

## Help

```

#include <stdlib.h>
#include "cirpp1d_std.h"
#include "pnl/pnl_vector.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2007+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(TR_CAPFLOOR)(void *Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(TR_CAPFLOOR)(void *Opt,void *Mod,PricingMethod *
    Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

/*//////////////////////////////////// Datas specific
   to Hull and White //////////////////////////////////////
   //////////////////////////////////*/

static double a;                                /*Speed reversion
   of the Hullwhite model.*/
static double b;
static double rx0;
static double sigma;                            /*Volatility of th
   e Hullwhite model.*/

/*////////////////////////////////////
   Tree data //////////////////////////////////////
   //////////////////////////////////*/

static struct Tree Tr;                          /* The unique tree
   variable create by Premia for all the fowoling computations*/

static double VarTree(double r)

```

```

{
    /* return the variable 'y' computed in the tree with res
       pect to the 'real' short rate variable r, for cir++  $y=r*r *$ 
       /
    return r*r;
}

```

```

static double Var_y(double s)
{
    /*Variation of the variable tree y at time s (must be ind
       ependent of a variable rate)*/
    double V;

    V=sigma*sqrt(s)/2.0;
    return V;
}

```

```

static double ExpectCond_y(double x0, double s)
{
    /*Conditional expectation of variable y used in tree at
       time s starting from the knowing rate x0*/
    double E, x00;
    x00=0.5*sqrt(s*(4*a*b-sigma*sigma)/(2-a*s));

    E=x0 + ((a*b/2-sigma*sigma/8)/x0 - a*x0/2.0)*s;
    if(x0<x00){E=x00 + ((a*b/2-sigma*sigma/8)/x00 - a*x00/2.0
        )*s;}

    return E;
}

```

```

/*//////////////////////////////////////
   ////////////////////////////////////////
   ////////////////////////////////////////
   //////////////////////////////////////// Functions of
   the tree ////////////////////////////////////////
   ////////////////////////////////////////
   ////////////////////////////////////////
   ////////////////////////////////////////

```

```

//////////*/
static int indiceTime(struct Tree *Meth, double s)
{
    int i=0;

    if(Meth->t==NULL){printf("FATALE ERREUR, PAS DE GRILLE DE
        TEMPS !");}
    else
    {
        while(Meth->t[i]<=s && i<=Meth->Ngrid)
        {
            i++;

        }
    }
    return i-1;
}

void initPayoff1_tr(struct Tree *Meth, double T0)
{
    int i,j,n;
    /*n is the index time of T0 for an initialization to 1
        at that time in the tree (T0 must be <= to Tf the terminal
        time of the tree*/
    n=indiceTime(Meth, T0);

    /*Allocation of Payoffunc which follows the structure of
        the tree*/
    Meth->Payoffunc= malloc((n+1)*sizeof(double*));
    for(i=0; i<n+1; i++){Meth->Payoffunc[i]= malloc((Meth->TS
        ize[i])*sizeof(double));}

    /*Initialization of the Payoffunc to one at indice time
        n corresponding to T0 */
    for(j=0;j<Meth->TSize[n]; j++){Meth->Payoffunc[n][j]=1;}

    /*For the other under value in the tree of payoffunc[][],
        0 must be choosen in case of european computation option
        */
    /*Rk: In case of american option this value must be the

```

```

        payoff of the corresponding time*/
for(i=n-1;i>=0; i--)
{
    for(j=0;j<Meth->TSize[i]; j++)
    {
        Meth->Payofffunc[i][j]=0;
    }
}
}

static int SetTimegrid(struct Tree *Meth, int n, double T)
{
    int i;

    Meth->Ngrid=n;
    Meth->Tf=T;

    Meth->t= malloc((Meth->Ngrid+1)*sizeof(double));

    for(i=0; i<Meth->Ngrid+1; i++){Meth->t[i]=i*Meth->Tf/
        Meth->Ngrid;}

    return 1;
}

static int DeleteTimegrid(struct Tree *Meth)
{
    free(Meth->t);
    return 1;
}

static void SetTree(struct Tree* Meth)
{
    int jmin, jmax, jminprev, jmaxprev;
    double x, xi;
    int h, i, j, k, nv;

    double M, sigmai, mujk, Mij, dx;
    if(Meth->t==NULL){printf("FATAL ERROR IN SetTree(), SetT

