

```

    Help
/*-----*/
/*   BERMUDAN SWAPTION PRICER           */
/* see LMM_bermudan_swptns.dvi   for   */
/* the DOC.                         */
/*-----*/
/*   Nicola Moreni, Premia 2005         */
/*-----*/

#include "lmm1d_std.h"
#include "enums.h"

#include "math/lmm/lmm_header.h"
#include "math/lmm/lmm_libor.h"
#include "math/lmm/lmm_products.h"
#include "math/lmm/lmm_volatility.h"
#include "math/lmm/lmm_basis.h"
#include "math/lmm/lmm_numerical.h"
#include "math/lmm/lmm_zero_bond.h"

#include <stdlib.h>
#include <string.h>

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2007+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(MC_PED)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_PED)(void *Opt,void *Mod,PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

static double (*Basis)(double *x, int i);
static int (*computeEvolution)(const PnlVect* ptRand,Libor*
    ptLibOld,Libor* ptLibNew,Volatility* ptVol,double dt,
    double t, double sigma_cost);

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static int check_parameters(float tenor , int numberTime
    Step, int *numFac, double swaptionMat , double swapMat ,
    double payoff_as_Regressor , long numberMCPaths , int *Regr_Basi
    s_Dimension , char* basis_name , char* measure_name , char
    Explanatory , double strike);
// added function for interface

/* Declaration of allocation/liberation/initialization rout
    ines.
    */
/*****
    *****/
/*          Auxiliary routines
    */
/*****

static void
mallocBermudaVar(double **RegrVar,double **Res,double** Br
    ownian,double** SwapPrices,
                double** Numeraire,double **FP, long numb
    erMCPaths,
                int ReprVarDimension,int ReprBasisDimensio
    n,int numberOfExerciseDates,
                int Brown_factors)
{
    if ((*RegrVar)==NULL){
        (*RegrVar)=(double*)malloc(numberMCPaths*RegrVarDimens
    ion*sizeof(double));
        if ((*RegrVar)==NULL) abort();
    }
    if ((*Res)==NULL){
        (*Res)=(double*)malloc(RegrBasisDimension*sizeof(
    double));
        if ((*Res)==NULL) abort();
    }
    if ((*Brownian)==NULL){
        (*Brownian)=(double*)malloc(numberMCPaths*numberOfExerc
    iseDates*Brown_factors*sizeof(double));
        if ((*Brownian)==NULL) abort();
    }
}

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    if ((*SwapPrices)==NULL){
        (*SwapPrices)=(double*)malloc(numberMCPaths*numberOfExerc
            iseDates*sizeof(double));
        if ((*SwapPrices)==NULL) abort();
    }
    if ((*Numeraire)==NULL){
        (*Numeraire)=(double*)malloc(numberMCPaths*numberOfExerc
            iseDates*sizeof(double));
        if ((*Numeraire)==NULL) abort();
    }
    if ((*FP)==NULL){
        (*FP)=(double*)malloc(numberMCPaths*sizeof(double));
        if ((*FP)==NULL) abort();
    }
}

static void freeBermudaVar(double **RegrVar,double **Res,
    double** Brownian,
                                double** SwapPrices,double**
    Numeraire, double **FP)
{

    free(*RegrVar);
    free(*Res);
    free(*Brownian);
    free(*SwapPrices);
    free(*Numeraire);
    free(*FP);
    (*RegrVar)=NULL;
    (*Res)=NULL;
    (*Brownian)=NULL;
    (*SwapPrices)=NULL;
    (*Numeraire)=NULL;
    *FP=NULL;
}

/*initialization of the Explicatory variable: Paying Value,
    Numeraire or Brownian Motion*/
static void
initStateVector(double *X,double *Brownian,double* SwapPric
    es,double *Numeraire,
                int j,long numberMCpaths,int numberOfExerc

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    iseDates,int numberOfFactors,char Rflag)
{
    int k,l;

    for(k=0;k<numberMCpaths;k++){
        if (Rflag=='B'){for(l=0;l<numberOfFactors;l++) X[k*number
            OfFactors+l]=Brownian[k*(numberOfFactors*numberOfExerciseD
            ates)+j*numberOfFactors+l];
        }
        else if(Rflag=='S') {X[k]=ppos(SwapPrices[k*numberOfEx
            erciseDates+j]);}
        else X[k]=Numeraire[k*numberOfExerciseDates+j];

    }
    return;
}

//*****
//*****/
//Regression FOR Bermudan Swaptions.
