```
Help
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
     (2008+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
#else
#include "common.h"
#include <cmath>
#include <iostream>
#include <cstdlib>
#ifndef MSC VER
#include "config.h"
#endif
extern "C"{
#include "pnl/pnl mathtools.h"
using namespace std;
//
//fonction Hh-1
long double Hh(const long double& x)
 return expl(-x*x/2.);
//gaussian pdf
long double dnorm(long double x)
 return (expl(-x*x/2.)/(sqrtl(2.*M_PI)));
}
long double MAXLOGL = 1.13565234062941439494919310779707648
    91253E4L;
long double SQRTHL = 7.071067811865475244008443621048490392
    8484E-1L;
#if (defined WIN32 || defined MSC VER || !defined HAVE
    ERFL)
/* erfc(x + 0.25) = erfc(0.25) + x R(x)
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0 \le x \le 0.125
   Peak relative error 1.4e-35 */
#define NRNr13 8
static long double RNr13[NRNr13 + 1] =
    -2.353707097641280550282633036456457014829E3L,
    3.871159656228743599994116143079870279866E2L,
    -3.888105134258266192210485617504098426679E2L.
    -2.129998539120061668038806696199343094971E1L,
    -8.125462263594034672468446317145384108734E1L,
    8.151549093983505810118308635926270319660E0L,
    -5.033362032729207310462422357772568553670E0L,
    -4.253956621135136090295893547735851168471E-2L,
    -8.098602878463854789780108161581050357814E-2L
  };
#define NRDr13 7
static long double RDr13[NRDr13 + 1] =
    2.220448796306693503549505450626652881752E3L,
    1.899133258779578688791041599040951431383E2L,
    1.061906712284961110196427571557149268454E3L,
    7.497086072306967965180978101974566760042E1L,
    2.146796115662672795876463568170441327274E2L,
    1.120156008362573736664338015952284925592E1L,
    2.211014952075052616409845051695042741074E1L,
    6.469655675326150785692908453094054988938E-1L
    /* 1.0E0 */
  };
/* erfc(0.25) = C13a + C13b to extra precision.
static long double C13a = 0.723663330078125L;
static long double C13b = 1.0279753638067014931732235184287
    934646022E-5L;
/* \operatorname{erfc}(x + 0.375) = \operatorname{erfc}(0.375) + x R(x)
   0 \le x \le 0.125
   Peak relative error 1.2e-35 */
#define NRNr14 8
static long double RNr14[NRNr14 + 1] =
    -2.446164016404426277577283038988918202456E3L,
    6.718753324496563913392217011618096698140E2L,
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-4.581631138049836157425391886957389240794E2L,
    -2.382844088987092233033215402335026078208E1L,
    -7.119237852400600507927038680970936336458E1L,
    1.313609646108420136332418282286454287146E1L,
    -6.188608702082264389155862490056401365834E0L,
    -2.787116601106678287277373011101132659279E-2L,
    -2.230395570574153963203348263549700967918E-2L
  }:
#define NRDr14 7
static long double RDr14[NRDr14 + 1] =
    2.495187439241869732696223349840963702875E3L,
    2.503549449872925580011284635695738412162E2L,
    1.159033560988895481698051531263861842461E3L,
    9.493751466542304491261487998684383688622E1L,
    2.276214929562354328261422263078480321204E2L,
    1.367697521219069280358984081407807931847E1L,
    2.276988395995528495055594829206582732682E1L,
    7.647745753648996559837591812375456641163E-1L
    /* 1.0E0 */
  };
/* \operatorname{erfc}(0.375) = C14a + C14b to extra precision.
static long double C14a = 0.5958709716796875L;
static long double C14b = 1.2118885490201676174914080878232
    469565953E-5L;
/* erfc(x + 0.5) = erfc(0.5) + x R(x)
   0 \le x \le 0.125
   Peak relative error 4.7e-36 */
#define NRNr15 8
static long double RNr15[NRNr15 + 1] =
  {
    -2.624212418011181487924855581955853461925E3L,
    8.473828904647825181073831556439301342756E2L,
    -5.286207458628380765099405359607331669027E2L,
    -3.895781234155315729088407259045269652318E1L,
    -6.200857908065163618041240848728398496256E1L,
    1.469324610346924001393137895116129204737E1L,
    -6.961356525370658572800674953305625578903E0L,
    5.145724386641163809595512876629030548495E-3L,
    1.990253655948179713415957791776180406812E-2L
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};
#define NRDr15 7
static long double RDr15[NRDr15 + 1] =
    2.986190760847974943034021764693341524962E3L,
    5.288262758961073066335410218650047725985E2L,
    1.363649178071006978355113026427856008978E3L,
    1.921707975649915894241864988942255320833E2L.
