

Help

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#include "mer1d_pad.h"
#include "pnl/pnl_cdf.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2009+2) //The "#else" part of the code will be freely available after the (year of creation of this file + 2)
static int CHK_OPT(MC_Merton_FloatingLookback)(void *Opt,
    void *Mod)
{
    return NONACTIVE;
}
int CALC(MC_Merton_FloatingLookback)(void*Opt,void *Mod,
    PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else
static int Merton_Mc_FloatingLookback(double s_maxmin,
    NumFunc_2*P,double S0,double T,double r,double divid,double sigma
    ,
    double lambda,double
    mean,double var,int generator,int n_points,long n_paths,
    double *ptprice,double *ptdelta,double *priceerror,double *deltaerror)
{
    double *s,s1,s2,*s3,**s4,s5,s6;
    double pas,sup,inf,supw,infw,exp_sup,exp_inf,exp_supw,exp_infw,beta;
    double *t,*jump_size_vect,*jump_time_vect,sup0,temp,nu,
        discount,*cov_payoff_control,var_payoff,**var_control;
    double cor_payoff_control,*coef_control,var_proba,determinant_control;
    double *X,*W,payoff,*control,proba,s0,s_shift,e1,e2,e3,
        expect_control_0, delta;
    int i,j,k,l,jump_number,*N;
    k=0;
    beta=0.5826;
    delta=sqrt(var);
    nu=(r-divid)-sigma*sigma/2-lambda*(exp(var/2-mean)-1);

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discount=exp(-r*T);
pas=T/n_points;
X=malloc((n_points+1)*sizeof(double));
W=malloc((n_points+1)*sizeof(double));
t=malloc((n_points+1)*sizeof(double));
N=malloc((n_points+1)*sizeof(int));
s=malloc((2)*sizeof(double));
s3=malloc((2)*sizeof(double));
control=malloc((2)*sizeof(double));
var_control=(double**) malloc((2)*sizeof(double));
s4=(double**) malloc((2)*sizeof(double));
for(i=0;i<=1;i++)
{
    var_control[i]=malloc((2)*sizeof(double));
    s4[i]=malloc((2)*sizeof(double));
}
cov_payoff_control=malloc((2)*sizeof(double));
coef_control=malloc((2)*sizeof(double));
jump_size_vect=malloc((int)(1000*lambda*T)*sizeof(double)
);
jump_time_vect=malloc((int)(1000*lambda*T)*sizeof(double)
);
N[0]=0;
X[0]=0;
s[0]=0;
s[1]=0;
s3[0]=0;
s3[1]=0;
s4[0][0]=0;
s4[0][1]=0;
s4[1][0]=0;
s4[1][1]=0;
s1=0;
s2=0;
s5=0;
s6=0;
for(k=0;k<=n_points;k++)
{
    t[k]=k*pas;
}
pnl_rand_init(generator,1,n_paths);

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//Call options case
if ((P->Compute)==&Call_StrikeSpot2)
{
    s_shift=exp(beta*sigma*sqrt(T/n_points))*s_maxmin;
    e1=(log(s_maxmin/S0)*(S0>s_maxmin)-(nu+sigma*sigma)
*T)/(sigma*sqrt(T));
    e2=e1+sigma*sqrt(T);
    e3=(log(s_maxmin/S0)*(S0>s_maxmin)+nu*T)/(sigma*sq
rt(T));
    //first control variable's expected value : it's th
e exponential of the infimum of the continuous part of the
Levy process
    if(S0>=s_maxmin)
        expect_control_0=exp(beta*sigma*sqrt(T/n_points))
*(discount*s_maxmin+S0*exp((sigma*sigma/2+nu-r)*T)*cdf_nor
(e1)-s_maxmin*discount*cdf_nor(e2)+S0*discount*(1/(1+2*nu/
(sigma*sigma)))*(-pow(S0/s_maxmin,-(2*nu/(sigma*sigma)+1))
*cdf_nor(e3)+exp((nu+sigma*sigma/2)*T)*cdf_nor(e1)));
    else
        expect_control_0=exp(beta*sigma*sqrt(T/n_points))
*(S0*exp(sigma*sigma/2+nu-r)*(1+1/(2*nu/(sigma*sigma)))*
cdf_nor(e1)+S0*exp(-r*T)*cdf_nor(e3)/(1+sigma*sigma/(2*nu)))
;
    for(i=1;i<=n_paths;i++)
    {
        jump_number=pnl_rand_poisson(lambda*T,generator);
// number of jumps
        W[0]=0;
        // simulation of the continuous part of the Levy
process : Brownian motion part
        for(j=1;j<=n_points;j++)
        {
            W[j]=sigma*pnl_rand_normal(generator)*sqrt(pas)
+nu*pas+W[j-1];
        }
        // simulation of the jump's times and the size of
the jumps
        jump_time_vect[0]=0;
        for(j=1;j<=jump_number;j++)
    {
        jump_time_vect[j]=pnl_rand_uni_ab(0.,T,generator);
    }
}

