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Help
/**********************************
   ***********/
/* Written and (C) by David Pommier <david.pommier@gmail.
   com>
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/*
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/* INRIA 2009
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/*********************
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#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "pnl/pnl_mathtools.h"
#include "pde_tools.h"
#include "gridsparse_functions.h"
static double mu=0.5;
static double eta=0.02;
static double Time_zero=1.0;
double function_square(const PnlVect * X)
{
 int i;
 double prod=1.0;
 for(i=0;i<X->size;i++)
   prod*=GET(X,i)*(1.0 -GET(X,i));
 return prod;
}
double function_Test(const PnlVect * X)
{
  int i;
 double prod=0.0;
  return 1.0;
  for(i=0;i<X->size;i++)
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prod+=GET(X,i)*(1.0 -GET(X,i));
  return prod;
}
double function Test2(const PnlVect * X)
  int i;
  double prod=1.0;
  for(i=0;i<X->size;i++)
    prod*=sin(M_PI*GET(X,i));
  return prod;
}
double function_Test3(const PnlVect * X)
  int i=0;
  double prod=1.0;
  for(i=0;i<X->size;i++)
    prod*=1.0/(sqrt(2*M PI*Time zero)*eta)*exp(-pow(GET(X,
    i)-mu,2)/(2.0*eta*eta*Time zero));
  return prod;
}
double function_Test4(const PnlVect * X)
  return MAX(0.5-exp(GET(X,0)),0.0);
void Test_SpGrid_Poisson(void )
  PnlVect *V,*W,*WO;
  FILE *fic ;
  LaplacienSparseOp * Op=create laplacien sparse operator()
  Op->G=grid_sparse_create01(2,8);
  printf(">>>>> Test Sparse Grid On Poisson Problem {n");
  initialise laplacien sparse operator(Op);
  V=pnl_vect_create_from_zero(Op->G->size);
  WO=pnl_vect_create_from_zero(Op->G->size);
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W=pnl vect create from zero(Op->G->size);
  GridSparse apply function(Op->G,V,function Test2);
  Nodal_to_Hier(V,Op->G);
  pnl vect clone(W0,V);
  Hier to Nodal(W0,Op->G);
  GridSparse Solve Laplacien(Op,V,W);
  Hier_to_Nodal(W,Op->G);
  pnl vect axpby(0.0,W0,-1*pow(M PI,2)*Op->G->dim,W);
  fic=fopen("Data/Test_Graphe_n","w");
  if( fic == NULL )
    {PNL_ERROR("Cannot open file", "GridSparse_fprint");}
  GridSparse_fprint(fic,Op->G,W);
  fclose(fic);
  fic=fopen("Data/Test_Graphe_n0","w");
  if( fic == NULL )
    {PNL_ERROR("Cannot open file", "GridSparse_fprint");}
  GridSparse_fprint(fic,Op->G,WO);
  fclose(fic);
  pnl vect axpby(-1.0,W0,1,W);
  fic=fopen("Data/Test_Graphe_n2","w");
  if( fic == NULL )
    {PNL_ERROR("Cannot open file", "GridSparse_fprint");}
  GridSparse_fprint(fic,Op->G,W);
  fclose(fic);
  printf(">> relativ error L2 = %7.4f{n",pnl vect norm two(
    W)/pnl_vect_norm_two(W0));
  laplacien_sparse_operator_free(&Op);
  pnl_vect_free(&V);
  pnl_vect_free(&W);
  pnl vect free(&WO);
  printf("end solve Laplacien on Sparse Grid {n");
  }
void Test SpGrid Heat(void )
  FILE *fic;
  int lev, dim;
  double delta_t=5.0*Time_zero;
  dim=4;
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{

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printf(">>>>> Test Sparse Grid On Heat Equation {n");
for(lev=4;lev<=10;lev++)</pre>
{
    PnlVect *V,*W,*WO;
    HeatSparseOp * Op=create heat sparse operator(eta);
    Op->G=grid sparse createO1(dim,lev);
    Op->TG=premia_pde_time_homogen_grid(delta_t,100);
    initialise heat sparse operator(Op);
    V=pnl vect create from zero(Op->G->size);
    WO=pnl_vect_create_from_zero(Op->G->size);
    W=pnl vect create from zero(Op->G->size);
    /* Initial condition, */
    GridSparse_apply_function(Op->G,V,function_Test3);
    Nodal to Hier(V,Op->G);
    GridSparse_Solve_heat(Op,V,W);
    Hier to Nodal(W,Op->G);
    /*pnl vect axpby(W,1,W0,0); */
    fic=fopen("Data/Test_Graphe_n","w");
    if( fic == NULL )
{PNL ERROR("Cannot open file", "GridSparse fprint");}
    GridSparse fprint(fic,Op->G,W);
    fclose(fic);
    Time zero+=delta t;
    GridSparse apply function(Op->G,WO,function Test3);
    fic=fopen("Data/Test Graphe n0","w");
    if( fic == NULL )
{PNL ERROR("Cannot open file", "GridSparse_fprint");}
    GridSparse fprint(fic,Op->G,WO);
    fclose(fic);
    pnl_vect_axpby(-1.0,W0,1.0,W);
    fic=fopen("Data/Test Graphe n2","w");
    if( fic == NULL )
{PNL_ERROR("Cannot open file", "GridSparse_fprint");}
    GridSparse_fprint(fic,Op->G,W);
    fclose(fic);
    printf(">> Size of the Sparse Grid in Dimension %d an
  d level %d is %d -> Relativ error L2 = %7.4f{n",dim,lev,Op-
  >G->size,pnl_vect_norm_two(W)/pnl_vect_norm_two(W0));
    Nodal to Hier(WO,Op->G);
    /*pnl vect print(W0); */
    fic=fopen("Data/Test_Graphe_nh","w");
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if( fic == NULL )
{PNL_ERROR("Cannot open file", "GridSparse_fprint");}
    GridSparse_fprint(fic,Op->G,WO);
    fclose(fic);
    heat_sparse_operator_free(&Op);
    pnl_vect_free(&V);
    pnl_vect_free(&W);
    pnl_vect_free(&WO);
    }
    printf("End solve Heat on Sparse Grid {n");
}
int main ()
{
    Test_SpGrid_Poisson ();
    Test_SpGrid_Heat ();
}
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References