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**bns**

## 1 Description

Come from [\[1\]](#).

The square volatility follows the SDE of the form :

$$d\sigma_t^2 = -\lambda\sigma_t^2 dt + dz_{\lambda t}$$

where  $\lambda > 0$  and  $z$  is a subordinator. The risk neutral dynamic of the log price  $x - t = \log S_t$  are given by

$$dW_t = (r - q - \lambda k(-\rho) - \sigma^2/2)dt + \sigma_t dW_t + \rho dz_t, \quad x_0 = \log(S_0).$$

where  $k(u) = \log E \exp -uz_1$ . Choice  $z_t$  as a compound poisson process,

$$z_t = \sum_{n=1}^{N_t} x_n$$

where  $N_t$  is a Poisson process with intensity parameter  $\alpha$  and each  $x_n$  follows an exponential law with mean  $\frac{1}{\beta}$ . One can show that the process  $\sigma_t^2$  is a stationary process with a marginal law that follows a Gamma distribution with mean  $\alpha$  and variance  $\frac{\alpha}{\beta}$ . In this case,

$$k(u) = \frac{-au}{b+u}.$$

## 2 Code Implementation

```
#ifndef _BNS_H
#define _BNS_H

#include "optype.h"
#include "var.h"
```

```
#define TYPEMOD BNS

typedef struct TYPEMOD {
    VAR T;
    VAR S0;
    VAR Divid;
    VAR R;
    VAR Sigma0;
    VAR Lambda;
    VAR Rho;
    VAR Beta;
    VAR Alpha;
} TYPEMOD;

#endif
```

## References

- [1] Ole E. Barndorff-Nielsen and Neil Shephard. Non-Gaussian Ornstein-Uhlenbeck-based models and some of their uses in financial economics. *J. R. Stat. Soc. Ser. B Stat. Methodol.*, 63(2):167–241, 2001. 1