {
```

```
          //Compute Conditional Expectation
          sum=0.;
          for (k=0;k<=M;k++)
            sum+=proba[k]*P[j+k];
          P[j]=sum;

          //American case
          if(am)
            {
              P[j]=MAX(P[j],(p->Compute)(p->Par,stock[j+M/2
    *i]*pow(dis,(double)i)));
            }
        }

     //Delta
      if(i==N-1)
        *ptdelta=(P[M/2+1]-P[M/2-1])/(2*S0*dx);
    }

  //Price
  *ptprice=P[0];

  //Memory deallocation
  free(P);
  free(stock);
  free(proba);
  free(x);

  return OK;


  return OK;
}

int CALC(TR_MSS_NIG)(void *Opt,void *Mod,PricingMethod *
    Met)
{
  TYPEOPT* ptOpt=( TYPEOPT*)Opt;
  TYPEMOD* ptMod=( TYPEMOD*)Mod;
  double r,divid;
```

```
  r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

  return TreeNIG(ptOpt->EuOrAm.Val.V_BOOL,ptMod->S0.Val.V_
    PDOUBLE,
                ptOpt->PayOff.Val.V_NUMFUNC_1,ptOpt->Matu
    rity.Val.V_DATE-ptMod->T.Val.V_DATE,r,divid,ptMod->Sigma.Val
    .V_SPDOUBLE,ptMod->Theta.Val.V_DOUBLE,ptMod->Kappa.Val.V_
    DOUBLE,Met->Par[0].Val.V_INT2,Met->Par[1].Val.V_ENUM.value,&(
    Met->Res[0].Val.V_DOUBLE),&(Met->Res[1].Val.V_DOUBLE));
}

static int CHK_OPT(TR_MSS_NIG)(void *Opt, void *Mod)
{
  if ( (strcmp( ((Option*)Opt)->Name,"CallEuro")==0) || (
    strcmp( ((Option*)Opt)->Name,"PutEuro")==0||(strcmp( ((
    Option*)Opt)->Name,"CallAmer")==0) || (strcmp( ((Option*)Opt)->
    Name,"PutAmer")==0)))
    return OK;

  return WRONG;
}
#endif //PremiaCurrentVersion


static int MET(Init)(PricingMethod *Met,Option *Opt)
{
  static int first=1;

  if (first)
    {
      Met->Par[0].Val.V_INT2=100;
      Met->Par[1].Val.V_ENUM.value=1;
      Met->Par[1].Val.V_ENUM.members=&PremiaEnumSchemeTree
    MSS;
      first=0;
    }

  return OK;
}
```

```
PricingMethod MET(TR_MSS_NIG)=
{
  "TR_MSS_NIG",
  {{"TimeStepNumber",INT2,{100},ALLOW},
   {"Type of tree",ENUM,{100},ALLOW},
   {" ",PREMIA_NULLTYPE,{0},FORBID}},
  CALC(TR_MSS_NIG),
  {{"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORB
    ID},{" ",PREMIA_NULLTYPE,{0},FORBID}},
  CHK_OPT(TR_MSS_NIG),
  CHK_split,
  MET(Init)
};
```

References