    2.588651100651029023069013885900085533226E2L,
    2.628752920321455606558942309396855629459E1L,
    2.455649035885114308978333741080991380610E1L,
    1.378826653595128464383127836412100939126E0L
    /* 1.0E0 */
  };
/* \operatorname{erfc}(0.5) = C15a + C15b  to extra precision. */
static long double C15a = 0.4794921875L;
static long double C15b = 7.9346869534623172533461080354712
    635484242E-6L;
/* \operatorname{erfc}(x + 0.625) = \operatorname{erfc}(0.625) + x R(x)
   0 \le x \le 0.125
   Peak relative error 5.1e-36 */
#define NRNr16 8
static long double RNr16[NRNr16 + 1] =
    -2.347887943200680563784690094002722906820E3L,
    8.008590660692105004780722726421020136482E2L,
    -5.257363310384119728760181252132311447963E2L,
    -4.471737717857801230450290232600243795637E1L,
    -4.849540386452573306708795324759300320304E1L,
    1.140885264677134679275986782978655952843E1L,
    -6.731591085460269447926746876983786152300E0L,
    1.370831653033047440345050025876085121231E-1L,
    2.022958279982138755020825717073966576670E-2L,
  };
#define NRDr16 7
static long double RDr16[NRDr16 + 1] =
  {
    3.075166170024837215399323264868308087281E3L,
    8.730468942160798031608053127270430036627E2L,
    1.458472799166340479742581949088453244767E3L,
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3.230423687568019709453130785873540386217E2L,
    2.804009872719893612081109617983169474655E2L,
    4.465334221323222943418085830026979293091E1L,
    2.612723259683205928103787842214809134746E1L,
    2.341526751185244109722204018543276124997E0L,
    /* 1.0E0 */
  };
/* \operatorname{erfc}(0.625) = C16a + C16b to extra precision.
static long double C16a = 0.3767547607421875L;
static long double C16b = 4.3570693945275513594941232097252
    997287766E-6L;
/* \operatorname{erfc}(x + 0.75) = \operatorname{erfc}(0.75) + x R(x)
   0 \le x \le 0.125
   Peak relative error 1.7e-35 */
#define NRNr17 8
static long double RNr17[NRNr17 + 1] =
  {
    -1.767068734220277728233364375724380366826E3L,
    6.693746645665242832426891888805363898707E2L,
    -4.746224241837275958126060307406616817753E2L,
    -2.274160637728782675145666064841883803196E1L,
    -3.541232266140939050094370552538987982637E1L,
    6.988950514747052676394491563585179503865E0L,
    -5.807687216836540830881352383529281215100E0L,
    3.631915988567346438830283503729569443642E-1L,
    -1.488945487149634820537348176770282391202E-2L
  };
#define NRDr17 7
static long double RDr17[NRDr17 + 1] =
  {
    2.748457523498150741964464942246913394647E3L,
    1.020213390713477686776037331757871252652E3L,
    1.388857635935432621972601695296561952738E3L,
    3.903363681143817750895999579637315491087E2L,
    2.784568344378139499217928969529219886578E2L.
    5.555800830216764702779238020065345401144E1L,
    2.646215470959050279430447295801291168941E1L,
    2.984905282103517497081766758550112011265E0L,
    /* 1.0E0 */
  };
```

```
/* \operatorname{erfc}(0.75) = C17a + C17b to extra precision.
static long double C17a = 0.2888336181640625L;
static long double C17b = 1.0748182422368401062165408589222
    625794046E-5L;
/* \operatorname{erfc}(x + 0.875) = \operatorname{erfc}(0.875) + x R(x)
   0 \le x \le 0.125
   Peak relative error 2.2e-35 */
#define NRNr18 8
static long double RNr18[NRNr18 + 1] =
  {
    -1.342044899087593397419622771847219619588E3L,
    6.127221294229172997509252330961641850598E2L,
    -4.519821356522291185621206350470820610727E2L,
    1.223275177825128732497510264197915160235E1L,
    -2.730789571382971355625020710543532867692E1L,
    4.045181204921538886880171727755445395862EOL,
    -4.925146477876592723401384464691452700539E0L,
    5.933878036611279244654299924101068088582E-1L.
    -5.557645435858916025452563379795159124753E-2L
  };
#define NRDr18 7
static long double RDr18[NRDr18 + 1] =
    2.557518000661700588758505116291983092951E3L,
    1.070171433382888994954602511991940418588E3L,
    1.344842834423493081054489613250688918709E3L,
    4.161144478449381901208660598266288188426E2L,
    2.763670252219855198052378138756906980422E2L,
    5.998153487868943708236273854747564557632E1L,
    2.657695108438628847733050476209037025318E1L,
    3.252140524394421868923289114410336976512EOL,
    /* 1.0E0 */
  };
/* \operatorname{erfc}(0.875) = C18a + C18b \text{ to extra precision.} */
static long double C18a = 0.215911865234375L;
static long double C18b = 1.3073705765341685464282101150637
    224028267E-5L;
/* erfc(x + 1.0) = erfc(1.0) + x R(x)
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```
0 \le x \le 0.125
   Peak relative error 1.6e-35 */
#define NRNr19 8
static long double RNr19[NRNr19 + 1] =
    -1.139180936454157193495882956565663294826E3L,
    6.134903129086899737514712477207945973616E2L,
    -4.628909024715329562325555164720732868263E2L.
