```
Help
 Author: Syoiti Ninomiya
 Tokyo Institute of Technology
 Implementation of Kusuoka-Ninomyia-Ninomyia algorithm "A
   new Weak approximation of stochastic differential equations
    by using Runge-Kutta method"
 */
#include "hes1d pad.h"
/***********************************
   *****/
/* */
*****/
#include <math.h>
#include <stdlib.h>
#include <stdio.h>
static double dt, sq_dt, mu, rho_gl, alpha_gl, theta_gl,
   beta gl;
static const double c1 = 0.5;
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <</pre>
     (2007+2) //The "#else" part of the code will be freely av
   ailable after the (year of creation of this file + 2)
static int CHK_OPT(MC_AsianKNN_Heston)(void *Opt, void *
   Mod)
 return NONACTIVE;
int CALC(MC AsianKNN Heston) (void *Opt, void *Mod, Pricing
   Method *Met)
return AVAILABLE IN FULL PREMIA;
}
#else
```

```
static double *vZ(double *sig, double *initial, double *de
   stination){
 double sq_y2;
 sq y2 = sqrt(fabs(initial[1]));
 destination[0] =
 c1*dt*initial[0]*(mu-0.5*initial[1]-rho_gl*beta_gl/4.0)
 + sig[0]*sq dt*initial[0]*sq y2;
 destination[1] =
 c1*dt*(alpha_gl*(theta_gl-initial[1])-beta_gl*beta_gl/4.0
   )
 + sig[0]*sq dt*rho gl*beta gl*sq y2
 + sig[1]*sq_dt*beta_gl*sqrt((1.0-rho_gl*rho_gl)*fabs(ini
   tial[1]));
 destination[2] = c1*dt*initial[0];
 return destination;
}
static double *ExpZ5th(double *sig, double *initial,
   double *destination){
  * order 5 method (6-stages)
  * 0 |
  * 2/5 | 2/5
  * 1/4 | 11/64 5/64
  * 1/2 | 0
                       1/2
                0
  * 3/4 | 3/64 -15/64 3/8
                                9/16
  * 1 | 0
               5/7 6/7
                                -12/7
                                       8/7
                      32/90 12/90 32/90 7/90
       | 7/90
               0
  * Corresponding Butcher Array
  */
 double Y1[3], Y2[3], Y3[3], Y4[3], Y5[3];
 double fY0[3], fY1[3], fY2[3], fY3[3], fY4[3], fY5[3];
 double *pf0, *pf1, *pf2, *pf3, *pf4, *pf5;
 int i;
 pf0 = vZ(sig, initial, fY0);
 for (i=0; i<3; i++)
```

```
Y1[i] = initial[i] + pf0[i];
  pf1 = vZ(sig, Y1, fY1);
  for (i=0; i<3; i++)
    Y2[i] = initial[i] + (11.0/64.0)*pf0[i] + (5.0/64.0)*pf
    1[i];
  pf2 = vZ(sig, Y2, fY2);
  for (i=0; i<3; i++)
    Y3[i] = initial[i] + (1.0/2.0)*pf2[i];
  pf3 = vZ(sig, Y3, fY3);
  for (i=0; i<3; i++)
    Y4[i] = initial[i] + (3.0/64.0)*pf0[i] - (15.0/64.0)*pf
    1[i]
    + (3.0/8.0)*pf2[i] + (9.0/16.0)*pf3[i];
  pf4 = vZ(sig, Y4, fY4);
  for (i=0; i<3; i++)
    Y5[i] = initial[i] + (5.0/7.0)*pf1[i] + (6.0/7.0)*pf2[
    i٦
    -(12.0/7.0)*pf3[i] + (8.0/7.0)*pf4[i];
  pf5 = vZ(sig, Y5, fY5);
  for (i=0; i<3; i++)
    destination[i] = initial[i] + (7.0/90.0)*pf0[i] + (32.0)
    /90.0)*pf2[i]
    + (12.0/90.0)*pf3[i] + (32.0/90.0)*pf4[i] + (7.0/90.0)*
    pf5[i];
 return destination;
}
static int MCAsianKNN(double x0, NumFunc_2 *p, double T,
    double r, double divid, double y0, double alpha, double theta,
    double beta, double rho, long niter, int n_steps, double inc,
    double *ptprice, double *ptdelta)
{
  double K, sqrt2;
  double *u_seq1, *u_seq2, *n_seq1, *n_seq2;
  K=p->Par[0].Val.V DOUBLE;
  mu=r-divid;
  dt = T/(double)n_steps; sq_dt = sqrt(dt);
 rho gl = rho; alpha gl = alpha; beta gl = beta; theta gl
    = theta;
  sqrt2 = sqrt(2.0);
```

```
u_seq1 = (double *)calloc(4*n_steps, sizeof(double));
u_seq2 = u_seq1 + 2*n_steps;
n seq1 = (double *)calloc(4*n steps, sizeof(double));
n \text{ seq2} = n \text{ seq1} + 2*n \text{ steps};
