

Help

```

extern "C"{
#include "temperedstable1d_std.h"
}

#include "math/numerics.h"
#include "math/fft.h"

extern "C"{

    static const int step=1;
    static const double xmax=1.6;
    static const double xmin=-1.2;
    static const double eps=1e-004;
    //static const double er=1e-008;
    //static const double minaccur=1e-008;
    static const double hh=0.002;
    /*static char *pfname="iprices.dat";
    static char *ebfname="iearly.dat";
    static char *pftitle="Option prices {n Spot {t Option
    Price{n";
    static char *ebftitle="Early exercise boundaries {n
    Time {t Boundary{n";*/

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2008+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(FD_KLZ_EPUT)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(FD_KLZ_EPUT)(void *Opt,void *Mod,PricingMethod *
    Met)
{
return AVAILABLE_IN_FULL_PREMIA;
}
#else

    static double intlpl(long k, double lp, double h, double
        nu,
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        double c, double er);
static double intlpo(long k, double lp, double h, double
    nu,
        double c, double er);
static double intlpl(long k, double lp, double h, double
    nu,
        double c, double er);
static double intlpp(long k, double lp, double h, double
    nu,
        double c, double er);
static void fillarray(double *v1, double *v2, long int N)
;
static void conffft(double *creal, double *cimage, double
    *v,
        double *vreal, double *vimage, double
    *res,
        double *resimage, long int n, long
    int m, long int Nbin, int d);
static void strike_correct(double strike, double *zz,
    long int N, int islog);
/*static void printoutDA(PnlVect *ptDA1, PnlVect *ptDA2,
    char *foutname, char *strtitle);*/
/*////////////////////////////////////*/
static int fds_ts_europut(double lm, double lp,
    double alpha_plus, double alpha_
    minus, double c_plus,
    double c_minus,
    double r, double divid,
    double T, double h, double Stri
    ke,
    double Spot,
    double eps, long errr, int step
    ,
    double *Price)
{
    double *t, *y, *HH, *v1, *payoff;
    long int N1, Nx, Ns, Nf, Nbin;
    double *v2;
    double *v3;
    double *tmp, *ureal, *uimage, *zreal, *zimage;
    double *vreal, *vimage, *tmpimage;

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PnlVect *TP, *EEB, *SP, *PP;

double *cp, *cm, *p, *cmm, *cpp, *ccm, *ccp,*alp,*alm;
long int *Lm;
double a2=0.;
double er, minaccur;

double logSpot;

double lpnu=exp(alpha_plus*log(lp));
double lmnu=exp(alpha_minus*log(lm));
double gamma_plus=tgamma(-alpha_plus);
double gamma_minus=tgamma(-alpha_minus);

double Am=-log(eps/c_minus/lmnu)/lm;
double Ap=-log(eps/c_plus/lpnu)/lp;
double mA=Ap>Am ? Ap :Am;

long int j, L;
long int kmax=(long int)ceil(mA/h);

//!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!
double mu=r-divid+c_minus*gamma_minus*(lmnu-exp(alpha_
minus*log(lm+1)))+c_plus*gamma_plus*(lpnu-exp(alpha_plus*
log(lp-1)));

//!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!

Ns=(long int)ceil((xmax-xmin)/h);
long int Nmax=Ns+kmax;
Nf=Nmax+kmax;
long int N0=(long int)ceil(-xmin/h)+kmax;
Nbin=2;
while(Nbin<Nf) Nbin*=2;
long int k;
double accur;
double dt;

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double sum_m;
double sum_p;
double cc00;

Nx=Nmax; /*number of space points*/

/*Memory allocation for space grid*/

cp=(double *)calloc(kmax+1,sizeof(double));
if (cp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
cm=(double *)calloc(kmax+1,sizeof(double));
if (cm==NULL)
    return MEMORY_ALLOCATION_FAILURE;
