# lintrans

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## 1 Analysis

One of the topics in the A Level Further Maths course is linear transformations, as represented by matrices. This is a topic all about how vectors move and get transformed in the plane. It's a topic that lends itself exceedingly well to visualization, but students often find it hard to visualize this themselves, and there is a considerable lack of good tools to provide visual intuition on the subject. There is the YouTube series *Essence of Linear Algebra* by 3blue1brown[1], which is excellent, but I couldn't find any good interactive visualizations.

My solution is to develop a desktop application that will allow the user to define  $2 \times 2$  matrices and view these matrices and compositions thereof as linear transformations of a 2D plane. This will give students a way to get to grips with linear transformations in a more hands-on way, and will give teachers the ability to easily and visually show concepts like the determinant and invariant lines.

#### 1.1 Computational Approach

This solution is particularly well suited to a computational approach since it is entirely focussed on visualizing transformations, which require complex mathematics to properly display. It will also have lots of settings to allow the user to configure aspects of the visualization. As previously mentioned, visualizing transformations in one's own head is difficult, so a piece of software to do it would be very valuable to teachers and learners, but current solutions are considerably lacking.

My solution will make use of abstraction by allowing the user to define a set of matrices which they can use in expressions. This allows them to use a matrix multiple times and they don't have to keep track of any of the numbers. All the actual processing and mathematics happens behind the scenes and the user never has to worry about it - they just compose their defined matrices into transformations. This abstraction allows the user to focus on exploring the transformations themselves without having to do any actual computations. This will make learning the subject much easier, as they will able to gain a visual intuition for linear transformations without worrying about computation until after they've built up that intuition.

I will also employ decomposition and modularization by breaking the project down into many smaller parts, such as one module to keep track of defined matrices, one module to validate and parse matrix expressions, one module for the main GUI, as well as sub-modules for the widgets and dialog boxes, etc. This decomposition allows for simpler project design, easier code maintenance (since module coupling is kept to a minimum, so bugs are isolated in their modules), inheritance of classes to reduce code repetition, and unit testing to inform development. I also intend this unit testing to be automated using GitHub Actions.

Selection will also be used widely in the application. The GUI will provide many settings for visualization, and these settings will need to be checked when rendering the transformation. For example, the user will have the option to render the determinant, so I will need to check this setting on every render cycle and only render the determinant parallelogram if the user has enabled that option. The app will have many options for visualization, which will be useful in learning, but if all these options were being rendered at the same time, then there would be too much information for the user to properly process, so I will let the user configure these display options to their liking and only render the things they want to be rendered.

Validation will also be prevalent because the matrix expressions will need to follow a strict format, which will be validated. The buttons to render and animate the matrix will only be clickable when the given expression is valid, so I will need to check this and update the buttons every time the text in the text box is changed. I will also need to parse matrix expressions so that I can evaluate them properly. All this validation ensures that crashes due to malformed input are practically impossible, and makes the user's life easier since they don't need to worry about if their input is in the right format - the app will tell them.

I will also make use of iteration, primarily in animation. I will have to re-calculate positions and

values to render everything for every frame of the animation and this will likely be done with a simple for loop. A for loop will allow me to just loop over every frame and use the counter variable as a way to measure how far through the animation we are on each frame. This is preferable to a while loop, since that would require me to keep track of which frame we're on with a separate variable.

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Finally, the core of the application is visualization, so that will definitely be used a lot. I will have to calculate positions of points and lines based on given matrices, and when animating, I will also have to calculate these matrices based on the current frame. Then I will have to use the rendering capabilities of the GUI framework that I choose to render these calculated points and lines onto a widget, which will form the viewport of the main GUI. I may also have to convert between coordinate systems. I will have the origin in the middle with positive x going to the right and positive y going up, but I may need to convert that to standard computer graphics coordinates with the origin in the top left, positive x going to the right, and positive y going down. This visualization of linear transformations is the core component of the app and is the primary feature, so it is incredibly important.

#### 1.2 Stakeholders

Stakeholders for my app include A Level Further Maths students and teachers, who learn and teach linear transformations respectively. They will be able to provide useful input as to what they would like to see in the app, and they can provide feedback on what they like and what I can add or improve. I already know from experience that linear transformations are tricky to visualize and a computer-based visualization would be useful. My stakeholders agreed with this. Many teachers said that a desktop app that could render and animate linear transformations would be useful in a classroom environment and students said that it would be helpful to have something that they could play around with at home and use to get to grips with matrices and linear transformations.

Some teachers also suggested that it would be useful to have an option to save and load sets of matrices. This would allow them to have a single save file containing some matrices, and then just load this file to use for demonstrations in the classroom. This would probably be quite easy to implement. I could just wrap all the relevant information into one object and use Python's pickle module to save the binary data to a file, and then load this data back into the app in a similar way.

My stakeholders agreed that being able to see incremental animation - where, for example, we apply matrix  $\bf A$  to the current scene, pause, and then apply matrix  $\bf B$  - would be beneficial. This would be a good demonstration of matrix multiplication being non-commutative.  $\bf AB$  is not always equal to  $\bf BA$ . Being able to see this in terms of animating linear transformations would be good for learning.

They also agreed that a tutorial on using the software would be useful, so I plan to implement this through an online written tutorial hosted with GitHub Pages, and perhaps a video tutorial as well. This would make the app much easier to use for people who have never seen it before. It wouldn't be a lesson on the maths itself, just a guide on how to use the software.

#### 1.3 Research on existing solutions

There are actually quite a few web apps designed to help visualize 2D linear transformations but many of them are hard to use and lacking many features.

#### 1.3.1 MIT 'Matrix Vector' Mathlet

Arguably the best app that I found was an MIT 'Mathlet' - a simple web app designed to help visualize a maths concept. This one is called 'Matrix Vector' [2] and allows the user to drag an input vector around the plane and see the corresponding output vector, transformed by a matrix that the user can define, although this definition is finicky since it involves sliders rather than keyboard input.

This app fails in two crucial ways in my opinion. It doesn't show the basis vectors or let the user drag them around, and the user can only define and therefore visualize a single matrix at once. This second problem was common among every solution I found, so I won't mention it again, but it is a big issue in my opinion and my app will allow for multiple matrices. I like the idea of having a draggable input vector and rendering its output, so I will probably have this feature in my app, but I also want the ability to define multiple matrices and be able to drag the basis vectors to visually define a matrix. Being able to drag the basis vectors will help build intuition, so I think this would greatly benefit the app.

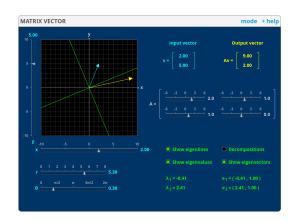


Figure 1: The MIT 'Matrix Vector' Mathlet

However, in the comments on this Mathlet, a user called 'David S. Bruce' suggested that the Mathlet should display the basis vectors, to which a user called 'hrm' (who I assume to be the 'H. Miller' to whom the copyright of the whole website is accredited) replied saying that this Mathlet is primarily focussed on eigenvectors, that it is perhaps badly named, and that displaying the basis vectors 'would make a good focus for a second Mathlet about  $2 \times 2$  matrices'. This Mathlet does not exist. But I do like the idea of showing the eigenvectors and eigenlines, so I will definitely have that in my app. Showing the invariant lines or lack thereof will help with learning, since these are often hard to visualize.

#### 1.3.2 Linear Transformation Visualizer

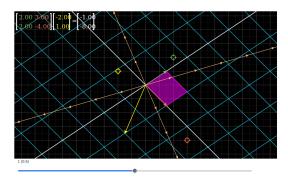


Figure 2: 'Linear Transformation Visualizer' halfway through an animation

Another web app that I found was one simply called 'Linear Transformation Visualizer' by Shad Sharma[3]. This one was similarly inspired by 3blue1brown's YouTube series. This app has the ability to render input and output vectors and eigenlines, but it can also render the determinant parallelogram; it allows the user to drag the basis vectors; and it has the option to snap vectors to the background grid, which is quite useful. It also implements a simple form of animation where the tips of the vectors move in straight lines from where they start to where they end, and the animation is controlled by dragging a slider labelled t. This isn't particularly intuitive.

I really like the vectors snapping to the grid, the input and output vectors, and rendering the determinant. This app also renders positive and negative determinants in different colours, which is really nice - I intend to use that idea in my own app, since it helps create understanding about negative determinants in terms of orientation changes. However, I think that the animation system here is flawed and not very easy to use. My animation will likely be a button, which just triggers an animation, rather than a slider. I also don't like the way vector dragging is handled. If you click anywhere on the grid, then the closest vector target (the final position of the target's associated vector) snaps to that location. I think it would be more intuitive to have to drag the vector from its current location to where you want it. This was also a problem with the MIT Mathlet.

#### 1.3.3 Desmos app

One of the solutions I found was a Desmos app[4], which was quite hard to use and arguably over-complicated. Desmos is not designed for this kind of thing - it's designed to graph pure mathematical functions - and it shows here. However, this app brings some really interesting ideas to the table, mainly functions. This app allows you to define custom functions and view them before and after the transformation. This is achieved by treating the functions parametrically as the set of points (t, f(t)) and then transforming each coordinate by the given matrix to get a new coordinate.

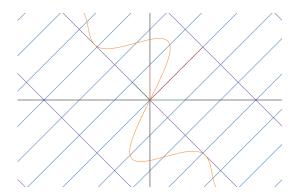


Figure 3: The Desmos app halfway through an animation, rendering  $f(x) = \frac{\sin^2 x}{x}$  in orange

Desmos does this for every point and then renders the resulting transformed function parametrically. This is a really interesting technique and idea, but I'm not going to use it in my app. I don't think arbitrary functions fit with the linearity of the whole app, and I don't think it's necessary. It's just overcomplicating things, and rendering it on a widget would be tricky, because I'd have to render every point myself, possibly using something like OpenGL. It's just not worth implementing.

Additionally, this Desmos app makes things quite hard to see. It's hard to tell where any of the vectors are - they just get lost in the sea of grid lines. This image also hides some of the extra information. For instance, this image doesn't show the original function  $f(x) = \frac{\sin^2 x}{x}$ , only the transformed version. This app easily gets quite cluttered. I will give my vectors arrowheads to make them easily identifiable amongst the grid lines.

