

Help

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#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "pnl/pnl_linalg_solver.h"
#include "pnl/pnl_vector.h"
#include "pnl/pnl_matrix.h"
#include "pnl/pnl_tridiag_matrix.h"

double sigma_sqr(double t, double S, double sig, double alp
    ha)
{
    return sig*sig*pow(S,2*(alpha-1));
}

void quadratic_interpolation(double Fm1,
                             double F0,
                             double Fp1,
                             double Xm1,
                             double X0,
                             double Xp1,
                             double X,
                             double * FX,
                             double * dFX)
{
    //quadratic interpolation
    double A = Fm1;
    double B = (F0-Fm1)/(X0-Xm1);
    double C = (Fp1-A-B*(Xp1-Xm1))/((Xp1-Xm1)*(Xp1-X0));
    (*FX) = A+B*(X-Xm1)+C*(X-Xm1)*(X-X0);
    (*dFX)= B + C*(2*X-Xm1-X0);
}

typedef struct Parisian_Option{
    int product;
    // 1 - Call ; 2 - Put;
    int product_type;
    // 1- Vanilla; 2 Up-and-Out ;3 Down-and-Out ; 4 Double
    barrier ;5
    // parisian ...

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```
double S0;
double K;
double T;
double rebate;
double barrier;
double duration;
double price;
double delta;
double implied_vol;
}Parisian_Option;

Parisian_Option * parisian_option_create(int product_,int
    product_type_,
    double S0_,
    double K_, double T_,double rebate_,double barrier_,double dur
    ation_)
{
    Parisian_Option * op = malloc(sizeof(Parisian_Option));
    op->product=product_;
    op->product_type=product_type_;
    op->S0=S0_;
    op->K=K_;
    op->T=T_;
    op->rebate=rebate_;
    op->barrier=barrier_;
    op->duration=duration_;
    op->price=0;
    op->delta=0;
    op->implied_vol=0;
    return op;
}

void parisian_option_compute_rigidity_matrix(PnlTridiagMa
    t *A_rhs,
    PnlTridiagMa
    t *A_lhs,
    PnlTridiagMa
    t *B_rhs,
    PnlTridiagMa
    t *B_lhs,
```

```

double t,
double dt,
double h,
double S0,
double Bnd,
double vol,
double coefc

ev,

double r,
double (*si
gma_sqr)(double t,double S, double sig, double alpha),
double theta,
int Index_Bar

rier,

int N)
{

int i;
double a,b,alpha,beta,gama;

pnl_tridiag_mat_resize(A_rhs,Index_Barrier);
pnl_tridiag_mat_resize(A_lhs,Index_Barrier);
pnl_tridiag_mat_resize(B_rhs,N-Index_Barrier);
pnl_tridiag_mat_resize(B_lhs,N-Index_Barrier);

//printf("%lf %lf %lf %lf %lf %lf %d\n",alpha,beta,gama,
dt,theta,S0*exp(-1+Index_Barrier*h),J);

for (i=0;i<Index_Barrier;i++)
{
a=sigma_sqr(t,S0*exp(-Bnd+(i+1)*h),vol,coefcev)/(2*h*
h);
b=(r-sigma_sqr(t,S0*exp(-Bnd+(i+1)*h),vol,coefcev)/2)
/(2*h);
alpha=a-b;
beta=-2*a-r;
gama=a+b;

pnl_tridiag_mat_set(A_rhs,i,0,1+beta*dt*(1-theta));
pnl_tridiag_mat_set(A_rhs,i,1,gama*dt*(1-theta));
pnl_tridiag_mat_set(A_lhs,i,0,1-beta*dt*(theta));

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    pnl_tridiag_mat_set(A_lhs,i,1,-gama*dt*(theta));

    pnl_tridiag_mat_set(A_rhs,i,-1,alpha*dt*(1-theta));
    pnl_tridiag_mat_set(A_lhs,i,-1,-alpha*dt*theta);
    pnl_tridiag_mat_set(A_rhs,i,1,gama*dt*(1-theta));
    pnl_tridiag_mat_set(A_lhs,i,1,-gama*dt*(theta));
}
pnl_tridiag_mat_set(A_rhs,0,-1,0);
pnl_tridiag_mat_set(A_lhs,0,-1,0);
pnl_tridiag_mat_set(A_rhs,Index_Barrier-1,1,0);
pnl_tridiag_mat_set(A_lhs,Index_Barrier-1,1,0);

