```
Help
#include "variancegamma1d pad.h"
#include "enums.h"
#include "pnl/pnl cdf.h"
#include "pnl/pnl random.h"
#include "pnl/pnl specfun.h"
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <</pre>
     (2010+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(MC_VarianceGamma_Fixed)(void *Opt, void
    *Mod)
{
  return NONACTIVE;
int CALC(MC_VarianceGamma_Fixed)(void*Opt,void *Mod,Pricing
    Method *Met)
  return AVAILABLE_IN_FULL_PREMIA;
}
#else
//Compute the positive or negative jump size between the sm
    allest and the biggest value of cdf_jump_points of the VG
    process
static double jump_generator_VG(double* cdf_jump_vect,
    double* cdf jump points, int cdf jump vect size, double M G, int generator)
{
   double z, v, y;
   int test,temp,l,j,q;
   test=0;
   v=pnl_rand_uni(generator);
   y=cdf jump vect[cdf jump vect size]*v;
   l=cdf_jump_vect_size/2;
   j=cdf_jump_vect_size;
   if(cdf jump vect[1]>y)
   {
    1=0;
    j=cdf jump vect size/2;
   }
   if(v==1)
```

```
{
     z=cdf_jump_points[cdf_jump_vect_size];
   }
   if(v==0)
   {
   z=cdf_jump_points[0];
   }
   if(v!=1 \&\& v!=0)
    while(test==0)
     if(cdf_jump_vect[l+1]>y)
      q=1;
      test=1;
     else
     {
      temp=(j-1-1)/2+1;
      if(cdf jump vect[temp]>y)
       j=temp;
       1=1+1;
      }
      else
       l=temp*(temp>l)+(l+1)*(temp<=l);</pre>
      }
     }
    z=cdf_jump_points[q]*exp((y-cdf_jump_vect[q])*exp(M_G*
    cdf jump points[q]));
   }
return z;
static int VG_Mc_Fixed(double s_maxmin,NumFunc_2*P,double
    SO, double T, double r, double divid, double sigma, double thet
    a,double kappa,int generator,long n_paths,double *ptprice,
    double *ptdelta,double *errorprice,double *errordelta)
{
    double K;
```

double payoff,s,s1,sup,inf,eps,err,*Xg,*Xd,*jump_time_v

```
ect p,*jump time vect m;
   double proba,lambda_p,lambda_m,cdf_jump_bound,drift,
   control, s2, s3, s4, s5, s6;
   double u,u0,w1,w2,z,C,G,M,control expec,cov payoff
   control, var payoff, var control;
   double cor_payoff_control,control_coef, tau,pas,*cdf_
   jump points,*cdf jump vect p;
   double *cdf_jump_vect_m,min_M_G,var_proba,infS,supS;
   int i,j,jump_number,jump_number_p,jump_number_m,cdf_
   jump vect size, m1, m2, k1, k2, k;
   G=sqrt(2/kappa+theta*theta/(sigma*sigma))/sigma+theta/(
   sigma*sigma);
   M=sqrt(2/kappa+theta*theta/(sigma*sigma))/sigma-theta/(
   sigma*sigma);
   C=1/kappa;
   control expec=exp((r-divid)*T)*S0;
   err=1e-16;
   eps=1e-1;
   cdf jump vect size=100000;
   s=0;
   s1=0;
   s2=0;
   s3=0;
   s4=0;
   s5=0;
   s6=0:
   lambda p=0;
   lambda m=0;
   proba=0;
   K=P->Par[0].Val.V DOUBLE;
lambda_p=C*pnl_sf_gamma_inc(0.,eps*M);//positive jump
   intensity
   while(lambda p*T<20)</pre>
   {
    eps=eps*0.9;
    lambda p=C*pnl sf gamma inc(0.,eps*M);
   lambda_m=C*pnl_sf_gamma_inc(0.,eps*G);//negative jump intensity
```

```
while(lambda m*T<20)</pre>
    eps=eps*0.9;
    lambda_m=C*pnl_sf_gamma_inc(0.,eps*G);
   lambda p=C*pnl sf gamma inc(0.,eps*M);
   drift=(r-divid)+log(1-(theta+sigma*sigma/2)*kappa)/kapp
