

Help

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#include <stdlib.h>
#include "bs2d_std2d.h"
#include "enums.h"

static int d=2;
static int l=1;
static long N_sim;
static double **X,**W,**Dw,**ln,**Z,*P,*Pn,*Qn,*Semi,*Obst,
               *P2,**Delta;
static double *drift,*diff_z;
static double *s,**sigma,*divid,**sigma_inv,**sigma_transf;

static void memory_allocation()
{
    int i;

    sigma=(double **)calloc(d,sizeof(double *));
    for (i=0;i<d;i++)
        sigma[i]=(double *)calloc(d,sizeof(double));

    sigma_inv=(double **)calloc(d,sizeof(double *));
    for (i=0;i<d;i++)
        sigma_inv[i]=(double *)calloc(d,sizeof(double));

    sigma_transf=(double **)calloc(d,sizeof(double *));
    for (i=0;i<d;i++)
        sigma_transf[i]=(double *)calloc(d,sizeof(double));

    s= malloc((d)*sizeof(double));
    divid= malloc((d)*sizeof(double));
    drift= malloc((d)*sizeof(double));
    diff_z= malloc((d)*sizeof(double));

    X=(double **)calloc(d,sizeof(double *));
    for (i=0;i<d;i++)
        X[i]=(double *)calloc(N_sim,sizeof(double));

    W=(double **)calloc(d,sizeof(double *));
    for (i=0;i<d;i++)
        W[i]=(double *)calloc(N_sim,sizeof(double));

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Dw=(double **)calloc(d,sizeof(double *));
for (i=0;i<d;i++)
    Dw[i]=(double *)calloc(N_sim,sizeof(double));

ln=(double **)calloc(d,sizeof(double *));
for (i=0;i<d;i++)
    ln[i]=(double *)calloc(N_sim,sizeof(double));

Z=(double **)calloc(d,sizeof(double *));
for (i=0;i<d;i++)
    Z[i]=(double *)calloc(N_sim,sizeof(double));

Delta=(double **)calloc(d,sizeof(double *));
for (i=0;i<d;i++)
    Delta[i]=(double *)calloc(N_sim,sizeof(double));

Pn= malloc((N_sim)*sizeof(double));
Qn= malloc((N_sim)*sizeof(double));
P= malloc((N_sim)*sizeof(double));
P2= malloc((N_sim)*sizeof(double));
Semi= malloc((N_sim)*sizeof(double));
Obst= malloc((N_sim)*sizeof(double));

return;
}

/*Memory Desallocation*/
static void free_memory()
{
    int i;

    for (i=0;i<d;i++)
        free(Delta[i]);
    free(Delta);

    for (i=0;i<d;i++)
        free(sigma[i]);
    free(sigma);

    for (i=0;i<d;i++)

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    free(sigma_inv[i]);
    free(sigma_inv);

    for (i=0;i<d;i++)
        free(sigma_transf[i]);
    free(sigma_transf);

    for (i=0;i<d;i++)
        free(X[i]);
    free(X);

    for (i=0;i<d;i++)
        free(W[i]);
    free(W);

    for (i=0;i<d;i++)
        free(Z[i]);
    free(Z);

    for (i=0;i<d;i++)
        free(Dw[i]);
    free(Dw);

    for (i=0;i<d;i++)
        free(ln[i]);
    free(ln);

    free(divid);
    free(drift);
    free(s);
    free(diff_z);

    free(Pn);
    free(Qn);
    free(P);
    free(P2);
    free(Semi);
    free(Obst);

    return;
}
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static double H(double x)
{
    double val;

    if (x>=0.) val=1.;
    else val=0.;

    return val;
}

static double g1(double x,double lambda)
{
    double val;

    val=0.5*lambda*exp(-lambda*fabs(x));

    return val;
}

static double GH1(double x,double lambda)
{
    double val;

    if (x<0.) val=0.5*exp(lambda*x);
    else val=1-0.5*exp(-lambda*x);

    return val;
}

static int LionsRegnier2DMC(double s1, double s2, NumFunc_2
    *p, double t, double r, double divid1, double divid2,
    double sigma1, double sigma2, double rho, long N, int
    a1, double *ptdelta2)
{
    int simulation_dim= 1,/*fermeture=1,*/init_mc;
    int i,j,k,jz,TimeIndex,n,ii;
    double eps,sum,sum1,sum2,eps2,att,semi0,c_price,c_delta1,
        c_delta2,delta1,delta2;
    double val,tmp1,tmp2;

