

## Comparing slopes

### Original Data

```
> y <- galton$child
> x <- galton$parent

> beta1 <- cor(y, x) * sd(y) / sd(x)
> beta1
[1] 0.6462906

> beta0 <- mean(y) - beta1 * mean(x)
> beta0
[1] 23.94153

> lm(y ~ x, galton)
```

Call:

```
lm(formula = y ~ x, data = galton)
```

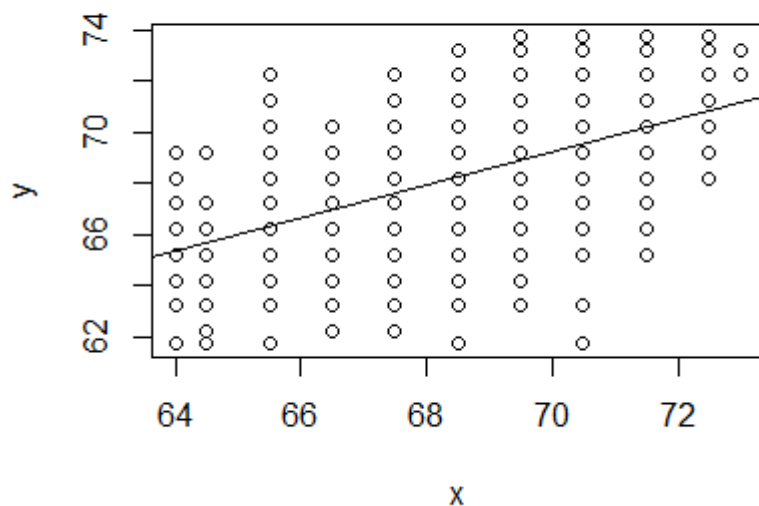
Coefficients:

(Intercept)	x
23.9415	0.6463

```
> plot(x, y)
> abline(coef = coef(lm(y~x)))
```

If we wanted a line that goes through the origin (0,0), we can calculate the slope by:

```
> sum(y * x) / sum(x  
^ 2)
[1] 0.9965439
```



## Centered Data

```
> yc <- y - mean(y)
> xc <- x - mean(x)
> beta1c <- cor(yc, xc) * sd(yc) / sd(xc)
> beta1c
[1] 0.6462906
> beta0c <- mean(yc) - beta1c * mean(xc)
> beta0c
[1] -1.50024e-16
> lm(yc ~ xc)
```

Call:

```
lm(formula = yc ~ xc)
```

Coefficients:

```
(Intercept)          xc
-1.485e-16      6.463e-01
```

```
> lm(yc ~ xc - 1)
```

Call:

```
lm(formula = yc ~ xc - 1)
```

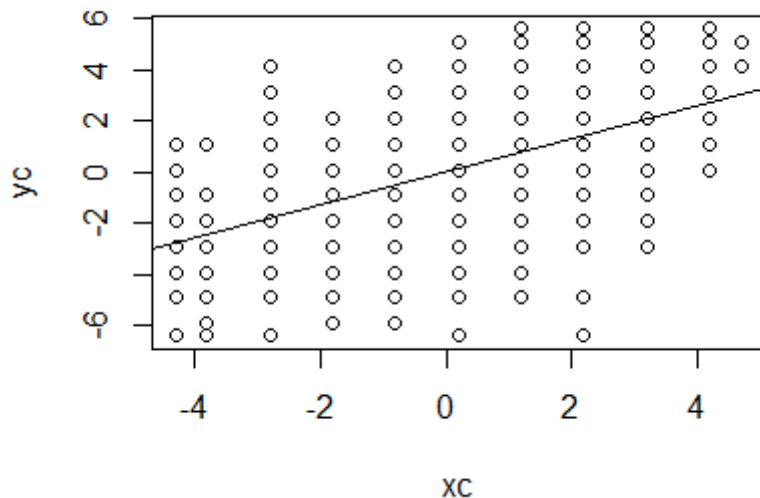
Coefficients:

```
xc
0.6463
```

```
> plot(xc, yc)
> abline(coef = coef(lm(yc~xc)))
```

Since the line is defined by data that is centered, the resulting line goes through the mean of x and y (0,0), we can calculate the slope by:

```
> sum(yc * xc) / sum(xc ^ 2)
[1] 0.6462906
```



## Scaled Data

```
> ys <- y/sd(y)
> xs <- x/sd(x)
> betas <- cor(ys, xs) * sd(ys) / sd(xs)
> betas
[1] 0.4587624
> beta0s <- mean(ys) - betas * mean(xs)
> beta0s
[1] 9.508375
> lm(ys ~ xs)
```

