

Help

```
#include "hes1d_std.h"
#include <pnl/pnl_mathtools.h>
#include <pnl/pnl_root.h>

#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <
    (2012+2) //The "#else" part of the code will be freely available after the (year of creation of this file + 2)
static int CHK_OPT(AP_SmallTime_ImpliedVolatility)(void *
    Opt, void *Mod)
{
    return NONACTIVE;
}
int CALC(AP_SmallTime_ImpliedVolatility)(void*Opt,void *
    Mod,PricingMethod *Met)
{
    return AVAILABLE_IN_FULL_PREMIA;
}
#else

//Calculating the implied volatility under Heston model for the short et long maturities
//This code is based on the works of Forde, Jacquier and Mijatovic
static double arctan(double y)
{
    double error = 0.000000000001;
    double inf = -0.5*M_PI;
    double sup = 0.5*M_PI;
    double res=0.0;
    double errorMethode = 1.0;

    while( (sup-inf >error) && errorMethode > error)
    {
        res = (sup+inf)/2.0 ;
        if(y > tan (res ))
            inf = res;
        else
            sup = res;
    }
}
```

```

        errorMethode = ABS(y- tan ( res ) );
    }
    return res;
}

//The Rate function. Used for the short maturity case
static double LambdaFunc(double kappa, double theta,
    double sigma, double rho,double v0,double p)
{
    double res;
    double Cot;

    Cot = cos(0.5*sigma*p*sqrt(1-rho*rho ) )/sin(0.5*sigma*p*
        sqrt(1-rho*rho ) );
    res= p*v0/( sigma*( sqrt(1-rho*rho ) *Cot-rho ) ) ;
    return res;
}

//The derivative of the Rate function
static double LambdaDerivee(double kappa, double theta,
    double sigma, double rho,double v0,double p)
{
    double res;
    double Cot;

    Cot = cos(0.5*sigma*p*sqrt(1-rho*rho ) )/sin(0.5*sigma*p*
        sqrt(1-rho*rho ) );
    res= v0/( sigma*( sqrt(1-rho*rho ) *Cot-rho ) ) +
    p*v0*(1-rho*rho )/( SQR( sqrt(1-rho*rho ) *Cot-rho ) * SQR(
        sin(0.5*sigma*p*sqrt(1-rho*rho ) ) ) );
    return res;
}

int ApIVSmallHeston(double S0,NumFunc_1 *Payoff, double T,
    double r, double div,double v0,double kappa,double theta,
    double sigma,double rho,double *implied_vol)
{
    double K;
    double x ;
    double p=0.0;
    double Lambda;

```

```

double Lambda1;
double p_plus=0.0, p_minus=0.0;
double sup, inf;
double Error = 0.0000000001;
double ErrorMethode = 1;

K=Payoff->Par[0].Val.V_PDDOUBLE;
x = log(K/S0);
if(rho<0)
{
    p_minus = arctan( sqrt( 1 -rho*rho )/rho )/( 0.5*sigma*sqrt(1-rho*rho ) );
    p_plus = (M_PI+arctan( sqrt( 1 -rho*rho )/rho ))/( 0.5*sigma*sqrt(1-rho*rho ) );
}
if(rho==0)
{
    p_minus = -M_PI/sigma ;
    p_plus = M_PI/sigma ;
}

if(rho>0)
{
    p_minus = (-M_PI+arctan( sqrt( 1 -rho*rho )/rho ))/( 0.5*sigma*sqrt(1-rho*rho ) );
    p_plus = arctan( sqrt( 1 -rho*rho )/rho )/( 0.5*sigma*sqrt(1-rho*rho ) );
}

if(x ==0)
    x = 0.00001;

//Legendre Transform of the Rate function function
inf = p_minus;
sup = p_plus;
while( (sup-inf)>Error && ErrorMethode > Error )
{
    p = (sup+inf)/2.0;

```

```

    Lambda1 = LambdaDerivee( kappa, theta, sigma, rho,
v0, p);

    if(Lambda1<x)
        inf = p;
    else
        sup =p;

    ErrorMethode = ABS(Lambda1-x);
}

Lambda = x*p- LambdaFunc( kappa, theta, sigma, rho,
v0, p);

/* Implied Volatility*/
*implied_vol=(ABS(x)/sqrt( 2.0*Lambda));

return OK;
}

int CALC(AP_SmallTime_ImpliedVolatility)(void *Opt, void *
Mod, PricingMethod *Met)
{
    TYPEOPT* ptOpt=(TYPEOPT*)Opt;
    TYPEMOD* ptMod=(TYPEMOD*)Mod;
    double r,divid;

    if(ptMod->Sigma.Val.V_PDDOUBLE==0.0)
    {
        Fprintf(TOSCREEN,"BLACK-SHOLES MODEL{n{n{n");
        return WRONG;
    }
    else
    {
        r=log(1.+ptMod->R.Val.V_DOUBLE/100.);
        divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);

        return ApIVSmallHeston(ptMod->S0.Val.V_PDDOUBLE,
                                ptOpt->PayOff.Val.V_NUMFUNC_1,
                                ptOpt->Maturity.Val.V_DATE-pt
Mod->T.Val.V_DATE,

```

```

        r,
        divid, ptMod->Sigma0.Val.V_PD0
    UBLE
        ,ptMod->MeanReversion.hal.V_
    PDOUBLE,
        ptMod->LongRunVariance.Val.V_
    PDOUBLE,
        ptMod->Sigma.Val.V_PDOUBLE,
        ptMod->Rho.Val.V_PDOUBLE,
        &(Met->Res[0].Val.V_DOUBLE)
    );
}

}

static int CHK_OPT(AP_SmallTime_ImpliedVolatility)(void *
    Opt, void *Mod)
{
    if ((strcmp(((Option*)Opt)->Name,"CallEuro")==0))

        return OK;
    return WRONG;
}

#endif //PremiaCurrentVersion
static int MET(Init)(PricingMethod *Met,Option *Opt)
{
    if ( Met->init == 0)
    {
        Met->init=1;
    }

    return OK;
}

PricingMethod MET(AP_SmallTime_ImpliedVolatility)=
{
    "AP_SmallTime_ImpliedVolatility",
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CALC(AP_SmallTime_ImpliedVolatility),
    {"Implied Volatility for Small-Time",DOUBLE,{100},FORBID

```

```
    },  
    {" ",PREMIA_NULLTYPE,{0},FORBID}},  
    CHK_OPT(AP_SmallTime_ImpliedVolatility),  
    CHK_ok,  
    MET(Init)  
};
```

References