//It is of type
//    FP~scalprod(Res,VBase(X))
//with FP's,X's as inputs, Res as output.
//Least squares approach:
//Res=argmin_a[sum_k (FP^k-scalprod(a,VBase(X^k)))^2]
//Solution obtained by differentiating wrt to Res, rewrit
    ing as M*Res=AuxR and then
//finding Cholesky square root of M.
//We regress only on at the money path (exercising value ar
    e needed by algorithm)
//*****
//*****/
static void Regression(long NumberMCPaths,int numberOfExerc
    iseDates,

                        int RegrBasis_Dimension,
                        int X_Dimension,
                        int Swap_Entry_Time,
                        int PayOff_As_Regressor,
                        double* X,double* FP,double* Swap_
    Prices,

                        double* Res)
{

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int i,j;
double *XPaths_ptr=X,AuxOption;
PnlVect *AuxR=NULL,*VBase=NULL;
PnlMat *M = NULL;
long k,InTheMoney=0;

//Memory Allocation for auxiliary pointers
M=pnl_mat_create (RegrBasis_Dimension, ReprBasis_Dimension);
AuxR = pnl_vect_create (RegrBasis_Dimension);
VBase = pnl_vect_create (RegrBasis_Dimension);

//Initialisation of auxiliary pointers
pnl_vect_set_double (AuxR, 0.0);
pnl_mat_set_double (M, 0.0);

for(k=0;k<NumberMCPaths;k++){
    //kth regressor value
    AuxOption=ppos(Swap_Prices[k*numberOfExerciseDates+Swap_Entry_Time]);
    //only the at-the-money path are taken into account
    if (AuxOption>0){
        InTheMoney++;
        //value of the regressor basis on the kth path
        if (PayOff_As_Regressor<=Swap_Entry_Time){
            //here, the payoff function is introduced in the
            regression basis
            pnl_vect_set (VBase, 0, AuxOption);
            for (i=1;i<RegrBasis_Dimension;i++){
                pnl_vect_set (VBase, i, Basis(XPaths_ptr,i-1));
            }
        } else {
            for (i=0;i<RegrBasis_Dimension;i++){
                pnl_vect_set (VBase, i, Basis(XPaths_ptr,i));
            }
        }
        //empirical regressor dispersion matrix
        for (i=0;i<RegrBasis_Dimension;i++){
            for (j=0;j<RegrBasis_Dimension;j++){
                double tmp = pnl_mat_get (M, i, j);
            }
        }
    }
}

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        pnl_mat_set (M, i, j , tmp + pnl_vect_get (VBase,
i) *
                                pnl_vect_get (VBase,j));
    }

    for (i=0;i<RegrBasis_Dimension;i++){
        double tmp = pnl_vect_get(AuxR, i);
        pnl_vect_set (AuxR, i, FP[k] * pnl_vect_get (VBase,
i) + tmp);
    }
}
XPaths_ptr+=X_Dimension;
}
if (InTheMoney==0){
    for (i=0;i<RegrBasis_Dimension;i++) {Res[i]=0.;}
}
else {
    /* solve in the least square sense, using a QR decompo
sition */
    pnl_mat_ls (M, AuxR);
    memcpy (Res, AuxR->array, AuxR->size*sizeof(double));
}

pnl_mat_free(&M);
pnl_vect_free(&AuxR);
pnl_vect_free(&VBase);
}

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static int computeBermudeanSwaption(long numberMCPaths,int
    numberTimeStep,
                                Libor *ptLib, Swaption*
    ptSwpt, Volatility* ptVol,
                                int RegrBasisDimension,
                                double payoff_as_regres
    sor,
                                char* Basis_Choice,cha
    r* Measure_Choice,
                                char Explanatory,int generator,double 10
{

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int i,j,l;
long k;