```

```

    imegrid must be used before  SetTree!");}

jmin=0;
jmax=0;
xi=0;
nv=1;
/* Allocation of all the tree variable*/
Meth->pLRij= malloc((Meth->Ngrid+1)*sizeof(double));
Meth->pLPDo= malloc((Meth->Ngrid)*sizeof(double));
Meth->pLPMi= malloc((Meth->Ngrid)*sizeof(double));
Meth->pLPUp= malloc((Meth->Ngrid)*sizeof(double));
Meth->pLRef= malloc((Meth->Ngrid)*sizeof( int* ));
Meth->>TSize= malloc( (Meth->Ngrid+1)*sizeof( int ) );

Meth->pLRij[0] = malloc(sizeof(double));

Meth->pLRij[0][0]=xi;
Meth->>TSize[0]=1;

/* one step backward translation of the tree, there are 3
   point in rank 0 for the delta computation */
{
    jmin=-1;
    jmax=+1;
    xi=0;
    nv=3;
    free(Meth->pLRij[0]);
    Meth->pLRij[0] = malloc(3*sizeof(double));
    Meth->pLRij[0][0]=-sqrt(3.)*Var_y(Meth->t[1]);
    Meth->pLRij[0][1]=xi;
    Meth->pLRij[0][2]=+sqrt(3.)*Var_y(Meth->t[1]);
    Meth->>TSize[0]=3;
}

/* iteration on the time step */
for(i=1; i<=Meth->Ngrid; i++)
{
    sigmai = Var_y( Meth->t[i]-Meth->t[i-1]);
    dx=sqrt(3.)*sigmai;
    xi=ExpectCond_y(xi,Meth->t[i]-Meth->t[i-1]);
    jminprev=jmin;

```

```

    jmaxprev=jmax;

    M=ExpectCond_y(Meth->pLRij[i-1][0],Meth->t[i]-Meth->
t[i-1]);
    jmin=intapprox((M-xi)/dx)-1;
    M=ExpectCond_y(Meth->pLRij[i-1][nv-1],Meth->t[i]-
Meth->t[i-1]);
    jmax=intapprox((M-xi)/dx)+1;

    Meth->pLPDo[i-1] = malloc(nv*sizeof(double));
    Meth->pLPMi[i-1] = malloc(nv*sizeof(double));
    Meth->pLPUp[i-1] = malloc(nv*sizeof(double));
    Meth->pLRef[i-1] = malloc(nv*sizeof( int ));

    nv=jmax-jmin+1;
    Meth->>TSize[i]=nv;

    Meth->pLRij[i] = malloc(nv*sizeof(double));

    for(k=jmin;k<=jmax;k++)
    {
        j=k-jmin;

        x=k*dx + xi;
        Meth->pLRij[i][j]=x;

    }
    for(k=jminprev;k<=jmaxprev;k++)
    {
        j=k-jminprev;
        Mij= ExpectCond_y(Meth->pLRij[i-1][j], Meth->t[i]
-Meth->t[i-1]); /*Moyenne de taux partant de t[i-1], xij
au temps t[i]*/
        h=intapprox((Mij-xi)/dx);

        mujk=Mij - h*dx - xi;

        Meth->pLPUp[i-1][j] =1./6. + pow(mujk/dx,2)/2. +
mujk/(2.*dx);