    4.165702387210732352564932347500364010833E1L,
    -2.286979913515229747204101330405771801610E1L,
    1.870695256449872743066783202326943667722E0L,
    -4.177486601273105752879868187237000032364E0L,
    7.533980372789646140112424811291782526263E-1L,
    -8.629945436917752003058064731308767664446E-2L
  };
#define NRDr19 7
static long double RDr19[NRDr19 + 1] =
    2.744303447981132701432716278363418643778E3L,
    1.266396359526187065222528050591302171471E3L,
    1.466739461422073351497972255511919814273E3L,
    4.868710570759693955597496520298058147162E2L,
    2.993694301559756046478189634131722579643E2L,
    6.868976819510254139741559102693828237440E1L,
    2.801505816247677193480190483913753613630E1L,
    3.604439909194350263552750347742663954481E0L,
    /* 1.0E0 */
  };
/* \operatorname{erfc}(1.0) = \operatorname{C19a} + \operatorname{C19b} to extra precision. */
static long double C19a = 0.15728759765625L;
static long double C19b = 1.1609394035130658779364917390740
    703933002E-5L;
/* \operatorname{erfc}(x + 1.125) = \operatorname{erfc}(1.125) + x R(x)
   0 \le x \le 0.125
   Peak relative error 3.6e-36 */
#define NRNr20 8
static long double RNr20[NRNr20 + 1] =
    -9.652706916457973956366721379612508047640E2L,
    5.577066396050932776683469951773643880634E2L,
```

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-4.406335508848496713572223098693575485978E2L,
    5.202893466490242733570232680736966655434E1L,
    -1.931311847665757913322495948705563937159E1L,
    -9.364318268748287664267341457164918090611E-2L,
    -3.306390351286352764891355375882586201069E0L,
    7.573806045289044647727613003096916516475E-1L,
    -9.611744011489092894027478899545635991213E-2L
  }:
#define NRDr20 7
static long double RDr20[NRDr20 + 1] =
    3.032829629520142564106649167182428189014E3L,
    1.659648470721967719961167083684972196891E3L,
    1.703545128657284619402511356932569292535E3L,
    6.393465677731598872500200253155257708763E2L,
    3.489131397281030947405287112726059221934E2L,
    8.848641738570783406484348434387611713070E1L,
    3.132269062552392974833215844236160958502E1L,
    4.430131663290563523933419966185230513168E0L
    /* 1.0E0 */
  };
/* \operatorname{erfc}(1.125) = C20a + C20b  to extra precision. */
static long double C20a = 0.111602783203125L;
static long double C20b = 8.9850951672359304215530728365232
    161564636E-6L;
#endif /* (defined WIN32 || defined MSC VER || !defined
    HAVE ERFL) */
/* \operatorname{erfc}(x) = \exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
   7/8 \le 1/x \le 1
   Peak relative error 1.4e-35 */
#define NRNr8 9
static long double RNr8[NRNr8 + 1] =
  {
    3.587451489255356250759834295199296936784E1L.
    5.406249749087340431871378009874875889602E2L,
    2.931301290625250886238822286506381194157E3L,
    7.359254185241795584113047248898753470923E3L,
    9.201031849810636104112101947312492532314E3L,
    5.749697096193191467751650366613289284777E3L,
```

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1.710415234419860825710780802678697889231E3L,
    2.150753982543378580859546706243022719599E2L,
    8.740953582272147335100537849981160931197E0L,
    4.876422978828717219629814794707963640913E-2L
  }:
#define NRDr8 8
static long double RDr8[NRDr8 + 1] =
    6.358593134096908350929496535931630140282E1L,
    9.900253816552450073757174323424051765523E2L,
    5.642928777856801020545245437089490805186E3L,
    1.524195375199570868195152698617273739609E4L,
    2.113829644500006749947332935305800887345E4L,
    1.526438562626465706267943737310282977138E4L,
    5.561370922149241457131421914140039411782E3L,
    9.394035530179705051609070428036834496942E2L,
    6.147019596150394577984175188032707343615E1L
    /* 1.0E0 */
  };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
   3/4 \le 1/x < 7/8
   Peak relative error 1.7e-36 */
#define NRNr7 9
static long double RNr7[NRNr7 + 1] =
  {
    1.293515364043117601705535485785956592493E2L,
    2.474534371269189867053251150063459055230E3L,
    1.756537563959875738809491329250457486510E4L,
    5.977479535376639763773153344676726091607E4L,
    1.054313816139671870123172936972055385049E5L,
    9.754699773487726957401038094714603033904E4L,
    4.579131242577671038339922925213209214880E4L,
    1.000710322164510887997115157797717324370E4L,
    8.496863250712471449526805271633794700452E2L,
    1.797349831386892396933210199236530557333E1L
  };
#define NRDr7 9
static long double RDr7[NRDr7 + 1] =
  {
    2.292696320307033494820399866075534515002E2L,
```

```
4.500632608295626968062258401895610053116E3L,
    3.321218723485498111535866988511716659339E4L.
    1.196084512221845156596781258490840961462E5L,
    2.287033883912529843927983406878910939930E5L,
    2.370223495794642027268482075021298394425E5L,
    1.305173734022437154610938308944995159199E5L,
    3.589386258485887630236490009835928559621E4L,
    4.339996864041074149726360516336773136101E3L.
