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Help
#include <stdlib.h>
#include "merhes1d_pad.h"
#include "pnl/pnl basis.h"
#include "math/alfonsi.h"
#include "enums.h"
#if defined(PremiaCurrentVersion) && PremiaCurrentVersion <</pre>
     (2010+2) //The "#else" part of the code will be freely av
    ailable after the (year of creation of this file + 2)
static int CHK OPT(MC Am Asian Alfonsi LongstaffSchwartz B
    ates)(void *Opt, void *Mod)
{
 return NONACTIVE;
}
int CALC(MC_Am_Asian_Alfonsi_LongstaffSchwartz_Bates)(void
    *Opt, void *Mod, PricingMethod *Met)
  return AVAILABLE_IN_FULL_PREMIA;
}
#else
static int MC_Am_Asian_Alfonsi_LoSc(NumFunc_2 *p, double
    SO, double Maturity, double r, double divid, double VO,
    double k, double theta, double sigma, double rho, double mu_
    jump, double gamma2, double lambda, long NbrMCsimulation, int
    NbrExerciseDates, int NbrStepPerPeriod, int generator,
    int basis name, int DimApprox, double confidence, int flag
    cir, double *ptPriceAm, double *ptPriceAmError, double *pt
    InfPriceAm, double *ptSupPriceAm)
{
  int j, m, nbr_var_explicatives, init_mc;
  int flag_SpotPaths, flag_VarPaths, flag_AveragePaths;
  double continuation_value, discounted_payoff, S_t, V_t,
    A_t, mean_price, var_price, z_alpha;
  double discount step, discount, step, exercise date, euro
    pean_price, european_delta, V_mean;
  double *VariablesExplicatives;
  PnlMat *SpotPaths, *VarPaths, *AveragePaths, *Explicati
    veVariables;
```

```
PnlVect *DiscountedOptimalPayoff, *RegressionCoeffVect;
PnlBasis *basis;
european price = 0.;
european delta = 0.;
/* Value to construct the confidence interval */
z alpha= pnl inv cdfnor((1.+ confidence)/2.);
// Time step and discount factor.
step = Maturity / (double)(NbrExerciseDates-1);
discount step = exp(-r*step);
discount = exp(-r*Maturity);
/* We store Spot, Variance and Average*/
flag SpotPaths = 1;
flag VarPaths = 1;
flag_AveragePaths = 1;
// Number of explicatives variables
nbr var explicatives = 2;
basis = pnl_basis_create(basis_name, DimApprox, nbr_var_e
  xplicatives);
VariablesExplicatives = malloc(nbr_var_explicatives*size
  of(double));
ExplicativeVariables = pnl_mat_create(NbrMCsimulation, nb
  r_var_explicatives);
DiscountedOptimalPayoff = pnl vect create(NbrMCsimulatio
 n); // Payoff if following optimal strategy.
RegressionCoeffVect = pnl_vect_create(0); // Regression
  coefficient.
SpotPaths = pnl mat create(0, 0); // Matrix of the whole
  trajectories of the spot.
VarPaths = pnl_mat_create(0, 0); // Matrix of the whole
  trajectories of the variance.
AveragePaths = pnl_mat_create(0, 0); // Matrix of the wh
  ole trajectories of the average.
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```
init mc=pnl rand init(generator, NbrExerciseDates*NbrStep
 PerPeriod, NbrMCsimulation);
if (init_mc != OK) return init_mc;
// Simulation of the whole paths
BatesSimulation_Alfonsi(flag_SpotPaths, SpotPaths, flag_
  VarPaths, VarPaths, flag AveragePaths, AveragePaths, SO, Matu
  rity, r, divid, VO, k, theta, sigma, rho, mu_jump, gamma2,
  lambda, NbrMCsimulation, NbrExerciseDates, NbrStepPerPeriod,
   generator, flag_cir);
// At maturity, DiscountedOptimalPayoff = discounted payoff
exercise_date = Maturity;
for (m=0; m<NbrMCsimulation; m++)</pre>
    S t = MGET(SpotPaths, NbrExerciseDates-1, m); // Simu
  lated Value of the spot at the maturity T
    A_t = MGET(AveragePaths, NbrExerciseDates-1, m); //
  Simulated Value of the average at the maturity T
    LET(DiscountedOptimalPayoff, m) = discount * (p->
  Compute)(p->Par, S_t, A_t); // Discounted payoff
  }
for (j=NbrExerciseDates-2; j>=1; j--)
    /** Least square fitting **/
    exercise date -= step;
    discount /= discount_step;
    for (m=0; m<NbrMCsimulation; m++)</pre>
        V_t = MGET(VarPaths, j, m); // Simulated value of
   the variance at t=exercise date
        S_t = MGET(SpotPaths, j, m); // Simulated value
  of the spot at t=exercise_date
        A_t = MGET(AveragePaths, j, m); // Simulated val
  ue of the average at t=exercise date
        // Regression basis contains price and delta of
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european asian option (under Black-Scholes model) and their
s power.
      // As BS volatility, we take sqrt of expectation
of V(Maturity) knowing that V(exercise date)=V t.
      V mean = theta + (V t-theta)*exp(-k*(Maturity-exe
rcise date));
      Ap_FixedAsian_BlackScholes(S_t, A_t, exercise_da
te, p, Maturity, r, divid, sqrt(V mean), &european price, &
european delta);
      MLET(ExplicativeVariables, m, 0) = discount*euro
pean price/S0;
      MLET(ExplicativeVariables, m, 1) = discount*euro
pean_delta*S_t*sqrt(V_t)/S0;
  pnl basis fit ls(basis, Regression Coeff Vect, Explicati
veVariables, DiscountedOptimalPayoff);
  /** Dynamical programming equation **/
  for (m=0; m<NbrMCsimulation; m++)</pre>
      V t = MGET(VarPaths, j, m);
      S t = MGET(SpotPaths, j, m);
      A_t = MGET(AveragePaths, j, m);
      discounted payoff = discount * (p->Compute)(p->
Par, S t, A t);
      if (discounted_payoff>0.) // If the payoff is nul
1, the OptimalPayoff doesnt change.
          V_{mean} = theta + (V_{t-theta})*exp(-k*(Maturit))
y-exercise_date));
          Ap FixedAsian BlackScholes(S t, A t, exercis
e date, p, Maturity, r, divid, sqrt(V mean), &european
price, &european_delta);
          VariablesExplicatives[0] = discount*european
price/S0;
          VariablesExplicatives[1] = discount*european_
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delta*S t*sqrt(V t)/S0;
            continuation_value = pnl_basis_eval(basis,Reg
  ressionCoeffVect, VariablesExplicatives);
            if (discounted payoff > continuation value)
                LET(DiscountedOptimalPayoff, m) = discoun
  ted_payoff;
              }
          }
      }
  }
discount /= discount_step;
// At initial date, no need for regression, continuation
  value is just a plain expectation estimated with empirical
 mean.
continuation_value = pnl_vect_sum(DiscountedOptimalPayof
  f)/(double)NbrMCsimulation;
discounted_payoff = discount*(p->Compute)(p->Par, S0, S0)
/* Price */
mean_price = MAX(discounted_payoff, continuation_value);
/* Sum of squares */
var_price = SQR(pnl_vect_norm_two(DiscountedOptimalPayof
  f))/(double)NbrMCsimulation;
var_price = MAX(var_price, SQR(discounted_payoff)) - SQR(
 mean price);
/* Price estimator */
*ptPriceAm = mean price;
*ptPriceAmError = sqrt(var_price/((double)NbrMCsimulatio
  n-1));
/* Price Confidence Interval */
*ptInfPriceAm= *ptPriceAm - z alpha*(*ptPriceAmError);
*ptSupPriceAm= *ptPriceAm + z_alpha*(*ptPriceAmError);
```

