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Help
#include <stdlib.h>
#include "merhes1d std.h"
#include "pnl/pnl basis.h"
#include "math/alfonsi.h"
#include "enums.h"
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <</pre>
     (2010+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK OPT(MC AM Alfonsi LongstaffSchwartz Bates)(
    void *Opt, void *Mod)
{
  return NONACTIVE;
}
int CALC(MC_AM_Alfonsi_LongstaffSchwartz_Bates)(void *Opt,
    void *Mod,PricingMethod *Met)
  return AVAILABLE_IN_FULL_PREMIA;
#else
/** Lower bound for american option using Longstaff-Schwa
    rtz algorithm **/
// Exercice dates are : T(0), T(1), ..., T(NbrExerciseDate
    s-1).
// with T(0)=0 and T(NbrExerciseDates-1)=Maturity.
static int MC_Am_Alfonsi_LoSc_Bates(NumFunc_1 *p, double S0
    , double Maturity, double r, double divid, double VO,
    double k, double theta, double sigma, double rho, double mu_
    jump, double gamma2, double lambda, long NbrMCsimulation, int Nb
    rExerciseDates, int NbrStepPerPeriod, int generator,
    basis name, int DimApprox, double confidence, int flag cir,
    double *ptPriceAm, double *ptPriceAmError, double *ptInfPriceAm,
     double *ptSupPriceAm)
{
  int j, m, nbr_var_explicatives, init_mc;
  int flag_SpotPaths, flag_VarPaths, flag_AveragePaths;
  double continuation value, discounted payoff, european
    price, european_delta, S_t, V_t, discount_step, discount, step,
     exercise_date, z_alpha, mean_price, var_price;
```

```
double *VariablesExplicatives;
PnlMat *SpotPaths, *VarPaths, *AveragePaths, *Explicati
  veVariables;
PnlVect *DiscountedOptimalPayoff, *RegressionCoeffVect;
PnlBasis *basis;
/* Value to construct the confidence interval */
z_alpha= pnl_inv_cdfnor((1.+ confidence)/2.);
step = Maturity / (double)(NbrExerciseDates-1);
discount step = exp(-r*step);
discount = exp(-r*Maturity);
/* We store Spot and Variance*/
flag SpotPaths = 1;
flag VarPaths = 1;
flag_AveragePaths = 0;
european price = 0.;
european delta = 0.;
nbr var explicatives = 2;
basis = pnl_basis_create(basis_name, DimApprox, nbr_var_e
  xplicatives);
VariablesExplicatives = malloc(nbr var explicatives*size
  of(double));
ExplicativeVariables = pnl mat create(NbrMCsimulation, nb
  r var explicatives);
DiscountedOptimalPayoff = pnl_vect_create(NbrMCsimulatio
  n); // Continuation Value
RegressionCoeffVect = pnl vect create(0);
SpotPaths = pnl_mat_create(0, 0); // Matrix of the whole
  trajectories of the spot
VarPaths = pnl mat create(0, 0); // Matrix of the whole
  trajectories of the variance
AveragePaths = pnl_mat_create(0, 0);
```

```
init mc=pnl rand init(generator, NbrExerciseDates*NbrStep
 PerPeriod, NbrMCsimulation);
if (init_mc != OK) return init_mc;
// Simulation of the whole paths
BatesSimulation_Alfonsi (flag_SpotPaths, SpotPaths, flag_
  VarPaths, VarPaths, flag AveragePaths, AveragePaths, SO, Matu
  rity, r, divid, VO, k, theta, sigma, rho, mu_jump, gamma2,
  lambda, NbrMCsimulation, NbrExerciseDates, NbrStepPerPeriod,
   generator, flag_cir);
// At maturity, the price of the option = discounted_payoff
exercise date = Maturity;
for (m=0; m<NbrMCsimulation; m++)</pre>
    S t = MGET(SpotPaths, NbrExerciseDates-1, m); // Simu
  lated Value of the spot at the maturity T
    LET(DiscountedOptimalPayoff, m) = discount * (p->
  Compute)(p->Par, S t); // Discounted payoff
  }
for (j=NbrExerciseDates-2; j>=1; j--)
  {
    /** Least square fitting **/
    exercise date -= step;
    discount /= discount step;
    for (m=0; m<NbrMCsimulation; m++)</pre>
        V t = MGET(VarPaths, j, m); // Simulated value of
   the variance
        S_t = MGET(SpotPaths, j, m); // Simulated value
  of the spot
        ApAlosHeston(S t, p, Maturity-exercise date, r,
  divid, V t, k, theta, sigma, rho, & european price, & european
  delta);
        MLET(ExplicativeVariables, m, 0) = discount*euro
  pean_price/S0;
        MLET(ExplicativeVariables, m, 1) = discount*euro
```

