

Help

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#include <stdlib.h>
#include "hw1d_std.h"
#include "pnl/pnl_cdf.h"
#include "enums.h"

/* Control Variables Kemna & Vorst Monte Carlo simulation
   for a Call or Put Fixed Asian option.
   In the case of Monte Carlo simulation, the program provides estimations for price and delta with a confidence interval.
   In the case of Quasi-Monte Carlo simulation, the program just provides estimations for price and delta. */

static double *m_Mu;

/* -----
   ----- */
/* Calculus of the average  $A'(T_0, T)$  and  $C'(T_0, T)$  of the asian option with one of the 3 different schemes
   One iteration of the Monte Carlo method called from the "FixedAsian_KemanVorst" function */
/* -----
   ----- */
static double gamma_step(int n, double a, double b)
{
    return a/(b+(double)n);
}

static double step(int n){
    return sqrt(log((double)n+1.)/6.)+1.;
}

static void Simul_StockAndAverage_RobbinsMonro(int generator, int step_number,
    double divid, double sigma0, double nu, double sigma2, double rho,
    NumFunc_1 *p)
{
    int RM=5000;
    int sig_iter=0;
    double S_t, g1, g2, K;

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double h = T / step_number;
double sqrt_h = sqrt(h), sqrt_rho = sqrt(1.-SQR(rho));
double trend= nu- 0.5 * SQR(sigma2);

int i,ii;
double dot1,a,b=1,payoff,payoffcarre,val_test,temp,expo,
    val;
double dot2;
double *NormalValue;
double *m_Theta;
double x_1=0.0925,x_2=0.725;
double V_t, value;
NormalValue = malloc(sizeof(double)*2*step_number*RM);
m_Theta= malloc(sizeof(double)*(2*(step_number+1)));
K=p->Par[0].Val.V_DOUBLE;
/* Average Computation */
/* Trapezoidal scheme */
/* Simulation of M gaussian variables according to the generator type,
    that is Monte Carlo or Quasi Monte Carlo. */

for(i=0;i<2*step_number;i++)
    m_Mu[i]=0.;

if ((p->Compute) == &Call)
{
    if(K==x)
a=0.01;
    else if(K<x)
a=0.001;
    else /*if(K>x)*/
a=5.;
}
else /*if ((p->Compute) == &Put)*/
{
    if(K==x)
a=0.1;
    else if(K<x)
a=5.;
    else /*if(K>x)*/
a=0.001;
}

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for(ii=0;ii<RM;ii++) {

    dot1=0.;
    dot2=0.;

    g1= pnl_rand_gauss(2*step_number, CREATE, 0,      generator);
    S_t=x;
    V_t=sigma0;
    for(i=0 ; i< step_number ; i++) {
        g1= pnl_rand_gauss(step_number, RETRIEVE, 2*i,      generator);
        NormalValue[i+ii*step_number]=g1;
        S_t*=(1+(r-divid)*h + sqrt(V_t)*sqrt_h*g1);

        g2= pnl_rand_gauss(step_number, RETRIEVE, (2*i)+1,      generator);
        NormalValue[i+(ii+RM)*step_number]=g2;
        dot1+=g1*m_Mu[i]+g2*m_Mu[i+step_number];
        dot2+=m_Mu[i]*m_Mu[i]+m_Mu[i+step_number]*m_Mu[i+step
_number];
        value=rho*g1+sqrt_rho*g2;
        V_t=V_t*exp(trend*h+sigma2*sqrt_h*value);
        V_t=MIN(V_t,2.0);

    }

    payoff=exp(-r*T)*(p->Compute)(p->Par,S_t);
    payoffcarre=payoff*payoff;
    expo=exp(-dot1+0.5*dot2);
    val_test=0.;

    for(i=0 ; i< step_number ; i++) {
        val=NormalValue[i+ii*step_number];
        temp=(m_Mu[i]-val)*expo*payoffcarre;
        m_Theta[i]=temp;
        val=NormalValue[i+(ii+RM)*step_number];
        temp=(m_Mu[i+step_number]-val)*expo*payoffcarre;
        m_Theta[i+step_number]=temp;
        val_test+=SQR(m_Mu[i]-gamma_step(ii,a,b)*m_Theta[i])+
SQR(m_Mu[i+step_number]-gamma_step(ii,a,b)*m_Theta[i+step
number]);
    }
    val_test=sqrt(val_test);