#### 1.3.4 Visualizing Linear Transformations

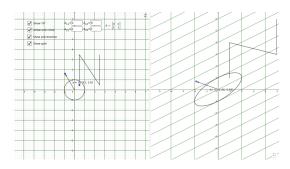


Figure 4: The GeoGebra applet rendering its default matrix

The last solution that I want to talk about is a GeoGebra applet simply titled 'Visualizing Linear Transformations'[5]. This applet has input and output vectors, original and transformed grid lines, a unit circle, and the letter N. It allows the user to define a matrix as 4 numbers and view the aforementioned N (which the user can translate to anywhere on the grid), the unit circle, the input/output vectors, and the grid lines. It also has the input vector snapping to integer coordinates, but that's a standard part of GeoGebra.

I've already talked about most of these features but the thing I wanted to talk about here is the N. I don't particularly want the letter N to be a prominent part of my own app, but I really like the idea of being able to define a custom polygon and see how that polygon gets transformed by a given transformation. I think that would really help with building intuition and it shouldn't be too hard to implement.

#### 1.4 Essential features

The primary aim of this application is to visualize linear transformations, so this will obviously be the centre of the app and an essential feature. I will have a widget which can render a background grid

and a second version of the grid, transformed according to a user-defined matrix expression. This is necessary because it is the entire purpose of the app. It's designed to visualize linear transformations and would be completely useless without this visual component. I will give the user the ability to render a custom matrix expression containing matrices they have previously defined, as well as reset the canvas to the default identity matrix transformation. This will obviously require an input box to enter the expression, a render button, a reset button, and various dialog boxes to define matrices in different ways. I want the user to be able to define a matrix as a set of 4 numbers, and by dragging the basis vectors i and j. These dialogs will allow the user to define new matrices to be used in expressions, and having multiple ways to do it will make it easier, and will aid learning.

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Another essential feature is animation. I want the user to be able to smoothly animate between matrices. I see two options for how this could work. If C is the matrix for the currently displayed transformation, and T is the matrix for the target transformation, then we could either animate from C to T or we could animate from C to TC. I would probably call these transitional and applicative animation respectively. Perhaps I'll give the user the option to choose which animation method they want to use. Either way, animation is used in most of the alternative solutions that I found, and it's a great way to build intuition, by allowing students to watch the transformation happen in real time. Compared to simply rendering the transformations, animating them would profoundly benefit learning, and since that's the main aim of the project, I think animation is a necessary part of the app.

Something that I thought was a big problem in every alternative solution I found was the fact that the user could only visualize a single matrix at once. I see this as a fatal flaw and I will allow the user to define 25 different matrices (all capital letters except I for the identity matrix) and use all of them in expressions. This will allow teachers to define multiple matrices and then just change the expression to demonstrate different concepts rather than redefine a new transformation every time. It will also make things easier for students as it will allow them to visualize compositions of different matrix transformations without having to do any computations themselves.

Additionally, being able to show information on the currently displayed matrix is an essential tool for learning. Rendering things like the determinant parallelogram and the invariant lines of the transformation will greatly assist with learning and building understanding, so I think that having the option to render these attributes of the currently displayed transformation is necessary for success.

#### 1.5 Limitations

The main limitation in this app is likely to be drawing grid lines. Most transformations will be fine but in some cases, the app will be required to draw potentially thousands of grid lines on the canvas and this will probably cause noticeable lag, especially in the animations. I will have to artificially limit the number of grid lines that can be drawn on the screen. This won't look fantastic, because it means that the grid lines will only extend a certain distance from the origin, but it's an inherent limitation of computers. Perhaps if I was using a faster, compiled language like C++ rather than Python, this processing would happen faster and I could render more grid lines, but it's impossible to render all the grid lines and any implementation of this idea must limit them for performance.

An interesting limitation is that I don't think I'll implement panning. I suspect that I'll have to convert between coordinate systems and having the origin in the centre of the canvas will probably make the code much simpler. Also, linear transformations always leave the origin fixed, so always having it in the centre of the canvas seems thematically appropriate. Panning is certainly an option - the Desmos solution in §1.3.3 and GeoGebra solution in §1.3.4 both allow panning as a default part of Desmos and GeoGebra respectively, for example - but I don't think I'll implement it myself. I just don't think it's worth it.

I'm also not going to do any work with 3D linear transformations. 3D transformations are often harder to visualize and thus it would make sense to target them in an app like this, designed to help with learning and intuition, but 3D transformations are also harder to code. I would have to use a full graphics package rather than a simple widget, and I think it would be too much work for this

project and I wouldn't be able to do it in the time frame. It's definitely a good idea, but I'm currently incapable of creating an app like that.

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There are other limitations inherent to matrices. For instance, it's impossible to take an inverse of a singular matrix. There's nothing I can do about that without rewriting most of mathematics. Matrices can also only represent linear transformations. There's definitely a market for an app that could render any arbitrary transformation from  $\mathbb{R}^2 \to \mathbb{R}^2$  - I know I'd want an app like that - but matrices can only represent linear transformations, so those are the only kind of transformations that I'll be looking at with this project.

#### 1.6 Hardware and software requirements

#### 1.6.1 Hardware

Hardware requirements for the project are the same between the release and development environments and they're quite simple. I expect the app to require a processor with at least 1 GHz clock speed, \$BINARY\_SIZE free disk space, and about 1 GB of available RAM. The processor and RAM requirements are needed by the Python runtime and mainly by Qt5 - the GUI library I'll be using. The \$BINARY\_SIZE disk space is just for the executable binary that I'll compile for the public release. The code itself is less than 1 MB, but the compiled binary has to package all the dependencies and the entire CPython runtime to allow it to run on systems that don't have that, so the file size is much bigger.

I will also require that the user has a monitor that is at least  $1920 \times 1080$  pixels in resolution. This isn't necessarily required, because the app will likely run in a smaller window, but a HD monitor is highly recommended. This allows the user to go fullscreen if they want to, and it gives them enough resolution to easily see everything in the app. A large, wall-mounted screen is also highly recommended for use in the classroom, although this is common among schools.

I will also require a keyboard with all standard Latin alphabet characters. This is because the matrices are defined as uppercase Latin letters. Any UK or US keyboard will suffice for this. The app will also require a mouse with at least one button. I don't intend to have right click do anything, so only the primary mouse button is required, although getting a single button mouse to actually work on modern computers is probably quite a challenge. A separate mouse is not strictly required - a laptop trackpad is equally sufficient.

#### 1.6.2 Software

Software requirements differ slightly between release and development, although everything that the release environment requires is also required by the development environment. I will require a modern operating system - namely Windows 10 or later, macOS 10.9 'Mavericks' or later, or any modern Linux distro<sup>2</sup>. Basically, it just requires an operating system that is compatible with Python 3.10 and Qt5, since I'll be using these in the project. Of course, Qt5 will need to be installed on the user's computer, although it's standard pretty much everywhere these days.

Python 3.10 won't actually be required for the end user, because I will be compiling the app into a stand-alone binary executable for release, and this binary will contain the required Python runtime and dependencies. However, if the user wishes to download and run the source code themself, then they will need Python 3.10 and the package dependencies: numpy, nptyping, and pyqt5. These can be automatically installed with the command python -m pip install -r requirements.txt from the root of the repository. numpy is a maths library that allows for fast matrix maths; nptyping is used by mypy for type-checking and isn't actually a runtime dependency but the imports in the typing module

 $<sup>^1\</sup>mathrm{Python}$  3.10 won't compile on any earlier versions of macOS[6]

<sup>&</sup>lt;sup>2</sup>Specifying a Linux version is practically impossible. Python 3.10 isn't available in many package repositories, but will compile on any modern distro. Qt5 is available in many package repositories and can be compiled on any x86 or x86\_64 generic Linux machine with gcc version 5 or later[7]

fail if it's not installed at runtime; and pyqt5 is a library that just allows interop between Python and Qt5, which is originally a C++ library.

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In the development environment, I use PyCharm for actually writing my code, and I use a virtual environment to isolate my project dependencies. There are also some development dependencies listed in the file dev\_requirements.txt. They are: mypy, pyqt5-stubs, flake8, pycodestyle, pydocstyle, and pytest. mypy is a static type checker<sup>3</sup>; pyqt5-stubs is a collection of type annotations for the PyQt5 API for mypy to use; flake8, pycodestyle, and pydocstyle are all linters; and pytest is a unit testing framework. I use these libraries to make sure my code is good quality and actually working properly during development.

#### 1.7 Success criteria

The main aim of the app is to help teach students about linear transformations. As such, the primary measure of success will be letting teachers get to grips with the app and then asking if they would use it in the classroom or recommend it to students to use at home.

Additionally, the app must fulfil some basic requirements:

- 1. It must allow the user to define multiple matrices in at least two different ways (numerically and visually)
- 2. It must be able to validate arbitrary matrix expressions
- 3. It must be able to render any valid matrix expression
- 4. It must be able to animate any valid matrix expression
- 5. It must be able to display information about the currently rendered transformation (determinant, eigenlines, etc.)
- 6. It must be able to save and load sessions (defined matrices, display settings, etc.)
- 7. It must allow the user to define and transform arbitrary polygons

Defining multiple matrices is a feature that I thought was lacking from every other solution I researched, and I think it would make the app much easier to use, so I think it's necessary for success. Validating matrix expressions is necessary because if the user tries to render an expression that doesn't make sense, has an undefined matrix, or contains the inverse of a singular matrix, then we have to disallow that or else the app will crash.

Visualizing matrix expressions as linear transformations is the core part of the app, so basic rendering of them is definitely a requirement for success. Animating these expressions is also a pretty crucial part of the app, so I would consider this necessary for success. Displaying the information of a matrix transformation is also very useful for building understanding, so I would consider this needed to succeed.

Saving and loading isn't strictly necessary for success, but it is a standard part of many apps, so will likely be expected by users, and it will benefit the app by allowing teachers to plan lessons in advance and save the matrices they've defined for that lesson to be loaded later.

Transforming polygons is the lowest priority item on this list and will likely be implemented last, but it would definitely benefit learning. I wouldn't consider it necessary for success, but it would be very good to include, and it's certainly a feature that I want to have.

If the majority of teachers would use and/or recommend the app and it meets all of these points, then I will consider the app as a whole to be a success.

