```
Help
/* Céline Labart and Jérôme Lelong
 * First version : August 2004
 * Last modified : July 2006
 * Computation of the prices of Parisian options using
 * Laplace transforms. This implementation is based on a
 * Research Report available on cermics website
 * http://cermics.enpc.fr/reports/CERMICS-2005/CERMICS-2005
    -294.pdf
 */
extern "C" {
#include "bs1d_lim.h"
}
#include <cmath>
#include <complex>
using namespace std;
typedef complex<double> complex_double;
typedef struct {
  double K;
  double T;
  double t;
  double D;
  double d;
  double L;
  double sigma;
  double r;
  double delta;
  double So;
} parisian t;
/* compute Laplace Transform of the price with respect to
 * maturity time. l is the laplace parameter
 * p : Parisian
 * d or u: down or out
```

```
* i or o: in or out
* c or p: call or put
*/
static complex_double pdic( complex_double 1, parisian_
    t *opt);
static complex double pdoc( complex double 1, parisian
   t *opt);
static complex double puic( complex double 1, parisian
    t *opt);
static complex_double puoc( complex_double 1, parisian_
    t *opt);
/* Laplace transform of the price of the call with respect
 * to maturity time */
static complex_double bs( complex_double 1, parisian t *
    opt);
/* defined in Src/common/complex_erf.C */
extern complex double normal cerf (const complex double z)
static parisian_t* NewParisian_t(parisian_t *orig)
 parisian_t *opt = new parisian_t;
 opt->K = orig->K;
 opt->T = orig->T;
 opt->t = orig->t;
 opt->D = orig->D;
 opt->d = orig->d;
 opt->L = orig->L;
 opt->sigma = orig->sigma;
  opt->r = orig->r;
 opt->So = orig->So;
 opt->delta = orig->delta;
 return opt;
}
static complex_double psi( complex_double z)
{
```

```
complex double res;
      double racine=sqrt(2.0*M PI);
      res = 1.0+z*racine*exp(pow(z,2)/2.0)*normal_cerf(z);
      return(res);
}
/* Laplace transform of the price of the call with respect
  * to maturity time */
static complex_double bs(complex_double 1, parisian_t *opt)
      complex_double theta;
      double m, k;
      m=(opt->r-opt->delta-pow(opt->sigma,2)/2.0)/opt->sigma;
      k=log(opt->K/opt->So)/opt->sigma;
      theta=sqrt(2.0*1);
      /* K < X */
      if(opt->K<=opt->So)
            return(2.0*opt->K/(m*m-2.0*1)-2.0*opt->So/(pow(m+opt->
            sigma, 2)-2.0*1)+opt->K*exp((m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/(m+theta)*k)/theta*(1.0/
            a)-1.0/(m+opt->sigma+theta)));
      /*K > x*/
      if(opt->K>opt->So)
            return(opt->K*exp((m-theta)*k)/theta*(1.0/(m-theta)-1.0
            /(m+opt->sigma-theta)));
      return -1;
}
static complex_double pdic(complex_double 1, parisian_t *