```
pean_delta*S_t*sqrt(V_t)/S0;
    pnl basis fit ls(basis, Regression Coeff Vect, Explicati
  veVariables, DiscountedOptimalPayoff);
    /** Dynamical programming equation **/
    for (m=0; m<NbrMCsimulation; m++)</pre>
      {
        V_t = MGET(VarPaths, j, m); // Simulated value of
   the variance
        S t = MGET(SpotPaths, j, m); // Simulated value
  of the spot
        discounted payoff = discount * (p->Compute)(p->
  Par, S_t); // Discounted payoff
        if (discounted payoff>0.) // If the payoff is nul
  1, the OptimalPayoff doesnt change.
            ApAlosHeston(S t, p, Maturity-exercise date,
  r, divid, V_t, k, theta, sigma, rho, &european_price, &euro
  pean_delta);
            VariablesExplicatives[0] = discount*european
  price/S0;
            VariablesExplicatives[1] = discount*european_
  delta*S t*sqrt(V t)/S0;
            continuation_value = pnl_basis_eval(basis,Reg
  ressionCoeffVect, VariablesExplicatives);
            if (discounted payoff > continuation value)
                LET(DiscountedOptimalPayoff, m) = discoun
  ted payoff;
              }
          }
      }
  }
discount /= discount_step;
```

```
// At initial date, no need for regression, continuation
   value is just a plain expectation estimated with empirical
   mean.
 continuation value = pnl vect sum(DiscountedOptimalPayof
   f)/(double)NbrMCsimulation;
 discounted_payoff = discount*(p->Compute)(p->Par, S0);
 /* Price */
 mean_price = MAX(discounted_payoff, continuation_value);
 /* Sum of squares */
 var_price = SQR(pnl_vect_norm_two(DiscountedOptimalPayof
   f))/(double)NbrMCsimulation;
 var_price = MAX(var_price, SQR(discounted_payoff)) - SQR(
   mean_price);
 /* Price estimator */
 *ptPriceAm = mean_price;
 *ptPriceAmError = sqrt(var price/((double)NbrMCsimulatio
   n-1));
 /* Price Confidence Interval */
 *ptInfPriceAm= *ptPriceAm - z alpha*(*ptPriceAmError);
 *ptSupPriceAm= *ptPriceAm + z_alpha*(*ptPriceAmError);
 free(VariablesExplicatives);
 pnl_basis_free (&basis);
 pnl mat free(&SpotPaths);
 pnl_mat_free(&VarPaths);
 pnl mat free(&AveragePaths);
 pnl mat free(&ExplicativeVariables);
 pnl_vect_free(&DiscountedOptimalPayoff);
 pnl vect free(&RegressionCoeffVect);
 return OK;
int CALC(MC_AM_Alfonsi_LongstaffSchwartz_Bates)(void *Opt,
```

}

