```
Help
#include "lrshjm1d stdi.h"
#include "math/InterestRateModelTree/TreeLRS1D/TreeLRS1D.h"
#include "pnl/pnl vector.h"
#include "math/read market zc/InitialYieldCurve.h"
//The "#else" part of the code will be freely available aft
    er the (year of creation of this file + 2)
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <</pre>
     (2007+2)
static int CHK_OPT(TR_ZCBondLRS1D)(void *Opt, void *Mod)
 return NONACTIVE;
}
int CALC(TR ZCBondLRS1D)(void *Opt,void *Mod,PricingMethod
    *Met)
{
return AVAILABLE_IN_FULL_PREMIA;
#else
/// TreeLRS1D : structure that contains components of
    the tree (see TreeLRS1D.h)
/// ModelLRS1D : structure that contains the paramete
    rs of the Hull&White one factor model (see TreeLRS1D.h)
/// ZCMarketData : structure that contains the Zero Coupon
    Bond prices of the market, or given by a constant yield-to-
    maturity (see InitialYieldCurve.h)
/// Computation of the payoff at the final time of the tre
    e (ie the ZCBond maturity)
static void ZCBond_InitialPayoffLRS1D(TreeLRS1D* Meth, PnlV
    ect* OptionPriceVect2)
{
    pnl vect resize(OptionPriceVect2, 6*(Meth->Ngrid) - 3);
    pnl_vect_set_double(OptionPriceVect2, 1.0); // Payoff =
     1 for a ZC bond
}
/// Backward computation of the price of a Zero Coupon Bond
```

```
static void ZCBond BackwardIterationLRS1D(TreeLRS1D* Meth,
   ModelLRS1D* ModelParam, ZCMarketData* ZCMarket, PnlVect*
   OptionPriceVect1, PnlVect* OptionPriceVect2, int index_last,
   int index first)
{
   double sigma, rho, kappa, lambda;
   int i, j, h;
   double delta_y, delta_t, sqrt_delta_t;
   double price_up, price_middle, price_down;
   double y_00, y_ih, r_ih, phi_ihj, phi_next;
   PnlVect* proba_from_ij;
   proba_from_ij = pnl_vect_create(3);
   ///***** Model parameters ******///
   kappa = (ModelParam->Kappa);
   sigma = (ModelParam->Sigma);
   rho = (ModelParam->Rho);
   lambda = (ModelParam->Lambda);
   delta_t = GET(Meth->t, 1) - GET(Meth->t,0);
   y_00 = r_to_y(ModelParam, -log(BondPrice(GET(Meth->t, 1
   ), ZCMarket))/delta t);
   for(i = index last-1; i>=index first; i--)
       pnl_vect_resize(OptionPriceVect1, 6*i-3); //
   OptionPriceVect1 := Price of the bond in the tree at time t(i)
        delta_t = GET(Meth->t, i+1) - GET(Meth->t,i);
        sqrt delta t = sqrt(delta t);
       delta y = lambda * sqrt delta t;
       for( h=0; h<=2*i; h++) /// h : numero de la box
            y_{ih} = y_{00} + (i-h) * delta_y;
            r_ih = y_to_r(ModelParam, y_ih);
```

```
for(j=0;j<number_phi_in_box(i, h);j++) /// Bouc</pre>
    le sur les valeurs de phi à (i,h)
                phi ihj = phi value(Meth, i, h, j);
                phi_next = phi_ihj * (1-2*kappa*delta_t) +
    SQR(sigma) * pow(y to r(ModelParam, y ih), (2*rho)) * delt
    a_t;
                price_up
                           = Interpolation(Meth, i+1, h
    , OptionPriceVect2, phi next);
                price_middle = Interpolation(Meth, i+1, h+1
    , OptionPriceVect2, phi_next);
                price_down = Interpolation(Meth, i+1, h+2
    , OptionPriceVect2, phi_next);
                probabilities(GET(Meth->t,i), y_ih, phi_ih
    j, lambda, sqrt_delta_t, ModelParam, ZCMarket, proba_from_
    ij);
                LET(OptionPriceVect1, index_tree(i,h,j)) =
    exp(-r_ih*delta_t) * (GET(proba_from_ij,0) * price_up + GET(
    proba from ij,1) * price middle + GET(proba from ij,2) *
    price down );
            }
        }
        pnl_vect_clone(OptionPriceVect2, OptionPriceVect1);
     // Copy OptionPriceVect1 in OptionPriceVect2
    } // END of the loop on i (time)
   pnl vect free(&proba from ij);
/// Price at time "s" of a ZC bond maturing at "T" using a
    trinomial tree.
