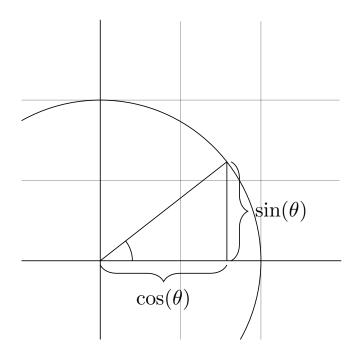
Trigonometry

Contents

Basics	2
Definitions	2
Identities	2
Calculus	3
Simplifying combinations of trig functions	3
Graphs	4

Basics

Definitions



Remember

$$\tan \theta \equiv \frac{\sin \theta}{\cos \theta}$$

$$\sec\theta \equiv \frac{1}{\cos\theta}$$

$$\csc\theta \equiv \frac{1}{\sin\theta}$$

$$\cot \theta \equiv \frac{1}{\tan \theta} \equiv \frac{\cos \theta}{\sin \theta}$$

<u>Identities</u>

Remember

$$\sin^2 \theta + \cos^2 \theta \equiv 1$$
 $1 + \tan^2 \theta \equiv \sec^2 \theta$ $1 + \cot^2 \theta \equiv \csc^2 \theta$

Formula Book

$$\sin(\alpha \pm \beta) \equiv \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$$

$$\cos(\alpha \pm \beta) \equiv \cos\alpha \cos\beta \mp \sin\alpha \sin\beta$$

$$\tan(\alpha \pm \beta) \equiv \frac{\tan \alpha \pm \tan \beta}{1 \mp \tan \alpha \tan \beta}$$

Remember

$$\sin 2\theta \equiv 2\sin\theta\cos\theta$$

$$\tan 2\theta \equiv \frac{2\tan\theta}{1-\tan^2\theta}$$

$$\cos 2\theta \equiv \cos^2 \theta - \sin^2 \theta$$
$$\equiv 2\cos^2 \theta - 1$$

$$\equiv 1 - 2\sin^2\theta$$

Calculus

Remember
$$\int \arcsin x \, dx = x \arcsin x + \sqrt{1 - x^2} + C$$

$$\frac{d}{dx} \sin x = \cos x \qquad \int \sin x \, dx = -\cos x + C$$

$$\frac{d}{dx} \cos x = -\sin x \qquad \int \cos x \, dx = \sin x + C$$

$$\int \arccos x \, dx = x \arcsin x + \sqrt{1 - x^2} + C$$

$$\int \arccos x \, dx = x \arccos x - \sqrt{1 - x^2} + C$$

$$\int \arctan x \, dx = x \arctan x - \frac{\ln(x^2 + 1)}{2} + C$$

$$\int \arcsin x \, dx = x \arcsin x + \sqrt{1 - x^2} + C$$

$$\int \arccos x \, dx = x \arccos x - \sqrt{1 - x^2} + C$$

$$\int \arctan x \, dx = x \arctan x - \frac{\ln(x^2 + 1)}{2} + C$$

Formula Book
$$\frac{d}{dx} \tan x = \sec^2 x \qquad \int \tan x \, dx = \ln|\sec x| + C \qquad \frac{d}{dx} \arcsin x = \frac{1}{\sqrt{1 - x^2}}$$

$$\frac{d}{dx} \sec x = \sec x \tan x \qquad \int \sec x \, dx = \ln|\tan x + \sec x| + C \qquad \frac{d}{dx} \arccos x = -\frac{1}{\sqrt{1 - x^2}}$$

$$\frac{d}{dx} \csc x = -\csc x \cot x \qquad \int \csc x \, dx = -\ln|\cot x + \csc x| + C \qquad \frac{d}{dx} \arctan x = \frac{1}{x^2 + 1}$$

$$\frac{d}{dx} \cot x = -\csc^2 x \qquad \int \cot x \, dx = \ln|\sin x| + C$$

Simplifying combinations of trig functions

Remember $a \sin x \pm b \cos x \equiv R \sin(x \pm \alpha)$ $a\cos x \pm b\sin x \equiv R\cos(x \mp \alpha)$ $R\cos\alpha = a \text{ and } R\sin\alpha = b \implies \tan\alpha = \frac{b}{a}$

Simplify the expression to use the R form with whichever trig function comes first in the pair. Then $\tan \alpha \equiv \frac{b}{a}$.

Graphs