 $<sup>^{3}</sup>$ Python has weak, dynamic typing with optional type annotations but mypy enforces these static type annotations

## 2 Design

Candidate name: D. Dyson

#### 2.1 Problem decomposition

I have decomposed the problem of visualization as follows:



Defining matrices is key to visualization because we need to have matrices to actually visualize. This is a key part of the app, and the user will be able to define multiple separate matrices numerically and visually using the GUI.

Evaluating expressions is another key part of the app and can be further broken down into validating, parsing, and computing the value. Validating an expression simply consists of checking that it adheres to a set of syntax rules for matrix expressions, and that it only contains matrices which have already been defined. Parsing consists of breaking an expression down into tokens, which are then much easier to evaluate. Computing the expression with these tokens is then just a series of simple operations, which will produce a final matrix at the end.

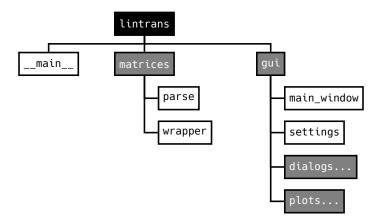
Rendering and animating will likely be the largest part in reality, but I've only decomposed it into simple blocks here. Evaluating positions involves evaluating the matrix expression that the user has input and using the columns of the resultant matrix to find the new positions of the basis vectors, and then extrapolating this for the rest of the plane. Rendering onto the widget is likely to be quite complicated and framework-dependent, so I've abstracted away the details for brevity here. Rendering will involve using the previously calculated values to render grid lines and vectors. Animating will probably be a for loop which just renders slightly different matrices onto the widget and sleeps momentarily between frames.

I have deliberately broken this problem down into parts that can be easily translated into modules in my eventual coded solution. This is simply to ease the design and development process, since now I already know my basic project structure. This problem could've been broken down into the parts that the user will directly interact with, but that would be less useful to me when actually starting development, since I would then have to decompose the problem differently to write the actual code.

#### 2.2 Structure of the solution

#### 2.2.1 The main project

I have decomposed my solution like so:



The lintrans node is simply the root of the whole project. \_\_main\_\_ is the Python way to make the project executable as python -m lintrans on the command line. For release, I will package it into a standalone binary executable.

matrices is the package that will allow the user to define, validate, parse, evaluate, and use matrices. The parse module will contain functions to validate matrix expressions - likely using regular expressions - and functions to parse matrix expressions. It will not know which matrices are defined, so validation will be naïve and evaluation will be elsewhere. The wrapper module will contain a MatrixWrapper class, which will hold a dictionary of matrix names and values. It is this class which will have aware validation - making sure that all matrices are actually defined - as well the ability to evaluate matrix expressions, in addition to its basic behaviour of setting and getting matrices. This matrices package will also have a create\_rotation\_matrix function that will generate a rotation matrix from an angle using the formula  $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$ . It will be in the wrapper module since it's related to defining and manipulating matrices, but it will be exported and accessible as lintrans.matrices.create\_rotation\_matrix.

gui is the package that will contain all the frontend code for everything GUI-related. main\_window is the module that will contain a LintransMainWindow class, which will act as the main window of the application and have an instance of MatrixWrapper to keep track of which matrices are defined and allow for evaluation of matrix expressions. It will also have methods for rendering and animating matrix expressions, which will be connected to buttons in the GUI. This module will also contain a simple main() function to instantiate and launch the application GUI.

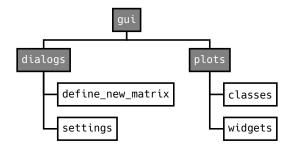
The settings module will contain a DisplaySettings dataclass<sup>4</sup> that will represent the settings for visualizing transformations. The LintransMainWindow class will have an instance of this class and check against it when rendering things. The user will be able to open a dialog to change these display settings, which will update the main window's instance of this class.

The settings module will also have a GlobalSettings class, which will represent the global settings for the application, such as the logging level, where to save the logs, whether to ask the user if they want to be prompted with a tutorial whenever they open the app, etc. This class will have defaults for everything, but the constructor will try to read these settings from a config file if possible. This allows for persistent settings between sessions. This config file will be ~/.config/lintrans.conf on Unix-like systems, including macOS, and C:\Users\%USER%\AppData\Roaming\lintrans\config.txt on Windows. This difference is to remain consistent with operating system conventions<sup>5</sup>.

<sup>&</sup>lt;sup>4</sup>This is the Python equivalent of a struct or record in other languages

 $<sup>^5\</sup>mathrm{And}$  also to avoid confusing Windows users with a .conf file

#### 2.2.2 The gui subpackages



The dialogs subpackage will contain modules with different dialog classes. It will have a define\_new\_matrices module, which will have a DefineDialog abstract superclass. It will also contain classes that inherit from this superclass and provide dialogs for defining new matrices visually, numerically, and as an expression in terms of other matrices. Additionally, this subpackage will contain a settings module, which will provide a SettingsDialog superclass and a DisplaySettingsDialog class, which will allow the user to configure the aforementioned display settings. It will also have a GlobalSettingsDialog class, which will similarly allow the user to configure the app's global settings through a dialog.

The plots subpackage will have a classes module and a widgets module. The classes module will have the abstract superclasses BackgroundPlot and VectorGridPlot. The former will provide helped methods to convert between coordinate systems and draw the background grid, while the latter will provide helper methods to draw transformations and their components. It will have point\_i and point\_j attributes and will provide methods to draw the transformed version of the grid, the vectors and their arrowheads, the eigenlines of the transformation, etc. These methods can then be called from the Qt5 paintEvent handler which will be declared abstract and must therefore be implemented by all subclasses.

The plots subpackage will also contain a widgets module, which will have the classes VisualizeTransformationWidget and DefineVisuallyWidget, both of which will inherit from VectorGridPlot. They will both implement their own paintEvent handler to actually draw the respective widgets, and DefineVisuallyWidget will also implement handlers for mouse events, allowing the user to drag around the basis vectors.

It's also worth noting here that I don't currently know how I'm going to implement the transformation of arbitrary polygons. It will likely consist of an attribute in VisualizeTransformationWidget which is a list of points, and these points can be dragged around with mouse event handlers and then the transformed versions can be rendered, but I'm not yet sure about how I'm going to implement it.

#### 2.3 Algorithm design

This section will be completed later.

#### 2.4 Usability features

My main concern in terms of usability is colour. In the 3blue1brown videos on linear algebra, red and green are used for the basis vectors, but these colours are often hard to distinguish in most common forms of colour blindness. The most common form is deuteranopia[8], which makes red and green look incredibly similar. I will use blue and red for my basis vectors. These colours are easy to distinguish for people with deuteranopia and protanopia - the two most common forms of colour blindness. Tritanopia makes it harder to distinguish blue and yellow, but my colour scheme is still be accessible for people with tritanopia, as red and blue are very distinct in this form of colour blindness.

I will probably use green for the eigenvectors and eigenlines, which will be hard to distinguish from the red basis vector for people with red-green colour blindness, but I think that the basis vectors and

eigenvectors/eigenlines will look physically different enough from each other that the colour shouldn't be too much of a problem. Additionally, I will use a tool called Color Oracle[9] to make sure that my app is accessible to people with different forms of colour blindness<sup>6</sup>.

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Another solution would be to have one default colour scheme, and allow the user to change the colour scheme to something more accessible for colour blind people, but I don't see the point in this. I think it's easier for colour blind people to just have the main colour scheme be accessible, and it's not really an inconvenience to non-colour blind people, so I think this is the best option.

The layout of my app will be self-consistent and follow standard conventions. I will have a menu bar at the top of the main window for actions like saving and loading, as well as accessing the tutorial (which will also be accessible by pressing F1 at any point) and documentation. The dialogs will always have the confirm button in the bottom right and the cancel button just to the left of that. They will also have the matrix name drop-down on the left. This consistency will make the app easier to learn and understand.

I will also have hotkeys for everything that can have hotkeys - buttons, checkboxes, etc. This makes my life easier, since I'm used to having hotkeys for everything, and thus makes the app faster to test because I don't need to click everything. This also makes things easier for other people like me, who prefer to stay at the keyboard and not use the mouse. Obviously a mouse will be required for things like dragging basis vectors and polygon vertices, but hotkeys will be available wherever possible to help people who don't like using the mouse or find it difficult.

#### 2.5 Variables and validation

This project won't actually have many variables. The main ones will be instance attributes on the LintransMainWindow class. It will have a MatrixWrapper instance, a DisplaySettings instance, and a GlobalSettings instance. These will handle the matrices and various settings respectively. Having these as instance attributes allows them to be referenced from any method in the class, and Qt5 uses lots of slots (basically callback methods) and handlers, so it's good to be able to access the attributes I need right there rather than having to pass them around from method to method.

The MatrixWrapper class will have a dictionary of names and matrices. The names will be single letters<sup>7</sup> and the matrices will be of type MatrixType. This will be a custom type alias representing a  $2 \times 2$  numpy array of floats. When setting the values for these matrices, I will have to manually check the types. This is because Python has weak typing, and if we got, say, an integer in place of a matrix, then operations would fail when trying to evaluate a matrix expression, and the program would crash. To prevent this, we have to validate the type of every matrix when it's set. I have chosen to use a dictionary here because it makes accessing a matrix by its name easier. We don't have to check against a list of letters and another list of matrices, we just index into the dictionary.

The settings dataclasses will have instance attributes for each setting. Most of these will be booleans, since they will be simple binary options like *Show determinant*, which will be represented with checkboxes in the GUI. The DisplaySettings dataclass will also have an attribute of type int representing the time in milliseconds to pause during animations.

The DefineDialog superclass have a MatrixWrapper instance attribute, which will be a parameter in the constructor. When LintransMainWindow spawns a definition dialog (which subclasses DefineDialog), it will pass in a copy of its own MatrixWrapper and connect the accepted signal for the dialog. The slot (method) that this signal is connected to will get called when the dialog is closed with the Confirm button<sup>8</sup>. This allows the dialog to mutate its own MatrixWrapper object and then the main window can copy that mutated version back into its own instance attribute when the user confirms the change. This reduces coupling and makes everything easier to reason about and debug, as well as reducing

 $<sup>^6</sup>$ I actually had to clone a fork of this project[10] to get it working on Ubuntu 20.04 and adapt it slightly to create a working jar file

<sup>&</sup>lt;sup>7</sup>I would make these char but Python only has a str type for strings

 $<sup>^8</sup>$ Actually when the dialog calls .accept(). The Confirm button is actually connected to a method which first takes the info and updates the instance MatrixWrapper, and then calls .accept()

the number of bugs, since the classes will be independent of each other. In another language, I could pass a pointer to the wrapper and let the dialog mutate it directly, but this is potentially dangerous, and Python doesn't have pointers anyway.