double time,dt,AuxNumSpot,AuxOption,AuxScal;
double *X=NULL,*Res=NULL,*FP=NULL; //X is the state vector for regression
double *Brownian=NULL,*SwapPrices=NULL,*Numeraire=NULL;
double *W=NULL;
int s,numberOfExerciseDates,PayOff_As_Regressor;
int RegrVarDimension;
char auxstring[10];
char ErrorMessage[1000];
Libor *ptLibTemp=NULL;
Libor *ptLibOld;
PnlVect *ptRand;
ErrorMessage[0]='{0';

/*Initialization of Auxiliary Constants:time step for SDE discretization
(Euler scheme), index of first exercising date, payoffas regressor.....*/
dt=ptLib->tenor/(double)numberTimeStep;
s=(int)(ptSwpt->swaptionMaturity/ptLib->tenor);
numberOfExerciseDates=ptLib->numberOfMaturities-s;
PayOff_As_Regressor=(int)(payoff_as_regressor/ptLib->tenor)-s;
ptRand = pnl_vect_create (ptVol->numberOfFactors);

/*RegrVarDim,nametobasis,nametomeasure*/
if(Explanatory=='B') RegrVarDimension=ptVol->numberOfFactors;
else RegrVarDimension=1;
sprintf(auxstring,"%d",RegrVarDimension);
strcat(Basis_Choice,auxstring);/*Basis_Choice Must be "CanD$(Regr_Var_Dimension)" or "HerD$(Regr_Var_Dimension)"/
Name_To_Basis(ErrorMessage,Basis_Choice,&Basis,RegrVarDimension);
Name_To_Measure(ErrorMessage, Measure_Choice, &computeEvolution);

/*Bermuda Variables Memory Allocation*/
mallocLibor(&ptLibOld,ptLib->numberOfMaturities,ptLib->

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    tenor,10);
/*ptLibOld keeps record of the initial values*/
mallocLibor(&ptLibTemp,ptLib->numberOfMaturities,ptLib->
    tenor,10);
pnl_rand_init(generator,ptVol->numberOfFactors,numberMCPa
    ths);
mallocBermudaVar(&X,&Res,&Brownian,&SwapPrices,&Numeraire,
    &FP,numberMCPaths,RegrVarDimension,RegrBasisDimension,
    numberOfExerciseDates,ptVol->numberOfFactors);
W=(double*)malloc(ptVol->numberOfFactors*sizeof(double));

/*Libor Time evolution + record of Brownian Paths, Numeraire
    Paths and Swap Prices */
for(k=0;k<numberMCPaths;k++){
    time=0.0;
    AuxNumSpot=(1.0+ptLib->tenor*GET(ptLib->libor,0));/*Aux
    NumSpot=NumeraireSpot(T_1)*/
    copyLibor(ptLibOld,ptLib);
    Set_to_Zero(W,ptVol->numberOfFactors);

    for (j=0;j<=(ptLib->numberOfMaturities-2);j++){
        for(i=0;i<numberTimeStep;i++){
            /*time evolution from T_j+i*dt to T_j+(i+1)*dt*/
            pnl_vect_rand_normal (ptRand, ptVol->numberOfFactor
            s, generator);
            computeEvolution(ptRand,ptLib,ptLibTemp,ptVol,dt,
            time, sigma_cost);
            copyLibor(ptLibTemp,ptLib);
            time+=dt;
            for(l=0;l<ptVol->numberOfFactors;l++) W[l]+=(sqrt(
            dt)*GET(ptRand, l));
        }
        AuxNumSpot*=(1.0+ptLib->tenor*GET(ptLib->libor,j+1));
        /*AuxNumSpot=NumeraireSpot(T_{j+2})*/
        computeNumeraire(Measure_Choice,ptLib,ptSwpt,Numeraire,
        j,k,AuxNumSpot);
        if ((s-1)<=j) {
            SwapPrices[k*numberOfExerciseDates+(j+1-s)]=computeSwapPrice(
            ptLib,ptSwpt,j+1,j+1,ptLib->numberOfMaturities);
            for(l=0;l<ptVol->numberOfFactors;l++) Brownian[k*(
            numberOfExerciseDates*ptVol->numberOfFactors)+(j+1-s)*ptVol->

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    numberOfFactors+1]=W[1];

    }
    putLiborToZero(ptLib,j+1);

}

}

/*Backward programming

    Price at last Exercicio date is just exercise price */
for(k=0;k<numberMCPaths;k++)
{
    FP[k]=ppos(SwapPrices[k*numberOfExerciseDates+(number
erOfExerciseDates-1)]);
    //If s=e-1 the option is indeed European, actualiza
tion changes....