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        jump_size_vect[j]=delta*pn1_rand_normal(    generator)+mean;
    }
    //rearranging jump's times in ascending order
    for(l=0;l<jump_number;l++)
    {
        sup0=jump_time_vect[0];
        for(j=0;j<jump_number+1-l;j++)
        {
            if(jump_time_vect[j]>sup0)
            {
                sup0=jump_time_vect[j];
                k=j;
            }
        }
        if(k!=jump_number-1)
        {
            temp=jump_time_vect[jump_number-1];
            jump_time_vect[jump_number-1]=jump_time_vect[k];
            jump_time_vect[k]=temp;
        }
    }

    // simulation of one Levy path
    for(k=1;k<=n_points;k++)
    {
        N[k]=0;
        for(j=1;j<=jump_number;j++)
        {
            if(jump_time_vect[j]<=t[k])
                N[k]++;
        }
        s0=0;
        for(j=N[k-1]+1;j<=N[k];j++)
            s0+=jump_size_vect[j];
        X[k]=X[k-1]+(W[k]-W[k-1])+s0;
    }

    //computation of the supremum and the infimum of
    the Levy path and its continuous parts
    inf=X[0];
    sup=X[0];
    infw=W[0];
    supw=W[0];

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for(j=1;j<=n_points;j++)
{
    if(inf>X[j])
        inf=X[j];
    if(sup<X[j])
        sup=X[j];
    if(infw>W[j])
        infw=W[j];
    if(supw<W[j])
        supw=W[j];
}
proba=0;
exp_inf=S0*exp(inf);
exp_infw=S0*exp(infw);
if(exp_inf>s_shift)
{
    exp_inf=s_shift;
    proba=1.;
}
if(exp_infw>s_shift)
{
    exp_infw=s_shift;
}
payoff=exp_inf;
control[0]=exp_infw;
exp_inf=S0*exp(X[n_points]-sup); //antithetic
variate associated with the exponential of the Levy infimum
exp_infw=S0*exp(W[n_points]-supw); //antithetic
variate associated with the first control variate
if(exp_inf>s_shift)
{
    exp_inf=s_shift;
    proba+=1.;
}
if(exp_infw>s_shift)
{
    exp_infw=s_shift;
}
proba=proba/2;
payoff=discount*(payoff+exp_inf)/2;
control[0]=discount*((control[0]+exp_infw)/2);