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generator, int exe

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double prod1,prod2,lambda1[10],lambda2[10],K,prodT,prodT1
    ,prodT_tot,prodT1_tot,prodR,prodR1,sumT,sumT1,sumR,sumR1,
    sumTD,lambdaT,lambdaT1,lambdaR,lambdaR1;

K=p->Par[0].Val.V_DOUBLE;
N_sim=N;
n=exercise_date_number;

/* MC sampling */
init_mc= pnl_rand_init(generator, simulation_dim,N);

/* Test after initialization for the generator */
if(init_mc == OK)
{

    memory_allocation();
    eps=t/(double)n;
    eps2=SQR(eps);
    att=exp(-r*eps);

    /* Covariance Matrix */
    /* Coefficients of the matrix A such that A(tA)=Gam
ma */
    sigma[0][0]= sigma1;
    sigma[0][1]= 0.0;
    sigma[1][0]= rho*sigma2;
    sigma[1][1]= sigma2*sqrt(1.0-SQR(rho));

    /*Sigma Transformed*/
    for (i=0;i<d;i++)
for (j=0;j<d;j++)
    sigma_transf[i][j]=sigma[i][j]/sigma[j][j];

    /*Inverse of Sigma Transformed sub-triangular */
    for (i=0;i<d;i++)
sigma_inv[i][i]=1.;

    for (j=0;j<d;j++)
{
    for (i=j+1;i<d;i++)

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    {
        sum=0.;
        for (k=j;k<i;k++)
sum+=sigma_transf[i][k]*sigma_inv[k][j];
        sigma_inv[i][j]=-sum;
    }
}

/*Drift,Diffusion*/
s[0]=s1;
s[1]=s2;
divid[0]=divid1;
divid[1]=divid2;

    for (i=0;i<d;i++) {
sum1=0.;
sum2=0.;
for (j=0;j<=i;j++)
    {
        sum1+=SQR(sigma[i][j]);
        sum2+=sigma[i][j];
    }
drift[i]=(r-divid[i]-0.5*sum1)*eps;
diff_z[i]=sqrt(eps)*sigma[i][i];
    }

/*Brownian motion at the end*/
for (i=0;i<d;i++)
for (j=0;j<N;j++)
    W[i][j]=pnl_rand_normal(generator)*sqrt(t);

/*Final Stock*/
for (i=0;i<d;i++)
{
    for (j=0;j<N;j++)
    {
        sum=0.;
        for (k=0;k<=i;k++)
        {
            sum+=sigma[i][k]*W[k][j];
        }
    }
}

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        X[i][j]=s[i]*exp(drift[i]*(double)n+sum);
    }
}

/*Final Price*/
for (j=0;j<N;j++)
Pn[j]=0.0;

/*Backward Cycle*/
for (TimeIndex=n-1;TimeIndex>0;TimeIndex--)
{
    tmp1=(double)(TimeIndex)/(double)(TimeIndex+1);
    tmp2=sqrt(tmp1*eps);

/*X,ln,Z,DW*/
    for (i=0;i<d;i++)
    {
        for (j=0;j<N;j++)
        {
            sum=0.;
            val=W[i][j];
            W[i][j]=W[i][j]*tmp1+tmp2*pn1_rand_normal(    generator);
            for (k=0;k<=i;k++)
            {
                sum+=sigma[i][k]*W[k][j];
            }

/*X*/
            X[i][j]=s[i]*exp(drift[i]*(double)TimeIndex+sum);

/*ln*/
            if(l==0)
                ln[i][j]=0.;
            else
            {
                if (i==0)
                    ln[0][j]=0.;
                else
                {
                    sum1=0.;
                    for (k=0;k<i;k++)

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        sum1+=sigma_inv[i][k]*
            (drift[k]*eps-(1./(eps*(double)(TimeIndex)))
*log(X[k][j]/s[k]));
        ln[i][j]=sum1;
    }
}
/*Z*/
Z[i][j]=s[i]*exp((double)TimeIndex*drift[i]+ln[i][
j]*(double)TimeIndex*eps+sigma[i][i]*W[i][j]);

/*Dw*/
Dw[i][j]=eps*W[i][j]-(val-W[i][j])*((double)TimeInd
ex*eps)
+eps2*(double)TimeIndex*sigma[i][i];
}
}
for (i=0;i<d;i++)
{
    lambda1[i]=1./sqrt(eps*(double)TimeIndex);
    lambda2[i]=1./sqrt(eps*(double)TimeIndex);
}