    if(numberOfExerciseDates==1)
    {
        FP[k]/=Numeraire[k*numberOfExerciseDates+0];
    }
    else
    {
        FP[k]*=(Numeraire[k*numberOfExerciseDates+(numb
erOfExerciseDates-2)]/Numeraire[k*numberOfExerciseDates+(
numberOfExerciseDates-1)]);
    }
}
//Price at time T_j: regression of FP over X(T_j))
for(j=numberOfExerciseDates-2;j>=0;j--)
{
    initStateVector(X,Brownian,SwapPrices,Numeraire,j,
    numberMCPaths,
        numberOfExerciseDates,ptVol->numberO
fFactors,Explanatory);
    Regression(numberMCPaths,numberOfExerciseDates,RegrB
asisDimension,ptVol->numberOfFactors,j,
        PayOff_As_Regressor,X,FP,SwapPrices,Res);

    for(k=0;k<numberMCPaths;k++){//exercise value

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        AuxOption=ppos(SwapPrices[k*numberOfExerciseDates+
j]);
        //approximated continuation value, only the at-the-
monney paths are taken into account
        if (AuxOption>0){
            // if PayOff_As_Regressor<=j, excercise value is
introduced into regression basis
            if (PayOff_As_Regressor<=j){
                AuxScal=AuxOption*Res[0];
                for (l=1;l<RegrBasisDimension;l++){
                    AuxScal+=Basis(X+k*RegrVarDimension,l-1)*Res[
1];
                }
            } else {
                AuxScal=0.;
                for (l=0;l<RegrBasisDimension;l++){
                    AuxScal+=Basis(X+k*RegrVarDimension,l)*Res[l]
;
                }
            }
            // AuxScal contains the approximated continuatio
n value
            // if AuxScal< exercise value, the optimal stopp
ing time is modified
            if (AuxOption>AuxScal){
                FP[k]=AuxOption;
            }
            //Discount Factor from time T_{s+j} to T_{s+j-1}}
            if(j>0) FP[k]*=(Numeraire[k*numberOfExerciseDates+
j-1]/Numeraire[k*numberOfExerciseDates+j]);
            //Discount from T_s downto time=0.0
            else FP[k]*=(1.0/Numeraire[k*numberOfExerciseDates+
0]);
        }
    }
}

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//price at time t=0.0 is only the mean discounted value
ptSwpt->price=0.0;

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for(k=0;k<numberMCPaths;k++){
    ptSwpt->price+=FP[k];
}
ptSwpt->price/=(double)numberMCPaths;

if (ErrorMessage[0] == '{0}')
    printf("Warning : {n}%s{n", ErrorMessage);
//freeing memory
freeBermudaVar(&X,&Res,&Brownian,&SwapPrices,&Numeraire,&
    FP);
freeLibor(&ptLibTemp);
freeLibor(&ptLibOld);
pnl_vect_free (&ptRand);
free(W);
return(1);
}

```

```

static double
lmm_swaption_payer_bermudan_LS_pricer(float tenor , int
    numberTimeStep,
                                int numFac, double
    swaptionMat, double swapMat,
                                double payoff_as_Reg
    regressor, long numberMCPaths,
                                int Regr_Basis_Dimens
    ion, char* basis_name ,
                                char* measure_name,
    char Explanatory, double strike,
                                int generator,
    double l0, double sigma_cost)
{
    // int numberTimeStep=10;
    // int numFac=1;
    // double swaptionMat in (years)
    // double swapMat in (years)
    // payoff_as_Regressor in (years) Maturity after which
    // payoff is included in regression
    // long numberMCPaths number of monte carlo paths
    // int Regr_Basis_Dimension=4; //finite-dimensional appro

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    x. of Lš
// char Explanatory = 'N' or 'B' or 'S' ---> Explanatory
    variable for regression B=Brownian, S=Nominal Swap Paying Value
