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cf_put_merton

Let

- $T = \text{maturity date} \quad (T > t)$
- K = strike price
- x = spot price
- t = pricing date
- $\sigma = \text{volatility}$
- r = interest rate
- $\delta = \text{dividend yields}$
- $\lambda = \text{jump intensity}$
- $\kappa = \mathbf{E}U 1$ where $\mathbf{E}U$ is the expectation over the random jump variable U
- $\theta = T t$

We assume [1] that the jump variable U is log-normally distributed with constant mean and variance. Specifically, let $\mathbf{E}[\ln U] = \mu$ and $\mathbf{E}[(\ln U)^2] = \mu^2 + v$, such that $\mathbf{E}U = e^{\mu + \frac{v}{2}}$.

Set:

$$d_1 = \frac{\log\left(\frac{x}{K}\right) + \left(r_n + \frac{\sigma_n^2}{2}\right)\theta}{\sigma_n\sqrt{\theta}} \qquad d_2 = d_1 - \sigma_n\sqrt{\theta},$$

where

$$\sigma_n^2 = \sigma^2 + \frac{nv}{\theta}$$
 $r_n = r - \delta - \lambda \kappa + \frac{n}{\theta} \ln(1 + \kappa).$

and N as the cumulative normal distribution function:

$$N(d) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{d} e^{-x^2/2} dx.$$

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Put Option

Payoff
$$P_T = (K - S_T)_+$$
 Price
$$C(t, x; K) = \sum_{n=0}^{\infty} \frac{(\lambda(1+\kappa)\theta)^n}{n!} e^{-\lambda(1+\kappa)\theta - \delta\theta} [Ke^{-r_n\theta}N(-d_2) - xN(-d_1)]$$
 Delta
$$\frac{\partial C(t, x; K)}{\partial x} = \sum_{n=0}^{\infty} \frac{(\lambda(1+\kappa)\theta)^n}{n!} e^{-\lambda(1+\kappa)\theta - \delta\theta} N(-d_1)$$

References

[1] R.C.MERTON. Option pricing when the underlying stocks returns are discontinuous. *Journ. Financ. Econ.*, 5:125–144, 1976. 1