

Further Stats 1

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Probability Distributions

Poisson

The Poisson distribution is used to model a situation where an event occurs at a fixed rate.

You can model X as a Poisson distribution if:

- The events must occur independently
- They must occur singly in space or time
- The events must occur at a constant average rate

$$\text{If } X \sim \text{Po}(\lambda), \text{ then } \boxed{P(X = x) = \frac{e^{-\lambda} \lambda^x}{x!}} \quad (x \geq 0)$$

Geometric

The Geometric distribution is used to model a situation where you try an event several times until a success occurs, and you want to know how many tries it will take.

You can model X as a Geometric distribution if:

- Each attempt is independent
- Each attempt has the same probability

$$\text{If } X \sim \text{Geo}(p), \text{ then } \boxed{P(X = x) = p(1 - p)^{x-1}} \quad (x > 0)$$

$$\begin{array}{ll} \bullet \quad \boxed{P(X \leq x) = 1 - (1 - p)^x} & \bullet \quad \boxed{P(X \geq x) = (1 - p)^{x-1}} \\ \bullet \quad P(X > x) = (1 - p)^x & \bullet \quad P(X < x) = 1 - (1 - p)^{x-1} \end{array}$$