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control[1]=discount*S0*exp(X[n_points]);
s1+=payoff;
s2+=payoff*payoff;
for(j=0;j<=1;j++)
{
    s[j]+=control[j];
    s3[j]+=control[j]*payoff;
    for(k=0;k<=1;k++)
        s4[j][k]+=control[j]*control[k];
}
s5+=proba;
s6+=proba*proba;
}
for(j=0;j<=1;j++)
{
    cov_payoff_control[j]=(s3[j]-s1*s[j]/((double)n_
paths))/(n_paths-1);
    for(k=0;k<=1;k++)
    {
        var_control[j][k]=(s4[j][k]-s[j]*s[k]/((double)n_
paths))/(n_paths-1);
    }
}
determinant_control=var_control[0][0]*var_control[1
][1]-var_control[0][1]*var_control[1][0]; //determinant of
the var_control matrix
coef_control[0]=(cov_payoff_control[0]*var_control[
1][1]-cov_payoff_control[1]*var_control[0][1])/determinant
_control;
coef_control[1]=(cov_payoff_control[1]*var_control[
0][0]-cov_payoff_control[0]*var_control[1][0])/determinant
_control;
var_payoff=(s2-s1*s1/((double)n_paths))/(n_paths-1)
;
cor_payoff_control=sqrt((coef_control[0]*cov_payo
ff_control[0]+coef_control[1]*cov_payoff_control[1])/var_pay
off);
var_proba=(s6-s5*s5/((double)n_paths))/(n_paths-1);
*ptprice=-exp(-beta*sigma*sqrt(T/n_points))*(s1/n_
paths-coef_control[0]*(s[0]/n_paths-expect_control_0)-coef_
control[1]*(s[1]/n_paths-S0*exp(-divid*T)))+S0*exp(-divid*T);

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        *priceerror=exp(-beta*sigma*sqrt(T/n_points))*1.96*
sqrt(var_payoff*(1-cor_payoff_control*cor_payoff_control))/
sqrt(n_paths);
        *ptdelta=(*ptprice+discount*s_maxmin*s5/n_paths)/S0
;
        *deltaerror=(*priceerror+discount*s_maxmin*1.96*sq
rt(var_proba)/sqrt((double)n_paths))/S0;
    }
else//Put
    if ((P->Compute)==&Put_StrikeSpot2)
    {
        s_shift=exp(-beta*sigma*sqrt(T/n_points))*s_maxmi
n;
        e1=(log(S0/s_maxmin)*(S0<s_maxmin)+(nu+sigma*si
gma)*T)/(sigma*sqrt(T));
        e2=e1-sigma*sqrt(T);
        e3=(log(S0/s_maxmin)*(S0<s_maxmin)-nu*T)/(sigma*
sqrt(T));
        //first control variable's expected value : it's
the exponential of the supremum of the continuous part of
the Levy process
        if(S0<=s_maxmin)
            expect_control_0=exp(-beta*sigma*sqrt(T/n_po
ints))*(discount*s_maxmin+S0*exp((sigma*sigma/2+nu-r)*T)*cdf_
nor(e1)-s_maxmin*discount*cdf_nor(e2)+ S0*discount*(1/(1+2*
nu/(sigma*sigma)))*(-pow(S0/s_maxmin,-(2*nu/(sigma*sigma)+1)
)*cdf_nor(e3)+exp((nu+sigma*sigma/2)*T)*cdf_nor(e1)));
        else
            expect_control_0=exp(-beta*sigma*sqrt(T/n_po
ints))*(S0*exp(sigma*sigma/2+nu-r)*(1+1/(2*nu/(sigma*sigma)))
*cdf_nor(e1)+S0*exp(-r*T)*cdf_nor(e3)/(1+sigma*sigma/(2*
nu)))+S0*exp(-divid*T);
        for(i=0;i<n_paths;i++)
        {
            jump_number=pnl_rand_poisson(lambda*T, generator);// number of jum
W[0]=0;
            //simulation of the continuous part of the Levy
: Brownian motion part
            for(j=1;j<=n_points;j++)
            {
                W[j]=sigma*pnl_rand_normal(generator)*sqrt(pas)

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+nu*pas+W[j-1];
    }
    jump_time_vect[0]=0;
    // simulation of the jump's times and the size
of the jumps
    for(j=1;j<=jump_number;j++)
    {
        jump_time_vect[j]=pnl_rand_uni_ab(0.,T,generator);
        jump_size_vect[j]=delta*pnl_rand_normal(    generator)+mean;
    }