```

}

```
static double tr lrs1d zcbond(TreeLRS1D* Meth, ModelLRS1D*
   ModelParam, ZCMarketData* ZCMarket, double T, double s, double
   r)
{
   double lambda;
   double delta_y; // delta_x1 = space step of the proces
   s x at time i ; delta x2 same at time i+1.
   double delta_t, sqrt_delta_t; // time step
   double OptionPrice, OptionPrice1, OptionPrice2;
   int is, hr;
   double theta;
   double y_r, y_ih, y_00, r_00;
   PnlVect* proba_from_ih;
   PnlVect* OptionPriceVect1; // Matrix of prices of the
   option at i
   PnlVect* OptionPriceVect2; // Matrix of prices of the
   option at i+1
   proba_from_ih = pnl_vect_create(3);
   OptionPriceVect1 = pnl_vect_create(1);
   OptionPriceVect2 = pnl vect create(1);
   ///***** Model parameters ******///
   lambda = (ModelParam->Lambda);
   ff at the maturity of the option ************///
   ZCBond InitialPayoffLRS1D(Meth,OptionPriceVect2);
   ///************* Backward computation of the
   option price until time s************///
   i_s = indiceTimeLRS1D(Meth, s); // Localisation of s on
    the tree
   delta_t = GET(Meth->t, 1) - GET(Meth->t,0);
   sqrt_delta_t = sqrt(delta_t);
```

```
r 00 = -log(BondPrice(GET(Meth->t, 1), ZCMarket))/delt
a_t;
y_00 = r_{to}y(ModelParam, r_00);
if(i s==0) // If s=0
    ZCBond BackwardIterationLRS1D(Meth, ModelParam, ZCM
arket, OptionPriceVect1, OptionPriceVect2, Meth->Ngrid, 1);
    probabilities(GET(Meth->t,0), y_00, 0, lambda, sq
rt delta t, ModelParam, ZCMarket, proba from ih);
    OptionPrice = exp(-r_00*delta_t) * ( GET(proba_fro
m_ih,0) * GET(OptionPriceVect1, 0) + GET(proba_from_ih,1) *
GET(OptionPriceVect1,1) + GET(proba_from_ih,2) * GET(
OptionPriceVect1, 2));
}
else
    // We compute the price of the option as a linear
interpolation of the prices at the nodes r(i_s,j_r) and r(i_s,
j_r+1)
   delta_t = GET(Meth->t, i_s+1) - GET(Meth->t,i_s);
    sqrt delta t = sqrt(delta t);
    delta y = lambda * sqrt delta t;
   y_r = r_to_y(ModelParam, r);
   h_r = (int) floor(i_s - (y_r-y_00)/delta_y); // y_
r between y(h r) et y(h r+1) : y(h r+1) < y r <= y(h r)
   y_{ih} = y_{00} + (i_s-h_r) * delta_y;
    if(h r < 0 || h r > 2*i s)
     printf("WARNING : Instantaneous futur spot rate
is out of tree\{n"\};
     exit(EXIT_FAILURE);
```

```
ZCBond BackwardIterationLRS1D(Meth, ModelParam, ZCM
    arket, OptionPriceVect1, OptionPriceVect2, Meth->Ngrid, i_
    s);
        theta = (y_ih - y_r)/delta_y;
        OptionPrice1 = MeanPrice(Meth, i s, h r, OptionPric
    eVect2); //Interpolation(Meth, i_s, h_r , OptionPriceVect2
    , phi0);
        OptionPrice2 = MeanPrice(Meth, i s, h r+1, OptionP
    riceVect2); // Interpolation(Meth, i_s, h_r+1 , OptionPric
