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## Model Presentation

## lrshjm1d

## 1 Description

Consider a one-factor HJM model. If the volatility function  $\sigma(t,T)$  is differentiable with respect to T, a necessary and sufficient condition for the price of any (interest-rate) derivative to be completely determined by a two-state Markov process  $\chi(.) = (r(.), \phi(.))$  is that the following condition holds:

$$\sigma(t,T) = \eta(t) \exp\left(-\int_{t}^{T} \kappa(x)dx\right)$$

where  $\eta$  is an adapted process and  $\kappa$  is a deterministic (integrable) function. In such a case, the second component of the process  $\chi$  is defined by

$$\phi(t) = \int_0^t \sigma(s, t)^2 ds$$

Accordingly, zero-coupon-bond prices are explicitly given by

$$P(t,T) = \frac{P(0,T)}{P(0,t)} \exp\left(-\frac{1}{2}\Lambda^{2}(t,T)\phi(t) + \Lambda(t,T)[f(0,t) - r(t)]\right)$$

where

$$\Lambda(t,T) = \int_{t}^{T} \exp\left(-\int_{t}^{u} \kappa(x)dx\right) du$$

Under the Ritchken and Sankarasubramanian class of volatilities, the process  $\chi$ , and hence the instantaneous short-rate r, evolve according to

$$d\chi(t) = \begin{pmatrix} dr(t) \\ d\phi(t) \end{pmatrix} = \begin{pmatrix} \mu(r,t)dt + \eta(t)dW(t) \\ [\eta^2(t) - 2\kappa(t)\phi(t)]dt \end{pmatrix}$$
(1)

with

$$\mu(r,t) = \kappa(t)[f(0,t) - r(t)] + \phi(t) + \frac{\partial}{\partial t}f(0,t)$$

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## 2 Code Implementation

```
#ifndef _LiRitchkenSankarasubramanian1D_H
#define _LiRitchkenSankarasubramanian1D_H
#include "optype.h"
#include "var.h"
#include "enums.h"
#define TYPEMOD LRSHJM1D
/*1D Li Ritchken Sankarasubramanian World*/
typedef struct TYPEMOD{
 VAR T;
 VAR flat_flag;
 VAR Sigma;
 VAR Kappa;
 VAR Rho;
 VAR Lambda;
} TYPEMOD;
extern double MOD(GetYield)(TYPEMOD *pt);
#endif
```