/*P,Semi*/
for (j=0;j<N;j++)
{
    PutMinAn(X[0][j],X[1][j],K,t-(double)TimeIndex*ep
s,r,divid[0],divid[1],sigma1,sigma2,rho,&c_price,&c_delta1,
&c_delta2);
    Obst[j]=(p->Compute)(p->Par,X[0][j],X[1][j])-c_
price;

    sum1=0.;
    sum2=0.;
    for(jz=0;jz<N;jz++)
    {
        prod1=1.;
        prod2=1.;
        for (i=0;i<d;i++)
        {
            prod1*=g1(Z[i][jz]-Z[i][j],lambda1[i])+(H(Z[i][
jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambda1[i]))*(Dw[i][jz]/

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Z[i][jz])*(1./(sigma[i][i]*eps2*(double)TimeIndex));
    prod2*=g1(Z[i][jz]-Z[i][j],lambda2[i])+(H(Z[i][
jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambda2[i]))*(Dw[i][jz]/
Z[i][jz])*(1./(sigma[i][i]*eps2*(double)TimeIndex));
    }

    sum1+=prod1*Pn[jz];
    sum2+=prod2;
}

    Semi[j]=sum1/sum2;

    /*Options Values*/
    P[j]=MAX(Obst[j],att*Semi[j]);

    if(TimeIndex==2)
{
    P2[j]=P[j];
}

    if(TimeIndex==1)
{

    if( P[j]==Obst[j])
    {
        PutMinAn(X[0][j],X[1][j],K,t-(double)TimeIndex*
eps,r,divid[0],divid[1],sigma1,sigma2,rho,&c_price,&c_delt
a1,&c_delta2);

        if((Z[0][j]<Z[1][j]))
        {
            Delta[0][j]=-H(K-MIN(Z[0][j],Z[1][j]))-c_delta1;
            Delta[1][j]=-c_delta2;
        }
        else
        if((Z[1][j]<Z[0][j]))
        {
            Delta[1][j]=-H(MIN(K-Z[0][j],Z[1][j]))-c_delt
a2;
            Delta[0][j]=-c_delta1;
        }
    }
}

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    }
else
{
    for (i=0;i<d;i++)
    {
        lambdaT1=1./sqrt(eps*(double)TimeIndex);
        lambdaT=1./sqrt(eps*(double)TimeIndex);
        lambdaR1=1./sqrt(eps*(double)TimeIndex);
        lambdaR=1./sqrt(eps*(double)TimeIndex);

        sumT=0.;
        sumT1=0.;
        sumTD=0.;
        sumR=0.;
        sumR1=0.;
        for(jz=0;jz<N;jz++)
        {
            prodT_tot=1.;
            prodT1_tot=1.;
            for (ii=0;ii<d;ii++)
            {
                prodT_tot*=g1(Z[ii][jz]-Z[ii][j],lambdaT)+(H(
Z[ii][jz]-Z[ii][j])-GH1(Z[ii][jz]-Z[ii][j],lambdaT))*(Dw[ii
][jz]/Z[ii][jz])*(1./(sigma[ii][ii]*eps2*(double)TimeInd
ex)));
                prodT1_tot*=g1(Z[ii][jz]-Z[ii][j],lambdaT1)+(
H(Z[ii][jz]-Z[ii][j])-GH1(Z[ii][jz]-Z[ii][j],lambdaT1))*(Dw
[ii][jz]/Z[ii][jz])*(1./(sigma[ii][ii]*eps2*(double)
TimeIndex)));
            }

            prodT=g1(Z[i][jz]-Z[i][j],lambdaT)+(H(Z[i][
jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambdaT))*(Dw[i][jz]/Z[i
][jz])*(1./(sigma[i][i]*eps2*(double)TimeIndex)));

            prodT1=g1(Z[i][jz]-Z[i][j],lambdaT1)+(H(Z[i]
[jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambdaT1))*(Dw[i][jz]/
Z[i][jz])*(1./(sigma[i][i]*eps2*(double)TimeIndex)));

            prodR=-g1(Z[i][jz]-Z[i][j],lambdaR)*(Dw[i][

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    jz]/Z[i][jz))*(1./(sigma[i][i]*eps2*(double)TimeIndex))-(H(
    Z[i][jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambdaR))*(1./(sigma
    [i][i]*eps2*(double)TimeIndex))*(1./SQR(Z[i][jz]))*(SQR(Dw
    [i][jz))*(1./(sigma[i][i]*eps2*(double)TimeIndex))+Dw[i][
    jz]-((double)TimeIndex*eps/sigma[i][i]));

