

[Help](#)

```
#include "hullwhite2d_std.h"
#include "hullwhite2d_includes.h"

//The "#else" part of the code will be freely available after the (year of creation of this file + 2)
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion < (2009+2)
int CALC(CF_ZCBONDHW2D)(void *Opt,void *Mod,PricingMethod *Met)
{
return AVAILABLE_IN_FULL_PREMIA;
}
static int CHK_OPT(CF_ZCBONDHW2D)(void *Opt, void *Mod)
{
return NONACTIVE;
}
#else

void ZCPrice_Coefficient(ZCMarketData* ZCMarket, double a,
double sigma1, double b, double sigma2, double rho, double t,
double T, double* A_tT, double* B_tT, double* C_tT)
{
double B_0t, B_0T, C_0t, C_0T;
double f0_t,P0_t,P0_T,P0_t_plus,P0_t_minus;
double exp_at, exp_aT, exp_bt, exp_bT;
double gamma1, gamma2, gamma3, gamma4, gamma5, gamma6;
double eta;
double epsilon = 1e-3;

/*Computation pure discount*/
P0_t=BondPrice(t, ZCMarket);
P0_T=BondPrice(T, ZCMarket);

/*Computation of Forward rate*/
P0_t_plus=BondPrice(t*(1.+epsilon), ZCMarket);
P0_t_minus=BondPrice(t*(1.-epsilon), ZCMarket);
f0_t=-(log(P0_t_plus)-log(P0_t_minus))/(2.*t*epsilon);

/*A,B,C coefficient*/
exp_at = exp(a*t);
```

```

exp_aT = exp(a*T);
exp_bt = exp(b*t);
exp_bT = exp(b*T);

(*B_tT) = (1 - exp_at/exp_aT) / a;
B_0T = (1 - 1./exp_aT) / a;
B_0t = (1 - 1./exp_at) / a;

(*C_tT) = exp_at/(exp_aT*a*(a-b)) - exp_bt/(exp_bT*b*(a-b)) + 1./(a*b);
C_0T = 1./(exp_aT*a*(a-b)) - 1./(exp_bT*b*(a-b)) + 1./(a*b);
C_0t = 1./(exp_at*a*(a-b)) - 1./(exp_bt*b*(a-b)) + 1./(a*b);

gamma1 = (exp_at*exp_bt-1)/(exp_aT*exp_bT * (a-b) * (a+b)) - (SQR(exp_at) -1)/(SQR(exp_aT)* 2*a * (a-b));
gamma2 = (gamma1 + (*C_tT) - C_0T + 0.5*(*B_tT)*(*B_tT) - 0.5*B_0T*B_0T + t/a - (exp_at/exp_aT - 1./exp_aT)/SQR(a)) / (a*b) ;
gamma3 = -(1/(exp_at*exp_bt)-1) / ((a-b)*(a+b)) + (1/(SQR(exp_at))-1)/(2*a*(a-b));
gamma4 = (gamma3 - C_0t - 0.5*SQR(B_0t) + t/a + (1/exp_at - 1)/SQR(a)) / (a*b);
gamma5 = (0.5*SQR(*C_tT) - 0.5*SQR(C_0T) + gamma2)/b;
gamma6 = (gamma4 - 0.5*SQR(C_0t))/b;

eta = SQR(sigma1)*(1 - 1/SQR(exp_at))*SQR(*B_tT)/(4*a) - rho*sigma1*sigma2*( B_0t*C_0t*(*B_tT) + gamma4 - gamma2);
eta = eta - 0.5*SQR(sigma2)*( SQR(C_0t)*(*B_tT) + gamma6 - gamma5);

(*A_tT) = (P0_T/P0_t)*exp((*B_tT)*f0_t-eta);

}

// Price of a ZC using the three coefficient A(t,T), B(t,T) and C(tT). H&W is a affine model.
double ZCPrice_Using_Coefficient(double r_t, double u_t, double A_tT, double B_tT, double C_tT)

```

```

{
    return A_tT*exp(-B_tT*r_t - C_tT*u_t);
}

// Price at date t of a ZC maturing at T, knowing that r(t)
// =r_t and u(t)=u_t.
double cf_hw2d_zcb(ZCMarketData* ZCMarket, double a,
    double sigma1, double b, double sigma2, double rho, double t,
    double r_t, double u_t, double T)
{
    if(t==0)
    {
        return BondPrice(T, ZCMarket);;
    }
    else
    {
        double price;
        double A_tT, B_tT, C_tT;
        A_tT=0; B_tT=0; C_tT=0;

        ZCPrice_Coefficient(ZCMarket, a, sigma1, b, sigma2,
            rho, t, T, &A_tT, &B_tT, &C_tT);
        price = ZCPrice_Using_Coefficient(r_t, u_t, A_tT,
            B_tT, C_tT);

        return price;
    }
}

static int cf_zcbond2d(int flat_flag,double r_t,double u_t,
    double a,double sigma1,double b,double sigma2,double rho,double
    T,double *price)
{
    ZCMarketData ZCMarket;

    /* Flag to decide to read or not ZC bond datas in "initia
        lyields.dat" */
    /* If P(0,T) not read then P(0,T)=exp(-r0*T) */
    if(flat_flag==0)
    {

```

```

        ZCMarket.FlatOrMarket = 0;
        ZCMarket.Rate = r_t;
    }

    else
    {
        ZCMarket.FlatOrMarket = 1;
        ReadMarketData(&ZCMarket);

        if(T > GET(ZCMarket.tm,ZCMarket.Nvalue-1))
        {
            printf("{nError : time bigger than the last time
value entered in initialyield.dat{n");
            exit(EXIT_FAILURE);
        }
    }

    //Price of an option on a ZC
    *price = cf_hw2d_zcb(&ZCMarket, a, sigma1, b,sigma2, rho,
        0, r_t, u_t, T);

    DeleteZCMarketData(&ZCMarket);

    return OK;
}

int CALC(CF_ZCBONDHW2D)(void *Opt,void *Mod,PricingMethod *
    Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;

    return  cf_zcbond2d(ptMod->flat_flag.Val.V_INT,
        MOD(GetYield)(ptMod),
        ptMod->InitialYieldsu.Val.V_PDOUBLE,
        ptMod->aR.Val.V_DOUBLE,
        ptMod->SigmaR.Val.V_PDOUBLE,
        ptMod->bu.Val.V_DOUBLE,
        ptMod->Sigmau.Val.V_PDOUBLE,
        ptMod->Rho.Val.V_PDOUBLE,
        ptOpt->BMaturity.Val.V_DATE-ptMod->T.

```

```

        Val.V_DATE,
                                &(Met->Res[0].Val.V_DOUBLE));
    }
    static int CHK_OPT(CF_ZCBONDHW2D)(void *Opt, void *Mod)
    {
        return strcmp( ((Option*)Opt)->Name,"ZeroCouponBond");
    }
#endif //PremiaCurrentVersion

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;
    }

    return OK;
}

PricingMethod MET(CF_ZCBONDHW2D)=
{
    "CF_ZCBondHW2d",
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(CF_ZCBONDHW2D),
    {"Price",DOUBLE,{100},FORBID}/*,{"Delta",DOUBLE,{100},FORBID}*/,
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(CF_ZCBONDHW2D),
    CHK_ok,
    MET(Init)
} ;

```

References