2 pages 1

```
Source | Model | Option | Model_Option | Help on fd methods | Archived Tests
```

# fd\_sor

## Input parameters:

- SpaceStepNumber N
- $\bullet$  TimeStepNumber M
- Theta  $\frac{1}{2} \le \theta \le 1$
- Omega  $1 \le \omega \le 2$
- Epsilon

#### Output parameters:

- Price
- Delta

```
/*Memory Allocation*/
```

# /\*Time Step\*/

Define the time step  $k = \frac{T}{N}$ .

# /\*Space localisation\*/

Define the integration domain D = [-l, l] using the probabilistic estimate there.

# /\*Space Step\*/

Define the space step  $h = \frac{2l}{M}$ .

# /\*Peclet Condition\*/

If  $|r - \delta|/\sigma^2$  is not small, then a more stable finite difference approximation is used. cf there.

2 pages 2

#### /\*Lhs factor of theta scheme\*/

Initialize the matrix  $M^h$  issued from the discretization of the operator A in the case of Dirichlet Boundary conditions. cf there.

#### /\*Rhs factor of theta scheme\*/

Initialize the matrix N issued from the  $\theta$ -scheme method in the cases of Dirichlet Boundary conditions. there

# /\*Terminal value\*/

After a logarithmic transformation, put the value of the payoff into a vector P which will be used to save the option value.

## /\*Finite difference Cycle\*/

At any time step, described by the loop in the variable i, we have to solve the system  $M^h v = NP$ .

```
/*Init Rhs*/
```

Compute NP and save the result in the vector Rhs.

## /\*Sor cycle\*/

We solve the system  $M^h v = NP$  using the SOR method which consists in constructing a convergent sequence  $u^p$  whose limit is v.

Variable loops stands for the exponent p.cf there.

- **Step 0** choose a relaxation parameter *omega* and a precision *epsilon*.
- **Step 1** compute the vector  $u^p$  using the variable y and save it in the vector P. Fill the variable error with the difference  $|u^{p+1}-u^p|$ .
- Step 3 indicates the end of the loop by stopping the algorithm when error > epsilon or the number of iteration is too large.

```
/*Price*/
/*Delta*/
/*Memory Desallocation*/
```