```

```

        Meth->pLPMi[i-1][j] = 2./3. - pow(mujk/dx,2);
        Meth->pLPDo[i-1][j] = 1./6. + pow(mujk/dx,2)/2. -
mujk/(2.*dx);
        Meth->pLRef[i-1][j]=h-jmin;

        if(h<=jmin){printf("ERROR FATAL JMIN JMAX IN SetT
ree(), ExpectCond_y() MUST BE A CREASING FUNCTION{n");}
        if(h>=jmax){printf("ERROR FATAL JMIN JMAX IN SetT
ree(), ExpectCond_y() MUST BE A CREASING FUNCTION{n");}

    }

}

static void TranslateTree(struct Tree* Meth, ZCMarketData*
    ZCMarket)
{

    int k, i, j;
    double alpha, sum, eps;

    if(Meth->t==NULL){printf("FATAL ERROR IN TranslateTree(),
        SetTimegrid() and SetTree() must be used before SetTree!
        ");}
    if(Meth->pLRij==NULL){printf("FATAL ERROR IN TranslateTre
        e(), SetTimegrid() and SetTree() must be used before SetT
        ree!");}

    eps=Meth->Tf/Meth->Ngrid;
    alpha=-log(BondPrice(eps, ZCMarket))/eps;

    Meth->pLQij= malloc((Meth->Ngrid+1)*sizeof(double*));
    Meth->pLQij[0] = malloc(sizeof(double));
    Meth->pLQij[0][0] =1.;

    {
        free(Meth->pLQij[0]);
        Meth->pLQij[0] = malloc(3*sizeof(double));
        Meth->pLQij[0][0] =0;
        Meth->pLQij[0][1] =1.;
    }
}

```

```

    Meth->pLQij[0][2] = 0;
}

/* Recalculate the 'x' the translated short rate variable
   in the tree : x=Vartree(y) and r=x+alpha, in HW model y=x
   */
for(i=0; i<Meth->Ngrid+1; i++){for(j=0; j<Meth->TSize[i];
    j++){Meth->pLRij[i][j]=VarTree(Meth->pLRij[i][j]);}}

/* Iteration for alpha translation to obtain the real short
   rate variable r in the tree */
for(i=0; i<Meth->Ngrid; i++)
{
    Meth->P_T=0.0;
    Meth->pLQij[i+1] = malloc(Meth->TSize[i+1]*sizeof(
double));

    for(j=0; j<Meth->TSize[i]; j++)
    {
        Meth->pLRij[i][j]+=alpha;
    }

    for(j=0; j<Meth->TSize[i+1]; j++)
    {
        sum=0.0;
        for(k=0; k<Meth->TSize[i]; k++)
        {
            if( Meth->pLRef[i][k] == j-1){sum+=( Meth->pL
PUUp[i][k] * Meth->pLQij[i][k] * exp(-Meth->pLRij[i][k]*(
Meth->t[i+1]-Meth->t[i])) );}
            if( Meth->pLRef[i][k] == j ){ sum+=( Meth->pL
PMi[i][k] * Meth->pLQij[i][k] * exp(-Meth->pLRij[i][k]*(
Meth->t[i+1]-Meth->t[i])) );}
            if( Meth->pLRef[i][k] == j+1){sum+=( Meth->pL
PDo[i][k] * Meth->pLQij[i][k] * exp(-Meth->pLRij[i][k]*(
Meth->t[i+1]-Meth->t[i])) );}
        }
    }
}