    1.753135522665469574605384979152863899099E2L
    /* 1.0E0 */
  };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
   5/8 \le 1/x \le 3/4
   Peak relative error 1.6e-35 */
#define NRNr6 9
static long double RNr6[NRNr6 + 1] =
  {
    1.423313561367394923305025174137639124533E1L,
    3.244462503273003837514629113846075327206E2L,
    2.784937282403293364911673341412846781934E3L,
    1.163060685810874867196849890286455473382E4L,
    2.554141394931962276102205517358731053756E4L,
    2.9827337825007295305033336931258698708782E4L,
    1.789683564523810605328169719436374742840E4L,
    5.056032142227470121262177112822018882754E3L,
    5.605349942234782054561269306895707034586E2L,
    1.561652599080729507274832243665726064881E1L
 };
#define NRDr6 9
static long double RDr6[NRDr6 + 1] =
  {
    2.522757606611479946069351519410222913326E1L,
    5.876797910931896554014229647006604017806E2L,
    5.211092128250480712011248211246144751074E3L,
    2.282679910855404599271496827409168580797E4L,
    5.371245819205596609986320599133109262447E4L,
    6.926186102106400355114925675028888924445E4L,
    4.794366033363621432575096487724913414473E4L,
    1.673190682734065914573814938835674963896E4L,
    2.589544846151313120096957014256536236242E3L,
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1.349438432583208276883323156200117027433E2L
   };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
  1/2 \le 1/x < 5/8
  Peak relative error 4.3e-36 */
#define NRNr5 10
static long double RNr5[NRNr5 + 1] =
  {
   6.743447478279267339131211137241149796763E-2L,
   2.031339015932962998168472743355874796350E0L,
   2.369234815713196480221800940201367484379E1L,
   1.387819614016107433603101545594790875922E2L,
   4.435600256936515839937720907171966121786E2L,
   7.881577949936817507981170892417739733047E2L,
   7.615749099291545976179905281851765734680E2L,
   3.752484528663442467089606663006771157777E2L,
   8.279644286027145214308303292537009564726E1L,
   6.201462983413738162709722770960040042647E0L.
   6.649631608720062333043506249503378282697E-2L
  };
#define NRDr5 9
static long double RDr5[NRDr5 + 1] =
   1.195244945161889822018178270706903972343E-1L,
   3.660216908153253021384862427197665991311EOL,
   4.373405883243078019655721779021995159854E1L,
   2.653305963056235008916733402786877121865E2L,
   8.921329790491152046318422124415895506335E2L,
   1.705552231555600759729260640562363304312E3L,
   1.832711109606893446763174603477244625325E3L,
   1.056823953275835649973998168744261083316E3L,
   2.975561981792909722126456997074344895584E2L,
   3.393149095158232521894537008472203487436E1L
   /* 1.0E0 */
  };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
  3/8 \le 1/x < 1/2
  Peak relative error 1.8e-36 */
```

```
#define NRNr4 10
static long double RNr4[NRNr4 + 1] =
  {
    3.558685919236420073872459554885612994007E-2L,
    1.460223642496950651561817195253277924528E0L,
    2.379856746555189546876720308841066577268E1L,
    2.005205521246554860334064698817220160117E2L,
    9.533374928664989955629120027419490517596E2L.
    2.623024576994438336130421711314560425373E3L.
    4.126446434603735586340585027628851620886E3L,
    3.540675861596687801829655387867654030013E3L,
    1.506037084891064572653273761987617394259E3L,
    2.630715699182706745867272452228891752353E2L,
    1.202476629652900619635409242749750364878E1L
 };
#define NRDr4 10
static long double RDr4[NRDr4 + 1] =
  {
    6.307606561714590590399683184410336583739E-2L,
    2.619717051134271249293056836082721776665E0L,
    4.344441402681725017630451522968410844608E1L,
    3.752891116408399440953195184301023399176E2L,
    1.849305988804654653921972804388006355502E3L,
    5.358505261991675891835885654499883449403E3L,
    9.091890995405251314631428721090705475825E3L,
    8.731418313949291797856351745278287516416E3L,
    4.420211285043270337492325400764271868740E3L,
    1.031487363021856106882306509107923200832E3L,
    8.387036084846046121805145056040429461783E1L
    /* 1.0E0 */
  };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
   1/4 \le 1/x < 3/8
   Peak relative error 8.1e-37 */
#define NRNr3 11
static long double RNr3[NRNr3 + 1] =
  {
    4.584481542956275354582319313040418316755E-5L,
    2.674923158288848442110883948437930349128E-3L,
    6.344232532055212248017211243740466847311E-2L,
```

```
7.985145965992002744933550450451513513963E-1L,
    5.845078061888281665064746347663123946270E0L,
    2.566625318816866587482759497608029522596E1L,
    6.736225182343446605268837827950856640948E1L,
    1.021796460139598089409347761712730512053E2L,
    8.344336615515430530929955615400706619764E1L,
    3.207749011528249356283897356277376306967E1L,
    4.386185123863412086856423971695142026036E0L.
