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    Help
/*
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    Implementation of Ninomyia-Victoir paper "Weak approxima
        tion of stochastic differential equations and application
        to derivative pricing"
*/

#include "hes1d_pad.h"

/*****
    *****/
/* */
/* */
/*****
    *****/

#include <math.h>
#include <stdlib.h>
#include <stdio.h>

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2007+2) //The "#else" part of the code will be freely av
        ailable after the (year of creation of this file + 2)
static int CHK_OPT(MC_AsianKusuoka_Heston)(void *Opt, void
    *Mod)
{
    return NONACTIVE;
}
int CALC(MC_AsianKusuoka_Heston)(void *Opt, void *Mod,
    PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else
static double *expV0(double s, double *initial, double *de
    stination,
        double mu, double rho, double alpha, double bet
    a,
        double theta){

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double J, A;

J = theta - 0.25*beta*beta/alpha;
A = mu - 0.25*rho*beta - 0.5*initial[1];
destination[0] =
    initial[0]*exp((mu-rho*beta*0.25-0.5*J)*s
        +(initial[1]-J)*0.5/alpha*(exp(-alpha*s)-1.0));
destination[1] = J+(initial[1]-J)*exp(-alpha*s);
destination[2] = initial[2]+initial[0]*(exp(A*s)-1.0)/A;
return destination;
}

static double *expV1(double s, double *initial, double *de
    stination,
        double mu, double rho, double alpha, double bet
    a,
        double theta){
double X, sqrt_y2;

sqrt_y2 = sqrt(initial[1]);
X = 0.5*rho*beta*s + sqrt_y2;
destination[0] =
    initial[0]*exp(s*(0.25*rho*beta*s + sqrt_y2));
destination[1] = X*X;
destination[2] = initial[2];
return destination;
}

static double *expV2(double s, double *initial, double *de
    stination,
        double mu, double rho, double alpha, double bet
    a,
        double theta){
double X;

X = 0.5*sqrt(1.0-rho*rho)*beta*s + sqrt(initial[1]);
destination[0] = initial[0];
destination[1] = X*X;
destination[2] = initial[2];
return destination;
}

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static int MCAAsianKusuoka(double x0, NumFunc_2 *p, double
    T, double r, double divid, double y0, double alpha, double th
    eta, double beta, double rho, long niter, int n_steps, double
    inc, double *ptprice, double *ptdelta)
{
    double K, mu, dt, sq_dt;
    double *u_seq1, *u_seq2, *n_seq1, *n_seq2, *ber_seq;

    K=p->Par[0].Val.V_DOUBLE;
    mu=r-divid;
    dt = T/(double)n_steps;
    sq_dt = sqrt(dt);

    u_seq1 = (double *)calloc(3*n_steps, sizeof(double));
    u_seq2 = u_seq1 + n_steps;
    ber_seq = u_seq1 + 2*n_steps;
    n_seq1 = (double *)calloc(2*n_steps, sizeof(double));
    n_seq2 = n_seq1 + n_steps;

    {
        double sum, x[4][3], dsum, dx[4][3];
        double *last=NULL, *dlast=NULL;
        long int i;
        int j;

        for (dsum=sum=0.0, i=0; i < niter; i++){
            b2_g_sobol_seq("G_SOBOL_1", 3*n_steps, u_seq1);
            {
                int k;
                for (k=0; k<n_steps; k++){
                    n_seq1[k] = sqrt(-2.0*log(u_seq1[k]))*cos(2.0*M_PI*u_
                        seq2[k]);
                    n_seq2[k] = sqrt(-2.0*log(u_seq1[k]))*sin(2.0*M_PI*u_
                        seq2[k]);
                }
                /** for (k) **/
                for(x[0][0]=x0, dx[0][1]=x[0][1]=y0, dx[0][2]=x[0][2]
                    =0.0,
                    dx[0][0]=x0*(1.0+inc), j=0;