for (i=0;i<N-Index_Barrier;i++)
{
    a=sigma_sqr(t,S0*exp(-Bnd+(i+1+Index_Barrier)*h),vol,
coefcev)/(2*h*h);
    b=(r-sigma_sqr(t,S0*exp(-Bnd+(i+1+Index_Barrier)*h),vol,coefcev)/2)/(2
    alpha=a-b;
    beta=-2*a-r;
    gama=a+b;
    if (i==0)
    {
        pnl_tridiag_mat_set(B_rhs,i,0,1+beta*dt*(1-theta)
);
        pnl_tridiag_mat_set(B_rhs,i,1,gama*dt*(1-theta));
        pnl_tridiag_mat_set(B_lhs,i,0,1-beta*dt*(theta));
        pnl_tridiag_mat_set(B_lhs,i,1,-gama*dt*(theta));
    }
    if ((i>0)&&(i<N-Index_Barrier-1))
    {
        pnl_tridiag_mat_set(B_rhs,i,-1,alpha*dt*(1-theta)
);
        pnl_tridiag_mat_set(B_rhs,i,0,1+beta*dt*(1-theta)
);
        pnl_tridiag_mat_set(B_rhs,i,1,gama*dt*(1-theta));
        pnl_tridiag_mat_set(B_lhs,i,-1,-alpha*dt*(theta))
;
        pnl_tridiag_mat_set(B_lhs,i,0,1-beta*dt*(theta));
        pnl_tridiag_mat_set(B_lhs,i,1,-gama*dt*(theta));
    }
    if (i==N-Index_Barrier-1)

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        {
            pnl_tridiag_mat_set(B_rhs,i,-1,alpha*dt*(1-theta)
        );
            pnl_tridiag_mat_set(B_rhs,i,0,1+beta*dt*(1-theta)
        );
            pnl_tridiag_mat_set(B_lhs,i,-1,-alpha*dt*(theta))
        ;
            pnl_tridiag_mat_set(B_lhs,i,0,1-beta*dt*(theta));
        }
    }

    // pnl_tridiag_mat_print(A_rhs);
    //pnl_tridiag_mat_print(A_lhs);
    //pnl_tridiag_mat_print(B_rhs);
    //pnl_tridiag_mat_print(B_lhs);
    //printf("ok for tri{n");

}

int main( )
{

    double S0;//=100;
    double T;//=1;
    double Y;//=140;
    double D;//=0.5;
    double K;//=100;
    double r;//=0.05;
    double vol;//=0.2;
    double price,price_1,price1,price_2,price2;
    double delta,delta_1,delta1;
    double gamma;
    double Teta;
    PnlTridiagMat *A_rhs,*A_lhs,*B_rhs,*B_lhs;
    PnlVect Vtmp,Vtmp2;
    PnlVect *VaA,*VbA;
    PnlMat *VaB,*VbB;
    PnlVect *ResAtmp,*ResBtmp;
    double Bnd,coefcev,dt,h,theta;

```

```

int i,j,k,J,Index_Barrier;
double t;
double a,b,gama,alpha;
int M,N;

M=3;
N=10;//500

A_rhs = pnl_tridiag_mat_create(0);
A_lhs = pnl_tridiag_mat_create(0);
B_rhs = pnl_tridiag_mat_create(0);
B_lhs = pnl_tridiag_mat_create(0);

t=0;// Sigma not depend of t
/*
    printf("Please input the parameters according to the fo
        llowing format{n");
    printf("S0 Vol R K Delay Barrier Maturity{n");
    scanf("%lf %lf %lf %lf %lf %lf %lf", &S0, &vol, &r, &K,
        &D, &Y, &T);
    printf("Your parameters are as follows{t{t{n");
    printf("S0{t %f{n", S0);
    printf("Vol{t %f{n", vol);
    printf("R{t %f{n", r);
    printf("K{t %f{n", K);
    printf("D{t %f{n", D);
    printf("Barrier{t %f{n", Y);
    printf("T{t %f{n",T);
*/
S0=100;
T=1;
Y=140;
D=0.5;
K=100;
r=0.05;
vol=2.0;

coefcev=0.5;
Bnd=vol*sqrt(T)*5*pow(S0,(coefcev-1));
//Bnd=MAX(Bnd,2*log(Y/So));

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dt=T/M;
h=2*Bnd/N;
theta=0.6;
J=floor(D/dt)+1;
Index_Barrier=floor((log(Y/S0)+Bnd)/h);

parisian_option_compute_rigidity_matrix(A_rhs,A_lhs,B_rhs,
    B_lhs,
    t,dt,h,S0,Bnd,vol,
    coefcev,r,
    &sigma_sqr, theta,
    Index_Barrier,N);

VaA=pnl_vect_create_from_double(Index_Barrier,0.);
VbA=pnl_vect_create_from_double(Index_Barrier,0.);
VaB=pnl_mat_create_from_double(J,N-Index_Barrier,0.);
VbB=pnl_mat_create_from_double(J,N-Index_Barrier,0.);

ResAtmp=pnl_vect_create_from_double(Index_Barrier,0.);
ResBtmp=pnl_vect_create_from_double(N-Index_Barrier,0.);

for (i=0;i<Index_Barrier;i++)
{
    pnl_vect_set(VaA,i,MAX(S0*exp(-Bnd+(i+1)*h)-K,0));
}

Vtmp=pnl_mat_wrap_row(VaB,1);
for (i=0;i<N-Index_Barrier;i++)
    pnl_vect_set(&Vtmp,i,MAX(S0*exp(-Bnd+(i+Index_Barrier+1)
        *h)-K,0));
for (j=2;j<J;j++)
{
    Vtmp2=pnl_mat_wrap_row(VaB,j);
    pnl_vect_clone(&Vtmp2,&Vtmp);
}

