

[Help](#)

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#include "bs1d_doublim.h"

/*Computation of Laplace transform*/
double fnRf_3(dcomplex z,double aa,double bb,double hh,
double nn)
{
double Rfs;
dcomplex Cun,Cnn,Cnn2,z1,z2,z3,z4,z5,z6,z7,z8,z9,z10,z11,
z12,z13,mu,Q_1,Q_2,Q;

Cun=Complex(1.0,0.0);
Cnn=Complex(nn,0.0);
mu=RCmul(2.0,z);
Cnn2=Cmul(Cnn,Cnn);
mu=Csqrt(Cadd(mu,Cnn2));

z1=Complex(cos(bb*mu.i)*sinh(mu.r*bb),sin(bb*mu.i)*cosh(
mu.r*bb)); /*sh(mu b)*/
z2=Complex(cos(aa*mu.i)*sinh(mu.r*aa),sin(aa*mu.i)*cosh(
mu.r*aa)); /*sh(mu a)*/
z3=Complex(cos((aa+bb)*mu.i)*sinh(mu.r*(aa+bb)),sin((aa+
bb)*mu.i)*cosh(mu.r*(aa+bb))); /*sh(mu(a+b))*/
z5=RCmul(exp(-aa*mu.r),Complex(cos(-mu.i*aa),sin(-mu.i*aa
))); /*exp(-mu a)*/

z4=RCmul(pow(hh,nn+1.0-mu.r),Complex(cos(-mu.i*log(hh)),
sin(-mu.i*log(hh))));
z6=Cmul(mu,Complex(mu.r-nn,mu.i));
z7=Cmul(z6,Complex(mu.r-nn-1.0,mu.i));

z8=Cmul(z4,z5);
z9=Cmul(z8,z1);
z10=Cmul(z7,z3);
Q_1=Cdiv(z9,z10);

z4=Cmul(mu,mu);
z5=Cdiv(Cun,Complex(z4.r-(nn+1.0)*(nn+1.0),z4.i));
z6=Cdiv(Cun,Complex(z4.r-nn*nn,z4.i));
z5=RCmul(exp((nn+1.0)*bb),z5);
z6=RCmul(hh*exp(nn*bb),z6);
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z7=RCmul(2.0,Csub(z5,z6));

z8=RCmul(exp(-bb*mu.r),Complex(cos(-mu.i*bb),sin(-mu.i*bb
))); /*exp(-mu b)*/
z9=RCmul(pow(hh,nn+1.0+mu.r),Complex(cos(mu.i*log(hh)),si
n(mu.i*log(hh))));
z10=Cmul(mu,Complex(mu.r+nn,mu.i));
z11=Cmul(z10,Complex(mu.r+nn+1.0,mu.i));
z12=Cdiv(Cmul(z8,z9),z11);

z13=Cadd(z7,z12);

Q_2=Cdiv(Cmul(z2,z13),z3);

Q=Cadd(Q_1,Q_2);

Rfs=Q.r;

return Rfs;
}

static int Out_Laplace(double s,NumFunc_1 *L,NumFunc_1 *Up,
    NumFunc_1 *Rebate,NumFunc_1 *PayOff,double t,double r,double div
    id,double sigma,double *ptprice,double *ptdelta)
{
    int N=15,M=11;
    int i;
    double price,delta,price2,delta2;
    double xx,y,hh,sum,sum2,Avg,Avg2,Fun,Fun2,j,S[13],Q[13],
        U,tt,d,K;
    double St,St2,Lower,Upper,v,pp;
    double sigma2;
    double nu,h,h2,a,a2,b,b2,CTtK;

    /* Inversion Variables*/
    double A;
    dcomplex z;

    /*Inversion parameters*/

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A=19.1;

Upper=(Up->Compute)(Up->Par,0.0);
Lower=(L->Compute)(L->Par,0.);
K=PayOff->Par[0].Val.V_PDOUBLE;
pp=1.e-8;
St=s;
St2=s*(1.+pp);
v=r-divid;
sigma2=sigma*sigma;

nu=(1.0/sigma2)*(v-0.5*sigma2);
h=K/St;
h2=K/St2;
a=log(St/Lower);
a2=log(St2/Lower);
b=log(Upper/St);
b2=log(Upper/St2);

