```
   Help
#include <stdlib.h>
#include "cgmy1d_pad.h"
#include "pnl/pnl_vector.h"
#include "pnl/pnl_matrix.h"
#include "pnl/pnl_complex.h"
#include "pnl/pnl_mathtools.h"
#include "pnl/pnl_fft.h"
#include  "math/ap_fusai_levy/DiscreteAsianFMM.h"

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
     (2012+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK_OPT(AP_Asian_FMMCGMY)(void *Opt, void *Mod)
{
  return NONACTIVE;
}
int CALC(AP_Asian_FMMCGMY)(void *Opt,void *Mod,Pricing
    Method *Met)
{
return AVAILABLE_IN_FULL_PREMIA;
}
#else
//-------------------------------------------------------
    -------------------
static dcomplex cfCGMY(double dt, dcomplex g, PnlVect *Para
    meters)
{
  //-------------------------------------------------------
    -----
  // CGMY-KoBol Characteristic Function
  //-------------------------------------------------------
    -----
  double  C,G,M,Y;
  dcomplex term1, term2;
  dcomplex charexp;

  C=pnl_vect_get(Parameters,0)*dt;
  G=pnl_vect_get(Parameters,1);
  M=pnl_vect_get(Parameters,2);
  Y=pnl_vect_get(Parameters,3);
```

```
  term1=Cmul(g,Complex(0,1));
  term2=Csub(Complex(M,0),term1);
  term2=Cpow_real(term2,Y);
    term2=Csub(term2,Complex(POW(M,Y)+POW(G,Y),0));
  term1=Cadd(Complex(G,0),term1);
  term1=Cpow_real(term1,Y);
  term2=Cadd(term2,term1);
  term2=RCmul(C*tgamma(-Y),term2);
  charexp=Cexp(term2);

  return charexp;
}
//------------------------------------------------------------
    -------------------
static double MomentsCGMY(int moment, double  rf, double dt
    , PnlVect *Parameters)
{
  //------------------------------------------------------
    -----
  // compute moments of the CGMY-KoBol model
  //------------------------------------------------------
    -----
  double  C,G,M,Y,gf;
  double mom=0.;

  C=pnl_vect_get(Parameters,0);
  G=pnl_vect_get(Parameters,1);
  M=pnl_vect_get(Parameters,2);
  Y=pnl_vect_get(Parameters,3);
  gf=tgamma(-Y);

  if(moment==1){
    mom=dt*(G*M*rf-C*(-POW(G,1+Y)*M-POW(G,Y)*M*Y+G*(M*(PO
    W(1+G,Y)+POW(M-1,Y))-POW(M,Y+1)+Y*POW(M,Y)))*gf)/(G*M);
  }
  if(moment==2){
    mom=dt*(C*(POW(G,Y)*POW(M,2)+POW(G,2)*POW(M,Y))*(Y-1)
    *Y*gf+dt*POW(G*M*rf-C*(-POW(G,1+Y)*M-POW(G,Y)*M*Y+G*((POW(
    1+G,Y)+POW(M-1,Y))*M-POW(M,1+Y)+POW(M,Y)*Y))*gf,2))/(POW(
    G,2)*POW(M,2));
  }
```

```
  return mom;
}
//-------------------------------------------------------------
    ------------------
static dcomplex charfunction(double r, double  divid,
    double dt, dcomplex g, PnlVect *Parameters)
{  //-----------------------------------------------------
    ------
  // Levy Characteristic Function
  //-----------------------------------------------------
    -----

  double m;
  dcomplex result, mdtg, temp;

  temp=cfCGMY(dt,Complex(0.,-1.), Parameters);
  m = Creal(Csub(Complex((r-divid)*dt, 0.), Clog(temp)));
  mdtg = Cmul(Complex(0., m), g);
  temp=cfCGMY(dt, g, Parameters);
  result=Cmul(Cexp(mdtg), temp);

  return result;
}//-----------------------------------------------------------
    --------------------
static double BoundUpperTailLevy(double x, double  rf,
    double divid, double dt, int maxmoment, PnlVect *Parameters)
{
  //-----------------------------------------------------
    -----
  // compute upper truncation
  //-----------------------------------------------------
    -----