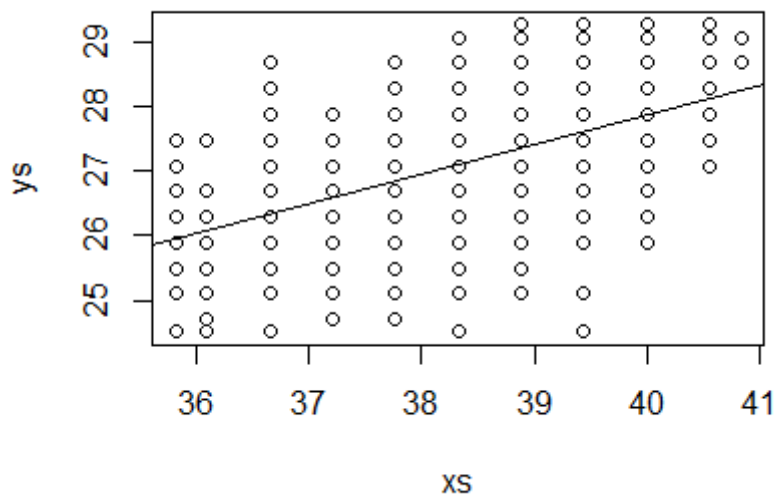
```
Call:
lm(formula = ys ~ xs)
```

```
Coefficients:
(Intercept)                xs
      9.5084         0.4588
> lm(ys ~ xs - 1)
```

```
Call:
lm(formula = ys ~ xs - 1)
```

```
Coefficients:
      xs
0.7074
```

```
> plot(xs, ys)
> abline(coef = coef(lm(ys~xs)))
```



The data is scaled but not centered, If we want a line that goes through the origin (0,0), we can calculate the slope by:

```
> sum(ys * xs) / sum(xs ^ 2)
[1] 0.7073859
```

but it will return an error

## Normalized Data

```
> yn <- (y - mean(y)) / sd(y)
> xn <- (x - mean(x)) / sd(x)
> beta1n <- cor(yn, xn) * sd(yn) / sd(xn)
> beta1n
[1] 0.4587624
> beta0n <- mean(yn) - beta1n * mean(xn)
> beta0n
[1] -3.400448e-17
> lm(yn ~ xn)
```

```
Call:
lm(formula = yn ~ xn)
```

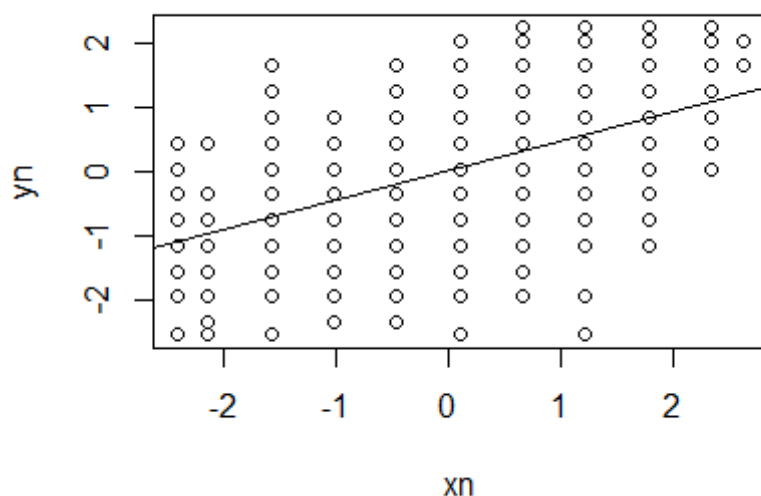
```
Coefficients:
(Intercept)          xn
-3.545e-17      4.588e-01
```

```
> lm(yn ~ xn - 1)
```

```
Call:
lm(formula = yn ~ xn - 1)
```

```
Coefficients:
          xn
0.4588
```

```
> plot(xn, yn)
> abline(coef = coef(lm(yn~xn)))
```



The data is scaled and centered, the line goes through the mean of  $x$  and  $y$  (0,0), we can calculate the slope by:

```
> sum(yn * xn) / sum(xn ^ 2)
[1] 0.4587624
```

## Comparing slope using lm

```
> coef(lm(y ~ x, galton))
(Intercept)          x
 23.9415302    0.6462906

> coef(lm(yc ~ xc))
(Intercept)          xc
-1.485327e-16  6.462906e-01

> coef(lm(ys ~ xs))
(Intercept)          xs
 9.5083748    0.4587624

> coef(lm(yn ~ xn))
(Intercept)          xn
-3.544656e-17  4.587624e-01
```