            opt)
{
      complex_double theta;
      double m;
      double b;
      double k:
      double d;
      double d3;
      double racine=sqrt(2.0*M PI);
      m=1.0/opt->sigma*(opt->r-opt->delta-pow(opt->sigma,2)/2.0
            );
```

```
b=1.0/opt->sigma*log(opt->L/opt->So);
k=1.0/opt->sigma*log(opt->K/opt->So);
theta=sqrt(2.0*1);
d=sqrt(opt->D);
d3=(b-k)/d;
/*K<L<x*/
if(opt->D>opt->T) return 0.0;
if(opt->K<=opt->L && opt->L<=opt->So)
  {return( exp((m+theta)*b)/psi(theta*d)*(2.0*opt->K/(m*
  m-2.0*1)*(psi(-d*m)+racine*d*exp(opt->D*m*m/2.0)*m*normal
  cerf(-d3-d*m))-2.0*opt->L/(pow((m+opt->sigma),2)-2.0*1)*(ps
  i(-d*(m+opt->sigma))+racine*d*exp(opt->D*pow(m+opt->sigma,2
  )/2.0)*(m+opt->sigma)*normal cerf(-d3-d*(m+opt->sigma))))+
  opt->K*exp((m+theta)*k)/(theta*psi(theta*d))*(1.0/(m+theta)-1
  .0/(m+opt->sigma+theta))*(psi(-theta*d)+theta*exp(1*opt->
  D)*racine*d*normal cerf(d3-d*theta))+exp(l*opt->D)*racine*
  d*opt->K/psi(theta*d)*exp(2.0*b*theta)*exp((m-theta)*k)*nor
  mal cerf(-d3-theta*d)*(1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)
  a)));
  }
/*x<L<K*/
if(opt->So<=opt->L && opt->L<=opt->K)
  {return( opt->K/theta*exp((m-theta)*k)*(1.0/(m-theta)-1
  .0/(m-theta+opt->sigma))-(exp((m-theta)*b)*normal cerf(th
  eta*d-b/d)+exp((m+theta)*b)*normal cerf(-theta*d-b/d))*ra
  cine*d*exp(l*opt->D)*opt->K*exp((m-theta)*log(opt->K/opt->L)
  /opt->sigma)/psi(theta*d)*(1.0/(m-theta)-1.0/(m+opt->sigma)
  -theta)));
  }
/*L<x et L<K*/
if(opt->L<=opt->So \&\& opt->L<=opt->K)
  {return(psi(-theta*d)/psi(theta*d)*opt->K/theta*exp(2.
  0*b*theta)*exp((m-theta)*k)*(1.0/(m-theta)-1.0/(m+opt->si
  gma-theta)));
  }
/*x<K<L*/
if(opt->So<=opt->K && opt->K<=opt->L)
  \{\text{return}(\text{opt->K/theta*exp}((\text{m-theta})*k)*(1.0/(\text{m-theta})-1.)\}
  0/(m+opt->sigma-theta))-(opt->L*(exp((m-theta)*b)*normal
  cerf(theta*d-b/d)+exp((m+theta)*b)*normal cerf(-theta*d-b/
  d)*(2.0*opt->K/(opt->L*(m*m-2.0*1))*(1.0-1.0/psi(theta*d)*
```

```
(psi(-d*m)+racine*d*exp(opt->D*m*m/2.0)*m*normal cerf(log(
   opt-K/opt-L)/(opt-sigma*d)-d*m))-2.0/(pow((m+opt-sigma),
   2)-2.0*1)*(1.0-1.0/psi(theta*d)*(psi(-d*(m+opt->sigma))+ra
   cine*d*exp(opt->D*pow((m+opt->sigma),2.0)/2.0)*(m+opt->sigma)
   )*normal cerf(log(opt->K/opt->L)/(opt->sigma*d)-d*(m+opt->
   sigma))))+opt->K/opt->L*exp((m+theta)*log(opt->K/opt->L)/
   opt->sigma)/(theta)*(1.0/(m+theta)-1.0/(m+opt->sigma+theta))*
    (1.0-1.0/psi(theta*d)*(psi(-theta*d)+theta*exp(l*opt->D)*
   racine*d*normal cerf(log(opt->L/opt->K)/(opt->sigma*d)-thet
   a*d)))-exp(l*opt->D)*racine*d*opt->K/(opt->L*psi(theta*d))*