  double minup,bound;
  int i;

  minup = 1.0;
  for(i = 1;i < maxmoment + 1; i++){
      bound = Creal(charfunction(rf, divid, dt, Complex(
    0,-i), Parameters))/exp(x*i);
      minup = MIN(minup, bound);
```

```
  }
  return minup;
}
//-------------------------------------------------------
    -------------------
static double BoundLowerTailLevy(double x, double  rf,
    double divid, double dt, int maxmoment, PnlVect *Parameters)
{
  //-------------------------------------------------------
    -----
  // compute lower truncation
  //-------------------------------------------------------
    -----
  double minlow, bound;
  int i;
  minlow = 1.0;


  for(i = 1;i < maxmoment + 1; i++){
      bound = Creal(charfunction(rf, divid, dt, Complex(
    0,i), Parameters))/exp(x*i);
      minlow = MIN(minlow, bound);
  }
  return minlow;
}
//-------------------------------------------------------
    -------------------
static double findlowuplimit(double rf, double dt, PnlVect
    *Parameters)
{
  //-------------------------------------------------------
    -----------
  // Truncate the transition density domain
  //-------------------------------------------------------
    -----------
  double mom1, mom2, levylow, levyup, bound;
  int maxnummoments, lowfactor, upfactor;

    maxnummoments=10;
  lowfactor=5;
  upfactor=5;
```

```
  mom1=MomentsCGMY(1, rf, dt, Parameters);
  mom2=MomentsCGMY(2, rf, dt, Parameters);

  levylow=mom1-lowfactor*POW(mom2-mom1*mom1,0.5);
    bound=BoundLowerTailLevy(-levylow, rf, 0., dt, maxnumm
    oments, Parameters);
  while(bound>POW(10.0,-8.0))
  {
    lowfactor=lowfactor+1;
    levylow=mom1-lowfactor*POW(mom2-mom1*mom1,0.5);
    bound=BoundLowerTailLevy(-levylow, rf, 0.,dt, maxnumm
    oments, Parameters);
  }

  levyup=mom1+upfactor*POW(mom2-mom1*mom1,0.5);
    bound=BoundUpperTailLevy(levyup, rf, 0., dt, maxnummom
    ents, Parameters);
  while(bound>POW(10.0,-8.0))
  {
    upfactor=upfactor+1;
    levyup=mom1+upfactor*POW(mom2-mom1*mom1,0.5);
    bound=BoundUpperTailLevy(levyup, rf, 0., dt, maxnumm
    oments, Parameters);
  }

  return MAX(ABS(levylow),levyup);
}
//-------------------------------------------------------
    -------------------
static double truncate(double  r, double divid, double dt,
    PnlVect *Parameters)
{
  //-----------------------------------------------------
    -----
  // find u for which cf(u)<10^-10
  //-----------------------------------------------------
    -----

  double abs_cf,step,umax;
  dcomplex cf;
```

```
  step = 1.5;
  umax = 5.0;
  cf = charfunction(r, divid,dt, Complex(umax, 0), Para
    meters);
  abs_cf = sqrt(Creal(cf)*Creal(cf) + Cimag(cf)*Cimag(cf))
    ;

  while (abs_cf > POW(10., -10.))
  {
    umax = umax * step;
    cf = charfunction(r, divid, dt, Complex(umax, 0),
    Parameters);
    abs_cf = sqrt(Creal(cf)*Creal(cf) + Cimag(cf)*Cimag(
    cf)); //compute abs error
  }

  return  (umax + umax / step) / 2;
}
//-------------------------------------------------------
    -------------------
static void kernel(double r, double divid, double  dt, lon
    g N, double b, PnlVect *Parameters, PnlVect *inv, PnlVect *
    logk)
{
  //-----------------------------------------------------
    -------------------------------
  // Compute the transition density function by using the
    Fractional Fourier Transform
