

Help

/* Standard Monte Carlo simulation for a Call - Put - Floating Asian option.

In the case of Monte Carlo simulation, the program provides estimations for price and delta with a confidence interval.

In the case of Quasi-Monte Carlo simulation, the program just provides estimations for price and delta. */

```
#include "bs1d_pad.h"
```

```
#include "enums.h"
```

/* Simulation of the final spot and the average with one of the three schemes */

```
static void Simul_StockAndAverage(int scheme, int generator, int step_number,
    id, double sigma, double *ptstock, double *ptaverage)
```

```
{
    double g1, g2, integral, bb, w_t, w_t_1, S_t=0., current_t;
    double h = T / step_number;
    double sqrt_h = sqrt(h);
    double trend = (r - divid)-0.5*SQR(sigma);
    int i;
```

/*Initialisation*/

```
w_t = 0.0;
current_t = 0.0;
integral= 0.;
```

/*Average and Stock Computation*/

/* Scheme 1 : Rieman sums */

```
if((scheme != 2) && (scheme != 3))
{
```

/* Simulation of M gaussian variables according to the generator type,

that is Monte Carlo or Quasi Monte Carlo. */

```
g1= pnl_rand_gauss(step_number, CREATE, 0, generator);
```

```

    for(i=0;i<step_number;i++)
    {
        S_t = x * exp(trend * current_t + sigma * w_t);
        integral += S_t;

        current_t += h;
        /* gaussian value from the table Gaussians */
        g1= pnl_rand_gauss(step_number, RETRIEVE, i, generator);
        w_t += sqrt_h*g1;
    }
}
else
{
    /* Scheme 2 : Trapezoidal method */
    if(scheme == 2)
    {
        /* Simulation of M gaussian variables according
to the generator type,
that is Monte Carlo or Quasi Monte Carlo. */
        g1= pnl_rand_gauss(step_number, CREATE, 0, generator);

        for(i=0;i<step_number;i++)
        {
            /* gaussian value from the table Gaussians */
            g1= pnl_rand_gauss(step_number, RETRIEVE, i, generator);
            /*printf("g= %.3lf\n", g1);*/
            w_t_1 = sqrt_h*g1 + w_t;

            S_t = x * exp(trend * current_t + sigma * w_
t);
            integral += S_t*(1+ (r-divid)*h/2.+sigma*(w_
t_1-w_t)/2.);

            current_t += h;
            w_t = w_t_1;
        }
        /*printf("{n}");*/
    }
    else
    {
        /* Scheme 3 : Brownian Bridge method */

```

```

/* Simulation of 2M gaussian variables according to the
generator type,
that is Monte Carlo or Quasi Monte Carlo. */
g1= pnl_rand_gauss(2*step_number, CREATE, 0, generator);

for(i=0;i<step_number;i++)
{
    g1= pnl_rand_gauss(step_number, RETRIEVE, 2*
i, generator);
    w_t_1 = sqrt_h*g1 + w_t;

    g2= pnl_rand_gauss(step_number, RETRIEVE, (2*i)+1,
generator);
    bb = (w_t+w_t_1)/2.+ g2*sqrt(h/6.);

    S_t = x * exp(trend * current_t + sigma * w_
t);
    integral += S_t*(1+ (r-divid)*h/2. + sigma*(
bb - w_t));

    current_t += h;
    w_t = w_t_1;
}
}

/*Stock*/
*ptstock= S_t;

/*Average*/
*ptaaverage= integral/step_number;

return;

}

static int FloatingAsian_StandardMC(double s, double
time_spent, double pseudo_strike, NumFunc_2 *p, double t,
double r, double divid, double sigma, long N, int M, int scheme,