   exp((m-theta)*log(opt->K/opt->L)/opt->sigma)*normal cerf(log
    (opt->K/opt->L)/(opt->sigma*d)-theta*d)*(1.0/(m-theta+opt-
   >sigma)-1.0/(m-theta)))));
 /*K<x<L*/
 if(opt->K<=opt->So && opt->So<=opt->L)
    \{return(2.0*opt->K/(m*m-2.0*1)-2.0*opt->So/(pow(m+opt->
   sigma, 2)-2.0*1)+opt-K/theta*exp((m+theta)*k)*(1.0/(m+theta)*k)
   a)-1.0/(m+opt->sigma+theta))-(opt->L*(exp((m-theta)*b)*nor
   mal cerf(theta*d-b/d)+exp((m+theta)*b)*normal cerf(-theta*d-
   b/d)*(2.0*opt->K/(opt->L*(m*m-2.0*1))*(1.0-1.0/psi(theta*
   d)*(psi(-d*m)+racine*d*exp(opt->D*m*m/2.0)*m*normal_cerf(
   log(opt->K/opt->L)/(opt->sigma*d)-d*m)))-2.0/(pow(m+opt->sigma*d)-d*m))
   gma, 2)-2.0*1)*(1.0-1.0/psi(theta*d)*(psi(-d*(m+opt->sigma))+
   racine*d*exp(opt->D*pow(m+opt->sigma,2.0)/2.0)*(m+opt->si
   gma)*normal cerf(log(opt->K/opt->L)/(opt->sigma*d)-d*(m+opt-
   >sigma))))+opt->K/opt->L*exp((m+theta)*log(opt->K/opt->L)/
   opt->sigma)/(theta)*(1.0/(m+theta)-1.0/(m+opt->sigma+theta))*
    (1.0-1.0/psi(theta*d)*(psi(-theta*d)+theta*exp(l*opt->D)*
   racine*d*normal_cerf(log(opt->L/opt->K)/(opt->sigma*d)-thet
   a*d)))-exp(l*opt->D)*racine*d*opt->K/(opt->L*psi(theta*d))*
   exp((m-theta)*log(opt->K/opt->L)/opt->sigma)*normal cerf(log
    (opt->K/opt->L)/(opt->sigma*d)-theta*d)*(1.0/(m-theta+opt-
   >sigma)-1.0/(m-theta)))));
 return -1;
static complex_double pdoc( complex_double 1, parisian_t *
```

}

```
opt)
complex_double theta;
double b, m, k, d;
double racine=sqrt(2.0*M PI);
m=(opt->r-opt->delta-pow(opt->sigma,2)/2.0)/opt->sigma;
b=log(opt->L/opt->So)/opt->sigma;
k=log(opt->K/opt->So)/opt->sigma;
d=sqrt(opt->D);
theta=sqrt(2.0*1);
/* L < K < X */
if(opt->D>opt->T) return (bs(1,opt));
if(opt->L<=opt->K && opt->K<=opt->So)
  return(2.0*opt->K/(m*m-2.0*1)-2.0*opt->So/(pow(m+opt->
  sigma, 2)-2.0*1)+(opt->K*exp((m+theta)*k))/theta*(1.0/(m+theta)*k))
  eta)-1.0/(m+opt->sigma+theta))-(psi(-theta*d))/(theta*psi(
  theta*d))*exp(2.0*b*theta)*opt->K*exp((m-theta)*k)*(1.0/(m-theta)*k)
  theta)-1.0/(m+opt->sigma-theta)));
/* L < x < K */
if(opt->L<=opt->So && opt->So<=opt->K)
  return((1.0-exp(2.0*b*theta)+(theta*exp(2.0*b*theta)*ra
  cine*d*exp(l*opt->D))/psi(theta*d))*opt->K/theta*exp((m-thet
  a)*k)*(1.0/(m-theta)-1.0/(m+opt->sigma-theta)));
/* x < L< K */
if(opt->So<=opt->L && opt->L<=opt->K)
  return(opt->L*(exp((m-theta)*b)*normal cerf(theta*d-b/
  d)+exp((m+theta)*b)*normal cerf(-theta*d-b/d))*racine*d*exp
  (l*opt->D)*opt->K*exp((m-theta)*log(opt->K/opt->L)/opt->si
  gma)/(opt->L*psi(theta*d))*(1.0/(m-theta)-1.0/(m+opt->sigma-max))
  theta)));
/* K < L < x */
if(opt->K<=opt->L && opt->L<=opt->So)
  return(2.0*opt-K/(m*m-2.0*1)*(1.0-exp((m+theta)*b)/ps