```
free(VariablesExplicatives);
  pnl basis free (&basis);
 pnl_mat_free(&VarPaths);
 pnl mat free(&AveragePaths);
  pnl mat free(&SpotPaths);
  pnl mat free(&ExplicativeVariables);
  pnl vect free(&DiscountedOptimalPayoff);
  pnl_vect_free(&RegressionCoeffVect);
 return OK;
}
*Opt, void *Mod, PricingMethod *Met)
{
  TYPEOPT* ptOpt=(TYPEOPT*)Opt;
  TYPEMOD* ptMod=(TYPEMOD*)Mod;
  double T, t 0, T 0;
  double r, divid, time_spent, pseudo_strike, true_strike,
   pseudo_spot;
  int return value;
  Met->Par[1].Val.V INT = MAX(2, Met->Par[1].Val.V INT); //
    At least two exercise dates.
  r=log(1.+ptMod->R.Val.V DOUBLE/100.);
  divid=log(1.+ptMod->Divid.Val.V_DOUBLE/100.);
  T= ptOpt->Maturity.Val.V DATE;
  T 0 = ptMod->T.Val.V DATE;
  t_0= (ptOpt->PathDep.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUB
    LE;
  time_spent= (T_0-t_0)/(T-t_0);
  if (T_0 < t_0)
     Fprintf(TOSCREEN, "T_0 < t_0, untreated case{n{n{n");}</pre>
     return_value = WRONG;
```

