

Help

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#include <stdlib.h>
#include "bs1d_std.h"
#include "error_msg.h"
#define PRECISION 1.0e-7 /*Precision for the localization
    of FD methods*/

static int restriction1(int l,double *d,double *u,double *
    GG,double *A,double *B,double *C,int N)
{
    int nl1,nl,i;
    double *aux;

    nl=pow(2, l+1)-1;

    aux= malloc((nl+2)*sizeof(double));
    if (aux==NULL)
        return MEMORY_ALLOCATION_FAILURE;

    nl1=pow(2, l)-1;

    for (i=1;i<nl+1;i++)
        aux[i]=u[i-1]*A[i*N/(nl+1)]+u[i]*B[i*N/(nl+1)]+u[i+1]*
            C[i*N/(nl+1)]-GG[i];

    for (i=1;i<nl1+1;i++)
        d[i]=aux[2*i]/2.0+(aux[2*i-1]+aux[2*i+1])/4.0;

    free(aux);
    return OK;
}

static void subtract_prolongation1(int l,double *u,double
    *v)
{
    int nl1,i;

    nl1=pow(2, l)-1;

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    for (i=0;i<nl1+1;i++)
    {
        u[2*i]=u[2*i]-v[i];
        u[2*i+1]=u[2*i+1]-(v[i]+v[i+1])/2.0;
    }
    return;
}

static int MGM1(int l,double *u,double *GG,double *a,
    double *b,double *c,int N)
{
    int nl,nl1,i,j;
    double *v,*d;

    nl=pow(2, l+1)-1;
    nl1=pow(2, l)-1;

    v= malloc((nl1+2)*sizeof(double));
    if (v==NULL)
        return MEMORY_ALLOCATION_FAILURE;
    d= malloc((nl1+2)*sizeof(double));
    if (d==NULL)
        return MEMORY_ALLOCATION_FAILURE;

    if (l==0) u[1]=GG[1]/b[N/2];
    else
    {
        /* 2 iterations of Gauss-Seidel*/
        for (i=1;i<3;i++)
        {
            for (j=1;j<nl+1;j++)
                u[j]=(-u[j-1]*a[j*N/(nl+1)]-u[j+1]*c[j*N/(nl+1)]+GG[j])/b[j*N/(nl+1)];
        }

        restriction1(l,d,u,GG,a,b,c,N);

        for (i=0;i<nl1+2;i++)

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v[i]=0.0;

MGM1(l-1,v,d,a,b,c,N);

subtract_prolongation1(l,u,v);

/* 2 iterations of Gauss-Seidel*/
for (i=1;i<3;i++)
{
  for (j=1;j<nl+1;j++)
    u[j]=(-u[j-1]*a[j*N/(nl+1)]-u[j+1]*c[j*N/(nl+1)]+GG[
j])/b[j*N/(nl+1)];
}
}

free(v);
free(d);
return OK;
}

static int mult_amer1(double s,NumFunc_1 *p,double t,
double r,double divid, double sigma,int l,int M,double theta,
double epsilon,double *ptprice,double *ptdelta)
{
double k,z,limit,h,x,alpha,beta,gamma,alpha1,beta1,gamma1
,error,g0,g1,vv,upwind_alphacoef;
double *P,*Obst,*R,*A,*B,*C,*GG,*u;
int *pp;
int i,j,Index,N;

/*Memory Allocation*/
N=pow(2, l+1)-1+1;
P= malloc((N+1)*sizeof(double));
if (P==NULL)
return MEMORY_ALLOCATION_FAILURE;
Obst= malloc((N+1)*sizeof(double));
if (Obst==NULL)
return MEMORY_ALLOCATION_FAILURE;
A= malloc((N+1)*sizeof(double));

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if (A==NULL)
    return MEMORY_ALLOCATION_FAILURE;
B= malloc((N+1)*sizeof(double));
if (B==NULL)
    return MEMORY_ALLOCATION_FAILURE;
C= malloc((N+1)*sizeof(double));
if (C==NULL)
    return MEMORY_ALLOCATION_FAILURE;
R= malloc((N+1)*sizeof(double));
if (R==NULL)
    return MEMORY_ALLOCATION_FAILURE;
P= malloc((N+1)*sizeof(double));
if (P==NULL)
    return MEMORY_ALLOCATION_FAILURE;
pp= malloc((N+1)*sizeof(int));
if (pp==NULL)
    return MEMORY_ALLOCATION_FAILURE;
GG= malloc((N+1)*sizeof(double));
if (GG==NULL)
    return MEMORY_ALLOCATION_FAILURE;
u= malloc((N+1)*sizeof(double));
if (u==NULL)
    return MEMORY_ALLOCATION_FAILURE;

/*Time Step*/
k=t/(double)M;

/*Space Localisation*/
z=(r-divid)-SQR(sigma)/2.0;
limit=(sigma*sqrt(t)*sqrt(log(1.0/PRECISION))+fabs(z)*t);