cpp=(double *)calloc(kmax+1,sizeof(double));
if (cpp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
cmm=(double *)calloc(kmax+1,sizeof(double));
if (cmm==NULL)
    return MEMORY_ALLOCATION_FAILURE;
ccp=(double *)calloc(kmax+1,sizeof(double));
if (ccp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
ccm=(double *)calloc(kmax+1,sizeof(double));
if (ccm==NULL)
    return MEMORY_ALLOCATION_FAILURE;
alp=(double *)calloc(kmax+1,sizeof(double));
if (alp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
alm=(double *)calloc(kmax+1,sizeof(double));
if (alm==NULL)
    return MEMORY_ALLOCATION_FAILURE;
ureal=(double *)calloc(Nbin,sizeof(double));
if (ureal==NULL)
    return MEMORY_ALLOCATION_FAILURE;
uimage=(double *)calloc(Nbin,sizeof(double));
if (uimage==NULL)
    return MEMORY_ALLOCATION_FAILURE;
zreal=(double *)calloc(Nbin,sizeof(double));
if (zreal==NULL)
    return MEMORY_ALLOCATION_FAILURE;

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zimage=(double *)calloc(Nbin,sizeof(double));
if (zimage==NULL)
    return MEMORY_ALLOCATION_FAILURE;
y=(double *)calloc(Nmax+1,sizeof(double)); /*space
grid points*/
if (y==NULL)
    return MEMORY_ALLOCATION_FAILURE;
payoff=(double *)calloc(Nmax+1,sizeof(double));
if (payoff==NULL)
    return MEMORY_ALLOCATION_FAILURE;
v1=(double *)calloc(Nmax+1,sizeof(double));/*prices at
previous time step*/
if (v1==NULL)
    return MEMORY_ALLOCATION_FAILURE;
v2=(double *)calloc(Nmax+1,sizeof(double));/*current
price*/
if (v2==NULL)
    return MEMORY_ALLOCATION_FAILURE;
v3=(double *)calloc(Nmax+1,sizeof(double));/*previous
iteration form current time step*/
if (v3==NULL)
    return MEMORY_ALLOCATION_FAILURE;
vreal=(double *)calloc(Nbin,sizeof(double));
if (vreal==NULL)
    return MEMORY_ALLOCATION_FAILURE;
vimage=(double *)calloc(Nbin,sizeof(double));
if (vimage==NULL)
    return MEMORY_ALLOCATION_FAILURE;
tmpimage=(double *)calloc(Nbin,sizeof(double));
if (tmpimage==NULL)
    return MEMORY_ALLOCATION_FAILURE;

tmp=(double *)calloc(Nbin,sizeof(double));/*previous
iteration form current time step*/
if (tmp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
TP=(PnlVect *)calloc(1,sizeof(PnlVect));/*time grid po
ints*/
if (TP==NULL)
    return MEMORY_ALLOCATION_FAILURE;
EEB=(PnlVect *)calloc(1,sizeof(PnlVect));/*early exerc

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sum_p=intlp1(kmax, lp, h, alpha_plus, c_plus, er);
sum_m=intlp1(kmax, lm, h, alpha_minus, c_minus, er);

cc00=(cp[1]+sum_p)/pow(h,alpha_plus)+(cm[1]+sum_m)/pow(
h,alpha_minus);

/*number of time steps*/
N1=step*(1+(long int)ceil(3*T*(fabs(mu/h)+cc00)/2));
//!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!!!!!!!!!

/*Memory allocation for time grid*/
Lm=(long int *)calloc(N1+2,sizeof(long int));
if (Lm==NULL)
    return MEMORY_ALLOCATION_FAILURE;
t=(double *)calloc(N1+2,sizeof(double)); /*time points*/
/
if (t==NULL)
    return MEMORY_ALLOCATION_FAILURE;
HH=(double *)calloc(N1+2,sizeof(double));/*early exerc
ise boundaries*/
if (HH==NULL)
    return MEMORY_ALLOCATION_FAILURE;

HH[1]=N1;
Lm[1]=N0;

/*Time step*/
dt=T/N1;
t[1]=0;
t[2]=dt;

//!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!!!!!1
if (mu>0)
{
    a2=1+dt*(mu/h+cc00+r-divid);
}
if (mu<=0)
{

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        a2=1+dt*(-mu/h+cc00+r-divid);
    }
//!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!
!!!!!!!!!!!!!!!!!!!!!!!!!!!!

k=0;
while(k<kmax-1)
{
    k++;
    alp[k]=dt*(ccp[k]+cp[k])/pow(h,alpha_plus)/a2;
    alm[k]=dt*(ccm[k]+cm[k])/pow(h,alpha_minus)/a2;
}

if (mu>0)
{
    alp[1]=alp[1]+dt*mu/h/a2;
}

if (mu<=0)
{
    alm[1]=alm[1]-dt*mu/h/a2;