    , N=Numeraire;
// int numMat ;          //WARNING: including T_0=0, maturities number is 'numMat+1'

Volatility *ptVol;
Libor *ptLib;
Swaption *ptSwpt;

double priceVal=0.20;
double K=strike;//strike
int numMat;
char Basis_Choice[10]; //See in the followings
char Measure_Choice[10];// " " " "
double p;
/*double DT=(tenor/(double)numberTimeStep);*/

check_parameters( tenor , numberTimeStep, &numFac, swaptionMat , swapMat , payoff_as_Regressor , numberMCPaths , &Regr_Basis_Dimension , basis_name , measure_name , Explanatory , strike);

strcpy(Basis_Choice,basis_name); //"CanD" for canonical basis or "HerD" for hermite
strcpy(Measure_Choice,measure_name); //"Spot" or "Fwd" cfr numerical.c for evolution

//Memory Allocation and Libor/Swap Structures Initialization
numMat=(int)(swapMat/tenor);

mallocLibor(&ptLib,numMat,tenor,10);
mallocVolatility(&ptVol,numFac,sigma_cost);
mallocSwaption(&ptSwpt,swaptionMat,swapMat,priceVal,K,tenor);

//Swaption Computation

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computeBermudeanSwaption(numberMCPaths,numberTimeStep,pt
    Lib,ptSwpt,ptVol,Regr_Basis_Dimension, payoff_as_Regressor,
    Basis_Choice,Measure_Choice,Explanatory,generator,l0,sigma_
    cost);

p=ptSwpt->price;
//Printing Results to STDOUTOutput
//printf("s=%d, e=%d, exdates=%d, payoffasregr=%d{n",s,pt
    Lib->numberOfMaturities,numberOfExerciseDates,PayOff_As_Reg
    ressor);

//initLibor(ptLib);
//I=computeSwaptionPriceSpot(numberMCPaths,numberTimeStep
    ,DT,ptLib,ptSwpt,ptVol);

//freeing Memory
freeSwaption(&ptSwpt);
freeLibor(&ptLib);
freeVolatility(&ptVol);

return(p);
}

static int
check_parameters(float tenor , int numberTimeStep, int *
    numFac, double swaptionMat,
                double swapMat , double payoff_as_Regres
    sor , long numberMCPaths,
                int *Regr_Basis_Dimension , char* basis_na
    me , char* measure_name ,
                char Explanatory , double strike)
{
    double s;
    double M;

    if(swaptionMat>=swapMat)
    {
        printf(" swaption maturity must be lower than swap
            maturity !{n");
        exit(-1);
    }
}

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    }
    s=(int)(swaptionMat/tenor);
    if (fabs(swaptionMat-s*tenor)> 0.00001)
    {
        printf(" swaption maturity must be a multiple of pe
        riode{n");
        exit(-1);
    }
    M=(int)(swapMat/tenor);
    if (fabs(swapMat-M*tenor)> 0.0)
    {
        printf(" swap maturity must be a multiple of period{
        n");
        exit(-1);
    }
    if((Explanatory!='N') && (Explanatory!='B') && (Explan
    atory!='S'))
    {
        printf("Explanatory variable must be either B, N or
        S {n");
        exit(-1);
    }
    if( *numFac>2 )
    {
        printf("Number of factors too high switching to 2 {n"
        );
        *numFac=2;
    }
    if( (*numFac==1) && (*Regr_Basis_Dimension>6))
    {
        printf("Regression basis dimension is too high swicth
        ing to 6 {n");
        *Regr_Basis_Dimension=6;
    }
    if( (*numFac==2) && (*Regr_Basis_Dimension>21))
    {
        printf("Regression basis dimension is too high swicth
        ing to 6 {n");
        *Regr_Basis_Dimension=6;
    }
    if( (payoff_as_Regressor<swaptionMat) || (payoff_as_Reg

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    reessor>(swapMat-tenor)) )
    {
        printf("payoff_as_Regressor value is not valid, must
        be within [ swaptionMat swapMat-tenor ] {n}");
        printf("choosing payoff_as_Regressor=swapMat-tenor wil