/* INVERSION */
tt=t;
xx=A/(2*tt);
hh=M_PI/tt;
z=Complex(xx/sigma2, 0.0);

sum=fnRf_3(z,a,b,h,nu)*.5/sigma2;
sum2=fnRf_3(z,a2,b2,h2,nu)*.5/sigma2;

/* Computation of S[0]=s(n) which approximate f(t) */
for(i=1;i<=N;i++)
{
    y=(double)i*hh;
    z=Complex(xx/sigma2, y/sigma2);
    j=PNL_ALTERNATE(i);
    sum=sum+j*fnRf_3(z,a,b,h,nu)/sigma2;
    sum2=sum2+j*fnRf_3(z,a2,b2,h2,nu)/sigma2;
}

S[0]=sum;
Q[0]=sum2;
/* End of Inversion */

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/* Computation of s(n+p) p<=M+1 for Euler appromations
*/
for(i=1;i<=M+1;i++)
{
    y=(double)(N+i)*hh;
    z=Complex(xx/sigma2,y/sigma2);
    j=PNL_ALTERNATE(N+i);
    S[i]=S[i-1]+j*fnRf_3(z,a,b,h,nu)/sigma2;
    Q[i]=Q[i-1]+j*fnRf_3(z,a2,b2,h2,nu)/sigma2;
}

/* Computation of Euler appromations */
Avg=0.;
Avg2=0.;
for(i=1;i<=M+1;i++)
{
    Avg=Avg+Cnp(M,i-1)*S[i-1];
    Avg2=Avg2+Cnp(M,i-1)*Q[i-1];
}

d=pow(2.0,(double)M);
U=exp(A/2.)/tt;

/*f(t) values*/
Fun=U*Avg/d;
Fun2=U*Avg2/d;

/*Black-Sholes price for call option*/

pnl_cf_call_bs(1.,h,t,r,divid,sigma,&price,&delta);
pnl_cf_call_bs(1.,h2,t,r,divid,sigma,&price2,&delta2);

CTtK=St*price-St*exp(-r*t)*Fun;

/*Price*/
*ptprice=CTtK;

/*Delta*/
*ptdelta=(CTtK-(price2-price)/(h2-h)*K)/St-exp(-r*t)*
    (Fun2-Fun)/pp;

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    return OK;
}

int CALC(AP_Out_Laplace)(void*Opt,void *Mod,PricingMethod *
    Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r,divid;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    return Out_Laplace(ptMod->S0.Val.V_PDOUBLE,ptOpt->LowerL
        imit.Val.V_NUMFUNC_1, ptOpt->UpperLimit.Val.V_NUMFUNC_1, pt
        Opt->Rebate.Val.V_NUMFUNC_1,ptOpt->PayOff.Val.V_NUMFUNC_1,pt
        Opt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,r,divid,ptMod->
        Sigma.Val.V_PDOUBLE,&(Met->Res[0].Val.V_DOUBLE),&(Met->Res[
        1].Val.V_DOUBLE));
}

static int CHK_OPT(AP_Out_Laplace)(void *Opt, void *Mod)
{Option* ptOpt=(Option*)Opt;
    TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);

    if ((opt->Parisian).Val.V_BOOL==WRONG)
        if((opt->RebOrNo).Val.V_BOOL==NOREBATE)
            if ((strcmp( ((Option*)Opt)->Name,"    DoubleCallOutEuro")==0))
                return OK;

    return WRONG;
}

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    return OK;
}

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PricingMethod MET(AP_Out_Laplace)=
{
    "AP_Out_Laplace",
    {{ " ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(AP_Out_Laplace),
    {{ "Price",DOUBLE,{100},FORBID},{ "Delta",DOUBLE,{100},FORB
        ID} ,{ " ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(AP_Out_Laplace),
    CHK_ok,
    MET(Init)
} ;
```

## References