  i(theta*d)*(psi(-d*m)+racine*d*exp(opt->D*m*m/2.0)*m*normal
```

```
cerf(-(b-k)/d-d*m)))-2.0/(pow(m+opt->sigma,2)-2.0*1)*(
        opt->So-exp((m+theta)*b)*opt->L/psi(theta*d)*(psi(-d*(m+opt->
        sigma))+racine*d*exp(opt->D*pow(m+opt->sigma,2)/2.0)*(m+
        opt->sigma)*normal cerf(-(b-k)/d-d*(m+opt->sigma))))+opt->K*
        \exp((m+theta)*k)/(theta)*(1.0/(m+theta)-1.0/(m+opt->sigma+th)
        eta))*(1.0-1.0/psi(theta*d)*(psi(-theta*d)+theta*exp(l*opt-
        >D)*racine*d*normal cerf((b-k)/d-theta*d)))-exp(l*opt->D)*
        racine*d*opt->K/psi(theta*d)*exp(2.0*b*theta)*exp((m-theta)
        *k)*normal cerf(-(b-k)/d-theta*d)*(1.0/(m-theta+opt->sigma)
        )-1.0/(m-theta)));
    /* K<L and x<L */
    if(opt->K<=opt->L && opt->So<=opt->L)
        return(opt->L*(exp((m-theta)*b)*normal cerf(theta*d-b/
        d)+exp((m+theta)*b)*normal cerf(-theta*d-b/d))*(2.0*opt->K/
         (opt->L*(m*m-2.0*1))*(1.0-1.0/psi(theta*d)*(psi(-d*m)+ra)
        cine*d*exp(opt->D*m*m/2.0)*m*normal cerf(log(opt->K/opt->L)/
         (opt->sigma*d)-d*m)))-2.0/(pow(m+opt->sigma,2.0)-2.0*1)*(1
         .0-1.0/psi(theta*d)*(psi(-d*(m+opt->sigma))+racine*d*exp(
        opt->D*pow(m+opt->sigma,2.0)/2.0)*(m+opt->sigma)*normal cerf(
        log(opt->K/opt->L)/(opt->sigma*d)-d*(m+opt->sigma))))+opt->
        K/opt->L*exp((m+theta)*log(opt->K/opt->L)/opt->sigma)/(thet
        a)*(1.0/(m+theta)-1.0/(m+opt->sigma+theta))*(1.0-1.0/psi(th)
        eta*d)*(psi(-theta*d)+theta*exp(l*opt->D)*racine*d*normal
        cerf(log(opt->L/opt->K)/(opt->sigma*d)-theta*d)))-exp(l*
        opt->D)*racine*d*opt->K/(opt->L*psi(theta*d))*exp((m-theta)*
        log(opt->K/opt->L)/opt->sigma)*normal cerf(log(opt->K/opt->
        L)/(opt->sigma*d)-theta*d)*(1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt->sigma)-1.0/(m-theta+opt
        m-theta))));
    return -1;
static complex double puoc(complex double 1, parisian t *
        opt)
    complex_double theta;
    double b, m, d;
    m = (opt->r - opt->delta - opt->sigma * opt->sigma / 2.0
          ) /opt->sigma;
```

}

{

```
b = log (opt->L / opt->So) / opt->sigma;
  theta = sqrt(2.0 * 1);
  d = sqrt(opt->D);
  if(opt->D>opt->T)
    return bs(1,opt);
  else if(opt->L>=opt->So)
    return bs(1,opt)-puic(1,opt);
  else
    {
     parisian_t opt_0;
      opt 0 = *opt;
      opt 0.K=opt->K/opt->L;
      opt 0.So=1.0;
      opt_0.L=1.0;
      return opt->L*(exp((m+theta)*b)*normal cerf(theta*d+
    b/d)+exp((m-theta)*b)*normal cerf(-theta*d+b/d))*puoc(1,&
    opt_0);
    }
}
static complex_double puic(complex_double 1, parisian_t *
    opt)
{
  complex double theta;