    eVect2, phi0);
        OptionPrice = (1-theta) * OptionPrice1 + theta *
    OptionPrice2 ;
    }
    pnl vect free(& OptionPriceVect1);
    pnl vect free(& OptionPriceVect2);
    pnl_vect_free(&proba_from_ih);
   return OptionPrice;
}
static int tr_zcbond1d(int flat_flag,double t,double r0,
    double kappa, double sigma, double rho, double lambda, double T,
    int N_steps,double *price)
{
    TreeLRS1D Tr;
    ModelLRS1D ModelParams;
    ZCMarketData ZCMarket;
    //N_steps = 300;
    //T = 6;
    /* Flag to decide to read or not ZC bond datas in "ini
    tialyields.dat" */
```

```
/* If P(0,T) not read then P(0,T)=\exp(-r0*T) */
if(flat_flag==0)
{
    ZCMarket.FlatOrMarket = 0;
    ZCMarket.Rate = r0;
}
else
    ZCMarket.FlatOrMarket = 1;
    ReadMarketData(&ZCMarket);
  if(T > GET(ZCMarket.tm, ZCMarket.Nvalue-1))
      printf("{nError : time bigger than the last time
value entered in initialyield.dat{n");
      exit(EXIT_FAILURE);
  }
ModelParams.Kappa = kappa;
ModelParams.Sigma = sigma;
ModelParams.Rho = rho;
ModelParams.Lambda = lambda;
// Construction of the Time Grid
SetTimegridLRS1D(&Tr, N steps, t, T);
// Construction of the tree, calibrated to the initial
yield curve
SetTreeLRS1D(&Tr, &ModelParams, &ZCMarket);
//Price of Zero Coupon Bond
*price = tr_lrs1d_zcbond(&Tr, &ModelParams, &ZCMarket,
T, t, r0);
DeleteTreeLRS1D(&Tr);
DeleteZCMarketData(&ZCMarket);
return OK;
```

}

```
int CALC(TR_ZCBondLRS1D)(void *Opt,void *Mod,PricingMethod
   *Met)
{
 TYPEOPT* ptOpt=(TYPEOPT*)Opt;
 TYPEMOD* ptMod=(TYPEMOD*)Mod;
 return tr_zcbond1d( ptMod->flat_flag.Val.V_INT,
                   ptMod->T.Val.V DATE,
                   MOD(GetYield)(ptMod),
                   ptMod->Kappa.Val.V_DOUBLE,
                   ptMod->Sigma.Val.V PDOUBLE,
                   ptMod->Rho.Val.V_PDOUBLE,
                   ptMod->Lambda.Val.V_PDOUBLE,
                   ptOpt->BMaturity.Val.V DATE,
                   Met->Par[0].Val.V LONG,
                   &(Met->Res[0].Val.V_DOUBLE));
static int CHK OPT(TR ZCBondLRS1D)(void *Opt, void *Mod)
 if ((strcmp(((Option*)Opt)->Name, "ZeroCouponBond")==0) )
   return OK;
 else
   return WRONG;
#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
 if (Met->init == 0)
   {
     Met->init=1;
     Met->Par[0].Val.V_LONG=100;
   }
```

```
return OK;
}

PricingMethod MET(TR_ZCBondLRS1D) =
{
    "TR_LRS1D_ZCBond",
    {{"TimeStepNumber",LONG,{100},ALLOW},
        {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(TR_ZCBondLRS1D),
    {{"Price",DOUBLE,{100},FORBID},{" ",PREMIA_NULLTYPE,{0},
        FORBID}},
    CHK_OPT(TR_ZCBondLRS1D),
    CHK_ok,
    MET(Init)
};
```

## References