```
}
/* Case t_0 <= T_0 */
else
  {
   pseudo spot= (1.-time spent)*ptMod->SO.Val.V PDOUBLE;
   pseudo_strike= (ptOpt->PayOff.Val.V_NUMFUNC_2)->Par[0
  ].Val.V_PDOUBLE-time_spent*(ptOpt->PathDep.Val.V_NUMFUNC_2
  )->Par[4].Val.V_PDOUBLE;
    true_strike= (ptOpt->PayOff.Val.V_NUMFUNC_2)->Par[0].
  Val.V PDOUBLE;
    (ptOpt->PayOff.Val.V_NUMFUNC_2)->Par[0].Val.V_PDOUB
  LE= pseudo_strike;
    return_value = MC_Am_Asian_Alfonsi_LoSc(
                                                ptOpt->
  PayOff.Val.V_NUMFUNC_2,
                                                pseudo_spo
  t,
                                                T-T 0,
                                                r,
                                                divid,
                                                ptMod->Si
  gma0.Val.V_PDOUBLE,
                                                ptMod->Mea
  nReversion.hal.V PDOUBLE,
                                                ptMod->Lon
  gRunVariance.Val.V_PDOUBLE,
                                                ptMod->Si
 gma.Val.V_PDOUBLE,
                                                ptMod->Rh
  o.Val.V_PDOUBLE,
                                                ptMod->Mea
 n.Val.V PDOUBLE,
                                                ptMod->
  Variance.Val.V_PDOUBLE,
                                                ptMod->Lam
  bda. Val. V PDOUBLE,
                                                Met->Par[0
  ].Val.V_LONG,
```

```
Met->Par[1
    ].Val.V_INT,
                                                    Met->Par[2
    ].Val.V_INT,
                                                    Met->Par[3
    ].Val.V_ENUM.value,
                                                    Met->Par[4
    ].Val.V ENUM.value,
                                                    Met->Par[5
    ].Val.V_INT,
                                                    Met->Par[6
    ].Val.V PDOUBLE,
                                                    Met->Par[7
    ].Val.V_ENUM.value,
                                                    &(Met->Res
    [0].Val.V_DOUBLE),
                                                    &(Met->Res
    [1].Val.V_DOUBLE),
                                                    &(Met->Res
    [2].Val.V DOUBLE),
                                                    &(Met->Res
    [3].Val.V_DOUBLE));
      (ptOpt->PayOff.Val.V NUMFUNC 2)->Par[0].Val.V PDOUB
    LE=true_strike;
  return return_value;
\verb|static| int CHK_OPT(MC\_Am\_Asian\_Alfonsi\_LongstaffSchwartz\_B|\\
    ates)(void *Opt, void *Mod)
{
  if ( (strcmp( ((Option*)Opt)->Name, "AsianCallFixedAmer")=
    =0) || (strcmp( ((Option*)Opt)->Name, "AsianPutFixedAmer")=
    =0))
    return OK;
  return WRONG;
}
#endif //PremiaCurrentVersion
```

```
static int MET(Init)(PricingMethod *Met,Option *Opt)
  if (Met->init == 0)
      Met->init=1;
      Met->HelpFilenameHint = "
                                    mc_am_asian_alfonsi_longstaffschwartz_merhes"
      Met->Par[0].Val.V LONG=100000;
      Met->Par[1].Val.V_INT=10;
      Met->Par[2].Val.V_INT=1;
      Met->Par[3].Val.V ENUM.value=0;
      Met->Par[3].Val.V ENUM.members=&PremiaEnumRNGs;
      Met->Par[4].Val.V ENUM.value=0;
      Met->Par[4].Val.V_ENUM.members=&PremiaEnumBasis;
      Met->Par[5].Val.V_INT=10;
      Met->Par[6].Val.V_DOUBLE= 0.95;
      Met->Par[7].Val.V_ENUM.value=2;
      Met->Par[7].Val.V_ENUM.members=&PremiaEnumCirOrder;
    }
  return OK;
}
PricingMethod MET(MC_Am_Asian_Alfonsi_LongstaffSchwartz_B
    ates)=
  "MC Am Asian Alfonsi LongstaffSchwartz Bates",
  {
    {"N Simulations", LONG, {100}, ALLOW},
    {"N Exercise Dates", INT, {100}, ALLOW},
    {"N Steps per Period", INT, {100}, ALLOW},
    {"RandomGenerator", ENUM, {100}, ALLOW},
    {"Basis", ENUM, {100}, ALLOW},
    {"Dimension Approximation", INT, {100}, ALLOW},
    {"Confidence Value", DOUBLE, {100}, ALLOW},
    {"Cir Order", ENUM, {100}, ALLOW},
    {" ",PREMIA_NULLTYPE, {O}, FORBID}},
  CALC(MC Am Asian Alfonsi LongstaffSchwartz Bates),
  {
    {"Price",DOUBLE,{100},FORBID},
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{"Error Price",DOUBLE,{100},FORBID},
    {"Inf Price",DOUBLE,{100},FORBID},
    {"Sup Price",DOUBLE,{100},FORBID},
    {" ",PREMIA_NULLTYPE,{0},FORBID}},
    CHK_OPT(MC_Am_Asian_Alfonsi_LongstaffSchwartz_Bates),
    CHK_ok,
    MET(Init)
};
```

References