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        if(val_test<=step(sig_itere)) {
            for(i=0;i<step_number;i++) {
m_Mu[i]=m_Mu[i]-gamma_step(ii,a,b)*m_Theta[i];
m_Mu[i+step_number]=m_Mu[i+step_number]-gamma_step(ii,a,
            b)*m_Theta[i+step_number];
            }
        }
        else {
            if(sig_itere-2*(sig_itere/2)==0)
for(i=0;i<step_number;i++){
            m_Mu[i]=x_1;
            m_Mu[i+step_number]=x_1;
        }
            else
for(i=0;i<step_number;i++){
            m_Mu[i]=x_2;
            m_Mu[i+step_number]=x_2;
        }
            sig_itere+=1;
        }
    }

    free(m_Theta);
    free(NormalValue);

    return;
}

static int MCRobbinsMonro(double s, NumFunc_1 *p, double
    t, double r, double divid, double sigma0,double nu,double
    sigma2,double rho, long nb, int M,int generator, double
    confidence, double *ptprice, double *ptdelta, double *pt
    error_price, double *pterror_delta , double *inf_price, double *
    sup_price, double *inf_delta, double *sup_delta)
{
    long i,ipath;
    double price_sample, delta_sample, mean_price, mean_delt
        a, var_price, var_delta;
    int init_mc;

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int simulation_dim;
double alpha, z_alpha,dot1,dot2; /* inc=0.001;*/
double *Normalvect;
double S_t,g1,g2;
double h = t /(double)M;
double sqrt_h = sqrt(h), sqrt_rho = sqrt(1.-SQR(rho));
int step_number=M;
double V_t, value;
double trend= nu- 0.5 * SQR(sigma2);

Normalvect= malloc(sizeof(double)*(2*(nb*step_number+1)))
;
m_Mu= malloc(sizeof(double)*50000);

/* Value to construct the confidence interval */
alpha= (1.- confidence)/2.;
z_alpha= pnl_inv_cdfnor(1.- alpha);

/*Initialisation*/
mean_price= 0.0;
mean_delta= 0.0;
var_price= 0.0;
var_delta= 0.0;

/* Size of the random vector we need in the simulation */
simulation_dim= M;

/* MC sampling */
init_mc= pnl_rand_init(generator, simulation_dim,nb);
/* Test after initialization for the generator */
if(init_mc == OK)
{

    /* Price */
    (void)Simul_StockAndAverage_RobbinsMonro(generator,
M, t, s,r, divid, sigma0,nu,sigma2,rho, p);

    dot2=0.0;
    for(i=0;i<step_number;i++)
dot2+=m_Mu[i]*m_Mu[i]+m_Mu[i+step_number]*m_Mu[i+step_

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number];

    for(ipath= 1;ipath<= nb;ipath++)
{
    /* Begin of the N iterations */

    g1= pnl_rand_gauss(step_number, CREATE, 0, generator);
    S_t=s;
    V_t=sigma0;
    for(i=0 ; i<step_number ; i++) {
        g1= pnl_rand_gauss(step_number, RETRIEVE, 2*i, generator);
        Normalvect[i+(ipath-1)*step_number]=g1;
        S_t*=(1+(r-divid)*h + sqrt(V_t)*sqrt_h*(g1+m_Mu[i]))
    ;
        g2= pnl_rand_gauss(step_number, RETRIEVE, (2*i)+1, generator);
        Normalvect[i+(ipath-1+nb)*step_number]=g2;
        value=rho*(g1+m_Mu[i])+sqrt_rho*(g2+m_Mu[i+step_number]);
    V_t=V_t*exp(trend*h+sigma2*sqrt_h*value);
    V_t=MIN(V_t,2.0);
    }

    dot1=0.;
    for(i=0;i<step_number;i++){
        dot1+=m_Mu[i]*Normalvect[i+(ipath-1)*step_number]+m_Mu[i+step_number]*Normalvect[i+(ipath-1+nb)*step_number];
    }

    price_sample=(p->Compute)(p->Par, S_t)*exp(-dot1-0.5*dot2);

    /* Delta */
    if(price_sample >0.0)
        delta_sample=(S_t/s)*exp(-dot1-0.5*dot2);
    else delta_sample=0.;

    /* Sum */
    mean_price+= price_sample;
    mean_delta+= delta_sample;

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    /* Sum of squares */
    var_price+= SQR(price_sample);
    var_delta+= SQR(delta_sample);
}

    /* End of the N iterations */

    /* Price estimator */
    *ptprice=(mean_price/(double)nb);
    *pterror_price= exp(-r*t)*sqrt(var_price/(double)nb-
SQR(*ptprice))/sqrt((double)nb-1);
    *ptprice= exp(-r*t)*(*ptprice);

    /* Price Confidence Interval */
    *inf_price= *ptprice - z_alpha*(pterror_price);
    *sup_price= *ptprice + z_alpha*(pterror_price);

    /* Delta estimator */
    *ptdelta=exp(-r*t)*(mean_delta/(double)nb);
    if((p->Compute) == &Put)
*ptdelta *= (-1);
    *pterror_delta= sqrt(exp(-2.0*r*t)*(var_delta/(
double)nb-SQR(*ptdelta)))/sqrt((double)nb-1);