```



```

        Meth->pLQij[i+1][j]=sum;
        Meth->P_T=Meth->P_T+sum;

    }

    sum=0;
    for(j=0;j<Meth->TSize[i+1];j++)
    {
        sum+= Meth->pLQij[i+1][j]*exp( -(Meth->t[i+1]-
Meth->t[i])*Meth->pLRij[i+1][j] );

    }

    sum=sum/BondPrice(Meth->t[i+1]+eps, ZCMarket);
    alpha=log(sum)/(Meth->t[i+1]-Meth->t[i]);

}

/* Last time step alpha translation */
for(j=0;j<Meth->TSize[Meth->Ngrid];j++)
{
    Meth->pLRij[Meth->Ngrid][j]=VarTree(Meth->pLRij[Meth->Ngrid][j]);
    Meth->pLRij[Meth->Ngrid][j]+=alpha;
}

/*printf("FIN de la translation de l'arbre des taux, sum
= %f\n", Meth->P_T); */
}

static void Computepayoff(struct Tree* Meth, double s)
{
    double ht;
    int i,j, i_end;
    i_end=indiceTime(Meth, s);

    if(Meth->t==NULL){printf("FATAL ERROR IN Computepayoff(),
        SetTimegrid() and SetTree() must be used before SetTree!
        ");}

```

```

if(Meth->pLRij==NULL){printf("FATAL ERROR IN Computepayof
    f(), SetTimegrid() and SetTree() must be used before SetT
    ree!");}

if(Meth->Payofffunc==NULL)
{
    initPayoff1_tr(Meth, Meth->Tf);
    printf("DEFAULT PAYOFF 1{n"); /*Payoff 1 par default.*
    /
}

/* pLQij[i_end][j] register the payoff at expiry time */
for(j=0; j<Meth->TSize[i_end]; j++)
{
    Meth->pLQij[i_end][j]=Meth->Payofffunc[i_end][j];
}

/* Computation in pLQij[i][j] of the value of payoff at
    time step i, backward iterations*/
for(i=i_end-1; i>=0; i--)
{
    for(j=0; j<Meth->TSize[i]; j++)
    {

        ht=0;
        ht=exp(- Meth->pLRij[i][j]*(Meth->t[i+1]-Meth->t[
i])) );
        ht=ht*( Meth->pLPDo[i][j]*(Meth->pLQij[i+1][
Meth->pLRef[i][j]-1 ])
            + Meth->pLPMi[i][j]*(Meth->pLQij[i+1][
Meth->pLRef[i][j] ])
            + Meth->pLPUi[i][j]*(Meth->pLQij[i+1][
Meth->pLRef[i][j]+1 ]) );

        /* Compare, in case of american, the computed val
        ue with the under next time step payoff value*/
        if(ht<Meth->Payofffunc[i][j]){ht=Meth->Payofffunc[
i][j];}

        Meth->pLQij[i][j]=ht;
    }
}

```

```

    }
}

/* printf("FIN de l'actualisation payoff de l'arbre des
   taux{n");    */
}

static double OPTION(struct Tree *Meth)
{
    return Meth->pLQij[0][1];
}

static int DeleteTree(struct Tree* Meth)
{
    int i;

    for(i=0; i<Meth->Ngrid+1; i++){free(Meth->pLRij[i]);}
    for(i=0; i<Meth->Ngrid; i++){free(Meth->pLQij[i]);}
    for(i=0; i<Meth->Ngrid; i++){free(Meth->pLPDo[i]);}
    for(i=0; i<Meth->Ngrid; i++){free(Meth->pLPMi[i]);}
    for(i=0; i<Meth->Ngrid; i++){free(Meth->pLPUp[i]);}
    for(i=0; i<Meth->Ngrid; i++){free(Meth->pLRef[i]);}

    free(Meth->pLRij);
    free(Meth->pLQij);
    free(Meth->pLPDo);
    free(Meth->pLPMi);
    free(Meth->pLPUp);
    free(Meth->pLRef);
    free(Meth->TSize);

    DeleteTimegrid(Meth);
    free(Meth->Payoffunc);
    return 1;
}

/*//////////////////////////////////////
   ////////////////////////////////////////
   ////////////////////////////////////////