  double b, m, k, d, d3;
  double racine=sqrt(2.0*M PI);
  m=(opt->r-opt->delta-pow(opt->sigma,2)/2.0)/opt->sigma;
  b=log(opt->L/opt->So)/opt->sigma;
 k=log(opt->K/opt->So)/opt->sigma;
  d=sqrt(opt->D);
  theta=sqrt(2.0*1);
  d3=(b-k)/d;
  if(opt->D>opt->T) return 0.0;
  /* X < L < K*/
  if(opt->So<=opt->L && opt->L<=opt->K)
    {
      return(exp((m-theta)*b)*racine*d/psi(theta*d)*(2.*
    opt-K/(m*m-2.*1)*exp(opt-D*m*m/2.)*m*normal cerf(d3+d*m)-2.
    *opt->L/(pow(m+opt->sigma,2)-2.*1)*exp(opt->D*pow(m+opt->
    sigma,2)/2.)*(m+opt->sigma)*normal_cerf(d3+d*(m+opt->sigma)
```

```
))+exp(-2.*b*theta)/psi(theta*d)*opt->K*exp((m+theta)*k)*
   exp(l*opt->D)*racine*d*normal_cerf(d3-theta*d)*(-1./(m+thet
   a)+1./(m+opt->sigma+theta))+exp((m-theta)*k)*opt->K/(theta*
   psi(theta*d))*(-1./(m+opt->sigma-theta)+1./(m-theta))*(psi(
   -theta*d)+theta*racine*d*exp(l*opt->D)*normal cerf(-d3-th
   eta*d)));
   }
 /* x>L */
 if(opt->So>opt->L)
   return(bs(1,opt)-puoc(1,opt));
 /* K<L and x<L*/
 if(opt->K<=opt->L && opt->So<=opt->L)
   return (exp((m-theta)*b)/psi(theta*d)*(2.0*opt->K/(m*m-
   2.0*1)*psi(m*d) - 2.0*opt->L/(pow(m+opt->sigma,2)-2.0*1)*
   psi(d*(m+opt->sigma))) + exp(-2.0*b*theta)*psi(-theta*d)/(
   theta*psi(theta*d))*opt->K*exp((m+theta)*k)*(1.0/(m+theta)-
   1.0/(m+theta+opt->sigma)));
 return -1;
}
/* computes the Laplace Transforms of the price of single
* barrier Parisian options using pdic,
* pdoc, puic, puoc. Put prices are computed using parity
* relationships */
static complex double Ltransform( complex double 1, int cho
   ice, parisian t *opt)
{
 switch(choice)
   case 1: return pdic(l,opt);
     break;
   case 2: return pdoc(1,opt);
     break;
   case 3: return puic(1,opt);
     break;
   case 4: return puoc(1,opt);
     break;
   case 9: return bs(1,opt);
```

```
break;
 return WRONG;
/* compute the numerical inversion of Laplace transforms
* using Euler summation */
static double euler(int choice, parisian_t *opt, int N,
    int M)
{
  int i, Cnp;
 double sum, a, pit, run_sum, m;
  /* int N=15;
  * int M=15; */
  double A=13.8;
  complex double I = complex double(0.0,1.0);
  a=A/(2.0*opt->T);
 pit=M PI/opt->T;
  sum=exp(A/2.0)*0.5*(Ltransform(a,choice,opt)).real();
  for(i=1;i<N+1;i++)
    sum=sum+exp(A/2.0)*PNL ALTERNATE(i)*(Ltransform(a+pit*
    i*I, choice, opt)).real();
  run sum=sum; /* partial sum of sn */
  sum=0.0; /* partial exponential sum */
  Cnp = 1; /* binomial coefficients */
  for(i=0;i<M+1;i++)
    {
      sum=sum+ run sum * (double) Cnp ;
      run sum=run sum + exp(A/2.0)*PNL ALTERNATE(i+N+1)*
              (Ltransform(a+pit*(i+N+1)*I, choice, opt)).