Validation will also play a very big role in the application. The user will be able to enter matrix expressions and these must be validated. I will define a BNF schema and either write my own RegEx or use that BNF to programmatically generate a RegEx. Every matrix expression input will be checked against it. This is to ensure that the matrix wrapper can actually evaluate the expression. If we didn't validate the expression, then the parsing would fail and the program could crash. I've chosen to use a RegEx here rather than any other option because it's the simplest. Creating a RegEx can be difficult, especially for complicated patterns, but it's then easier to use it. Also, Python can compile a RegEx pattern, which makes it much faster to match against, so I will compile the pattern at initialization time and just compare expressions against that pre-compiled pattern, since we know it won't change at runtime.

Additionally, the buttons to render and animate the current matrix expression will only be enabled when the expression is valid. Textboxes in Qt5 emit a textChanged signal, which can be connected to a slot. This is just a method that gets called whenever the text in the textbox is changed, so I can use this method to validate the input and update the buttons accordingly. An empty string will count as invalid, so the buttons will be disabled when the box is empty.

I will also apply this matrix expression validation to the textbox in the dialog which allows the user to define a matrix as an expression involving other matrices, and I will validate the input in the numeric definition dialog to make sure that all the inputs are floats. Again, this is to prevent crashes, since a matrix with non-number values in it will likely crash the program.

#### 2.6 Iterative test data

In unit testing, I will test the validation, parsing, and generation of rotation matrices from an angle. I will also unit test the utility functions for the GUI, like is\_valid\_float.

For the validation of matrix expressions, I will have data like the following:

Valid	Invalid
"A"	11 11
"AB"	"A^"
"-3.4A"	"rot()"
"A^2"	"A^{2"
"A^T"	"^12"
"A^{-1}"	"A^3.2"
"rot(45)"	"A^B"
"3A^{12}"	".A"
"2B^2+A^TC^{-1}"	"A"
"3.5A^45.6rot(19.2^T-B^-14.1C^5"	"AB"

This list is not exhaustive, mostly to save space and time, but the full unit testing code is included in appendix B.

The invalid expressions presented here have been chosen to be almost valid, but not quite. They are edge cases. I will also test blatantly invalid expressions like "This is a matrix expression" to make sure the validation works.

Here's an example of some test data for parsing:

Input	Expected
"A"	[[("", "A", "")]]
"AB"	[[("", "A", ""), ("", "B", "")]]
"2A+B^2"	[[("2", "A", ""), ("", "B", "2")]]
"3A^T2.4B^{-1}-C"	[[("3", "A", "T"), ("2.4", "B", "-1")], [("-1", "C", "")]]

The parsing output is pretty verbose and this table doesn't have enough space for most of the more complicated inputs, so here's a monster one:

which should parse to give:

Any invalid expression will also raise a parse error, so I will check every invalid input previously mentioned and make sure it raises the appropriate error.

Again, this section is brief to save space and time. All unit tests are included in appendix B.

#### 2.7 Post-development test data

This section will be completed later.

## 3 Development

Please note, throughout this section, every code snippet will have two comments at the top. The first is the git commit hash that the snippet was taken from<sup>9</sup>. The second comment is the file name. The line numbers of the snippet reflect the line numbers of the file from where the snippet was taken. After a certain point, I introduced copyright comments at the top of every file. These are always omitted here

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#### 3.1 Matrices backend

#### 3.1.1 MatrixWrapper class

The first real part of development was creating the MatrixWrapper class. It needs a simple instance dictionary to be created in the constructor, and it needs a way of accessing the matrices. I decided to use Python's \_\_getitem\_\_() and \_\_setitem\_\_() special methods[12] to allow indexing into a MatrixWrapper object like wrapper['M']. This simplifies using the class.

```
# 29ec1fedbf307e3b7ca731c4a381535fec899b0b
        # src/lintrans/matrices/wrapper.pv
        """A module containing a simple MatrixWrapper class to wrap matrices and context."""
        import numpy as np
        from lintrans.typing import MatrixType
 6
 8
        class MatrixWrapper:
 9
            """A simple wrapper class to hold all possible matrices and allow access to them."""
10
11
            def __init__(self):
                  "Initialise a MatrixWrapper object with a matrices dict."""
12
13
                self._matrices: dict[str, MatrixType | None] = {
14
                     'A': None, 'B': None, 'C': None, 'D': None,
                    'E': None, 'F': None, 'G': None, 'H': None,
15
                    'I': np.eye(2), # I is always defined as the identity matrix
16
17
                    'J': None, 'K': None, 'L': None, 'M': None,
18
                    'N': None, '0': None, 'P': None, 'Q': None,
19
                     'R': None, 'S': None, 'T': None, 'U': None,
                    'V': None, 'W': None, 'X': None, 'Y': None,
20
21
                    'Z': None
22
23
24
            def __getitem__(self, name: str) -> MatrixType | None:
25
                 """Get the matrix with `name` from the dictionary.
26
27
28
                    KevError:
29
                        If there is no matrix with the given name
30
                return self._matrices[name]
31
32
33
            def __setitem__(self, name: str, new_matrix: MatrixType) -> None:
34
                 """Set the value of matrix `name` with the new_matrix.
35
36
                Raises:
37
                    ValueError:
38
                        If `name` isn't a valid matrix name
39
40
                name = name.upper()
41
                if name == 'I' or name not in self. matrices:
42
43
                    raise NameError('Matrix name must be a capital letter and cannot be "I"')
```

 $<sup>^9\</sup>mathrm{A}$  history of all commits can be found in the GitHub repository[11]

```
self._matrices[name] = new_matrix
```

This code is very simple. The constructor (\_\_init\_\_()) creates a dictionary of matrices which all start out as having no value, except the identity matrix I. The \_\_getitem\_\_() and \_\_setitem\_\_() methods allow the user to easily get and set matrices just like a dictionary, and \_\_setitem\_\_() will raise an error if the name is invalid. This is a very early prototype, so it doesn't validate the type of whatever the user is trying to assign it to yet. This validation will come later.

I could make this class subclass dict, since it's basically just a dictionary at this point, but I want to extend it with much more functionality later, so I chose to handle the dictionary stuff myself.

I then had to write unit tests for this class, and I chose to do all my unit tests using a framework called pytest.

```
# 29ec1fedbf307e3b7ca731c4a381535fec899b0b
        # tests/test matrix wrapper.py
        """Test the MatrixWrapper class."""
 3
        import numpy as np
        import pytest
        from lintrans.matrices import MatrixWrapper
        valid_matrix_names = 'ABCDEFGHJKLMNOPQRSTUVWXYZ'
 8
        test_matrix = np.array([[1, 2], [4, 3]])
10
11
        @pytest.fixture
12
        def wrapper() -> MatrixWrapper:
            """Return a new MatrixWrapper object."""
13
            return MatrixWrapper()
14
15
16
17
        def test_get_matrix(wrapper) -> None:
             """Test MatrixWrapper.__getitem__()."""
18
19
            for name in valid_matrix_names:
20
                assert wrapper[name] is None
21
22
            assert (wrapper['I'] == np.array([[1, 0], [0, 1]])).all()
23
24
25
        def test_get_name_error(wrapper) -> None:
             """Test that MatrixWrapper.__getitem__() raises a KeyError if called with an invalid name."""
26
27
            with pytest.raises(KeyError):
                _ = wrapper['bad name']
28
                _ = wrapper['123456']
29
                _ = wrapper['Th15 Is an 1nV@l1D n@m3']
30
31
                _ = wrapper['abc']
32
33
34
        def test_set_matrix(wrapper) -> None:
            """Test MatrixWrapper.__setitem__()."""
35
36
            for name in valid_matrix_names:
37
                wrapper[name] = test_matrix
38
                assert (wrapper[name] == test_matrix).all()
39
40
41
        def test_set_identity_error(wrapper) -> None:
             """Test that MatrixWrapper.__setitem__() raises a NameError when trying to assign to I."""
42
43
            with pytest.raises(NameError):
44
                wrapper['I'] = test_matrix
45
46
47
        def test set name error(wrapper) -> None:
            """Test that MatrixWrapper.__setitem__() raises a NameError when trying to assign to an invalid name."""
48
            with pvtest.raises(NameError):
50
                wrapper['bad name'] = test matrix
51
                wrapper['123456'] = test_matrix
```

```
52 wrapper['Th15 Is an 1nV@l1D n@m3'] = test_matrix
53 wrapper['abc'] = test_matrix
```

These tests are quite simple and just ensure that the expected behaviour works the way it should, and that the correct errors are raised when they should be. It verifies that matrices can be assigned, that every valid name works, and that the identity matrix  $\mathbf{I}$  cannot be assigned to.

The function decorated with <code>@pytest.fixture</code> allows functions to use a parameter called <code>wrapper</code> and <code>pytest</code> will automatically call this function and pass it as that parameter. It just saves on code repetition.