```

```

//////////////////////////////////// End of the
    functions of the tree //////////////////////////////////////
    ////
////////////////////////////////////
    //////////////////////////////////////
    //////////////////////////////////////
    //////////////////////////////////*/

/*////////////////////////////////////
    //////////////////////////////////////
    //////////////////////////////////
//////////////////////////////////// Specific
    functions of the product computed //////////////////////////////////
    //////////////////////////////////
////////////////////////////////////
    //////////////////////////////////
    //////////////////////////////////
    //////////////////////////////////*/

static void initPayoffCAPFLOOR(struct Tree *Meth,double T1,
    double T2,double K, NumFunc_1 *p)
{
    double Ki;
    int i,j, n;
    /* Give the incice time for T1 the maturity of the
        option on the forward Libor rate L(T1, T2) */
    /* Rk : Tf, the final time of the tree is set to be matu
        rity of the ZC bond B(T0,Tf) of the option */
    n=indiceTime(Meth, T1);

    Ki=1./((T2-T1)*K + 1);
    p->Par[0].Val.V_DOUBLE=Ki;

    /* Compute in the tree the ZC bond B(T1,T2), the option
        on the Libor will be seen as an option of strike Ki on this
        ZC bond*/
    initPayoff1_tr(Meth, T2);
    Computepayoff(Meth, T2);

    /* Allocate the Payoffunc of the tree till time step n*/
    Meth->Payoffunc= malloc((n+1)*sizeof(double*));
    for(i=0; i<n+1; i++){Meth->Payoffunc[i]= malloc((Meth->TS

```

```

    ize[i])*sizeof(double));}

/* Initialization of the Payofffunc at the index time n of
   T1, thanks to the previous computation */
for(j=0;j<Meth->TSize[n]; j++){Meth->Payofffunc[n][j]=(p->
    Compute)(p->Par,Meth->pLQij[n][j]);}

/* For European payoff the value of the payoff under n=
   indiceTime(T1) are zero */
for(i=n-1;i>=0; i--)
{
    for(j=0;j<Meth->TSize[i]; j++)
    {
        Meth->Payofffunc[i][j]=0;
    }
}

}

double OPTIONr_tr(struct Tree* Meth, double r, double s)
{
    double  theta, R_T;
    int j, Ns, Nr;

    Ns=indiceTime(Meth, s);
    j=0;

    while(Meth->pLRij[Ns][j]<r && j<Meth->TSize[Ns]-1)
    {
        j++;
    }
    if(j==0){theta=0;}
    else{theta=(r-Meth->pLRij[Ns][j-1])/(Meth->pLRij[Ns][j]-
        Meth->pLRij[Ns][j-1]);}
    if(theta>1){theta=1;j=j+1;}

    Nr=j-1;

    if(Nr<0){Nr=0;}
    if(j>Meth->TSize[Ns]-2){printf("WARNING : Instantaneous
        futur spot rate is out of tree\n");}

```

```

    if(Nr==0){printf("WARNING : Instantaneous futur spot ra
        te is out of tree{n");}

    R_T=theta*Meth->pLQij[Ns][Nr+1] +(1-theta)*Meth->pLQij[Ns
        ][Nr];

    return R_T;
}

/*Cap Floor=Portfolio of zero-bond options*/
/*All details comments for the functions used here are mai
    nly in "hwtree1dincludes.h" and partially in this file*/
static int capfloor_cirpp1d(int flat_flag,double a0,double
    b0,double t0, double sigma0,double rcc,double T,NumFunc_1 *
    p,double Nominal,double K,double periodicity,double first_
    payement,long NtY,double *price/*,double *delta*/)
{

    long Ns;
    double cap;
    int i,N;
    double r0;
    ZCMarketData ZCMarket;

    a=a0;
    b=b0;
    sigma=sigma0;
    Ns=NtY*(long)((T-t0)/periodicity);
    Tr.Ngrid=Ns;

    r0=rcc;
    rx0=rcc;

    N=(int)floor((T-first_payement)/periodicity);

    Ns=NtY*N;
    cap=0;