    //rearranging jump's times in ascending order
    for(l=0;l<jump_number;l++)
    {
        sup0=jump_time_vect[0];
        for(j=0;j<jump_number+1-l;j++)
        {
            if(jump_time_vect[j]>sup0)
            {
                sup0=jump_time_vect[j];
                k=j;
            }
        }
        if(k!=jump_number-l)
        {
            temp=jump_time_vect[jump_number-l];
            jump_time_vect[jump_number-l]=jump_time_vect[k];
            jump_time_vect[k]=temp;
        }
    }
    // simulation of one Levy path
    for(k=1;k<=n_points;k++)
    {
        N[k]=0;
        for(j=1;j<=jump_number;j++)
        {
            if(jump_time_vect[j]<=t[k])
                N[k]++;
        }
        s0=0;
        for(j=N[k-1]+1;j<=N[k];j++)
            s0+=jump_size_vect[j];
    }

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    X[k]=X[k-1]+(W[k]-W[k-1])+s0;
}

    //computation of the supremum and the infimum of
the Levy path and its continuous parts
    sup=X[0];
    inf=X[0];
    infw=W[0];
    supw=W[0];
    for(j=1;j<=n_points;j++)
    {
        if(inf>X[j])
            inf=X[j];
        if(sup<X[j])
            sup=X[j];
        if(infw>W[j])
            infw=W[j];
        if(supw<W[j])
            supw=W[j];
    }
    proba=0;
    exp_sup=S0*exp(sup);
    exp_supw=S0*exp(supw);
    if(exp_sup<s_shift)
    {
        exp_sup=s_shift;
        proba=1.;
    }
    if(exp_supw<s_shift)
    {
        exp_supw=s_shift;
    }
    payoff=exp_sup;
    control[0]=exp_supw;
    exp_sup=S0*exp(X[n_points]-inf);//antithetic
variat associated with the exponential of the Levy supremum
    exp_supw=S0*exp(W[n_points]-infw);//antithetic
variate associated with the first control variate
    if(exp_sup<s_shift)
    {
        exp_sup=s_shift;
        proba+=1.;
    }

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    }
    if(exp_supw<s_shift)
    {
        exp_supw=s_shift;
    }
    proba=proba/2.;
    payoff=discount*(payoff+exp_sup)/2;
    control[0]=discount*(control[0]+exp_supw)/2;
    control[1]=discount*S0*exp(X[n_points]);
    s1+=payoff;
    s2+=payoff*payoff;
    for(j=0;j<=1;j++)
    {
        s[j]+=control[j];
        s3[j]+=control[j]*payoff;
        for(k=0;k<=1;k++)
            s4[j][k]+=control[j]*control[k];
    }
    s5+=proba;
    s6+=proba*proba;
}
for(j=0;j<=1;j++)
{
    cov_payoff_control[j]=(s3[j]-s1*s[j])/((double)
n_paths))/(n_paths-1);
    for(k=0;k<=1;k++)
    {
        var_control[j][k]=(s4[j][k]-s[j]*s[k])/((
double)n_paths))/(n_paths-1);
    }
}
determinant_control=var_control[0][0]*var_control[1][1]-var_control[0][1]*var_control[1][0]; //determinant
of the var_control matrix
coef_control[0]=(cov_payoff_control[0]*var_control[1][1]-cov_payoff_control[1]*var_control[0][1])/determina
nt_control;
coef_control[1]=(cov_payoff_control[1]*var_control[0][0]-cov_payoff_control[0]*var_control[1][0])/determina
nt_control;
var_payoff=(s2-s1*s1/((double)n_paths))/(n_paths-