/*Space Step*/
h=2*limit/(double)N;

/*Peclet Condition-Coefficient of diffusion augmented */
vv=0.5*SQR(sigma);
if ((h*fabs(z))<=vv)
    upwind_alphacoef=0.5;
else {
    if (z>0.) upwind_alphacoef=0.0;
    else upwind_alphacoef=1.0;
}

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}
vv=-z*h*(upwind_alphacoef-0.5);

/*Factor of theta-schema*/
alpha=theta*k*(-vv/(h*h)+z/(2.0*h));
beta=1.0+k*theta*(r+2.*vv/(h*h));
gamma=k*theta*(-vv/(h*h)-z/(2.0*h));

alpha1=k*(1.0-theta)*(vv/(h*h)-z/(2.0*h));
beta1=1.0-k*(1.0-theta)*(r+2.*vv/(h*h));
gamma1=k*(1.0-theta)*(vv/(h*h)+z/(2.0*h));

/*Terminal Values*/
x=log(s);
for (i=0;i<N+1;i++)
{
    Obst[i]=(p->Compute)(p->Par,exp(x-limit+i*h));
    P[i]=Obst[i];
}

/*Finite Difference Cycle*/
for (i=1;i<M+1;i++)
{
    /*Init pp and R*/
    for(j=1;j<N;j++)
    {
        pp[j]=0;
        R[j]=P[j]*beta1+alpha1*P[j-1]+gamma1*P[j+1];
    }

    /*Howard Cycle*/
    do
    {
        error=0.;

        for (j=1;j<N;j++)
        {
            g0=P[j-1]*alpha+P[j]*beta+P[j+1]*gamma-R[j];
            g1=P[j]-Obst[j];
            if (g0<g1) pp[j]=0;else pp[j]=1;

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    }

    for (j=1;j<N;j++)
    {
        if (pp[j]==0)
        {
            GG[j]=R[j];A[j]=alpha;B[j]=beta;C[j]=gamma;
        }
        else {GG[j]=Obst[j];
A[j]=0;B[j]=1;C[j]=0;
        }
    }

    for (j=1;j<N;j++)
        u[j]=P[j];
    MGM1(1,P,GG,A,B,C,N);
    for (j=1;j<N;j++)
        error+=fabs(P[j]-u[j]);
}

    while (error>epsilon);
    /*End Howard Cycle*/
}
/*End Finite Difference Cycle*/

Index=(int) floor ((double)N/2.0);

/*Price*/
*ptprice=P[Index];

/*Delta*/
*ptdelta=(P[Index+1]-P[Index-1])/(2.0*s*h);

/*Memory Desallocation*/
free(P);
free(pp);
free(A);
free(B);
free(C);
free(R);
free(Obst);
free(GG);

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    free(u);

    return OK;
}

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int CALC(FD_FMGH)(void *Opt,void *Mod,PricingMethod *Met)
{
    TYPEOPT* ptOpt=( TYPEOPT*)Opt;
    TYPEMOD* ptMod=( TYPEMOD*)Mod;
    double r,divid;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    return mult_amer1(ptMod->S0.Val.V_PDDOUBLE,ptOpt->PayOff.
        Val.V_NUMFUNC_1,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,r,
        divid,ptMod->Sigma.Val.V_PDDOUBLE,
        Met->Par[0].Val.V_INT,Met->Par[1].Val.V_INT,Met->
        Par[2].Val.V_RGDOUBLE,
        Met->Par[3].Val.V_RGDOUBLE,
        &(Met->Res[0].Val.V_DOUBLE),&(Met->Res[1].Val.V_
        DOUBLE));
}

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static int CHK_OPT(FD_FMGH)(void *Opt, void *Mod)
{
    Option* ptOpt=(Option*)Opt;
    TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);

    if ((opt->EuOrAm). Val.V_BOOL==AMER)
        return OK;

    return WRONG;
}

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```

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_INT2=6;
        Met->Par[1].Val.V_INT2=128;
        Met->Par[2].Val.V_RGDOUBLE=0.5;
        Met->Par[3].Val.V_RGDOUBLE=0.000001;

    }

    return OK;
}

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PricingMethod MET(FD_FMGH)=
{
    "FD_FMGH",
    {{"Number of Grids",INT2,{100},ALLOW    },{"TimeStepNumber",INT2,{100},ALLOW},
    {"Theta",RGDOUBLE,{100},ALLOW}, {"Epsilon",RGDOUBLE,{100},ALLOW}, {" " ,PREMIA_NULLTYPE,{0},FORBID}},
    CALC(FD_FMGH),
    {{"Price",DOUBLE,{100},FORBID}, {"Delta",DOUBLE,{100},FORBID}, {" " ,PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(FD_FMGH),
    CHK_fdiff,
    MET(Init)
};

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References