  //-----------------------------------------------------
    -------------------------------
  int j;
  double wj,eta,alpha,dx,umax;
  dcomplex term1,ft,aa,a,cgyz;
  PnlVectComplex *y1, *y2;

  y1=pnl_vect_complex_create(2*N);
  y2=pnl_vect_complex_create(2*N);

  // bound of characteristic function grid
  umax = truncate(r, divid, dt, Parameters);
```

```
// bound of the density function grid
b=b*1.25;

// grids'steps
eta = umax / N;
dx = 2 * b / N;
alpha = eta * dx / (2 * M_PI);

for (j=0; j<=N-1; j++)
{
  // trapezoidal quadrature weights
  if( (j == 0) || j == (N - 1)){
    wj = 0.5*eta;
  }
  else {
    wj = eta;
  }
  a = Complex(cos(SQR(j) * alpha * M_PI), sin(SQR(j) *
  alpha * M_PI));
  pnl_vect_complex_set(y2,j,a);
  aa = Complex(cos(SQR(N-j) * alpha * M_PI), sin(SQR(N-
  j) * alpha * M_PI));
  pnl_vect_complex_set(y2,j+N,aa);

  ft = charfunction(r, divid, dt, Complex(j * eta, 0),
  Parameters);
  term1 = Cexp(Complex(0,b*eta* j));
  ft = Cmul(term1, ft);
  pnl_vect_complex_set(y1,j,Cmul(RCdiv(wj,a),ft));
  pnl_vect_complex_set(y1,j+N,CZERO);
}
pnl_fft_inplace(y1);
pnl_fft_inplace(y2);
pnl_vect_complex_mult_vect_term(y1,y2);

//FFT inversion
pnl_ifft_inplace(y1);
for( j = 0; j<= N - 1;j++)
{
  a = Complex(cos(SQR(j) * alpha * M_PI), sin(SQR(j) *
```

```
    alpha * M_PI));
    cgyz = Cdiv(pnl_vect_complex_get(y1,j),CRmul(a,M_PI));
    pnl_vect_set(logk,j,-b+j*dx);
    pnl_vect_set(inv,j,Creal(cgyz));
  }
  pnl_vect_complex_free(&y1);
  pnl_vect_complex_free(&y2);
}

static int FusaiMeucciCGMY_FixedAsian(double pseudo_stock,
    double pseudo_strike,NumFunc_2  *po,double t,double r,double div
    id,double C,double G,double M,double Y,int Mdates,int N,
    double *ptprice,double *ptdelta)
{

  //-------------------------------------------------------
    -------------------
  //Compute price and delta of an Asian call option under
    the CGMY process
  // RECURSIVE PROCEDURE
  //-------------------------------------------------------
    -------------------
  //Recursive approach proposed in
  //Fusai, Marazzina, Marena, SIAM JOURNAL OF FINANCIAL
    MATHEMATICS, 2011
  //-------------------------------------------------------
    -------------------
  int c,i,j,Ni,start,count,flag,startcol,max_len_b;
  long nfft;
  double dt,low,up,b,x,y,xy,h,price,delta;
  PnlVect *CoeffLambda, *abscissa, *weights, *a_temp, *w_
    temp, *xdens, *dens, *Parameters, *vector, *vector1;
  PnlMat *Kmatrix;
  //-------------------------------------------------------
    -------------------
   int flagCP=0,asian_type=0;
  //-------------------------------------------------------
    -------------------
//Call Fixed
  if((po->Compute)==&Call_OverSpot2)
    {flagCP=0;
```

```
    asian_type=0;
  }
//Put Fixed
else if((po->Compute)==&Put_OverSpot2)
  { flagCP=1;
    asian_type=0;
  }
//Call Floating
else if((po->Compute)==&Call_StrikeSpot2)
  { flagCP=0;
    asian_type=1;
  }
 //Put Floating
else if((po->Compute)==&Put_StrikeSpot2)
  { flagCP=1;
    asian_type=1;
  }

Parameters=pnl_vect_create_from_list(4,C,G,M,Y);
// STEP 0: PREPARE GRID AND COEFFICIENTS
//-- payoff coefficients
if (asian_type==0) {
   CoeffLambda=pnl_vect_create_from_double(2,1./(Mdates+1
  ));
   pnl_vect_set(CoeffLambda,0,pnl_vect_get(CoeffLambda,0)
  -pseudo_strike/pseudo_stock);
   c=0;
}
else{
   CoeffLambda=pnl_vect_create_from_double(2,-1./(Mdates+