    real();
      Cnp=(Cnp*(M-i))/(i+1);
 m=(opt->r-opt->delta-opt->sigma*opt->sigma/2.0)/opt->si
  return(exp(-(opt->r+m*m/2.0)*opt->T)*sum/opt->T/pow(2.0,
   M));
```

```
}
/* Parameter choice defines the option type as follows
 * 1. Parisian Down and In Call
 * 2. Parisian Down and Out Call
* 3. Parisian Up and In Call
 * 4. Parisian Up and Out Call
 * 5. Parisian Down and In Put
 * 6. Parisian Down and Out Put
 * 7. Parisian Up and In Put
* 8. Parisian Up and Out Put
 */
/* Computes the price of the corresponding single barrier
* Parisian option using Laplace inversion*/
static double SingleParisian(int choice, parisian_t *opt,
    int N, int M)
{
  parisian_t *new_opt = NewParisian_t(opt);
  double res;
  switch(choice)
    case 1: new opt->T=opt->T-opt->t; res = euler(choice,ne
    w_opt, N, M);
     break;
    case 2: new_opt->T=opt->T-opt->t; res = euler(choice,ne
    w_opt, N, M);
     break;
    case 3: new_opt->T=opt->T-opt->t; res = euler(choice,ne
    w_opt, N, M);
     break;
    case 4: new opt->T=opt->T-opt->t; res = euler(choice,
    new_opt, N, M);
     break;
    case 5:
```

new\_opt->So=1.0/opt->So;

```
new opt->L=1.0/opt->L;
    new opt->K=1.0/opt->K;
    new_opt->r=opt->delta;
    new opt->delta=opt->r;
    res = opt->K*opt->So*SingleParisian(3,new opt, N,
M);
  }
  break;
case 6:
  {
    new_opt->So=1.0/opt->So;
    new opt->L=1.0/opt->L;
    new_opt->K=1.0/opt->K;
    new opt->r=opt->delta;
    new_opt->delta=opt->r;
    res = opt->K*opt->So*SingleParisian(4,new_opt, N,
M);
  }
  break;
case 7:
  {
    new_opt->So=1.0/opt->So;
    new_opt->L=1.0/opt->L;
    new opt->K=1.0/opt->K;
    new_opt->r=opt->delta;
    new opt->delta=opt->r;
    res = opt->K*opt->So*SingleParisian(1,new opt, N,
M);
  }
  break;
case 8:
  {
    new opt->So=1.0/opt->So;
    new_opt->L=1.0/opt->L;
    new_opt->K=1.0/opt->K;
    new_opt->r=opt->delta;
    new_opt->delta=opt->r;
    res = opt->K*opt->So*SingleParisian(2,new_opt, N,
M);
  break;
```

```
case 9 : new opt->T=opt->T-opt->t; res = euler(9, new
    opt, N, M);
      break;
    case 10 :
        new opt->So=1.0/opt->So;
        new_opt->L=1.0/opt->L;
       new opt->K=1.0/opt->K;
       new_opt->r=opt->delta;
       new_opt->delta=opt->r;
        res = opt->K*opt->So*SingleParisian(9,new_opt, N,
    M);
      }
      break;
    default:
      {printf("wrong choice in SingleParisian{n"); abort();
    }
    }
  delete new opt;
  return(res);
}
static int LaplaceParisian(int outorin,int upordown,double
    s,NumFunc_1 *p,double l,double t,double delay,double r,
    double divid, double sigma, double inc, int N, int M, double *pt
    price,double *ptdelta)
{
  int choice;
  parisian_t *opt = new parisian_t;
  opt->T = t;
  opt->t = 0.0;
  opt->D = delay;
  opt->r = r;
  opt->sigma = sigma;