#### 3.1.2 Rudimentary parsing and evaluating

This first thing I did here was improve the <code>\_\_setitem\_\_()</code> and <code>\_\_getitem\_\_()</code> methods to validate input and easily get transposes and simple rotation matrices.

```
# f89fc9fd8d5917d07557fc50df3331123b55ad6b
        # src/lintrans/matrices/wrapper.pv
60
            def __setitem__(self, name: str, new_matrix: MatrixType) -> None:
                 """Set the value of matrix `name` with the new_matrix.
61
62
63
                :param str name: The name of the matrix to set the value of
64
                :param MatrixType new_matrix: The value of the new matrix
65
66
67
                :raises NameError: If the name isn't a valid matrix name or is 'I'
68
                if name not in self._matrices.keys():
69
                    raise NameError('Matrix name must be a single capital letter')
70
71
                if name == 'I':
73
                    raise NameError('Matrix name cannot be "I"')
74
75
                # All matrices must have float entries
76
                a = float(new_matrix[0][0])
                b = float(new_matrix[0][1])
78
                c = float(new_matrix[1][0])
79
                d = float(new_matrix[1][1])
80
                self._matrices[name] = np.array([[a, b], [c, d]])
81
```

In this method, I'm now casting all the values to floats. This is very simple validation, since this cast will raise **ValueError** if it fails to cast the value to a float. I should've declared :raises ValueError: in the docstring, but this was an oversight at the time.

```
# f89fc9fd8d5917d07557fc50df3331123b55ad6b
        # src/lintrans/matrices/wrapper.py
            def __getitem__(self, name: str) -> Optional[MatrixType]:
28
                  ""Get the matrix with the given name.
29
30
                If it is a simple name, it will just be fetched from the dictionary.
                If the name is followed with a 't', then we will return the transpose of the named matrix.
                If the name is 'rot()', with a given angle in degrees, then we return a new rotation matrix with that angle.
32
                :param str name: The name of the matrix to get
                :returns: The value of the matrix (may be none)
35
36
                :rtype: Optional[MatrixType]
37
                :raises NameError: If there is no matrix with the given name
38
39
40
                # Return a new rotation matrix
```

```
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```

```
match = re.match(r'rot(((d+)))', name)
42
                if match is not None:
43
                    return create_rotation_matrix(float(match.group(1)))
44
45
                # Return the transpose of this matrix
46
                match = re.match(r'([A-Z])t', name)
                if match is not None:
47
                    matrix = self[match.group(1)]
48
49
50
                    if matrix is not None:
51
                        return matrix.T
52
                    else:
53
                        return None
54
55
                if name not in self._matrices:
56
                    raise NameError(f'Unrecognised matrix name "{name}"')
57
58
                return self._matrices[name]
```

This <code>\_\_getitem\_\_()</code> method now allows for easily accessing transposes and rotation matrices by checking input with regular expressions. This makes getting matrices easier and thus makes evaluating full expressions simpler.

The create\_rotation\_matrix() method is also defined in this file and just uses the  $\begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$  formula from before:

```
# f89fc9fd8d5917d07557fc50df3331123b55ad6b
         # src/lintrans/matrices/wrapper.py
158
         def create_rotation_matrix(angle: float) -> MatrixType:
159
             """Create a matrix representing a rotation by the given number of degrees anticlockwise.
160
161
             :param float angle: The number of degrees to rotate by
162
             :returns MatrixType: The resultant rotation matrix
163
             rad = np.deg2rad(angle)
164
165
             return np.array([
166
                 [np.cos(rad), -1 * np.sin(rad)],
167
                 [np.sin(rad), np.cos(rad)]
168
             1)
```

At this stage, I also implemented a simple parser and evaluator using regular expressions. It's not great and it's not very flexible, but it can evaluate simple expressions.

```
# f89fc9fd8d5917d07557fc50df3331123b55ad6b
         # src/lintrans/matrices/wrapper.py
83
             def parse_expression(self, expression: str) -> MatrixType:
                 """Parse a given expression and return the matrix for that expression.
84
85
86
                 Expressions are written with standard LaTeX notation for exponents. All whitespace is ignored.
87
88
                 Here is documentation on syntax:
89
                     A single matrix is written as 'A'.
90
                     Matrix A multiplied by matrix B is written as 'AB'
91
                     Matrix A plus matrix B is written as 'A+B'
92
                     Matrix A minus matrix B is written as 'A-B'
93
                     Matrix A squared is written as 'A^2'
94
                     Matrix A to the power of 10 is written as 'A^10' or 'A^{10}'
95
                     The inverse of matrix A is written as 'A^-1' or 'A^{-1}
                     The transpose of matrix A is written as 'A^T' or 'At'
96
97
98
                 :param str expression: The expression to be parsed
99
                 :returns MatrixType: The matrix result of the expression
100
101
                 :raises ValueError: If the expression is invalid, such as an empty string
102
```

```
if expression == '':
103
104
                     raise ValueError('The expression cannot be an empty string')
105
                 match = re.search(r'[^-+A-Z^{{}}rot()\d.]', expression)
106
107
                 if match is not None:
108
                     raise ValueError(f'Invalid character "{match.group(0)}"')
109
                 # Remove all whitespace in the expression
110
                 expression = re.sub(r'\s', '', expression)
111
112
                 # Wrap all exponents and transposition powers with {}
113
                 expression = re.sub(r'(?<=\^)(-?\d+|T)(?=[^{}]|\$)', r'{\g<0>}', expression)
114
115
116
                 # Replace all subtractions with additions, multiplied by -1
117
                 expression = re.sub(r'(? <= .) - (? = [A-Z])', '+-1', expression)
118
119
                 # Replace a possible leading minus sign with -1
                 expression = re.sub(r'^-(?=[A-Z])', '-1', expression)
120
121
122
                 # Change all transposition exponents into lowercase
123
                 expression = expression.replace('^{T}', 't')
124
125
                 # Split the expression into groups to be multiplied, and then we add those groups at the end
126
                 # We also have to filter out the empty strings to reduce errors
127
                 multiplication_groups = [x for x in expression.split('+') if x != '']
128
129
                 # Start with the O matrix and add each group on
                 matrix_sum: MatrixType = np.array([[0., 0.], [0., 0.]])
130
131
132
                 for group in multiplication_groups:
                     # Generate a list of tuples, each representing a matrix
133
                     # These tuples are (the multiplier, the matrix (with optional
134
135
                     # 't' at the end to indicate a transpose), the exponent)
136
                     string_matrices: list[tuple[str, str, str]]
137
                     # The generate tuple is (multiplier, matrix, full exponent, stripped exponent)
138
139
                     # The full exponent contains ^{}, so we ignore it
                     # The multiplier and exponent might be '', so we have to set them to '1'
140
                     string\_matrices = [(t[0] if t[0] != '' else '1', t[1], t[3] if t[3] != '' else '1')
141
142
                                        for t in re.findall(r'(-?\d^*).(A-Z]t?|rot(\d^*))(^{(-?\d^+|T)})?', group)]
143
                     # This list is a list of tuple, where each tuple is (a float multiplier,
145
                     # the matrix (gotten from the wrapper's __getitem__()), the integer power)
146
                     matrices: list[tuple[float, MatrixType, int]]
147
                     matrices = [(float(t[0]), self[t[1]], int(t[2]))  for t in string matrices]
148
                     # Process the matrices and make actual MatrixType objects
149
150
                     processed_matrices: list[MatrixType] = [t[0] * np.linalg.matrix_power(t[1], t[2]) for t in matrices]
151
152
                     # Add this matrix product to the sum total
153
                     matrix_sum += reduce(lambda m, n: m @ n, processed_matrices)
154
```

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I think the comments in the code speak for themselves, but we basically split the expression up into groups to be added, and then for each group, we multiply every matrix in that group to get its value, and then add all these values together at the end.

This code is objectively bad. At the time of writing, it's now quite old, so I can say that. This code has no real error handling, and line 48 introduces the glaring error that 'A++B' is now a valid expression because we disregard empty strings. Not to mention the fact that the method is called parse\_expression() but actually evaluates an expression. All these issues will be fixed in the future, but this was the first implementation of matrix evaluation, and it does the job decently well.

I then implemented several tests for this parsing.

```
# 60e0c713b244e097bab8ee0f71142b709fde1a8b
# tests/test matrix wrapper parse expression.py
```

return matrix sum

155

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assert (wrapper.parse\_expression('AI') == wrapper['A']).all()

assert (wrapper.parse\_expression('IA') == wrapper['A']).all()

72

73