```

```

    int generator, double confidence, double *ptprice,
    double *ptdelta, double *pterror_price, double *pterror_delta,
    double *inf_price, double *sup_price, double *inf_delta, double
    *sup_delta)
{
    long i;
    int init_mc;
    int simulation_dim;
    double price_sample, delta_sample, mean_price, mean_delta,
    a, var_price, var_delta, average, St;
    double alpha, z_alpha;

    /* Value to construct the confidence interval */
    alpha= (1.- confidence)/2.;
    z_alpha= pnl_inv_cdfnor(1.- alpha);

    /*Initialisation*/
    mean_price= 0.0;
    mean_delta= 0.0;
    var_price= 0.0;
    var_delta= 0.0;
    /* Size of the random vector we need in the simulation */
    if(scheme == 3)
        simulation_dim= 2*M;
    else
        simulation_dim= M;

    /*MC sampling*/
    init_mc= pnl_rand_init(generator, simulation_dim,N);
    /* Test after initialization for the generator */
    if(init_mc == OK)
    {

        /* Begin N iterations */
        for(i=1;i<=N;i++)
        {
            Simul_StockAndAverage(scheme, generator, M, t, s, r,
            divid, sigma, &St, &average);

```

```

/*Price*/
price_sample= (p->Compute)(p->Par, St, pseudo_strike+
average*(1.-time_spent));
/*price_inc1 = (p->Compute)(p->Par, (1.+inc)*St, pseu
do_strike+(1.+inc)*average*(1.-time_spent));
    price_inc2 = (p->Compute)(p->Par, (1.-inc)*St, pseu
do_strike+(1.-inc)*average*(1.-time_spent));*/
/*Delta*/
if(price_sample > 0)
    /*delta_sample= (price_inc1 - price_inc2)/(2.*s*inc)
;*/
    delta_sample=(St-(1-time_spent)*average)/s;
else
    delta_sample= 0;
/*delta_sample= (price_inc1 - price_inc2)/(2.*s*inc);*
/
/*Sum*/
mean_price+= price_sample;
mean_delta+= delta_sample;

/*Sum of squares*/
var_price+= SQR(price_sample);
var_delta+= SQR(delta_sample);
}

/* End N iterations */

/*Price*/
*ptprice= exp(-r*t)*(mean_price/(double) N);
*pterror_price= sqrt(exp(-2.0*r*t)*var_price/(double)
N-SQR(*ptprice))/sqrt((double)N-1);
/* Price Confidence Interval */
*inf_price= *ptprice - z_alpha*(*pterror_price);
*sup_price= *ptprice + z_alpha*(*pterror_price);

/*Delta*/
*ptdelta= exp(-r*t)*mean_delta/(double) N;
/* Put Case */
if((p->Compute) == &Put_StrikeSpot2)
*ptdelta *= (-1);

```

```

        *pterror_delta= sqrt(exp(-2.0*r*t)*(var_delta/(
double)N-SQR(*ptdelta)))/sqrt((double)N-1);

        /* Delta Confidence Interval */
        *inf_delta= *ptdelta - z_alpha*(pterror_delta);
        *sup_delta= *ptdelta + z_alpha*(pterror_delta);
    }
    return init_mc;
}

int CALC(MC_FloatingAsian_Standard)(void *Opt,void *Mod,
    PricingMethod *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r, divid, time_spent, pseudo_strike;

    double T, t_0, T_0;
    int return_value;

    r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

    T= ptOpt->Maturity.Val.V_DATE;
    T_0 = ptMod->T.Val.V_DATE;
    t_0= (ptOpt->PathDep.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUNB
        LE;
    time_spent= (T_0-t_0)/(T-t_0);

    if(T_0 < t_0)
    {
        Fprintf(TOSCREEN,"T_0 < t_0, untreated case{n{n{n}}n");
        return_value =WRONG;
    }

    /* Case t_0 <= T_0 */
    else
    {
        pseudo_strike=time_spent*(ptOpt->PathDep.Val.V_