}
alp[kmax]=dt*cp[kmax]/pow(h,alpha_plus)/a2;
alm[kmax]=dt*cm[kmax]/pow(h,alpha_minus)/a2;

for(j=0;j<kmax;j++)
{ ureal[j]=alp[kmax-j];
  uimage[j]=0;
  zreal[j]=alm[j+1];
  zimage[j]=0;
}
for(j=kmax;j<Nbin;j++)
{ ureal[j]=0;
  uimage[j]=0;
  zreal[j]=0;
  zimage[j]=0;
}
fft1d(ureal, uimage, Nbin, -1);

fft1d(zreal, zimage, Nbin, -1);

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k=0;

/*Put Pay-off function*/
for(j=0;j<N0;j++)
{
    y[j]=(j-N0)*h;
    payoff[j]=1-exp(y[j]);
}
for(j=N0; j<=Nx;j++)
{
    y[j]=(j-N0)*h;
    payoff[j]=0;
}

fillarray(v1, payoff, Nmax+1);
fillarray(v2, payoff, Nmax+1);

minaccur=eps/(N1+1)/3.0;

/*Main Loop on time grid*/
for(L=2; L<=N1+1; L++)
{
    t[L]=t[L-1]+dt;
    //j=Lm[L-1]+2; /*early exercise boundary */
    //ereq=1;
    /* first approximation*/
    /* computation of the price to the left to the bound
dary */

    /*computation of the price to the right */
    confit(ureal, uimage, v1, vreal, vimage, tmp, tmpi
mage, Ns, kmax, Nbin, 1);
    v2[1]=v1[1]/a2+tmp[0];
    for(j=2;j<=Nmax;j++)
    {
        v2[j]=v1[j]/a2+tmp[j-1];
    }
}

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    conffft(zreal, zimage, v1, vreal, vimage, tmp, tmpi
mage, Ns, kmax, Nbin, -1);
    v2[1]+=tmp[Nbin-1];
    for(j=2;j<=Nmax;j++)
    {
        v2[j]+=tmp[j-2];
    }

    fillarray(v3, v2, Nmax+1);

    /*Iterative solution for prices*/
    accur=0;

    /*computation of residual*/
    for(j=1;j<=Nmax;j++)
    {
        if (fabs(v1[j]-v2[j])>accur)
        {
            accur=fabs(v1[j]-v2[j]);
        }
    }

    /* iterative computation of price */
    while (accur>minaccur)
    {
        accur=0;
        //j=Lm[L-1]+2;
        //ereq=1;

        /* computation of the price to the left to the
boundary */

        /* computation of the price to the right */

        conffft(ureal, uimage, v3, vreal, vimage, tmp,
tmpimage, Ns, kmax, Nbin, 1);
        v2[1]=v1[1]/a2+tmp[0];
        for(j=2;j<=Nmax;j++)
        {
            v2[j]=v1[j]/a2+tmp[j-1];

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    }

    conffft(zreal, zimage, v3, vreal, vimage, tmp,
tmpimage, Ns, kmax, Nbin, -1);
    v2[1]+=tmp[Nbin-1];
    for(j=2;j<=Nmax;j++)
    {
        v2[j]+=tmp[j-2];
        if (fabs(v2[j]-v3[j])>accur)
        {
            accur=fabs(v2[j]-v3[j]);
        }
    }

    fillarray(v3, v2, Nmax+1);

    }
    p=v1;
    v1=v2;
    v2=p;
}

/*Memory desallocation*/
free(cp);
free(cm);
free(cpp);
free(cmm);
free(ccp);
free(ccm);
free(alp);
free(alm);
free(v2);
free(v3);
free(Lm);
free(vreal);
free(vimage);
free(tmp);
free(tmpimage);
free(ureal);
free(uimage);

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    free(zreal);
    free(zimage);

    logSpot=log(Spot/Strike);
    j=(long int)ceil((logSpot-xmin)/h)+kmax;

    strike_correct(Strike, y, Nx+1, 1);
    strike_correct(Strike, v1, Nx+1, 0);
    strike_correct(Strike, HH, N1+1, 0);

    *Price=(Spot-y[j])/(y[j+1]-y[j])*(v1[j+1]-v1[j])+v1[j];

    // SP->size=Nx+1;
    // SP->array=y;
    // PP->size=Nx+1;
    // PP->array=v1;
    TP->size=N1+1;
    TP->array=t;
    EEB->size=N1+1;
    EEB->array=HH;

    //printf("Look 'iprices.dat' for results{n");
    // printoutDA(SP, PP, pfname, pftitle);

    return OK;
}
/*////////////////////////////////////*/
static void conffft(double *creal, double *cimage, double
    *v,
                    double *vreal, double *vimage, double
    *res,
                    double *resimage, long int n, long
    int m, long int Nbin, int d)
{

    long int Nz=Nbin-n-m-m;
    long int j;

    if(d>0)