## Comparing slope using

$\text{sum}(y * x) / \text{sum}(x ^ 2)$

```
> sum(y * x) / sum(x ^ 2)
[1] 0.9965439

> sum(yc * xc) / sum(xc ^ 2)
[1] 0.6462906

> sum(ys * xs) / sum(xs ^ 2)
[1] 0.7073859

> sum(yn * xn) / sum(xn ^ 2)
[1] 0.4587624
```

## Regression through the origin

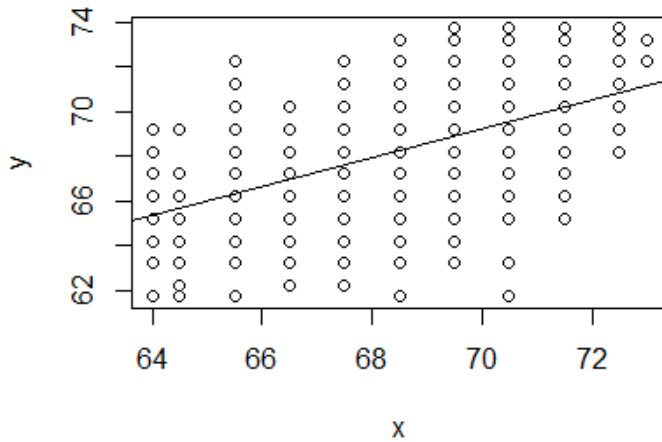
```
> coef(lm(y ~ x - 1, galton))
          x
0.9965439

> coef(lm(yc ~ xc - 1, galton))
          xc
0.6462906

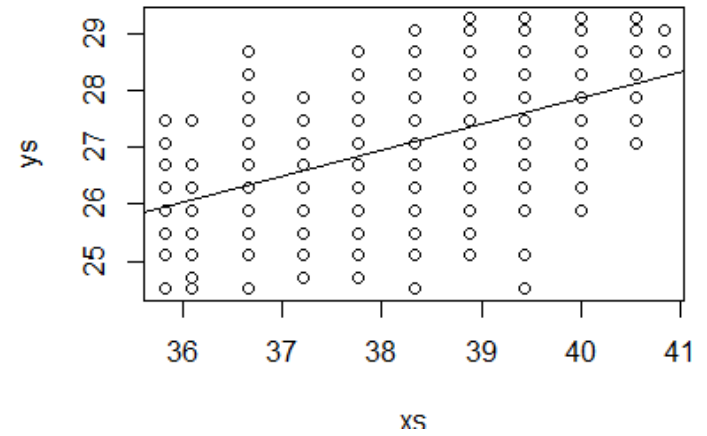
> coef(lm(ys ~ xs - 1, galton))
          xs
0.7073859

> coef(lm(yn ~ xn - 1, galton))
          xn
0.4587624
```

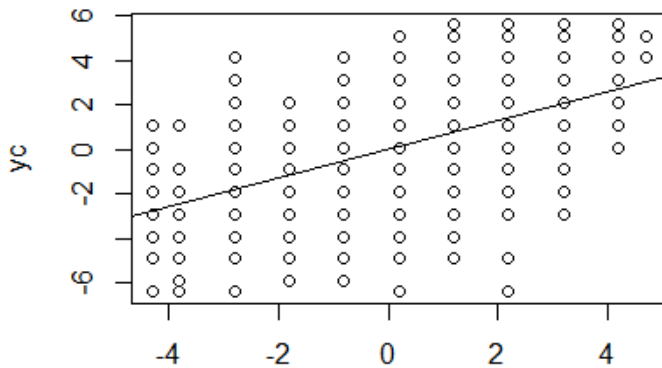
## Comparing plots



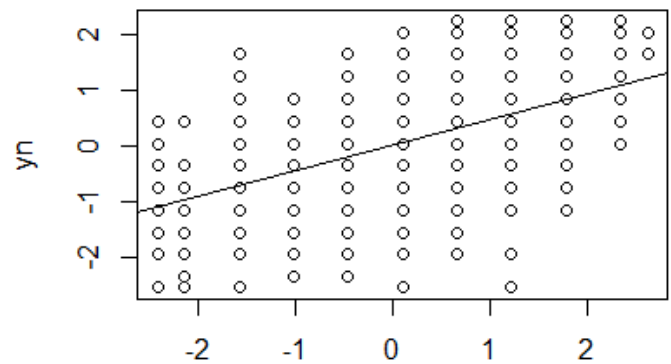
```
> coef(lm(y ~ x, galton))
(Intercept)          x
23.9415302      0.6462906
```



```
> coef(lm(ys ~ xs))
(Intercept)          xs
9.5083748      0.4587624
```



```
> coef(lm(yc ~ xc))
(Intercept)          xc
-1.485327e-16  6.462906e-01
```



```
> coef(lm(yn ~ xn))
(Intercept)          xn
-3.544656e-17  4.587624e-01
```