    /* Delta Confidence Interval */
    *inf_delta= *ptdelta - z_alpha*(pterror_delta);
    *sup_delta= *ptdelta + z_alpha*(pterror_delta);
}

free(Normalvect);
free(m_Mu);

return init_mc;
}

int CALC(MC_RobbinsMonro_HullWhite)(void *Opt, void *Mod,
PricingMethod *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;

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TYPEMOD* ptMod=(TYPEMOD*)Mod;
double r,divid;

r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

return MCRobbinsMonro(ptMod->S0.Val.V_PDOUBLE,
    ptOpt->PayOff.Val.V_NUMFUNC_1,
    ptOpt->Maturity.Val.V_DATE-ptMod->T.Val.V_DATE,
    r,
    divid, ptMod->Sigma0.Val.V_PDOUBLE
    ,ptMod->Mean.Val.V_PDOUBLE,
    ptMod->Sigma.Val.V_PDOUBLE,
    ptMod->Rho.Val.V_PDOUBLE,
    Met->Par[0].Val.V_LONG,
    Met->Par[1].Val.V_INT,
    Met->Par[2].Val.V_ENUM.value,
    Met->Par[3].Val.V_PDOUBLE,
    &(Met->Res[0].Val.V_DOUBLE),
    &(Met->Res[1].Val.V_DOUBLE),
    &(Met->Res[2].Val.V_DOUBLE),
    &(Met->Res[3].Val.V_DOUBLE),
    &(Met->Res[4].Val.V_DOUBLE),
    &(Met->Res[5].Val.V_DOUBLE),
    &(Met->Res[6].Val.V_DOUBLE),
    &(Met->Res[7].Val.V_DOUBLE));

}

static int CHK_OPT(MC_RobbinsMonro_HullWhite)(void *Opt,
    void *Mod)
{
    /*Option* ptOpt=(Option*)Opt;
    TYPEOPT* opt=(TYPEOPT*)(ptOpt->TypeOpt);*/

    if ((strcmp( ((Option*)Opt)->Name,"CallEuro")==0)|| (strcmp
        mp( ((Option*)Opt)->Name,"PutEuro")==0))
        return OK;

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    /*if ((opt->EuOrAm).Val.V_BOOL==EURO)
        return OK;*/

    return WRONG;
}

static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    int type_generator;
    if ( Met->init == 0)
    {
        Met->init=1;

        Met->Par[0].Val.V_LONG=10000;
        Met->Par[1].Val.V_INT=100;
        Met->Par[2].Val.V_ENUM.value=0;
        Met->Par[2].Val.V_ENUM.members=&PremiaEnumMCRNGs;
        Met->Par[3].Val.V_DOUBLE= 0.95;

    }

    type_generator= Met->Par[2].Val.V_ENUM.value;

    if(pnl_rand_or_quasi(type_generator)==PNL_QMC)
    {
        Met->Res[2].Viter=IRRELEVANT;
        Met->Res[3].Viter=IRRELEVANT;
        Met->Res[4].Viter=IRRELEVANT;
        Met->Res[5].Viter=IRRELEVANT;
        Met->Res[6].Viter=IRRELEVANT;
        Met->Res[7].Viter=IRRELEVANT;

    }
    else
    {
        Met->Res[2].Viter=ALLOW;
        Met->Res[3].Viter=ALLOW;
        Met->Res[4].Viter=ALLOW;
    }
}
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        Met->Res[5].Viter=ALLOW;
        Met->Res[6].Viter=ALLOW;
        Met->Res[7].Viter=ALLOW;
    }
    return OK;
}

PricingMethod MET(MC_RobbinsMonro_HullWhite)=
{
    "MC_RobbinsMoro_HW",
    {"N iterations",LONG,{100},ALLOW},
    {"TimeStepNumber",LONG,{100},ALLOW},
    {"RandomGenerator",ENUM,{100},ALLOW},
    {"Confidence Value",DOUBLE,{100},ALLOW},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(MC_RobbinsMonro_HullWhite),
    {"Price",DOUBLE,{100},FORBID},
    {"Delta",DOUBLE,{100},FORBID} ,
    {"Error Price",DOUBLE,{100},FORBID},
    {"Error Delta",DOUBLE,{100},FORBID} ,
    {"Inf Price",DOUBLE,{100},FORBID},
    {"Sup Price",DOUBLE,{100},FORBID} ,
    {"Inf Delta",DOUBLE,{100},FORBID},
    {"Sup Delta",DOUBLE,{100},FORBID} ,
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(MC_RobbinsMonro_HullWhite),
    CHK_mc,
    MET(Init)
};

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References