    8.971576448581208351826868348023528863856E-2L
  };
#define NRDr3 10
static long double RDr3[NRDr3 + 1] =
  {
    8.125781965218112303281657065320409661370E-5L,
    4.781806762611504685247817818428945295520E-3L,
    1.147785538413798317790357996845767614561E-1L,
    1.469285552007088106614218996464752307606E0L,
    1.101712261349880339221039938999124077650E1L,
    5.008507527095093413713171655268276861071E1L,
    1.383058691613468970486425146336829447433E2L,
    2.264114250278912520501010108736339599752E2L,
    2.081377197698598680576330179979996940039E2L,
    9.724438129690013609440151781601781137944E1L,
    1.907905050771832372089975877589291760121E1L
    /* 1.0E0 */
  };
/* erfc(x) = exp(-x^2) 1/x R(1/x^2) / S(1/x^2)
   1/8 \le 1/x < 1/4
   Peak relative error 1.5e-36 */
#define NRNr2 11
static long double RNr2[NRNr2 + 1] =
    6.928615158005256885698045840589513728399E-7L,
    5.616245938942075826026382337922413007879E-5L,
    1.871624980715261794832358438894219696113E-3L,
    3.349922063795792371642023765253747563009E-2L,
    3.531865233974349943956345502463135695834E-1L,
    2.264714157625072773976468825160906342360E0L,
    8.810720294489253776747319730638214883026E0L,
    2.014056685571655833019183248931442888437E1L,
```

```
2.524586947657190747039554310814128743320E1L,
    1.520656940937208886246188940244581671609E1L,
    3.334145500790963675035841482334493680498E0L,
    1.122108380007109245896534245151140632457E-1L
  }:
#define NRDr2 10
static long double RDr2[NRDr2 + 1] =
    1.228065061824874795984937092427781089256E-6L,
    1.001593999520159167559129042893802235969E-4L,
    3.366527555699367241421450749821030974446E-3L,
    6.098626947195865254152265585991861150369E-2L,
    6.541547922508613985813189387198804660235E-1L,
    4.301130233305371976727117480925676583204E0L,
    1.737155892350891711527711121692994762909E1L,
    4.206892112110558214680649401236873828801E1L,
    5.787487996025016843403524261574779631219E1L,
    4.094047148590822715163181507813774861621E1L,
    1.230603930056944875836549716515643997094E1L
    /* 1.0E0 */
  };
/* \operatorname{erfc}(x) = \exp(-x^2) \frac{1}{x} R(\frac{1}{x^2}) / S(\frac{1}{x^2})
   1/128 \le 1/x < 1/8
   Peak relative error 2.2e-36 */
#define NRNr1 9
static long double RNr1[NRNr1 + 1] =
  {
    1.293111801138199795250035229383033322539E-6L,
    9.785224720880980456171438759161161816706E-5L,
    2.932474396233212166056331430621176065943E-3L,
    4.496429595719847083917435337780697436921E-2L,
    3.805989855927720844877478869846718877846E-1L,
    1.789745532222426292126781724570152590071EOL,
    4.465737379634389318903237306594171764628E0L,
    5.268535822258082278401240171488850433767E0L,
    2.258357766807433839494276681092713991651E0L.
    1.504459334078750002966538036652860809497E-1L
  };
#define NRDr1 8
static long double RDr1[NRDr1 + 1] =
  {
```

```
2.291980991578770070179177302906728371406E-6L,
    1.745845828808028552029674694534934620384E-4L.
    5.283248841982102317072923869576785278019E-3L,
    8.221212297078141470944454807434634848018E-2L,
    7.120500674861902950423510939060230945621E-1L,
    3.475435367560809622183983439133664598155EOL,
    9.243253391989233533874386043611304387113E0L,
    1.227894792475280941511758877318903197188E1L.