    prodR1=-g1(Z[i][jz]-Z[i][j],lambdaR1)*(Dw[i]
    [jz]/Z[i][jz))*(1./(sigma[i][i]*eps2*(double)TimeIndex))-(
    H(Z[i][jz]-Z[i][j])-GH1(Z[i][jz]-Z[i][j],lambdaR1))*(1./(si
    gma[i][i]*eps2*(double)TimeIndex))*(1./SQR(Z[i][jz]))*(SQR(
    Dw[i][jz))*(1./(sigma[i][i]*eps2*(double)TimeIndex))+Dw[i][
    jz]-((double)TimeIndex*eps/sigma[i][i]));

    sumT+=prodT_tot*P2[jz];
    sumT1+=prodT1;

    sumR+=prodR*(prodT_tot/prodT)*P2[jz];
    sumR1+=prodR1;
    sumTD+=prodT1_tot;

    }
    Delta[i][j]=att*(sumR*sumT1-sumT*sumR1)/(sumT1*
    sumTD);
    }
    }
}
}

for (j=0;j<N;j++)
    Pn[j]=P[j];
}

/*Final Step*/
PutMinAn(s[0],s[1],K,t,r,divid[0],divid[1],sigma1,si
gma2,rho,&c_price,&c_delta1,&c_delta2);
sum=0.;
for (jz=0;jz<N;jz++)
sum+=Pn[jz];

semi0=sum/(double)N;

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        sum=0.;
        sum1=0.;
        for (jz=0;jz<N;jz++)
        {
            sum+=Delta[0][jz];
            sum1+=Delta[1][jz];
        }

        delta1=sum/(double)N+c_delta1;
        delta2=sum1/(double)N+c_delta2;

        *ptprice=MAX((p->Compute)(p->Par,s1,s2)-c_price,att*
semi0)+c_price;
        *ptdelta1=delta1;
        *ptdelta2=delta2;
    }

    free_memory();
    return init_mc;
}

int CALC(MC_LionsRegnier2D)(void *Opt, void *Mod, Pricing
    Method *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r,divid1,divid2;

    r= log(1.+ptMod->R.Val.V_DOUBLE/100.);
    divid1= log(1.+ptMod->Divid1.Val.V_DOUBLE/100.);
    divid2= log(1.+ptMod->Divid2.Val.V_DOUBLE/100.);

    return LionsRegnier2DMC(ptMod->S01.Val.V_PDOUBLE,
        ptMod->S02.Val.V_PDOUBLE,
        ptOpt->PayOff.Val.V_NUMFUNC_2,
        ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,
        r,
        divid1,
        divid2,
        ptMod->Sigma1.Val.V_PDOUBLE,
        ptMod->Sigma2.Val.V_PDOUBLE,

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        ptMod->Rho.Val.V_RGDOUBLE,
        Met->Par[0].Val.V_LONG,
        Met->Par[1].Val.V_ENUM.value,
        Met->Par[2].Val.V_INT,
        &(Met->Res[0].Val.V_DOUBLE),
        &(Met->Res[1].Val.V_DOUBLE),
        &(Met->Res[2].Val.V_DOUBLE));
    }

static int CHK_OPT(MC_LionsRegnier2D)(void *Opt, void *Mod)
{
    if ((strcmp( ((Option*)Opt)->Name,"PutMinimumAmer")==0) )
        return OK;

    return WRONG;
}

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;
        Met->Par[0].Val.V_LONG=1000;
        Met->Par[1].Val.V_ENUM.members=&PremiaEnumRNGs;
        Met->Par[1].Val.V_ENUM.value=0;
        Met->Par[2].Val.V_INT=10;

    }
    return OK;
}

PricingMethod MET(MC_LionsRegnier2D)=
{
    "MC_LionsRegnier2d",
    {"N iterations",LONG,{100},ALLOW},
    {"RandomGenerator",ENUM,{100},ALLOW},
    {"Number of Exercise Dates ",INT,{100},ALLOW},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},

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CALC(MC_LionsRegnier2D),  
  {"Price",DOUBLE,{100},FORBID},  
  {"Delta1",DOUBLE,{100},FORBID} ,  
  {"Delta2",DOUBLE,{100},FORBID},  
  {" ",PREMIA_NULLTYPE,{0},FORBID}},  
CHK_OPT(MC_LionsRegnier2D),  
CHK_mc,  
MET(Init)  
};
```

References