        l not include the payoff in the basis! {n}");
        exit(-1);
    }

    return(1);
}

static int
mc_pederesen_bermswaptionlmm1d(NumFunc_1 *p,double l0,
    double t0, double sigma,
                                int numFac,double swapMat,
    double swaptionMat,
                                int am,double Nominal,
    double strike,double tenor,
                                int generator,int numberTime
    Step,long numberMCPaths,double *price)
{
    int numMat;
    double* maturities;
    int Reqr_Basis_Dimension=4 ;    //finite-dimensional app
    rox. of Lš
    char Explanatory='N';           //Explanatory variable fo
    r regression B=Brownian,
    //          S=Nominal Swap Paying Value, N=Numera
    ire;
    char* basis_name="HerD";        //Hermite basis
    char* measure_name="Spot" ;    // spot " " " "
    double payoff_as_Regressor; //(years) Maturity after whic
    h payoff is included in regression

    swapMat=swapMat-t0;
    swaptionMat=swaptionMat-t0;

    payoff_as_Regressor=swaptionMat+tenor;
    numMat=(int)(swapMat/tenor);

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maturities=(double*)malloc(numMat*sizeof(double));

/* if ((p->Compute)==&Put) */
/*   payer_or_receiver=1; */
/* else */
/*   if ((p->Compute)==&Call) */
/*     payer_or_receiver=0; */

*price = Nominal * lmm_swaption_payer_bermudan_LS_pricer(
    tenor ,numberTimeStep, numFac, swaptionMat , swapMat,payoff_
    as_Regressor,numberMCPaths,Regr_Basis_Dimension ,basis_name,
    measure_name , Explanatory,strike,generator,l0,sigma);

free(maturities);

return OK;
}

int CALC(MC_PED)(void *Opt,void *Mod,PricingMethod *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;

    return mc_pederesen_bermswaptionlmm1d(ptOpt->PayOff.Val.
        V_NUMFUNC_1,ptMod->l0.Val.V_PDOUBLE,
                                                    ptMod->T.Val.V_DA
        TE,
                                                    ptMod->Sigma.Val.V_
        PDOUBLE,
                                                    ptMod->NbFactors.
        Val.V_ENUM.value,
                                                    ptOpt->BMaturity.
        Val.V_DATE,
                                                    ptOpt->OMaturity.
        Val.V_DATE,
                                                    ptOpt->EuOrAm.Val.
        V_BOOL,
                                                    ptOpt->Nominal.Val.
        V_PDOUBLE,
                                                    ptOpt->FixedRate.
        Val.V_PDOUBLE,

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Val.V_DATE,
ENUM.value,
PINT,
LONG,
V_DOUBLE));

ptOpt->ResetPeriod.
Met->Par[0].Val.V_
Met->Par[1].Val.V_
Met->Par[2].Val.V_
&(Met->Res[0].Val.

}

static int CHK_OPT(MC_PED)(void *Opt, void *Mod)
{
    if ((strcmp(((Option*)Opt)->Name,"PayerBermudanSwaption")
        ==0))
        return OK;
    else
        return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_ENUM.value=0;
        Met->Par[0].Val.V_ENUM.members=&PremiaEnumRNGs;
        Met->Par[1].Val.V_INT=10;
        Met->Par[2].Val.V_LONG=10000;
    }
    return OK;
}

PricingMethod MET(MC_PED)=
{

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"MC_Pedersen_BermSwaption",
{{"RandomGenerator",ENUM,{100},ALLOW},
 {"Time Steps",INT,{100},ALLOW},
 {"N Simulation",LONG,{100},ALLOW},
 {" ",PREMIA_NULLTYPE,{0},FORBID}},
CALC(MC_PED),
{{"Price",DOUBLE,{100},FORBID}/*,{"Delta",DOUBLE,{100},FORBID}*/ ,{" ",PREMIA_NULLTYPE,{0},FORBID}},
CHK_OPT(MC_PED),
CHK_ok,
MET(Init)
} ;

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References