    6.789361410398841316638617624392719077724E0L
    /* 1.0E0 */
  };
/* \operatorname{erf}(z+1) = \operatorname{erf} \operatorname{const} + P(z)/Q(z)
   -.125 \le z \le 0
   Peak relative error 7.3e-36 */
#if (defined WIN32 || defined MSC VER || !defined HAVE
    ERFL)
static long double erf_const = 0.845062911510467529296875L;
#define NTN2 8
static long double TN2[NTN2 + 1] =
  {
    -4.088889697077485301010486931817357000235E1L,
    7.157046430681808553842307502826960051036E3L,
    -2.191561912574409865550015485451373731780E3L,
    2.180174916555316874988981177654057337219E3L,
    2.848578658049670668231333682379720943455E2L,
    1.630362490952512836762810462174798925274E2L,
    6.317712353961866974143739396865293596895EOL,
    2.450441034183492434655586496522857578066E1L,
    5.127662277706787664956025545897050896203E-1L
  };
#define NTD2 8
static long double TD2[NTD2 + 1] =
    1.731026445926834008273768924015161048885E4L,
    1.209682239007990370796112604286048173750E4L,
    1.160950290217993641320602282462976163857E4L,
    5.394294645127126577825507169061355698157E3L,
    2.791239340533632669442158497532521776093E3L,
```

```
8.989365571337319032943005387378993827684E2L,
   2.974016493766349409725385710897298069677E2L,
   6.148192754590376378740261072533527271947E1L,
   1.178502892490738445655468927408440847480E1L
   /* 1.0E0 */
  };
/* erf(x) = x + x P(x^2)/Q(x^2)
  0 \le x \le 7/8
  Peak relative error 1.8e-35 */
#define NTN1 8
static long double TN1[NTN1 + 1] =
   -3.858252324254637124543172907442106422373E10L,
   9.580319248590464682316366876952214879858E10L,
   1.302170519734879977595901236693040544854E10L,
   2.922956950426397417800321486727032845006E9L,
   1.764317520783319397868923218385468729799E8L,
   1.573436014601118630105796794840834145120E7L,
   4.028077380105721388745632295157816229289E5L,
   1.644056806467289066852135096352853491530E4L,
   3.390868480059991640235675479463287886081E1L
  };
#define NTD1 8
static long double TD1[NTD1 + 1] =
  {
    -3.005357030696532927149885530689529032152E11L,
   -1.342602283126282827411658673839982164042E11L,
   -2.777153893355340961288511024443668743399E10L,
   -3.483826391033531996955620074072768276974E9L,
   -2.906321047071299585682722511260895227921E8L,
   -1.653347985722154162439387878512427542691E7L,
   -6.245520581562848778466500301865173123136E5L,
   -1.402124304177498828590239373389110545142E4L,
   -1.209368072473510674493129989468348633579E2L
   };
static long double INFINITYL=1000.0;
#endif /* #if (defined _WIN32 || defined _MSC_VER || !de
```

```
fined HAVE ERFL) */
/*abs*/
long double polevll( long double x, void *PP, int n )
  register long double y;
  long double *P;
  P = (long double *) PP;
  y = *P++;
  do
      y = y * x + *P++;
  while( --n );
  return(y);
}
long double p1evll(long double x, void *PP, int n )
{
  register long double y;
  long double *P;
 P = (long double *) PP;
  n = 1;
  y = x + *P++;
  do
      y = y * x + *P++;
  while( --n );
  return( y );
long double neval (long double x, long double *p, int n)
  long double y;
  p += n;
  y = *p--;
  do
```

```
y = y * x + *p--;
 while (--n > 0);
 return y;
}
long double deval (long double x, long double *p, int n)
 long double y;
 p += n;
 y = x + *p--;
 do
     y = y * x + *p--;
 while (--n > 0);
 return y;
}
#if (defined _WIN32 || defined _MSC_VER || !defined HAVE_
    ERFL)
long double erfl(long double x);
long double erfcl(long double a)
  long double x, y=0., z;
 int i;
  if( a == INFINITYL )
   return(0.0L);
  if( a == -INFINITYL )
   return(2.0L);
  if(a < 0.0L)
    x = -a;
  else
   x = a;
  if(x < 0.25L)
```

```
return( 1.0L - erfl(a) );
if (x < 1.25L)
    i = int(8.0 * x);
    switch (i)
      case 2:
        z = x - 0.25L;
        y = C13b + z * neval (z, RNr13, NRNr13) / deval (
  z, RDr13, NRDr13);
        y += C13a;
       break;
      case 3:
        z = x - 0.375L;
        y = C14b + z * neval (z, RNr14, NRNr14) / deval (
  z, RDr14, NRDr14);
        y += C14a;
        break;
      case 4:
        z = x - 0.5L;
        y = C15b + z * neval (z, RNr15, NRNr15) / deval (
  z, RDr15, NRDr15);
        y += C15a;
        break;
      case 5:
        z = x - 0.625L;