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1);
    cor_payoff_control=sqrt((coef_control[0]*cov_payo
ff_control[0]+coef_control[1]*cov_payoff_control[1])/var_pay
off);
    var_proba=(s6-s5*s5/((double)n_paths))/(n_paths-1
);
    *ptprice=exp(beta*sigma*sqrt(T/n_points))*(s1/n_
paths-coef_control[0]*(s[0]/n_paths-expect_control_0)-coef_
control[1]*(s[1]/n_paths-S0*exp(-divid*T)))-S0*exp(-divid*T);
    *priceerror=exp(beta*sigma*sqrt(T/n_points))*1.96
*sqrt(var_payoff*(1-cor_payoff_control*cor_payoff_control)
)/sqrt(n_paths);
    *ptdelta=(*ptprice-discount*s_maxmin*s5/n_paths)/
S0;
    *deltaerror=(*priceerror+discount*s_maxmin*1.96*
sqrt(var_proba)/sqrt((double)n_paths))/S0;
}
free(X);
free(W);
free(t);
free(N);
free(coef_control);
free(control);
free(s);
free(s3);
free(cov_payoff_control);
for(i=0;i<=1;i++)
{
    free(var_control[i]);
    free(s4[i]);
}
free(var_control);
free(s4);
free(jump_time_vect);
free(jump_size_vect);
return OK;
}

int CALC(MC_Merton_FloatingLookback)(void*Opt,void *Mod,
PricingMethod *Met)
{

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TYPEOPT* ptOpt=(TYPEOPT*)Opt;
TYPEMOD* ptMod=(TYPEMOD*)Mod;
double r,divid;

r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

return Merton_Mc_FloatingLookback((ptOpt->PathDep.Val.V_
    NUMFUNC_2)->Par[4].Val.V_PDOUBLE,
                                ptOpt->PayOff.Val.V_
    NUMFUNC_2,
                                ptMod->S0.Val.V_PDOUB
    LE,
                                ptOpt->Maturity.Val.V_
    DATE-ptMod->T.Val.V_DATE,
                                r,divid,ptMod->Sigma.
    Val.V_PDOUBLE,
                                ptMod->Lambda.Val.V_
    PDOUBLE,ptMod->Mean.Val.V_PDOUBLE,ptMod->Variance.Val.V_PDO
    UBLE,
                                Met->Par[0].Val.V_
    ENUM.value,Met->Par[1].Val.V_PINT,Met->Par[2].Val.V_LONG,
                                &(Met->Res[0].Val.V_
    DOUBLE),&(Met->Res[1].Val.V_DOUBLE),&(Met->Res[2].Val.V_DOUBLE),
                                &(Met->Res[3].Val.V_DOUBLE));
}

static int CHK_OPT(MC_Merton_FloatingLookback)(void *Opt,
    void *Mod)
{
    if ((strcmp(((Option*)Opt)->Name,"    LookBackCallFloatingEuro")==0) || (strcmp
        return OK;
    return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Mod)
{
    if ( Met->init == 0)
    {

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        Met->init=1;
        Met->Par[0].Val.V_ENUM.value=0;
        Met->Par[0].Val.V_ENUM.members=&PremiaEnumMCRNGs;
        Met->Par[1].Val.V_PINT=100;
        Met->Par[2].Val.V_LONG=10000;
    }
    return OK;
}

PricingMethod MET(MC_Merton_FloatingLookback)=
{
    "MC_Merton_FloatingLookback",
    {{ "RandomGenerator", ENUM, {100}, ALLOW },
      { "Number of discretization steps", LONG, {100}, ALLOW }, { "N
        iterations", LONG, {100}, ALLOW }, { " ", PREMIA_NULLTYPE, {0}, FORBID }
    },
    CALC(MC_Merton_FloatingLookback),
    {{ "Price", DOUBLE, {100}, FORBID }, { "Delta", DOUBLE, {100}, FORB
        ID }, { "Price Error", DOUBLE, {100}, FORBID }, { "Delta Error",
        DOUBLE, {100}, FORBID }, { " ", PREMIA_NULLTYPE, {0}, FORBID } },
    CHK_OPT(MC_Merton_FloatingLookback),
    CHK_ok,
    MET(Init)
} ;

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References