```

```

/* Flag to decide to read or not ZC bond datas in "initialyields.dat" */
/* If B(0,T) not read then B(0,T)=exp(-FM*T) */
/* If B(0,T) read then rcc becomes the futur knowing rate name here r0 */
if(flat_flag==0)
{
    ZCMarket.FlatOrMarket = 0;
    ZCMarket.Rate = r0;
}

else
{
    ZCMarket.FlatOrMarket = 1;
    ReadMarketData(&ZCMarket);

    if(T > GET(ZCMarket.tm,ZCMarket.Nvalue-1))
    {
        printf("\nError : time bigger than the last time value entered in initialyield.dat\n");
        exit(EXIT_FAILURE);
    }
}

/* T defines the final time tree variable (no time can be larger), Ns is the number of time step */
SetTimegrid(&Tr, Ns, T);
/* Allocate and initialize the tree*/
SetTree(&Tr);
/* translate the tree by "alpha" */
TranslateTree(&Tr, &ZCMarket);

/* iteration for any caplet/floorlet */
for(i=0; i<N; i++)
{
    /* Initialize the payoff for an option on L(first_payment+i*periodicity,first_payment+(i+1)*periodicity) */
    initPayoffCAPFLOOR(&Tr,first_payment+i*periodicity,first_payment+(i+1)*periodicity,K, p); /* comments of this functions above */
    /* Compute the option from first_payment+i*periodic

```

```

ity to 0 in pLQij[][] tree variable */
    Computepayoff(&Tr,first_payment+i*periodicity);
    /* cumul cap/floor value in case or futur or not */
    if(t0==0){cap+=(1+K*periodicity)*OPTION(&Tr);}
    else {cap+=(1+K*periodicity)*OPTIONr_tr(&Tr,r0,t0);}
}

/**delta=0;*/
*price=cap;
DeleteTree(&Tr);

return OK;
}

int CALC(TR_CAPFLOOR)(void *Opt,void *Mod,PricingMethod *
    Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;

    return capfloor_cirpp1d(ptMod->flat_flag.Val.V_INT,ptMod->
        a.Val.V_DOUBLE,ptMod->b.Val.V_DOUBLE,ptMod->T.Val.V_DATE,
        ptMod->Sigma.Val.V_PDOUBLE,MOD(GetYield)(ptMod),ptOpt->BM
        aturity.Val.V_DATE,ptOpt->PayOff.Val.V_NUMFUNC_1,ptOpt->Nom
        inal.Val.V_PDOUBLE,ptOpt->FixedRate.Val.V_PDOUBLE,ptOpt->Res
        etPeriod.Val.V_DATE,ptOpt->FirstResetDate.Val.V_DATE,Met->
        Par[0].Val.V_LONG,&(Met->Res[0].Val.V_DOUBLE)/*,&(Met->Res[1]
        .Val.V_DOUBLE)*/*);
}

static int CHK_OPT(TR_CAPFLOOR)(void *Opt, void *Mod)
{
    if ((strcmp(((Option*)Opt)->Name,"Cap")==0) || (strcmp(((
        Option*)Opt)->Name,"Floor")==0))
        return OK;
    else
        return WRONG;
}

```



```

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_LONG=10;

    }
    return OK;
}

PricingMethod MET(TR_CAPFLOOR)=
{
    "TR_Cirpp1d_CAPFLOOR",
    {{ "TimeStepNumber for Period",LONG,{100},ALLOW},
      { " ",PREMIA_NULLTYPE,{0},FORBID}}},
    CALC(TR_CAPFLOOR),
    {{ "Price",DOUBLE,{100},FORBID}/*,{ "Delta",DOUBLE,{100},FORBID}*/,
      { " ",PREMIA_NULLTYPE,{0},FORBID}}},
    CHK_OPT(TR_CAPFLOOR),
    CHK_ok,
    MET(Init)
} ;

```

## References