{
  double sum, x[2][3], dsum, dx[2][3];
  double *last=NULL, *dlast=NULL;
  long int i;
  int j;
  for (dsum=sum=0.0, i=0; i < niter; i++){
    b2_g_sobol_seq("G_SOBOL_1", 4*n_steps, u_seq1);
      int k;
      for (k=0; k<2*n_steps; k++){
        n \text{ seq1[k]} = \text{sqrt}(-2.0*\log(u \text{ seq1[k]}))*\cos(2.0*M)
  PI*u seq2[k]);
        n_{seq2[k]} = sqrt(-2.0*log(u_{seq1[k]}))*sin(2.0*M_{seq1[k]})
  PI*u seq2[k]);
      } /** for (k) **/
    for (x[0][0]=x0, dx[0][1]=x[0][1]=y0, dx[0][2]=x[0][2]
  =0.0,
        dx[0][0]=x0*(1.0+inc), j=0;
        j < n steps; j++){</pre>
      double sig1[2], sig2[2]; /** sig1 is for Z 1, sig2
  is for Z 2 **/
      sig1[0] = 0.5*n seq1[2*j] + n seq1[2*j+1]/sqrt2;
      sig2[0] = 0.5*n_seq1[2*j] - n_seq1[2*j+1]/sqrt2;
      sig1[1] = 0.5*n_seq2[2*j] + n_seq2[2*j+1]/sqrt2;
      sig2[1] = 0.5*n seq2[2*j] - n seq2[2*j+1]/sqrt2;
      last = ExpZ5th(sig2, ExpZ5th(sig1, x[0], x[1]), x[0]
  ]);
      dlast = ExpZ5th(sig2, ExpZ5th(sig1, dx[0], dx[1]),
  dx[0]);
    } /** for (j) **/
    if ((p->Compute) == &Call_OverSpot2){
      sum += (last[2]/(double)T - K > 0)? last[2]/(
  double)T - K : 0;
      dsum += (dlast[2]/(double)T - K > 0)? dlast[2]/(
```

```
double)T - K : 0;
      }else{
        if ((p->Compute) == &Put_OverSpot2){
          sum += (K-last[2]/(double)T > 0)? K-last[2]/(
    double)T : 0;
          dsum += (K-dlast[2]/(double)T > 0)? K-dlast[2]/(
    double)T
             : 0;
        }
    } /** for (i) **/
    *ptprice = exp(-r*T)*sum/(double)niter;
    *ptdelta=exp(-r*T)*(dsum-sum)/(double)niter/inc/x0;
  free(u seq1);
  free(n_seq1);
 b2_g_sobol_free();
 return OK;
}
int CALC(MC_AsianKNN_Heston)(void *Opt, void *Mod, Pricing
    Method *Met)
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
  TYPEMOD* ptMod=(TYPEMOD*)Mod;
 double r, divid;
  r=log(1.+ptMod->R.Val.V DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
 return MCAsianKNN(ptMod->SO.Val.V PDOUBLE,
                    ptOpt->PayOff.Val.V NUMFUNC 2,
                    ptOpt->Maturity.Val.V_DATE-ptMod->T.Val
    .V DATE, r, divid,
                    ptMod->SigmaO.Val.V PDOUBLE,ptMod->Mea
    nReversion.hal.V_PDOUBLE,
                    ptMod->LongRunVariance.Val.V_PDOUBLE,
                    ptMod->Sigma.Val.V PDOUBLE,
                    ptMod->Rho.Val.V_PDOUBLE,
                    Met->Par[0].Val.V_LONG,
```

```
Met->Par[1].Val.V INT,
                    Met->Par[2].Val.V DOUBLE,
                    &(Met->Res[0].Val.V_DOUBLE),
                    &(Met->Res[1].Val.V DOUBLE)
    );
}
static int CHK_OPT(MC_AsianKNN_Heston)(void *Opt, void *
    Mod)
{
  if ( (strcmp( ((Option*)Opt)->Name, "AsianCallFixedEuro")=
       || (strcmp( ((Option*)Opt)->Name," AsianPutFixedEuro")==0) )
    return OK;
  return WRONG;
}
#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if (Met->init == 0)
    {
      Met->init=1;
      Met->Par[0].Val.V LONG=10000;
      Met->Par[1].Val.V_INT=100;
      Met->Par[2].Val.V_PDOUBLE=0.001;
  return OK;
}
PricingMethod MET(MC AsianKNN Heston)=
  "MC_Asian_KNN_Hes",
  {{"N iterations",LONG,{100},ALLOW},
   {"TimeStepNumber", LONG, {100}, ALLOW},
   {"Delta Increment Rel", PDOUBLE, {100}, ALLOW},
   {" ",PREMIA_NULLTYPE, {0}, FORBID}},
```

```
CALC(MC_AsianKNN_Heston),
   {{"Price",DOUBLE,{100},FORBID},
        {"Delta",DOUBLE,{100},FORBID} ,
        {" ",PREMIA_NULLTYPE,{0},FORBID}},
        CHK_OPT(MC_AsianKNN_Heston),
        CHK_mc,
        MET(Init)
};
```

References