```

```

NUMFUNC_2)->Par[4].Val.V_PDOUBLE;
    return_value= FloatingAsian_StandardMC(ptMod->S0.Val.
V_PDOUBLE,
        time_spent,
        pseudo_strike,
        ptOpt->PayOff.Val.V_NUMFUNC_2,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val
.V_DATE,
        r,
        divid,
        ptMod->Sigma.Val.V_PDOUBLE,
        Met->Par[2].Val.V_LONG,
        Met->Par[0].Val.V_INT2,
        Met->Par[3].Val.V_ENUM.value,
        Met->Par[1].Val.V_ENUM.value,
        Met->Par[4].Val.V_DOUBLE,
        &(Met->Res[0].Val.V_DOUBLE),
        &(Met->Res[1].Val.V_DOUBLE),
        &(Met->Res[2].Val.V_DOUBLE),
        &(Met->Res[3].Val.V_DOUBLE),
        &(Met->Res[4].Val.V_DOUBLE),
        &(Met->Res[5].Val.V_DOUBLE),
        &(Met->Res[6].Val.V_DOUBLE),
        &(Met->Res[7].Val.V_DOUBLE));
}

return return_value;
}

static int CHK_OPT(MC_FloatingAsian_Standard)(void *Opt,
void *Mod)
{
    if ( (strcmp( ((Option*)Opt)->Name,"    AsianCallFloatingEuro")==0) || (strcmp
        return OK;
    return WRONG;
}

static int MET(Init)(PricingMethod *Met,Option *Opt)
{

```

```

int type_generator;
if ( Met->init == 0)
{
    Met->init=1;

    Met->Par[0].Val.V_INT2= 100;
    Met->Par[1].Val.V_ENUM.value=0;
    Met->Par[1].Val.V_ENUM.members=&PremiaEnumRNGs;
    Met->Par[2].Val.V_LONG= 20000;
    Met->Par[3].Val.V_ENUM.value=2;
    Met->Par[3].Val.V_ENUM.members=&PremiaEnumIntegralsS
cheme;
    Met->Par[4].Val.V_DOUBLE= 0.95;

}

type_generator= Met->Par[1].Val.V_ENUM.value;

if(pnl_rand_or_quasi(type_generator)==PNL_QMC)
{
    Met->Res[2].Viter=IRRELEVANT;
    Met->Res[3].Viter=IRRELEVANT;
    Met->Res[4].Viter=IRRELEVANT;
    Met->Res[5].Viter=IRRELEVANT;
    Met->Res[6].Viter=IRRELEVANT;
    Met->Res[7].Viter=IRRELEVANT;

}
else
{
    Met->Res[2].Viter=ALLOW;
    Met->Res[3].Viter=ALLOW;
    Met->Res[4].Viter=ALLOW;
    Met->Res[5].Viter=ALLOW;
    Met->Res[6].Viter=ALLOW;
    Met->Res[7].Viter=ALLOW;
}
return OK;
}

```



```

PricingMethod MET(MC_FloatingAsian_Standard)=
{
    "MC_FloatingAsian_Standard",
    {"TimeStepNumber",INT2,{100},ALLOW},
    {"RandomGenerator",ENUM,{100},ALLOW},
    {"N iterations",LONG,{100},ALLOW},
    {"Integral Scheme:",ENUM,{100},FORBID},
    {"Confidence Value",DOUBLE,{100},ALLOW},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(MC_FloatingAsian_Standard),
    {"Price",DOUBLE,{100},FORBID},
    {"Delta",DOUBLE,{100},FORBID} ,
    {"Error Price",DOUBLE,{100},FORBID},
    {"Error Delta",DOUBLE,{100},FORBID} ,
    {"Inf Price",DOUBLE,{100},FORBID},
    {"Sup Price",DOUBLE,{100},FORBID} ,
    {"Inf Delta",DOUBLE,{100},FORBID},
    {"Sup Delta",DOUBLE,{100},FORBID} ,
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(MC_FloatingAsian_Standard),
    CHK_ok,
    MET(Init)
};

```

References