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Source | Model Presentation

fps2d

1 Description

We consider a two-factor stochastic volatility model (S_t, Y_t, Z_t) , where S_t is the underlying price, and Y_t and Z_t are correlated diffusion processes. Under the risk-neutral probability measure, the model is described by the following equations:

$$dS_{t} = rS_{t}dt + \sigma_{t}S_{t}dW_{t}^{S},$$

$$\sigma_{t} = f(Y_{t}, Z_{t}),$$

$$dY_{t} = \left(\alpha(m_{f} - Y_{t}) - \nu_{f}\sqrt{2\alpha}\mathbf{i}_{f}(Y_{t}, Z_{t})\right)dt$$

$$+\nu_{f}\sqrt{2\alpha}\left(\rho_{1}dW_{t}^{S} + \sqrt{1 - \rho_{1}2}dW_{t}^{Y}\right),$$

$$dZ_{t} = \left(\delta(m_{s} - Z_{t}) - \nu_{s}\sqrt{2\delta}\mathbf{i}_{s}(Y_{t}, Z_{t})\right)dt$$

$$+\nu_{s}\sqrt{2\delta}\left(\rho_{2}dW_{t}^{S} + \rho_{12}dW_{t}^{Y} + \sqrt{1 - \rho_{2}2 - \rho_{12}2}dW_{t}^{Z}\right).$$

Here (W_t^S, W_t^Y, W_t^Z) are independent standard Brownian motions, and the correlation coefficients ρ_1 , ρ_2 , and ρ_{12} satisfy $-1 < \rho_1 < 1$, $\rho_2 2 + \rho_{12} 2 < 1$ respectively.

2 Code Implementation

```
#ifndef _FPS2D_H
#define _FPS2D_H

#include "optype.h"
#include "var.h"
#include "error msg.h"
```

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#define TYPEMOD FPS2D

```
/*2D Fouque Papanicolau Sircar World*/
typedef struct TYPEMOD{
  VAR T;
  VAR SO;
  VAR Divid;
  VAR R;
  VAR InitialSlow;
  VAR InitialFast;
  VAR SigmaSlow;
  VAR SigmaFast;
  VAR MeanReversionSlow;
  VAR MeanReversionFast;
  VAR LongRunVarianceSlow;
  VAR LongRunVarianceFast;
  VAR Rho1;
  VAR Rho2;
  VAR Rho12;
} TYPEMOD;
```

#endif