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    j < n_steps; j++){
/* int k;*/
if (ber_seq[j] > 0.5){
    last=
        expV0(0.5*dt,
        expV1(sq_dt*n_seq1[j],
        expV2(sq_dt*n_seq2[j],
            expV0(0.5*dt,
                x[0], x[1], mu, rho, alpha, beta, theta),
                x[2], mu, rho, alpha, beta, theta),
            x[3], mu, rho, alpha, beta, theta),
            x[0], mu, rho, alpha, beta, theta);
    dlast=
        expV0(0.5*dt,
        expV1(sq_dt*n_seq1[j],
        expV2(sq_dt*n_seq2[j],
            expV0(0.5*dt,
                dx[0], dx[1], mu, rho, alpha, beta, theta),
                dx[2], mu, rho, alpha, beta, theta),
            dx[3], mu, rho, alpha, beta, theta),
            dx[0], mu, rho, alpha, beta, theta);
}else{ /** ber_seq[j] <= 0.5 **/
    last=
        expV0(0.5*dt,
        expV2(sq_dt*n_seq1[j],
        expV1(sq_dt*n_seq2[j],
            expV0(0.5*dt,
                x[0], x[1], mu, rho, alpha, beta, theta),
                x[2], mu, rho, alpha, beta, theta),
            x[3], mu, rho, alpha, beta, theta),
            x[0], mu, rho, alpha, beta, theta);
    dlast=
        expV0(0.5*dt,
        expV2(sq_dt*n_seq1[j],
        expV1(sq_dt*n_seq2[j],
            expV0(0.5*dt,
                dx[0], dx[1], mu, rho, alpha, beta, theta),
                dx[2], mu, rho, alpha, beta, theta),
            dx[3], mu, rho, alpha, beta, theta),
            dx[0], mu, rho, alpha, beta, theta);
}

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        } /** for (j) */
        if ((p->Compute) == &Call_OverSpot2){
sum += (last[2]/(double)T - K > 0)? last[2]/(double)T -
    K : 0;
dsum += (dlast[2]/(double)T - K > 0)? dlast[2]/(double)
    T - K : 0;
        }else{
if ((p->Compute) == &Put_OverSpot2){
    sum += (K-last[2]/(double)T > 0)? K-last[2]/(double)
        T : 0;
    dsum += (K-dlast[2]/(double)T > 0)? K-dlast[2]/(
        double)T : 0;
}
    }
} /** for (i) */

*ptprice = exp(-r*T)*sum/(double)niter;
*ptdelta=exp(-r*T)*(dsum-sum)/(double)niter/inc/x0;
}

free(u_seq1);
free(n_seq1);
b2_g_sobol_free();

return OK;
}

int CALC(MC_AasianKusuoka_Heston)(void *Opt, void *Mod,
    PricingMethod *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r,divid;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    return MCAAsianKusuoka(ptMod->S0.Val.V_PDOUBLE,
        ptOpt->PayOff.Val.V_NUMFUNC_2,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,r,

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divid, ptMod->Sigma0.Val.V_PDOUBLE,ptMod->MeanReversion.hal.
V_PDOUBLE,
    ptMod->LongRunVariance.Val.V_PDOUBLE,
    ptMod->Sigma.Val.V_PDOUBLE,
    ptMod->Rho.Val.V_PDOUBLE,
    Met->Par[0].Val.V_LONG,
    Met->Par[1].Val.V_INT,
    Met->Par[2].Val.V_DOUBLE,
    &(Met->Res[0].Val.V_DOUBLE),
    &(Met->Res[1].Val.V_DOUBLE));

}

static int CHK_OPT(MC_AasianKusuoka_Heston)(void *Opt, void
    *Mod)
{
    if ( (strcmp( ((Option*)Opt)->Name,"AsianCallFixedEuro")=
        =0)
        || (strcmp( ((Option*)Opt)->Name,"    AsianPutFixedEuro")==0) )
        return OK;

    return  WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_LONG=10000;
        Met->Par[1].Val.V_INT=100;
        Met->Par[2].Val.V_PDOUBLE=0.001;

    }

    return OK;
}

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PricingMethod MET(MC_AsianKusuoka_Heston)=
{
    "MC_Asian_NV_Hes",
    {"N iterations",LONG,{100},ALLOW},
    {"TimeStepNumber",LONG,{100},ALLOW},
    {"Delta Increment Rel",PDOUBLE,{100},ALLOW},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(MC_AsianKusuoka_Heston),
    {"Price",DOUBLE,{100},FORBID},
    {"Delta",DOUBLE,{100},FORBID} ,
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(MC_AsianKusuoka_Heston),
    CHK_mc,
    MET(Init)
};
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## References