  1));
   c=-1;
}

//-- price grid
low=-(3./2+30./Mdates);  //lower bound
up=pnl_vect_get(CoeffLambda,1);  //upper bound
//-- generate abscissa and weights for quadrature
if (asian_type==0){
Ni=N; //number of nodes for x<0
N=Ni+N; //total number of nodes
```

```
abscissa=pnl_vect_create_from_zero(N);
weights=pnl_vect_create_from_zero(N);
a_temp=pnl_vect_create_from_zero(Ni);
w_temp=pnl_vect_create_from_zero(Ni);
gauleg_pn(low,0,a_temp,w_temp,Ni);
for (i=0;i<Ni;i++){
  x=pnl_vect_get(a_temp,i);
  y=pnl_vect_get(w_temp,i);
  pnl_vect_set(abscissa,i,x);
  pnl_vect_set(weights,i,y);
  //--- we consider the same number of nodes
  pnl_vect_set(abscissa,i+Ni,(x-low)*up/(-low));
  pnl_vect_set(weights,i+Ni, y*up/(-low));
}
pnl_vect_free(&a_temp);
pnl_vect_free(&w_temp);
}
else{
abscissa=pnl_vect_create_from_zero(N);
weights=pnl_vect_create_from_zero(N);
gauleg_pn(low,up,abscissa,weights,N);
Ni=N;
}

//-- time grid
dt=t/Mdates;

//-- compute the transition density
b=findlowuplimit(r,dt,Parameters);
nfft=32768;
dens=pnl_vect_create_from_zero(nfft);//contains the dens
  ity
xdens=pnl_vect_create_from_zero(nfft);//contains the ab
  scissa of the density
kernel(r,divid,dt,nfft,b,Parameters,dens,xdens);

// STEP 2: CREATE MATRICES AND VECTORS
vector=pnl_vect_create_from_zero(N);
for (j=0; j<=N-1; j++) {
  x=pnl_vect_get(abscissa,j)-(double)c;
  if (x>0.0)
```

```
    pnl_vect_set(vector,j,x);
}

// MATRIX
startcol=0; max_len_b=0; count=0;
Kmatrix=pnl_mat_create_from_double(Ni,N+2,0.0);
for (i=0; i<=Ni-1; i++){
  flag=0; start=0;
  x=pnl_vect_get(abscissa,i);
        for (j=startcol; j<=N-1; j++){
    y=pnl_vect_get(abscissa,j);
    xy=log(x/(y-pnl_vect_get(CoeffLambda,1)));
    if (ABS(xy)<=b){
      if (flag==0){
        flag=1; // start to fill the row
        pnl_mat_set(Kmatrix,i,0,j); // first element
  of the band
        startcol=j;
        count=1;
      }
      count=count+1;
      xy=MAX(interp_lin(xy, nfft, &start, xdens, dens)
  ,0.0);
      pnl_mat_set(Kmatrix,i,count,-exp(-r*dt)*xy*(x/SQ
  R(y-pnl_vect_get(CoeffLambda,1))));
      if (j==N-1){ // stop to fill the row (since it
  is finished)
      pnl_mat_set(Kmatrix,i,1,(N-1)-(int)pnl_mat_get(
  Kmatrix,i,0)+1); // length of the band
      max_len_b=MAX(max_len_b,(int)pnl_mat_get(Kmatr
  ix,i,1));
      }
    }else if (flag==1){ // stop to fill the row
      pnl_mat_set(Kmatrix,i,1,(j-1)-(int)pnl_mat_get(
  Kmatrix,i,0)+1); // length of the band
      max_len_b=MAX(max_len_b,(int)pnl_mat_get(Kmatrix
  ,i,1));
      break;
    }
   }
}
```

```
 // STEP 3: RECURSIVE APPROACH
 vector1=pnl_vect_create_from_zero(Ni);
 if (asian_type==0){
   for(i=0;i<Mdates;i++){
     pnl_vect_mult_vect_term(vector,weights);
     bmat_mult_vect(Kmatrix,vector,vector1,Ni,N+2);
     for (j=0;j<Ni;j++)
        pnl_vect_set(vector,j,pnl_vect_get(vector1,j));
     xy=pnl_vect_get(CoeffLambda,1)*exp((r-divid)*dt)*(1
   -exp((i+1)*(r-divid)*dt))/(1-exp((r-divid)*dt));
     for (j=Ni;j<N;j++)
           pnl_vect_set(vector,j,exp(-r*(i+1)*dt)*(pnl_vec
   t_get(abscissa,j)+xy));
   }
}else{
   for(i=0;i<Mdates;i++){
     pnl_vect_mult_vect_term(vector,weights);
     bmat_mult_vect(Kmatrix,vector,vector1,Ni,N+2);
         pnl_vect_clone(vector,vector1);
   }
 }

 xy=interp_lin1(pnl_vect_get(CoeffLambda,0),N,abscissa,vec
   tor);
 price=pseudo_stock*xy;