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    {
        for(j=0; j<n; j++)
            {
                vreal[j]=v[m+j+1];
                vimage[j]=0;
            }
        for(j=n; j<n+m+Nz; j++)
            {
                vreal[j]=0;
                vimage[j]=0;
            }
        for(j=1; j<m+1; j++)
            {
                vreal[n+m+Nz-1+j]=v[j];
                vimage[n+m+Nz-1+j]=0;
            }
    }
else
    {
        for(j=0; j<n+m; j++)
            {
                vreal[j]=v[j+1];
                vimage[j]=0;
            }
        for(j=n+m; j<Nbin; j++)
            {
                vreal[j]=0;
                vimage[j]=0;
            }
    }

fft1d(vreal, vimage, Nbin, -1);

for(j=0; j<Nbin; j++)
    {
        res[j]=creal[j]*vreal[j]-cimage[j]*vimage[j];
        resimage[j]=cimage[j]*vreal[j]+creal[j]*vimage[j];
    }
fft1d(res, resimage, Nbin, 1);
}

/*////////////////////////////////////////*/
static void fillarray(double *v1, double *v2, long int N)
{
    long int j;
    for(j=0; j<N; j++)
        v1[j]=v2[j];
}

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}

/*////////////////////////////////////////*/
static void strike_correct(double strike, double *zz, long
    int N, int islog)
{
    long int j;
    if (islog)
        for(j=0;j<N;j++)
            zz[j]=strike*exp(zz[j]);
    else
        for(j=0;j<N;j++)
            zz[j]=strike*zz[j];
}

/*////////////////////////////////////////*/
static double intlp(long k, double lp, double h, double
    nu,
                    double c, double er)
{
    double err=1;
    long int j, n=1;
    double st=0.5;
    double w, s1, s2, v1, v2, res;
    s1=exp(-lp*(k+1)*h)*pow(k+1, -1-nu);
    s2=exp(-lp*(k+st)*h)*pow(k+st, -1-nu)*st;
    v2=st*(s1+4.0*s2)/3.0;
    v1=0;

    n=2;

    while(err>er)
    {
        v1=v2;
        s1+=2.0*s2;
        s2=0;
        w=k+st/2.0;
        for(j=1;j<=n;j++)
        {
            s2+=exp(-lp*w*h)*pow(w,-1-nu)*(w-k);

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        w+=st;
    }
    st=st/2.0;
    n=n*2;
    v2=st*(s1+4.0*s2)/3.0;
    err=v2>0?fabs((v1-v2)/v2):1;
    if(n>1200000) err=er/2.0;

}

res=c*v2;
return res;
}

/*////////////////////////////////////*/
static double intl0(long k, double lp, double h, double
    nu,
                double c, double er)
{
    double err=1;
    long int j, n=1;
    double st=0.5;
    double w, s1, s2, v1, v2, res;
    s1=exp(-lp*h);
    s2=exp(-lp*st*h)*pow(st, 3-nu);
    v2=st*(s1+4.0*s2)/3.0;
    v1=0;

    n=2;

    while(err>er)
    {
        v1=v2;
        s1+=2.0*s2;
        s2=0;
        w=st/2.0;
        for(j=1;j<=n;j++)
        {
            s2+=exp(-lp*w*h)*pow(w,3-nu);
            w+=st;

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        }
        st=st/2.0;
        n=n*2;
        v2=st*(s1+4.0*s2)/3.0;
        err=v2>0?fabs((v1-v2)/v2):1;
        if(n>1200000) err=er/2.0;

    }

    res=c*(v2*pow(lp*h,3)/(2-nu)/(3-nu)/(1-nu)+exp(-lp*h)*(
    1+lp*h/(2-nu)+pow(lp*h,2)/(2-nu)/(3-nu))/(1-nu));
    return res;
}

/*////////////////////////////////////*/
static double intlpp(long k, double lp, double h, double
    nu,
                        double c, double er)
{
    double err=1;
    long int j, n=1;
    double st=0.5;
    double w, s1, s2, v1, v2, res;
    s1=exp(-lp*k*h)*pow(k, -1-nu);
    s2=exp(-lp*(k+st)*h)*pow(k+st, -1-nu)*0.5;
    v2=st*(s1+4.0*s2)/3.0;
    v1=0;

    n=2;

    while(err>er)
    {
        v1=v2;
        s1+=2.0*s2;
        s2=0;
        w=k+st/2.0;
        for(j=1;j<=n;j++)
        {
            s2+=exp(-lp*w*h)*pow(w, -1-nu)*(k+1-w);
            w+=st;