```

```
opt->delta = divid;
opt->So = s;
opt->L = 1;
opt->d = 0.0;
opt->K = p->Par[0].Val.V_DOUBLE;
if ((p->Compute) == &Put) {
  /* puop */
  if(outorin && upordown)
    choice = 8;
  /* pdop */
  else if(outorin && !upordown)
    choice = 6;
  /* puip */
  else if(!outorin && upordown)
    choice = 7;
  /* pdip */
  else /* (!outorin && !upordown) */
    choice = 5;
}
else{
  /* puoc */
  if(outorin && upordown)
    choice = 4;
  /* pdoc */
  else if(outorin && !upordown)
    choice = 2;
  /* puic */
  else if(!outorin && upordown)
    choice = 3;
  /* pdic */
  else /*if(!outorin && !upordown)*/
    choice = 1;
}
/*Price*/
*ptprice=SingleParisian(choice, opt, N, M);
/*Delta*/
opt->So = opt->So * (1.0+inc);
*ptdelta= ( SingleParisian(choice, opt, N, M) - *ptprice
  )/(s*inc);
```

```
delete opt;
 return OK;
extern "C"{
  int CALC(AP LaplaceParisian)(void *Opt,void *Mod,Pricing
    Method *Met)
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r,divid,limit;
    int upordown,outorin;
    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V DOUBLE/100.);
    limit=((ptOpt->Limit.Val.V_NUMFUNC_1)->Compute)((ptOpt-
    >Limit.Val.V_NUMFUNC_1)->Par,ptMod->T.Val.V_DATE);
    if ((ptOpt->DownOrUp).Val.V BOOL==DOWN)
      upordown=0;
    else upordown=1;
    if ((ptOpt->OutOrIn).Val.V_BOOL==OUT)
      outorin=1;
    else outorin=0;
    return LaplaceParisian(outorin,upordown,ptMod->SO.Val.
    V_PDOUBLE,
                           ptOpt->PayOff.Val.V_NUMFUNC_1,
                           limit,
                           ptOpt->Maturity.Val.V_DATE-pt
    Mod->T.Val.V_DATE,
                            (ptOpt->Limit.Val.V NUMFUNC 1)->
    Par[4].Val.V PDOUBLE,
                           r,
                           divid,
                           ptMod->Sigma.Val.V PDOUBLE, Met->
    Par[0].Val.V_DOUBLE,
                           Met->Par[1].Val.V_PINT,
```

```
Met->Par[2].Val.V PINT,
                         &(Met->Res[0].Val.V_DOUBLE),
                         &(Met->Res[1].Val.V_DOUBLE)
                         );
}
       int CHK_OPT(AP_LaplaceParisian)(void *Opt, void *
static
  Mod)
  Option* ptOpt=(Option*)Opt;
  TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
  if ((opt->RebOrNo).Val.V_BOOL==NOREBATE)
    if ((opt->EuOrAm).Val.V_BOOL==EURO)
      if ((opt->Parisian).Val.V_BOOL==OK)
        return OK;
  return WRONG;
}
static int MET(Init)(PricingMethod *Met,Option *Opt)
  static int first=1;
  if (first)
    {
      Met->Par[0].Val.V_PDOUBLE=0.01;
      Met->Par[1].Val.V_PINT=15;
      Met->Par[2].Val.V_PINT=15;
      first=0;
    }
 return OK;
}
PricingMethod MET(AP_LaplaceParisian)=
{
  "AP Laplace Parisian",
  { {"Delta Increment Rel", PDOUBLE, {100}, ALLOW},
    {"sum truncation", PINT, {15}, ALLOW},
```

## References