 if (asian_type==0){
   h=exp((up-low)/N);
   x=(pseudo_stock-h)*interp_lin1(pnl_vect_get(CoeffLambd
   a,1)-pseudo_strike/(pseudo_stock-h),N,abscissa,vector);
   y=(pseudo_stock+h)*interp_lin1(pnl_vect_get(CoeffLambd
   a,1)-pseudo_strike/(pseudo_stock+h),N,abscissa,vector);
   xy=(y-x)/(2*h);
 }
 delta=xy;

 if (flagCP==1){
   price=price-pseudo_stock*(pnl_vect_get(CoeffLambda,0)*
   exp(-r*Mdates*dt)-c);
 delta=delta-(pnl_vect_get(CoeffLambda,1)*exp(-r*Mdates*
```

```
    dt)-c);
  for(i=0;i<Mdates;i++)
  {
    price=price-pseudo_stock*pnl_vect_get(CoeffLambda,1)*
    exp(-r*i*dt);
    delta=delta-pnl_vect_get(CoeffLambda,1)*exp(-r*i*dt);
  }
  }

  *ptprice=price;
  *ptdelta=delta;
  //------DESTROY-----------------------------------------
    -----------------
  pnl_vect_free(&xdens);
  pnl_vect_free(&dens);
  pnl_vect_free(&Parameters);
  pnl_vect_free(&vector);
  pnl_vect_free(&vector1);
  pnl_mat_free(&Kmatrix);
  pnl_vect_free(&abscissa);
  pnl_vect_free(&weights);
  pnl_vect_free(&CoeffLambda);
  return OK;
}

int CALC(AP_Asian_FMMCGMY)(void *Opt,void *Mod,Pricing
    Method *Met)
{
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
  TYPEMOD* ptMod=(TYPEMOD*)Mod;

  int return_value;
  double r,divid,time_spent,pseudo_spot,pseudo_strike;
  double t_0, T_0;

  r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

  T_0 = ptMod->T.Val.V_DATE;
  t_0= (ptOpt->PathDep.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUB
    LE;
```

```
  if(T_0 < t_0)
    {
      Fprintf(TOSCREEN,"T_0 < t_0, untreated case{n{n{n");
      return_value = WRONG;
    }
  /* Case t_0 <= T_0 */
  else
    {
      time_spent=(ptMod->T.Val.V_DATE-(ptOpt->PathDep.Val.
    V_NUMFUNC_2)->Par[0].Val.V_PDOUBLE)/(ptOpt->Maturity.Val.V_
    DATE-(ptOpt->PathDep.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUB
    LE);
      pseudo_spot=(1.-time_spent)*ptMod->S0.Val.V_PDOUBLE;
      pseudo_strike=(ptOpt->PayOff.Val.V_NUMFUNC_2)->Par[0]
    .Val.V_PDOUBLE-time_spent*(ptOpt->PathDep.Val.V_NUMFUNC_2)
    ->Par[4].Val.V_PDOUBLE;

  return_value= FusaiMeucciCGMY_FixedAsian(pseudo_spot,ps
    eudo_strike,ptOpt->PayOff.Val.V_NUMFUNC_2,ptOpt->Maturity.
    Val.V_DATE-ptMod->T.Val.V_DATE,r,divid,ptMod->C.Val.V_PDOUB
    LE,ptMod->G.Val.V_PDOUBLE,ptMod->M.Val.V_PDOUBLE,ptMod->Y.
    Val.V_PDOUBLE,Met->Par[0].Val.V_INT2,Met->Par[1].Val.V_INT2,
    &(Met->Res[0].Val.V_DOUBLE),&(Met->Res[1].Val.V_DOUBLE));
    }

  return return_value;
}

static int CHK_OPT(AP_Asian_FMMCGMY)(void *Opt, void *Mod)
{
    if ( (strcmp(((Option*)Opt)->Name,"AsianCallFixedEuro")
    ==0) || (strcmp( ((Option*)Opt)->Name,"AsianPutFixedEuro")
    ==0)|| (strcmp(((Option*)Opt)->Name,"    AsianCallFloatingEuro")==0) || (str
    return OK;
  return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
```

```
{
   if ( Met->init == 0)
    {
      Met->init=1;
      Met->Par[0].Val.V_INT2=52;
      Met->Par[1].Val.V_INT2=5000;
    }
  return OK;
}

PricingMethod MET(AP_Asian_FMMCGMY)=
{
  "AP_Asian_FMM_CGMY",
  {{"Nb.of Monitoring Dates",INT2,{2000},ALLOW },
   {"Nb.of Integration Points ",INT2,{1000},ALLOW},
   {" ",PREMIA_NULLTYPE,{0},FORBID}},
  CALC(AP_Asian_FMMCGMY),
  {{"Price",DOUBLE,{100},FORBID},{"Delta",DOUBLE,{100},FORB
    ID} ,{" ",PREMIA_NULLTYPE,{0},FORBID}},
  CHK_OPT(AP_Asian_FMMCGMY),
  CHK_ok,
  MET(Init)
};
```

References