```



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        }
        st=st/2.0;
        n=n*2;
        v2=st*(s1+4.0*s2)/3.0;
        err=v2>0?fabs((v1-v2)/v2):1;
        if(n>1200000) err=er/2.0;

    }

    res=c*v2;
    return res;
}

/*////////////////////////////////////*/
static double intlpl1(long k, double lp, double h, double
    nu,
                        double c, double er)
{
    double err=1;
    long int j, n=1;
    double st=(k-1)*0.5;
    double w, s1, s2, v1, v2, res;
    s1=exp(-lp*h)+exp(-lp*k*h)*pow(k,-1-nu);
    s2=exp(-lp*(1+st)*h)*pow(1+st, -1-nu);
    v2=st*(s1+4.0*s2)/3.0;
    v1=0;

    n=2;

    while(err>er)
    {
        v1=v2;
        s1+=2.0*s2;
        s2=0;
        w=1+st/2.0;
        for(j=1;j<=n;j++)
        {
            s2+=exp(-lp*w*h)*pow(w,-1-nu);
            w+=st;
        }
    }
}

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```

        st=st/2.0;
        n=n*2;
        v2=st*(s1+4.0*s2)/3.0;
        err=v2>0?fabs((v1-v2)/v2):1;
        if(n>1200000) err=er/2.0;

    }

    res=c*v2;
    return res;
}
/*////////////////////////////////////////*/

/*////////////////////////////////////////*/
/*static void printoutDA(PnlVect *ptDA1, PnlVect *ptDA2,
    char *foutname, char *strtitle)
{

    FILE *fic;
    long int i, nn;
    double *ptd1, *ptd2;

    if((fic = fopen(foutname,"w")) == NULL)
    {
        printf("Unable to open output File %s\n",foutname);
        return;
    }

    nn=ptDA1->size;
    ptd1=ptDA1->array;
    ptd2=ptDA2->array;
    fprintf(fic, "%s", strtitle);
    i=2;
    do
    {
        fprintf(fic, "%f {t%f {n",ptd1[i], ptd2[i]);
        i++;
    }while(i<nn);

    fclose(fic);

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    }*/

    /*////////////////////////////////////////*/

int CALC(FD_KLZ_EPUT)(void *Opt,void *Mod,PricingMethod *
    Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r, divid, strike, spot;
    NumFunc_1 *p;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
    p=ptOpt->PayOff.Val.V_NUMFUNC_1;
    strike=p->Par[0].Val.V_DOUBLE;
    spot=ptMod->S0.Val.V_DOUBLE;

    return fds_ts_europut(
        ptMod->LambdaMinus.Val.V_DOUBLE, ptMod->LambdaPlus.
        Val.V_DOUBLE,
        ptMod->AlphaPlus.Val.V_RGDOUBLE,ptMod->AlphaMinus.Val
        .V_RGDOUBLE,
        ptMod->CPlus.Val.V_DOUBLE,ptMod->CMinus.Val.V_DOUBLE
        ,r,divid,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,
        Met->Par[0].Val.V_RGDOUBLE/*xstep*/,strike,
        spot, Met->Par[1].Val.V_RGDOUBLE, 1,step,/*multiplie
        r*/
        &(Met->Res[0].Val.V_DOUBLE));
}

static int CHK_OPT(FD_KLZ_EPUT)(void *Opt, void *Mod)
{
    if ((strcmp( ((Option*)Opt)->Name,"PutEuro")==0) )
        return OK;

    return WRONG;
}

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```

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    static int first=1;

    if (first)
    {
        Met->Par[0].Val.V_RGDOUBLE=hh;
        Met->Par[1].Val.V_RGDOUBLE=eps;

        first=0;
    }

    return OK;
}

PricingMethod MET(FD_KLZ_EPUT)=
{
    "FD_KLZ_EPUT",
    { {"SpaceStep",RGDOUBLE,{100},ALLOW },
      {"Accuracy ", RGDOUBLE, {100},ALLOW },
      {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(FD_KLZ_EPUT),
    { {"Price", DOUBLE, {100}, FORBID},
      {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(FD_KLZ_EPUT),
    CHK_ok ,
    MET(Init)
} ;

/*////////////////////////////////////////*/

}

```

References