```
assert (wrapper.parse_expression('GI') == wrapper['G']).all()
 75
            assert (wrapper.parse_expression('IG') == wrapper['G']).all()
 76
 77
            assert (wrapper.parse_expression('EID') == wrapper['E'] @ wrapper['D']).all()
 78
            assert (wrapper.parse_expression('IED') == wrapper['E'] @ wrapper['D']).all()
 79
            assert (wrapper.parse_expression('EDI') == wrapper['E'] @ wrapper['D']).all()
            assert (wrapper.parse_expression('IEIDI') == wrapper['E'] @ wrapper['D']).all()
80
            assert (wrapper.parse_expression('EI^3D') == wrapper['E'] @ wrapper['D']).all()
81
82
83
        def test_simple_three_matrix_multiplication(wrapper: MatrixWrapper) -> None:
84
             """Test simple multiplication of two matrices."""
85
86
            assert wrapper['A'] is not None and wrapper['B'] is not None and wrapper['C'] is not None and \
                   87
88
                    wrapper['G'] is not None
89
Q٨
            assert (wrapper.parse_expression('ABC') == wrapper['A'] @ wrapper['B'] @ wrapper['C']).all()
91
            assert (wrapper.parse_expression('ACB') == wrapper['A'] @ wrapper['C'] @ wrapper['B']).all()
            assert (wrapper.parse_expression('BAC') == wrapper['B'] @ wrapper['A'] @ wrapper['C']).all()
92
93
            assert (wrapper.parse_expression('EFG') == wrapper['E'] @ wrapper['F'] @ wrapper['G']).all()
94
            assert (wrapper.parse_expression('DAC') == wrapper['D'] @ wrapper['A'] @ wrapper['C']).all()
            assert \ (wrapper.parse\_expression('GAE') == wrapper['G'] \ @ \ wrapper['A'] \ @ \ wrapper['E']).all()
95
            assert (wrapper.parse_expression('FAG') == wrapper['F'] @ wrapper['A'] @ wrapper['G']).all()
96
            assert (wrapper.parse_expression('GAF') == wrapper['G'] @ wrapper['A'] @ wrapper['F']).all()
97
98
99
100
        def test_matrix_inverses(wrapper: MatrixWrapper) -> None:
             """Test the inverses of single matrices."""
101
102
            assert wrapper['A'] is not None and wrapper['B'] is not None and wrapper['C'] is not None and \
                   wrapper['D'] is not None and wrapper['E'] is not None and wrapper['F'] is not None and \
103
104
                    wrapper['G'] is not None
105
            assert (wrapper.parse_expression('A^{-1}') == la.inv(wrapper['A'])).all()
106
            assert (wrapper.parse_expression('B^{-1}') == la.inv(wrapper['B'])).all()
107
            assert (wrapper.parse_expression('C^{-1}') == la.inv(wrapper['C'])).all()
108
109
            assert (wrapper.parse_expression('D^{-1}') == la.inv(wrapper['D'])).all()
110
            assert (wrapper.parse_expression('E^{-1}') == la.inv(wrapper['E'])).all()
            assert (wrapper.parse_expression('F^{-1}') == la.inv(wrapper['F'])).all()
111
112
             assert (wrapper.parse_expression('G^{-1}') == la.inv(wrapper['G'])).all()
113
114
            assert (wrapper.parse_expression('A^-1') == la.inv(wrapper['A'])).all()
            assert (wrapper.parse_expression('B^-1') == la.inv(wrapper['B'])).all()
115
            assert (wrapper.parse_expression('C^-1') == la.inv(wrapper['C'])).all()
116
117
            assert (wrapper.parse_expression('D^-1') == la.inv(wrapper['D'])).all()
            assert (wrapper.parse_expression('E^-1') == la.inv(wrapper['E'])).all()
118
            assert (wrapper.parse_expression('F^-1') == la.inv(wrapper['F'])).all()
119
            assert (wrapper.parse_expression('G^-1') == la.inv(wrapper['G'])).all()
120
121
122
         def test_matrix_powers(wrapper: MatrixWrapper) -> None:
123
124
             ""Test that matrices can be raised to integer powers."""
125
             assert wrapper['A'] is not None and wrapper['B'] is not None and wrapper['C'] is not None and \
126
                   wrapper['D'] is not None and wrapper['E'] is not None and wrapper['F'] is not None and \
127
                   wrapper['G'] is not None
128
            assert (wrapper.parse expression('A^2') == la.matrix power(wrapper['A'], 2)).all()
129
130
            assert (wrapper.parse_expression('B^4') == la.matrix_power(wrapper['B'], 4)).all()
            assert (wrapper.parse_expression('C^{12}') == la.matrix_power(wrapper['C'], 12)).all()
131
            assert (wrapper.parse_expression('D^12') == la.matrix_power(wrapper['D'], 12)).all()
132
133
            assert (wrapper.parse_expression('E^8') == la.matrix_power(wrapper['E'], 8)).all()
134
            assert (wrapper.parse_expression('F^{-6}') == la.matrix_power(wrapper['F'], -6)).all()
135
            assert (wrapper.parse_expression('G^-2') == la.matrix_power(wrapper['G'], -2)).all()
```

These test lots of simple expressions, but don't test any more complicated expressions, nor do they test any validation, mostly because validation doesn't really exist at this point. 'A++B' is still a valid expression and is equivalent to 'A+B'.

#### 3.1.3 Simple matrix expression validation

My next major step was to implement proper parsing, but I procrastinated for a while and first implemented proper validation.

```
# 39b918651f60bc72bc19d2018075b24a6fc3af17
        # src/lintrans/_parse/matrices.py
9
        def compile_valid_expression_pattern() -> Pattern[str]:
10
            """Compile the single regular expression that will match a valid matrix expression."""
11
           digit_no_zero = '[123456789]'
           digits = '\\d+'
12
13
            integer_no_zero = '-?' + digit_no_zero + '(' + digits + ')?'
14
            15
            index_content = f'({integer_no_zero}|T)'
16
            index = f'(\\^\\{{\index_content}\\}}|\\^{\index_content}|t)'
17
           matrix_identifier = f'([A-Z]|rot\\({real_number}\\))'
           matrix = '(' + real_number + '?' + matrix_identifier + index + '?)'
19
20
            expression = f'\{matrix\}+(()+|-)\{matrix\}+)*'
21
            return re.compile(expression)
23
24
25
        # This is an expensive pattern to compile, so we compile it when this module is initialized
26
        valid_expression_pattern = compile_valid_expression_pattern()
27
28
29
       def validate_matrix_expression(expression: str) -> bool:
             ""Validate the given matrix expression.
30
31
32
           This function simply checks the expression against a BNF schema. It is not
           aware of which matrices are actually defined in a wrapper. For an aware
           version of this function, use the MatrixWrapper().is_valid_expression() method.
34
35
36
           Here is the schema for a valid expression given in a version of BNF:
37
                                 ::= matrices { ( "+" | "-" ) matrices };
38
               expression
39
               matrices
                                 ::= matrix { matrix };
40
               matrix
                                ::= [ real_number ] matrix_identifier [ index ];
               matrix_identifier ::= "A" .. "Z" | "rot(" real_number ")";
41
                                 ::= "^{" index_content "}" | "^" index_content | "t";
42
                                ::= integer_not_zero | "T";
43
               index content
44
45
               digit_no_zero
                                 ::= "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
                                ::= "0" | digit_no_zero;
46
               digit
47
                                 ::= digit | digits digit;
               digits
               integer_not_zero ::= [ "-" ] digit_no_zero [ digits ];
48
                                ::= ( integer_not_zero [ "." digits ] | [ "-" ] [ "0" ] "." digits );
49
               real_number
51
            :param str expression: The expression to be validated
52
            :returns bool: Whether the expression is valid according to the schema
53
54
           match = valid expression pattern.match(expression)
55
            return expression == match.group(0) if match is not None else False
```

Here, I'm using a BNF schema to programmatically generate a regular expression. I use a function to generate this pattern and assign it to a variable when the module is initialized. This is because the pattern compilation is expensive and it's more efficient to compile the pattern once and then just use it in the validate\_matrix\_expression() function.

I also created a method is\_valid\_expression() in MatrixWrapper, which just validates a given expression. It uses the aforementioned validate\_matrix\_expression() and also checks that every matrix referenced in the expression is defined in the wrapper.

```
# 39b918651f60bc72bc19d2018075b24a6fc3af17
# src/lintrans/matrices/wrapper.py
```

```
def is_valid_expression(self, expression: str) -> bool:
100
                   ""Check if the given expression is valid, using the context of the wrapper,
101
102
                 This method calls _parse.validate_matrix_expression(), but also ensures
103
                 that all the matrices in the expression are defined in the wrapper.
104
105
                 :param str expression: The expression to validate
106
                 :returns bool: Whether the expression is valid according the schema
107
                 # Get rid of the transposes to check all capital letters
108
                 expression = re.sub(r'\^T', 't', expression)
109
                 expression = re.sub(r'\^{T}', 't', expression)
110
111
                 # Make sure all the referenced matrices are defined
112
                 for matrix in {x for x in expression if re.match('[A-Z]', x)}:
113
114
                     if self[matrix] is None:
115
                         return False
116
117
                 return _parse.validate_matrix_expression(expression)
```

I then implemented some simple tests to make sure the function works with valid and invalid expressions.

```
# a0fb029f7da995803c24ee36e7e8078e5621f676
         # tests/ parse/test parse and validate expression.pv
         """Test the _parse.matrices module validation and parsing."""
 2
         import pytest
         from lintrans._parse import validate_matrix_expression
         valid_inputs: list[str] = [
             'A', 'AB', '3A', '1.2A', '-3.4A', 'A^2', 'A^-1', 'A^{-1}', 'A^{-1}', 'A^12', 'A^T', 'A^{5}', 'A^{T}', '4.3A^7', '9.2A^{18}',
 8
             'rot(45)', 'rot(12.5)', '3rot(90)',
10
11
             'rot(135)^3', 'rot(51)^T', 'rot(-34)^-1',
12
             'A+B', 'A+2B', '4.3A+9B', 'A^2+B^T', '3A^7+0.8B^{16}',
13
             'A-B', '3A-4B', '3.2A^3-16.79B^T', '4.752A^{17}-3.32B^{36}', 'A--1B', '-A', '--1A'
15
16
             '3A4B', 'A^TB', 'A^{T}B', '4A^6B^3',
17
             '2A^{3}4B^5', '4rot(90)^3', 'rot(45)rot(13)',
18
             'Arot(90)', 'AB^2', 'A^2B^2', '8.36A^T3.4B^12',
19
20
21
             '3.5A^{4}5.6rot(19.2)^T-B^{-1}4.1C^5',
22
23
24
         invalid_inputs: list[str] = [
              '', 'rot()', 'A^', 'A^1.2', 'A^{3.4}', '1,2A', 'ro(12)', '5', '12^2',
25
             '^T', '^{12}', 'A^{13', 'A^3}', 'A^A', '^2', 'A--B', '--A'
26
27
28
             'This is 100% a valid matrix expression, I swear'
29
        1
30
31
        @pytest.mark.parametrize('inputs,output', [(valid_inputs, True), (invalid_inputs, False)])
32
33
         def test_validate_matrix_expression(inputs: list[str], output: bool) -> None:
             """Test the validate_matrix_expression() function.
34
35
             for inp in inputs:
                 assert validate_matrix_expression(inp) == output
```

Here, we test some valid data, some definitely invalid data, and some edge cases. At this stage, 'A--1B' was considered a valid expression. This was a quirk of the validator at the time, but I fixed it later. This should obviously be an invalid expression, especially since 'A--B' is considered invalid, but 'A--1B' is valid.

The <code>@pytest.mark.parametrize</code> decorator on line 35 means that <code>pytest</code> will run one test for valid inputs, and then another test for invalid inputs, and these will count as different tests. This makes it easier to see which tests failed and then debug the app.

#### 3.1.4 Parsing matrix expressions

Parsing is quite an interesting problem and something I didn't feel able to tackle head-on, so I wrote the unit tests first. I had a basic idea of what I wanted the parser to return, but no real idea of how to implement that. My unit tests looked like this:

```
# e9f7a81892278fe70684562052f330fb3a02bf9b
          # tests/_parse/test_parse_and_validate_expression.py
40
          expressions_and_parsed_expressions: list[tuple[str, MatrixParseList]] = [
41
              # Simple expressions
              ('A', [[('', 'A', '')]]),
('A^2', [[('', 'A', '2')]]),
42
43
              ('A^{2}', [[('', 'A', '2')]]),
('3A', [[('3', 'A', '')]]),
44
45
46
              ('1.4A^3', [[('1.4', 'A', '3')]]),
47
48
              # Multiplications
              ('4A^{3} 6B^2', [[('4', 'A', '3'), ('6', 'B', '2')]]),
49
              ('4.2A^{T} 6.1B^-1', [[('4.2', 'A', 'T'), ('6.1', 'B', '-1')]]), ('-1.2A^2 rot(45)^2', [[('-1.2', 'A', '2'), ('', 'rot(45)', '2')]]),
50
51
              ('3.2A^T 4.5B^{5} 9.6rot(121.3)', [[('3.2', 'A', 'T'), ('4.5', 'B', '5'), ('9.6', 'rot(121.3)', '')]]), ('-1.18A^{-2} 0.1B^{2} 9rot(34.6)^-1', [[('-1.18', 'A', '-2'), ('0.1', 'B', '2'), ('9', 'rot(34.6)', '-1')]]),
52
53
54
55
              # Additions
56
              ('A + B', [[('', 'A', '')], [('', 'B', '')]]),
              ('A + B - C', [[('', 'A', '')], [('', 'B', '')], [('-1', 'C', '')]]),
('2A^3 + 8B^T - 3C^-1', [[('2', 'A', '3')], [('8', 'B', 'T')], [('-3', 'C', '-1')]]),
57
58
59
60
              # Additions with multiplication
              ('2.14A^{3} 4.5rot(14.5)^-1 + 8B^T - 3C^-1', [[('2.14', 'A', '3'), ('4.5', 'rot(14.5)', '-1')],
61
                                                                     [('8', 'B', 'T')], [('-3', 'C', '-1')]]),
62
              ('2.14A^{3} 4.5rot(14.5)^-1 + 8.5B^T 5.97C^4 - 3.14D^{-1} 6.7E^T',
63
               [[('2.14', 'A', '3'), ('4.5', 'rot(14.5)', '-1')], [('8.5', 'B', 'T'), ('5.97', 'C', '4')],
64
65
                [('-3.14', 'D', '-1'), ('6.7', 'E', 'T')]]),
         1
66
67
68
69
          @pytest.mark.skip(reason='parse_matrix_expression() not implemented')
70
          def test_parse_matrix_expression() -> None:
71
               """Test the parse_matrix_expression() function."""
              for expression, parsed_expression in expressions_and_parsed_expressions:
73
                   # Test it with and without whitespace
74
                   assert parse matrix expression(expression) == parsed expression
75
                   assert parse_matrix_expression(expression.replace(' ', '')) == parsed_expression
```

I just had example inputs and what I expected as output. I also wanted the parser to ignore whitespace. The decorator on line 33 just skips the test because the parser wasn't implemented yet.

When implementing the parser, I first had to tighten up validation to remove anomalies like 'A--1B' being valid. I did this by factoring out the optional minus signs from being part of a number, to being optionally in front of a number. This eliminated this kind of repetition and made 'A--1B' invalid, as it should be.

```
# fd80d8d3b0e975e92dcc7c10f1f0f1276879f408
# src/lintrans/_parse/matrices.py

def compile_valid_expression_pattern() -> Pattern[str]:
    """Compile the single regular expression that will match a valid matrix expression."""
    digit_no_zero = '[123456789]'
    digits = '\\d+'
```

```
36
            integer_no_zero = digit_no_zero + '(' + digits + ')?'
37
            real_number = f'({integer_no_zero}(\\.{digits})?|0?\\.{digits})'
38
39
            index_content = f'(-?{integer_no_zero}|T)'
40
            index = f'(\\^\\{{index_content}\\}}|\\^{index_content}|t)'
41
            matrix_identifier = f'([A-Z]|rot\\(-?{real_number}\\))'
            matrix = '(' + real_number + '?' + matrix_identifier + index + '?)'
42
43
            expression = f'-?{matrix}+(()+|-){matrix}+)*'
44
            return re.compile(expression)
```

The code can be a bit hard to read with all the RegEx stuff, but the BNF illustrates these changes nicely.

Compare the old version:

```
# 39b918651f60bc72bc19d2018075b24a6fc3af17
        # src/lintrans/_parse/matrices.py
                         ::= matrices { ( "+" | "-" ) matrices };
38
       expression
39
       matrices
                         ::= matrix { matrix };
40
       matrix
                         ::= [ real_number ] matrix_identifier [ index ];
       matrix_identifier ::= "A" .. "Z" | "rot(" real_number ")";
41
                        ::= "^{" index_content "}" | "^" index_content | "t";
42
        index
                        ::= integer_not_zero | "T";
43
        index content
44
                       ::= "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
45
        digit_no_zero
                         ::= "0" | digit_no_zero;
46
       diait
47
       digits
                         ::= digit | digits digit;
48
        integer_not_zero ::= [ "-" ] digit_no_zero [ digits ];
                        ::= ( integer_not_zero [ "." digits ] | [ "-" ] [ "0" ] "." digits );
49
        real number
        to the new version:
        # fd80d8d3b0e975e92dcc7c10f1f0f1276879f408
        # src/lintrans/_parse/matrices.py
                         ::= [ "-" ] matrices { ( "+" | "-" ) matrices };
61
        expression
62
       matrices
                        ::= matrix { matrix };
63
       matrix
                         ::= [ real_number ] matrix_identifier [ index ];
64
       matrix_identifier ::= "A" .. "Z" | "rot(" [ "-" ] real_number ")";
                        ::= "^{" index_content "}" | "^" index_content | "t";
65
        index
66
        index_content
                      ::= [ "-" ] integer_not_zero | "T";
67
68
                         ::= "1" | "2" | "3" | "4" | "5" | "6" | "7" | "8" | "9";
       digit_no_zero
                         ::= "0" | digit_no_zero;
69
        digit
70
        digits
                         ::= digit | digits digit;
71
        integer_not_zero ::= digit_no_zero [ digits ];
72
        real_number
                         ::= ( integer_not_zero [ "." digits ] | [ "0" ] "." digits );
```

Then once I'd fixed the validation, I could implement the parser itself.

```
# fd80d8d3b0e975e92dcc7c10f1f0f1276879f408
        # src/lintrans/_parse/matrices.py
86
        def parse_matrix_expression(expression: str) -> MatrixParseList:
87
             ""Parse the matrix expression and return a list of results.
88
89
            The return value is a list of results. This results list contains lists of tuples.
90
            The top list is the expressions that should be added together, and each sublist
91
            is expressions that should be multiplied together. These expressions to be
92
            multiplied are tuples, where each tuple is (multiplier, matrix identifier, index).
93
            The multiplier can be any real number, the matrix identifier is either a named
            matrix or a new rotation matrix declared with 'rot()', and the index is an
94
95
            integer or 'T' for transpose.
96
```

```
:param str expression: The expression to be parsed
98
             :returns MatrixParseTuple: A list of results
99
100
             # Remove all whitespace
101
             expression = re.sub(r'\s', '', expression)
102
103
             # Check if it's valid
             if not validate_matrix_expression(expression):
104
105
                 raise MatrixParseError('Invalid expression')
106
107
             # Wrap all exponents and transposition powers with {}
             expression = re.sub(r'(?<=\^)(-?\d+|T)(?=[^{}]|\$)', r'{\g<0>}', expression)
108
109
110
             # Remove any standalone minuses
             expression = re.sub(r'-(?=[A-Z])', '-1', expression)
111
112
113
             # Replace subtractions with additions
114
             expression = re.sub(r'-(?=\d+\.?\d*([A-Z]|rot))', '+-', expression)
115
116
             # Get rid of a potential leading + introduced by the last step
117
             expression = re.sub(r'^\+', '', expression)
118
             return [
119
120
                 Ε
121
                     # The tuple returned by re.findall is (multiplier, matrix identifier, full index, stripped index),
122
                     # so we have to remove the full index, which contains the {}
123
                     (t[0], t[1], t[3])
124
                     for t in re.findall(r'(-?\d+\..?\d^*)?([A-Z]|rot\(-?\d+\..?\d^*\))(\^{(-?\d+|T)})?', group)
125
                 \# We just split the expression by '+' to have separate groups
126
127
                 for group in expression.split('+')
128
             1
```

It works similarly to the old MatrixWrapper.parse\_expression() method in §3.1.2 but with a powerful list comprehension at the end. It splits the expression up into groups and then uses some RegEx magic to find all the matrices in these groups as a tuple.

This method passes all the unit tests, as expected.

My next step was then to rewrite the evaluation to use this new parser, like so (method name and docstring removed):

```
# a453774bcdf824676461f9b9b441d7b94969ea55
         # src/lintrans/matrices/wrapper.py
168
                 if not self.is_valid_expression(expression):
169
                     raise ValueError('The expression is invalid')
170
171
                 parsed_result = _parse.parse_matrix_expression(expression)
172
                 final_groups: list[list[MatrixType]] = []
173
174
                 for group in parsed_result:
175
                     f_group: list[MatrixType] = []
176
177
                     for matrix in group:
                         if matrix[2] == 'T':
178
179
                             m = self[matrix[1]]
180
                             assert m is not None
181
                             matrix_value = m.T
                         else:
182
183
                             matrix_value = np.linalg.matrix_power(self[matrix[1]],
                                                                    1 if (index := matrix[2]) == '' else int(index))
184
185
                         matrix_value *= 1 if (multiplier := matrix[0]) == '' else float(multiplier)
186
187
                         f_group.append(matrix_value)
188
189
                     final_groups.append(f_group)
190
191
                 return reduce(add, [reduce(matmul, group) for group in final_groups])
```

Here, we go through the list of tuples and evaluate the matrix represented by each tuple, putting this together in a list as we go. Then at the end, we simply reduce the sublists and then reduce these new matrices using a list comprehension in the reduce() call using add and matmul from the operator library. It's written in a functional programming style, and it passes all the previous tests.

#### 3.2 Initial GUI

#### 3.2.1 First basic GUI

The discrepancy in all the GUI code between snake\_case and camelCase is because Qt5 was originally a C++ framework that was adapted into PyQt5 for Python. All the Qt API is in camelCase, but my Python code is in snake\_case.