        y = C16b + z * neval (z, RNr16, NRNr16) / deval (
  z, RDr16, NRDr16);
        y += C16a;
       break;
      case 6:
        z = x - 0.75L;
        y = C17b + z * neval (z, RNr17, NRNr17) / deval (
  z, RDr17, NRDr17);
        y += C17a;
        break;
      case 7:
        z = x - 0.875L;
        y = C18b + z * neval (z, RNr18, NRNr18) / deval (
  z, RDr18, NRDr18);
```

```
y += C18a;
        break;
      case 8:
        z = x - 1.0L;
        y = C19b + z * neval (z, RNr19, NRNr19) / deval (
  z, RDr19, NRDr19);
        y += C19a;
        break;
      case 9:
        z = x - 1.125L;
        y = C20b + z * neval (z, RNr20, NRNr20) / deval (
  z, RDr20, NRDr20);
        y += C20a;
        break;
      }
    if(a < 0.0L)
      y = 2.0L - y;
    return y;
z = -a * a;
if(z < -MAXLOGL)
    if(a < 0)
      return( 2.0L );
    else
      return( 0.0L );
  }
y = \exp(-a*a) * erfcel (x);
if(a < 0.0L)
 y = 2.0L - y;
if(y == 0.0L)
  {
    if(a < 0)
      return( 2.0L );
    else
```

```
return( 0.0L );
 return y;
long double erfl(long double x)
 long double a, y, z;
  if(x == 0.0L)
   return(x);
  if(x == -INFINITYL)
    return(-1.0L);
  if(x == INFINITYL)
   return(1.0L);
  a = abs(x);
  if(a > 1.0L)
   return( 1.0L - erfcl(x) );
 z = x * x;
  if (a < 0.875)
      y = a + a * neval (z, TN1, NTN1) / deval (z, TD1, NT
   D1);
   }
  else
    {
      a = a - 1.0L;
      y = erf_const + neval (a, TN2, NTN2) / deval (a, TD2,
    NTD2);
    }
  if (x < 0)
   y = -y;
 return( y );
#endif /* (defined WIN32 || defined MSC VER || !defined
    HAVE_ERFL) */
```

```
long double erfcel(long double x)
  long double p,y,z;
  int i;
  z = 1.0L/(x*x);
  i = int(8.0 / x);
  switch (i)
    {
    default:
    case 0:
      p = neval (z, RNr1, NRNr1) / deval (z, RDr1, NRDr1);
      break;
    case 1:
      p = neval (z, RNr2, NRNr2) / deval (z, RDr2, NRDr2);
      break;
    case 2:
      p = neval (z, RNr3, NRNr3) / deval (z, RDr3, NRDr3);
      break;
    case 3:
      p = neval (z, RNr4, NRNr4) / deval (z, RDr4, NRDr4);
      break;
    case 4:
      p = neval (z, RNr5, NRNr5) / deval (z, RDr5, NRDr5);
      break;
    case 5:
      p = neval (z, RNr6, NRNr6) / deval (z, RDr6, NRDr6);
     break;
    case 6:
      p = neval (z, RNr7, NRNr7) / deval (z, RDr7, NRDr7);
      break;
    case 7:
      p = neval (z, RNr8, NRNr8) / deval (z, RDr8, NRDr8);
      break;
    }
  y = p / x;
  return(y);
}
```

long double cumnorm(long double a)

```
long double x, y, z;
  x = a * SQRTHL;
  z = abs(x);
  if(z < 0.25L)
    y = 0.5L + 0.5L * erfl(x);
  else if (z < 1.25)
      y = 0.5L * erfcl(z);
      if (x > 0)
        y = 1.0L - y;
    }
  else
    {
      y = 0.5L * (erfcel(z));
      z = expl(-a*a);
      y = y * sqrtl(z);
      if(x > 0.0L)
        y = 1.0L - y;
    }
  return(y);
}
//fonction Hh0
long double Hh0(const long double& x)
  return sqrtl(2.0L*M_PI)*(cumnorm(-x));
//fonctions qui retourne le vecteur des n premiers fonctio
std::vector<long double> Hhn(const long double& x,const
    int& n)
  std::vector<long double> Hhv(n);
  long double H1, H2;
  int i;
  if(n>=1)
    {
```

```
Hhv[0]=Hh0(x);
      H1=Hh(x);
      H2=Hhv[0];
      for(i=1;i<n;i++)
          Hhv[i]=(H1-x*H2)/(double)i;
          H1=H2;
          H2=Hhv[i];
          if(Hhv[i]<0)
            {
              Hhv[i]=0;
              H1=0;
              H2=0;
            }
        }
      return Hhv;
    }
  else
    {
      //printf("Fonction long double *Hhn : l'argument 2
    doit Ãłtre > 0 {n");
      exit(0);
}
//fonction I-1
long double I(const long double& c,const long double& alpha
    ,const long double&beta, const long double& delta)
  long double cst=0.;
  if(alpha!=0 && beta!=0)
    cst=expl(alpha*delta/beta+alpha*alpha/(2*beta*beta))/
    beta;
  if(beta>0 && alpha!=0)
    return cst*Hh0(beta*c-delta-alpha/beta);
  if(beta<0 && alpha<0)</pre>
    return -cst*Hh0(-beta*c+delta+alpha/beta);
  if(beta>0 && alpha==0)
    return Hh0(-delta+beta*c)/beta;
 printf("Fonction long double I, parametres incorrects {n"
```

```
);
  exit(0);
}
//fonction IO
long double IO(const long double& c,const long double& alp
    ha, const long double&beta, const long double& delta)
  long double x, y, h, cst=0.0,cst3=0.0;