   a+theta-C*(exp(-M)/M-exp(-G)/G)-C*((exp(-M*eps)-exp(-M))/M-exp(-M))
    (\exp(-G*\exp(-G))/G);
m1=(int)(10*lambda p*T);
   m2=(int)(10*lambda m*T);
   jump time vect p=malloc((m1)*sizeof(double));
   jump time vect m=malloc((m2)*sizeof(double));
   Xd=malloc((m2+m1)*sizeof(double));//right value of X
   at jump times
   Xg=malloc((m2+m1)*sizeof(double));//left value of X at
   jump times
   jump time_vect_p[0]=0;
   jump time vect m[0]=0;
   Xd[0]=0;
   Xg[0]=0;
   cdf jump bound=5;
   min M G=MIN(M,G);
   //Computation of the biggest jump that we tolerate
   while(C*exp(-min M G*cdf jump bound)/(min M G*cdf jump
   bound)>err)
     cdf jump bound++;
   pas=(cdf_jump_bound-eps)/cdf_jump_vect_size;
   cdf jump points=malloc((cdf jump vect size+1)*sizeof(
   double));
   cdf jump vect p=malloc((cdf jump vect size+1)*sizeof(
   double));
   cdf jump vect m=malloc((cdf jump vect size+1)*sizeof(
   double));
   cdf_jump_points[0] = eps;
   cdf_jump_vect_p[0]=0;
   cdf jump vect m[0]=0;
   //computation of the cdf of the positive and negative
   jumps at some points
```

```
for(i=1;i<=cdf jump vect size;i++)</pre>
    cdf_jump_points[i]=i*pas+eps;
    cdf_jump_vect_p[i]=cdf_jump_vect_p[i-1]+exp(-M*cdf_
   jump_points[i-1])*log(cdf_jump_points[i]/cdf_jump_points[i-1])
    cdf_jump_vect_m[i]=cdf_jump_vect_m[i-1]+exp(-G*cdf_
   jump_points[i-1])*log(cdf_jump_points[i]/cdf_jump_points[i-1])
pnl_rand_init(generator,1,n_paths);
 //Call options case
 if ((P->Compute) == &Call_OverSpot2)
  s maxmin=MAX(s maxmin,K);
  for(i=0;i<n_paths;i++)</pre>
    //simulation of the positive jump times and number
    tau=-1/(lambda p)*log(pnl rand uni(generator));
    jump_number_p=0;
    while(tau<T)</pre>
    {
     jump_number_p++;
     jump_time_vect_p[jump_number_p]=tau;
     tau+=-1/(lambda p)*log(pnl rand uni(generator));
    jump_time_vect_p[jump_number_p+1]=T;
    //simulation of the negative jump times and number
    tau=-1/(lambda m)*log(pnl rand uni(generator));
    jump number m=0;
    while(tau<T)</pre>
     jump_number_m++;
     jump_time_vect_m[jump_number_m]=tau;
     tau+=-1/(lambda_m)*log(pnl_rand_uni(generator));
    jump_time_vect_m[jump_number_m+1]=T;
    jump_number=jump_number_p+jump_number_m;
```

```
//computation of Xg and Xd
    k1=1;
    k2=1;
    u0=0;
    for(k=1;k<=jump_number;k++)</pre>
     w1=jump_time_vect_p[k1];
     w2=jump_time_vect_m[k2];
     if(w1<w2)
      u=w1;
      k1++;
      z=jump_generator_VG(cdf_jump_vect_p,cdf_jump_points,
   cdf_jump_vect_size,M,generator);
     }
     else
     {
      u=w2;
      k2++;
      z=-jump_generator_VG(cdf_jump_vect_m,cdf_jump_points
   ,cdf_jump_vect_size,G,generator);
   Xg[k]=drift*(u-u0)+Xd[k-1];
   Xd[k]=Xg[k]+z;
     u0=u;
    }
    Xg[jump number+1]=drift*(T-u0)+Xd[jump number];
  Xd[jump_number+1] = Xg[jump_number+1];
/
    //computation of the supremum and the infimum of the
   Levy path
    inf=0;
    sup=0;
    for(j=1;j<=jump_number;j++)</pre>
      if(drift>0)
      {
       if(inf>Xd[j])
```

```
inf=Xd[i];
     if(sup<Xg[j])</pre>