//pnl_vect_print(VaA);
//pnl_mat_print(VaB);

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//printf("ok for Va initial {n}");

for (k=1;k<=M;k++)
{
    a=sigma_sqr(t,S0*exp(-Bnd+Index_Barrier*h),vol,coefcev)/(
        2*h*h);
    b=(r-sigma_sqr(t,S0*exp(-Bnd+Index_Barrier*h),vol,coefcev
        )/2)/(2*h);
    gama=a+b;
    //printf(">>> %d {n ",(int)((double)k/(double)M*100));
    pnl_tridiag_mat_mult_vect_inplace(ResAtmp,A_rhs,VaA);
    pnl_vect_set(ResAtmp,Index_Barrier-1,pnl_vect_get(ResAtm
        p,Index_Barrier-1)
        +dt*gama*pnl_mat_get(VaB,J-2,0));
    //pnl_vect_print(ResAtmp);
    pnl_tridiag_mat_lu_syslin(VbA,A_lhs,ResAtmp);
    //pnl_vect_print(VbA);
    a=sigma_sqr(t,S0*exp(-Bnd+(Index_Barrier+1)*h),vol,coefc
        ev)/(2*h*h);
    b=(r-sigma_sqr(t,S0*exp(-Bnd+(Index_Barrier+1)*h),vol,coe
        fcev)/2)/(2*h);
    alpha=a-b;
    for (j=0;j<J-1;j++)
    {
        Vtmp=pnl_mat_wrap_row(VaB,j);
        pnl_tridiag_mat_mult_vect_inplace(ResBtmp,B_rhs,&Vtmp
        );
        pnl_vect_set(ResBtmp,0,pnl_vect_get(ResBtmp,0)+(1-th
            eta)*dt*alpha*pnl_vect_get(VaA,Index_Barrier-1)+theta*dt*
            alpha*pnl_vect_get(VbA,Index_Barrier-1));
        Vtmp=pnl_mat_wrap_row(VbB,j+1);
        pnl_tridiag_mat_lu_syslin(&Vtmp,B_lhs,ResBtmp);
    }
    //pnl_vect_print(VbA);
    //pnl_mat_print(VbB);
    if(k==M)
    {
        if (N/2<=Index_Barrier)
            Teta=(pnl_vect_get(VaA,N/2-1)-pnl_vect_get(VbA,N/2-
                1))/dt;
    }
}

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        else
            Teta=(pnl_mat_get(VaB,J-1,N/2-1-Index_Barrier)-pnl_
mat_get(VbB,J-1,N/2-1-Index_Barrier))/dt;
        }
pnl_vect_clone(VaA,VbA);
pnl_mat_clone(VaB,VbB);
}

if ((N/2-2)<=Index_Barrier)
    price_2=pnl_vect_get(VaA,N/2-3);
else
    price_2=pnl_mat_get(VaB,J-1,N/2-3-Index_Barrier);

if ((N/2-1)<=Index_Barrier)
    price_1=pnl_vect_get(VaA,N/2-2);
else
    price_1=pnl_mat_get(VaB,J-1,N/2-2-Index_Barrier);

if (N/2<=Index_Barrier)
    price=pnl_vect_get(VaA,N/2-1);
else
    price=pnl_mat_get(VaB,J-1,N/2-1-Index_Barrier);

if ((N/2+1)<=Index_Barrier)
    price1=pnl_vect_get(VaA,N/2);
else
    price1=pnl_mat_get(VaB,J-1,N/2-Index_Barrier);

if ((N/2+2)<=Index_Barrier)
    price2=pnl_vect_get(VaA,N/2+1);
else
    price2=pnl_mat_get(VaB,J-1,N/2+1-Index_Barrier);

delta_1=0.5*((price_1-price_2)/(S0*exp(-h)-S0*exp(-2*h)))+(
    price-price_1)/(S0-S0*exp(-h));
delta=0.5*((price-price_1)/(S0-S0*exp(-h))+(price1-price)/
    (S0*exp(h)-S0));
delta1=0.5*((price1-price)/(S0*exp(h)-S0)+(price2-price1)/
    (S0*exp(2*h)-S0*exp(h)));

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```
gamma=0.5*((delta-delta_1)/(S0-S0*exp(-h))+(delta1-delta)/
(S0*exp(h)-S0));

printf("{nprice is %lf{n",price);
printf("delta is %lf{n",delta);
printf("gamma is %lf{n",gamma);
printf("theta is %lf{n",Teta);

pnl_tridiag_mat_free(&A_rhs);
pnl_tridiag_mat_free(&A_lhs);
pnl_tridiag_mat_free(&B_rhs);
pnl_tridiag_mat_free(&B_lhs);
pnl_vect_free(&ResAtmp);
pnl_vect_free(&ResBtmp);
pnl_mat_free(&VaB);
pnl_mat_free(&VbB);
pnl_vect_free(&VaA);
pnl_vect_free(&VbA);

return 0;
}
```

References