 h=beta/alpha;
  x=beta*c-delta;
  y=x-1/h;
  if(alpha!=0 && beta!=0)
      cst=expl(alpha*delta/beta+alpha*alpha/(2*beta*beta))/
      cst3=-expl(alpha*c)/alpha;
  if(beta>0 && alpha!=0)
    {
      return cst3*Hh0(x)+h*cst*Hh0(y);
  if(beta<0 && alpha<0)
    {
      return cst3*Hh0(x)-h*cst*Hh0(-y);
  if(beta>0 && alpha==0)
      return (Hh(x)-x*Hh0(x))/beta;
 printf("Fonction long double IO, parametres incorrects {
   n");
  exit(0);
//fonction qui retourne le vecteur des n premiers fonctions
std::vector<long double> In(const long double& c,const lon
    g double& alpha, const
                            long double& beta, const long
    double& delta, const int& Nb)
{
```

```
long double x, y, h, cst=0.0,cst3=0.0;
std::vector<long double> Hhv, Iv;
int n;
h=beta/alpha;
x=beta*c-delta;
y=x-1/h;
Iv.resize(Nb);
if(alpha!=0 && beta!=0)
    cst=expl(alpha*delta/beta+alpha*alpha/(2*beta*beta))/
  beta;
    cst3=-expl(alpha*c)/alpha;
  }
if(beta>0 && alpha!=0)
    Hhv.resize(Nb);
    Hhv=Hhn(x,Nb);
    Iv[0]=cst3*Hhv[0]+h*cst*Hh0(y);
    if([v[0]<0)
      for(int i=0;i<Nb;i++)</pre>
           Iv[i]=0.0;
    for(n=1;n<Nb;n++)
        Iv[n]=h*Iv[n-1]+cst3*Hhv[n];
        if(Iv[n]<0)
           for(int i=n;i<Nb;i++)</pre>
               Iv[i]=0.0;
             }
      }
    return Iv;
if(beta<0 && alpha<0)</pre>
  {
    Hhv.resize(Nb);
```

```
Hhv=Hhn(x,Nb);
      Iv[0]=cst3*Hhv[0]-h*cst*Hh0(-y);
      if([v[0]<0)
        for(int i=0;i<Nb;i++)</pre>
            Iv[i]=0.0;
      for(n=1;n<Nb;n++)
          Iv[n]=h*Iv[n-1]+cst3*Hhv[n];
          if(Iv[n]<0)
            for(int i=n;i<Nb;i++)</pre>
              {
                Iv[i]=0.0;
        }
      return Iv;
  if(beta>0 && alpha==0)
      Hhv.resize(Nb+1);
      Hhv=Hhn(x,Nb+1);
      for(n=0;n<Nb;n++)
        {
          Iv[n]=Hhv[n+1]/beta;
        }
      return Iv;
  printf("Fonction long double In : parametres non valides
    {n");
 exit(0);
//fonction qui retourne le vecteur des n premiers fonctions
     derivÃl's de In % a sa premiÃlre variable
std::vector<long double> dIn(const long double& c,const lon
    g double& alpha, const
                              long double& beta, const long
    double& delta, const int& Nb)
{
  long double s, x, y, h, cst=0.0L,cst3=0.0L;
```

```
std::vector<long double> Hhv, Iv;
int i,k;
h=beta/alpha;
x=beta*c-delta;
y=x-1/h;
Iv.resize(Nb);
if(alpha!=0 && beta!=0)
    cst=(sqrtl(2*M_PI)/beta)*expl(alpha*delta/beta+alpha*
  alpha/(2*beta*beta));
    cst3=-expl(alpha*c);
if(beta>0 && alpha!=0)
    Hhv.resize(Nb);
    Hhv=Hhn(x,Nb);
    for(k=0;k<Nb;k++)
      {
        Iv[k]=0.0L;
        for(i=0;i<=k;i++)
            Iv[k]=Iv[k]+powl(h,k-i)*Hhv[i];
          }
        s=0.0L;
        for(i=1;i<=k;i++)
            s=s+powl(h,k-i)*Hhv[i-1];
          }
        s=s+Hh(x)*powl(h,k);
        Iv[k]=cst3*Iv[k]-cst3*h*s-beta*powl(h,k+1)*cst*dn
  orm(-y);
      }
    return Iv;
if(beta<0 && alpha<0)</pre>
    Hhv.resize(Nb);
    Hhv=Hhn(x,Nb);
    for(k=0;k<Nb;k++)</pre>
      {
        Iv[k]=0.0L;
```

```
for(i=0;i<=k;i++)
              Iv[k]=Iv[k]+powl(h,k-i)*Hhv[i];
            }
          s=0.0L;
          for(i=1;i<=k;i++)
              s=s+powl(h,k-i)*Hhv[i-1];
          s=s+Hh(x)*powl(h,k);
          Iv[k]=cst3*Iv[k]-cst3*h*s-beta*powl(h,k+1)*cst*dn
    orm(y);
      return Iv;
  if(beta>0 && alpha==0)
      Hhv.resize(Nb);
      Hhv=Hhn(x,Nb);
      for(k=0;k<Nb;k++)
        Iv[k] = -Hhv[k];
      return Iv;
  printf("Fonction long double In : parametres non valides
    {n");
  exit(0);
//fonction factorielle
unsigned long long int fact_dia(const int & n)
  if(n==0)
    return 1;
  if(n==1)
    return 1;
  if(n>1)
    return n*fact_dia(n-1);
  printf("Fonction int fact(const int & n) : parametre non
    valide {n");
  exit(0);
}
//coefficients binomiaux
```

```
unsigned long long int bin_dia(const int& n,const int& k)
{
  if(n>=0 && n<k)
    return 0;
  if(n>=0 && n==k)
    return 1;
  if(n>=0 && n>=k)
    {
     return fact_dia(n)/(fact_dia(k)*fact_dia(n-k));
    }
  else return 0;
  printf("Fonction long double bin(const int& n,const int& k): parametres non valides {n" );
}
#endif //PremiaCurrentVersion
```

References