      sup=Xg[j];
   }
   else
   {
     if(inf>Xg[j])
      inf=Xg[j];
     if(sup<Xd[j])</pre>
      sup=Xd[j];
   }
 }
 supS=S0*exp(sup);
 if(supS<s_maxmin)</pre>
  supS=s_maxmin;
 proba=1;
 payoff=supS;
 supS=S0*exp(Xd[jump number+1]-inf);//antithetic variat
e associated with the exponential of the Levy supremum
 if(supS<s_maxmin)</pre>
 {
 supS=s_maxmin;
 proba+=1;
 }
 payoff=(payoff+supS)/2;
 proba/=2;
 s1+=payoff;
 s+=payoff*payoff;
 control=S0*exp(Xd[jump_number+1]);
 s2+=control;
 s3+=control*control;
 s4+=control*payoff;
s5+=proba;
 s6+=proba*proba;
cov_payoff_control=s4/n_paths-s1*s2/((double)n_paths*n_
paths);
var_payoff=(s-s1*s1/((double)n_paths))/(n_paths-1);
var_control=(s3-s2*s2/((double)n_paths))/(n_paths-1);
```

```
cor payoff control=cov payoff control/(sqrt(var payoff)
  *sqrt(var control));
  control_coef=cov_payoff_control/var_control;
  var proba=(s6-s5*s5/((double)n paths))/(n paths-1);
  *ptprice=exp(-r*T)*(s1/n paths-control coef*(s2/n paths
  -control expec))-K*exp(-r*T);
  *errorprice=1.96*sqrt(var_payoff*(1-cor_payoff_control*
  cor payoff control))/sqrt(n paths);
  *ptdelta=(*ptprice+(K*exp(-r*T)-S0*exp(-divid*T))-exp(-
  r*T)*s_maxmin*s5/(n_paths))/S0+exp(-divid*T);
  *errordelta=(*errorprice+1.96*exp(-r*T)*s maxmin*sqrt(
  var proba)/sqrt(n paths))/S0;
}
else//Put
 if ((P->Compute) == &Put OverSpot2)
  s maxmin=MIN(s maxmin,K);
  for(i=0;i<n paths;i++)</pre>
   //simulation of the positive jump times and number
   tau=-1/(lambda p)*log(pnl rand uni(generator));
   jump_number_p=0;
   while(tau<T)
   {
    jump number p++;
    jump time vect p[jump number p]=tau;
   tau+=-1/(lambda p)*log(pnl rand uni(generator));
   }
   jump_time_vect_p[jump_number_p+1]=T;
   //simulation of the negative jump times and number
   tau=-1/(lambda m)*log(pnl rand uni(generator));
   jump number m=0;
   while(tau<T)</pre>
   {
    jump number m++;
    jump time vect m[jump number m]=tau;
    tau+=-1/(lambda_m)*log(pnl_rand_uni(generator));
   }
   jump time vect m[jump number m+1]=T;
   jump_number=jump_number_p+jump_number_m;//total jump
  number
```

```
k1=1;
    k2=1;
    u0=0;
    //computation of Xg and Xd
    for(k=1;k<=jump_number;k++)</pre>
     w1=jump_time_vect_p[k1];
     w2=jump_time_vect_m[k2];
     if(w1<w2)
      u=w1;
      k1++;
      z=jump_generator_VG(cdf_jump_vect_p,cdf_jump_points,
   cdf_jump_vect_size,M,generator);
     }
     else
     {
      u=w2;
      k2++;
      z=-jump_generator_VG(cdf_jump_vect_m,cdf_jump_points
   ,cdf_jump_vect_size,G,generator);
     Xg[k]=drift*(u-u0)+Xd[k-1];
     Xd[k]=Xg[k]+z;
     u0=u;
    }
    Xg[jump number+1]=drift*(T-u0)+Xd[jump number];
  Xd[jump_number+1] = Xg[jump_number+1];
/
    //computation of the supremum and the infimum of the
   Levy path
    inf=0;
    sup=0;
    for(j=1;j<=jump_number;j++)</pre>
      if(drift>0)
      {
       if(inf>Xd[j])
```

```
inf=Xd[i];
     if(sup<Xg[j])</pre>
      sup=Xg[j];
   }
   else
   {
     if(inf>Xg[j])
      inf=Xg[j];
     if(sup<Xd[j])</pre>
      sup=Xd[j];
   }
 }
 infS=S0*exp(inf);
 if(infS>s_maxmin)