```
void *Mod, PricingMethod *Met)
TYPEOPT* ptOpt=(TYPEOPT*)Opt;
TYPEMOD* ptMod=(TYPEMOD*)Mod;
double r, divid;
r=log(1.+ptMod->R.Val.V DOUBLE/100.);
divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
return MC_Am_Alfonsi_LoSc_Bates(ptOpt->PayOff.Val.V_
  NUMFUNC 1,
                                 ptMod->SO.Val.V PDOUBLE,
                                 ptOpt->Maturity.Val.V_DA
  TE-ptMod->T.Val.V_DATE,
                                 r,
                                 divid,
                                 ptMod->SigmaO.Val.V_PDOUB
  LE,
                                 ptMod->MeanReversion.hal.
  V PDOUBLE,
                                 ptMod->LongRunVariance.
  Val.V_PDOUBLE,
                                 ptMod->Sigma.Val.V PDOUB
  LE,
                                 ptMod->Rho.Val.V PDOUBLE,
                                 ptMod->Mean.Val.V PDOUB
  LE,
                                 ptMod->Variance.Val.V PDO
  UBLE,
                                 ptMod->Lambda.Val.V_PDOUB
  LE,
                                 Met->Par[0].Val.V_LONG,
                                 Met->Par[1].Val.V_INT,
                                 Met->Par[2].Val.V INT,
                                 Met->Par[3].Val.V ENUM.
  value,
                                 Met->Par[4].Val.V_ENUM.
  value,
                                 Met->Par[5].Val.V_INT,
                                 Met->Par[6].Val.V_PDOUB
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LE,
                                  Met->Par[7].Val.V ENUM.
    value,
                                  &(Met->Res[0].Val.V
    DOUBLE),
                                  &(Met->Res[1].Val.V
    DOUBLE),
                                  &(Met->Res[2].Val.V
    DOUBLE),
                                  &(Met->Res[3].Val.V
    DOUBLE));
}
static int CHK_OPT(MC_AM_Alfonsi_LongstaffSchwartz_Bates)(
    void *Opt, void *Mod)
  Option* ptOpt=(Option*)Opt;
 TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);
  if ((opt->EuOrAm).Val.V BOOL==AMER)
    return OK;
    return WRONG;
#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if (Met->init == 0)
      Met->init=1;
      Met->HelpFilenameHint = " mc am alfonsi longstaffschwartz merhes";
      Met->Par[0].Val.V LONG=100000;
      Met->Par[1].Val.V_INT=10;
      Met->Par[2].Val.V INT=1;
      Met->Par[3].Val.V ENUM.value=0;
      Met->Par[3].Val.V_ENUM.members=&PremiaEnumRNGs;
      Met->Par[4].Val.V_ENUM.value=0;
      Met->Par[4].Val.V ENUM.members=&PremiaEnumBasis;
      Met->Par[5].Val.V_INT=10;
      Met->Par[6].Val.V_DOUBLE= 0.95;
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Met->Par[7].Val.V ENUM.value=2;
      Met->Par[7].Val.V ENUM.members=&PremiaEnumCirOrder;
    }
  return OK;
}
PricingMethod MET(MC_AM_Alfonsi_LongstaffSchwartz_Bates)=
  "MC_AM_Alfonsi_LongstaffSchwartz_Bates",
  {
    {"N Simulations", LONG, {100}, ALLOW},
    {"N Exercise Dates", INT, {100}, ALLOW},
    {"N Steps per Period", INT, {100}, ALLOW},
    {"RandomGenerator", ENUM, {100}, ALLOW},
    {"Basis", ENUM, {100}, ALLOW},
    {"Dimension Approximation", INT, {100}, ALLOW},
    {"Confidence Value", DOUBLE, {100}, ALLOW},
    {"Cir Order", ENUM, {100}, ALLOW},
    {" ",PREMIA NULLTYPE, {O}, FORBID}},
  CALC(MC_AM_Alfonsi_LongstaffSchwartz_Bates),
  {
    {"Price", DOUBLE, {100}, FORBID},
    {"Error Price", DOUBLE, {100}, FORBID},
    {"Inf Price", DOUBLE, {100}, FORBID},
    {"Sup Price", DOUBLE, {100}, FORBID},
    {" ",PREMIA NULLTYPE, {0}, FORBID}},
  CHK OPT(MC AM Alfonsi LongstaffSchwartz Bates),
  CHK ok,
  MET(Init)
};
```

## References