 {
  infS=s_maxmin;
 proba=1;
 payoff=infS;
 infS=S0*exp(Xd[jump number+1]-sup);//antithetic variat
e associated with the exponential of the Levy infimum
 if(infS>s_maxmin)
 {
  infS=s_maxmin;
 proba+=1;
 }
 payoff=(payoff+infS)/2;
 proba/=2;
 s1+=payoff;
 s+=payoff*payoff;
 control=S0*exp(Xd[jump_number+1]);
 s2+=control;
 s3+=control*control;
 s4+=control*payoff;
s5+=proba;
 s6+=proba*proba;
cov_payoff_control=s4/n_paths-s1*s2/((double)n_paths*n_
paths);
var_payoff=(s-s1*s1/((double)n_paths))/(n_paths-1);
var_control=(s3-s2*s2/((double)n_paths))/(n_paths-1);
```

```
cor payoff control=cov payoff control/(sqrt(var payoff)
    *sqrt(var control));
    control_coef=cov_payoff_control/var_control;
    var proba=(s6-s5*s5/((double)n paths))/(n paths-1);
    *ptprice=K*exp(-r*T)-(exp(-r*T)*s1/n paths-control coe
    f*(s2/n paths-control expec));
    *errorprice=1.96*sqrt(var_payoff*(1-cor_payoff_control*
    cor payoff control))/sqrt(n paths);
    *ptdelta=(*ptprice+(S0*exp(-divid*T)-K*exp(-r*T))+exp(-
    r*T)*s_maxmin*s5/(n_paths))/S0-exp(-divid*T);
    *errordelta=(*errorprice+1.96*exp(-r*T)*s maxmin*sqrt(
    var proba)/sqrt(n paths))/S0;
  free(jump time vect p);
  free(jump_time_vect_m);
  free(cdf_jump_vect_p);
  free(cdf jump vect m);
  free(cdf_jump_points);
  free(Xd);
  free(Xg);
  return OK;
}
int CALC(MC VarianceGamma Fixed)(void*Opt,void *Mod,Pricing
   Method *Met)
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
  TYPEMOD* ptMod=(TYPEMOD*)Mod;
  double r, divid;
  r=log(1.+ptMod->R.Val.V DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V DOUBLE/100.);
  return VG Mc Fixed((ptOpt->PathDep.Val.V NUMFUNC 2)->
    Par[4].Val.V PDOUBLE,ptOpt->PayOff.Val.V NUMFUNC 2,ptMod->SO.
    Val.V PDOUBLE, ptOpt->Maturity.Val.V DATE-ptMod->T.Val.V DA
    TE,r,divid,ptMod->Sigma.Val.V_PDOUBLE,ptMod->Theta.Val.V_
    DOUBLE, ptMod->Kappa. Val. V_SPDOUBLE, Met->Par[0]. Val. V_ENUM. value,
    Met->Par[1].Val.V LONG,&(Met->Res[0].Val.V DOUBLE),&(Met->Res
    [1]. Val. V DOUBLE), & (Met->Res[2]. Val. V DOUBLE), & (Met->Res[3]
    ].Val.V_DOUBLE));
```

```
}
static int CHK_OPT(MC_VarianceGamma_Fixed)(void *Opt, void
    *Mod)
{
  if ((strcmp(((Option*)Opt)->Name, "LookBackCallFixedEuro")
    ==0) || (strcmp( ((Option*)Opt)->Name," LookBackPutFixedEuro")==0) )
    return OK;
  return WRONG;
}
#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Mod)
  if (Met->init == 0)
      Met->init=1;
      Met->Par[0].Val.V_ENUM.value=0;
      Met->Par[0].Val.V_ENUM.members=&PremiaEnumMCRNGs;
      Met->Par[1].Val.V LONG=10000;
    }
  return OK;
PricingMethod MET(MC VarianceGamma Fixed)=
{
  "MC VG LookbackFixed",
  {{"RandomGenerator", ENUM, {100}, ALLOW},
  {"N iterations",LONG,{100},ALLOW},{" ",PREMIA_NULLTYPE,{0
    },FORBID}},
  CALC(MC VarianceGamma Fixed),
  {{"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORB
    ID},{"Price Error",DOUBLE,{100},FORBID},{"Delta Error",
    DOUBLE,{100},FORBID},{" ",PREMIA_NULLTYPE,{0},FORBID}},
  CHK_OPT(MC_VarianceGamma Fixed),
  CHK ok,
 MET(Init)
} ;
```

References