```
# 93ce763f7b993439fc0da89fad39456d8cc4b52c
        # src/lintrans/qui/main window.py
        """The module to provide the main window as a QMainWindow object."""
 3
        import sys
        from PyQt5 import QtCore, QtGui, QtWidgets
        from PyQt5.QtWidgets import QApplication, QHBoxLayout, QMainWindow, QVBoxLayout
 8
        from lintrans.matrices import MatrixWrapper
10
11
        class LintransMainWindow(QMainWindow):
12
            """The class for the main window in the lintrans GUI."""
13
14
            def __init__(self):
                 """Create the main window object, creating every widget in it."""
15
16
                super().__init__()
17
                self.matrix_wrapper = MatrixWrapper()
18
19
20
                self.setWindowTitle('Linear Transformations')
21
                self.setMinimumWidth(750)
23
                # === Create widgets
24
25
                # Left layout: the plot and input box
26
27
                # NOTE: This QGraphicsView is only temporary
28
                self.plot = QtWidgets.QGraphicsView(self)
29
                self.text_input_expression = QtWidgets.QLineEdit(self)
31
                self.text_input_expression.setPlaceholderText('Input matrix expression...')
32
                \verb|self.text_input_expression.textChanged.connect(self.update_render_buttons)| \\
33
34
                # Right layout: all the buttons
35
36
                # Misc buttons
37
                self.button_create_polygon = QtWidgets.QPushButton(self)
38
39
                self.button_create_polygon.setText('Create polygon')
40
                # TODO: Implement create_polygon()
                # self.button_create_polygon.clicked.connect(self.create_polygon)
                \verb|self.button_create_polygon.setToolTip('Define a new polygon to view the transformation of')| \\
42
43
                self.button_change_display_settings = QtWidgets.QPushButton(self)
45
                {\tt self.button\_change\_display\_settings.setText('Change \verb| ndisplay settings')}
46
                # TODO: Implement change_display_settings()
47
                # self.button_change_display_settings.clicked.connect(self.change_display_settings)
48
                self.button_change_display_settings.setToolTip('Change which things are rendered on the plot')
50
                # Define new matrix buttons
51
```

Centre number: 123456

```
self.label_define_new_matrix = QtWidgets.QLabel(self)
53
                 self.label_define_new_matrix.setText('Define a\nnew matrix')
                 self.label_define_new_matrix.setAlignment(QtCore.Qt.AlignCenter)
 54
 55
 56
                 # TODO: Implement defining a new matrix visually, numerically, as a rotation, and as an expression
57
 58
                 self.button_define_visually = QtWidgets.QPushButton(self)
                 self.button_define_visually.setText('Visually')
59
60
                 self.button_define_visually.setToolTip('Drag the basis vectors')
 61
                 self.button define numerically = OtWidgets.OPushButton(self)
62
                 self.button_define_numerically.setText('Numerically')
 63
                 self.button_define_numerically.setToolTip('Define a matrix just with numbers')
64
65
                 self.button_define_as_rotation = QtWidgets.QPushButton(self)
 66
67
                 self.button_define_as_rotation.setText('As a rotation')
68
                 self.button_define_as_rotation.setToolTip('Define an angle to rotate by')
 69
                 self.button_define_as_expression = QtWidgets.QPushButton(self)
 70
 71
                 self.button_define_as_expression.setText('As an expression')
 72
                 self.button define as expression.setToolTip('Define a matrix in terms of other matrices')
                 # Render buttons
 74
 75
 76
                 self.button_render = QtWidgets.QPushButton(self)
 77
                 self.button_render.setText('Render')
 78
                 self.button_render.setEnabled(False)
                 self.button_render.clicked.connect(self.render_expression)
 79
 80
                 self.button_render.setToolTip('Render the expression<br/>b>(Ctrl + Enter)
81
                 self.button_render_shortcut = QtWidgets.QShortcut(QtGui.QKeySequence('Ctrl+Return'), self)
 82
83
                 self.button render shortcut.activated.connect(self.button render.click)
84
 85
                 self.button_animate = QtWidgets.QPushButton(self)
86
                 self.button_animate.setText('Animate')
                 self.button_animate.setEnabled(False)
87
88
                 self.button_animate.clicked.connect(self.animate_expression)
                 self.button_animate.setToolTip('Animate the expression<br/>cb>(Ctrl + Shift + Enter)')
89
 90
91
                 self.button_animate_shortcut = QtWidgets.QShortcut(QtGui.QKeySequence('Ctrl+Shift+Return'), self)
92
                 self.button_animate_shortcut.activated.connect(self.button_animate.click)
 93
94
                 # === Arrange widgets
95
 96
                 self.setContentsMargins(10, 10, 10, 10)
97
98
                 self.vlay_left = QVBoxLayout()
99
                 self.vlay_left.addWidget(self.plot)
100
                 self.vlay_left.addWidget(self.text_input_expression)
101
                 self.vlay_misc_buttons = QVBoxLayout()
102
103
                 self.vlay_misc_buttons.setSpacing(20)
104
                 self.vlay_misc_buttons.addWidget(self.button_create_polygon)
105
                 self.vlay_misc_buttons.addWidget(self.button_change_display_settings)
106
                 self.vlay_define_new_matrix = QVBoxLayout()
107
108
                 self.vlay_define_new_matrix.setSpacing(20)
109
                 self.vlay_define_new_matrix.addWidget(self.label_define_new_matrix)
110
                 self.vlay_define_new_matrix.addWidget(self.button_define_visually)
                 self.vlay_define_new_matrix.addWidget(self.button_define_numerically)
111
                 self.vlay_define_new_matrix.addWidget(self.button_define_as_rotation)
112
113
                 self.vlay_define_new_matrix.addWidget(self.button_define_as_expression)
114
                 self.vlay render = QVBoxLayout()
115
116
                 self.vlay_render.setSpacing(20)
117
                 self.vlay_render.addWidget(self.button_animate)
                 self.vlay_render.addWidget(self.button_render)
118
119
120
                 self.vlay_right = QVBoxLayout()
                 self.vlay_right.setSpacing(50)
121
122
                 self.vlay_right.addLayout(self.vlay_misc_buttons)
123
                 self.vlay right.addLayout(self.vlay define new matrix)
124
                 self.vlay_right.addLayout(self.vlay_render)
```

```
125
126
                 self.hlay_all = QHBoxLayout()
127
                 self.hlay_all.setSpacing(15)
128
                 self.hlay_all.addLayout(self.vlay_left)
129
                 self.hlay_all.addLayout(self.vlay_right)
130
                 self.central_widget = QtWidgets.QWidget()
131
132
                 self.central widget.setLayout(self.hlay all)
133
                 self.setCentralWidget(self.central_widget)
134
135
             def update render buttons(self) -> None:
                  """Enable or disable the render and animate buttons according to the validity of the matrix expression."""
136
137
                 valid = self.matrix_wrapper.is_valid_expression(self.text_input_expression.text())
138
                 self.button_render.setEnabled(valid)
139
                 self.button_animate.setEnabled(valid)
140
141
             def render_expression(self) -> None:
142
                  """Render the expression in the input box, and then clear the box."""
                 # TODO: Render the expression
143
144
                 self.text_input_expression.setText('')
145
146
             def animate_expression(self) -> None:
                 """Animate the expression in the input box, and then clear the box."""
147
148
                 # TODO: Animate the expression
149
                 self.text_input_expression.setText('')
150
151
152
         def main() -> None:
             """Run the GUI."""
153
154
             app = QApplication(sys.argv)
155
             window = LintransMainWindow()
156
             window.show()
157
             sys.exit(app.exec_())
158
159
160
         if __name__ == '__main__':
161
             main()
```

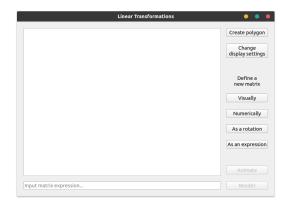


Figure 5: The first version of the GUI

A lot of the methods here don't have implementations yet, but they will. This version is just a very early prototype to get a rough draft of the GUI.

I create the widgets and layouts in the constructor as well as configuring all of them. The most important non-constructor method is update\_render\_buttons(). It gets called whenever the text in text\_input\_expression is changed. This happens because we connect it to the textChanged signal on line 35.

The big white box here will eventually be replaced with an actual viewport. This is just a prototype.

#### 3.2.2 Numerical definition dialog

3

4

My next major addition was a dialog that would allow the user to define a matrix numerically.

```
# cedbd3ed126a1183f197c27adf6dabb4e5d301c7
# src/lintrans/gui/dialogs/define_new_matrix.py
"""The module to provide dialogs for defining new matrices."""
from numpy import array
from PyQt5 import QtGui, QtWidgets
from PyQt5.QtWidgets import QDialog, QGridLayout, QHBoxLayout, QVBoxLayout
```

```
6
               from lintrans.matrices import MatrixWrapper
 8
 9
               ALPHABET_NO_I = 'ABCDEFGHJKLMNOPQRSTUVWXYZ'
10
11
               def is_float(string: str) -> bool:
                       """Check if a string is a float."""
13
14
15
                              float(string)
16
                              return True
                       except ValueError:
17
18
                             return False
19
20
21
               class DefineNumericallyDialog(QDialog):
22
                       """The dialog class that allows the user to define a new matrix numerically."""
23
                      def __init__(self, matrix_wrapper: MatrixWrapper, *args, **kwargs):
24
25
                               """Create the dialog, but don't run it yet.
26
27
                              :param matrix_wrapper: The MatrixWrapper that this dialog will mutate
28
                              :type matrix_wrapper: MatrixWrapper
29
30
                              super().__init__(*args, **kwargs)
31
32
                              self.matrix_wrapper = matrix_wrapper
33
                              self.setWindowTitle('Define a matrix')
34
35
                              # === Create the widgets
36
                              self.button_confirm = QtWidgets.QPushButton(self)
37
38
                              self.button_confirm.setText('Confirm')
39
                              self.button_confirm.setEnabled(False)
                              self.button_confirm.clicked.connect(self.confirm_matrix)
40
41
                              self.button_confirm.setToolTip('Confirm this as the new matrix<br><<b>(Ctrl + Enter)</b>')
42
43
                              QtWidgets. QShortcut(QtGui.QKeySequence('Ctrl+Return'), self). activated.connect(self.button\_confirm.click) and the self-button confirm. Click) and the self-button confirm. Click (self-button\_confirm.click) are self-button confirm. Click (self-button\_confirm.click) and the self-button confirm. Click (self-button\_confirm.click) are self-button. Click (self-button\_confirm.click) are self-but
44
                              self.button_cancel = QtWidgets.QPushButton(self)
45
46
                              self.button_cancel.setText('Cancel')
47
                              self.button_cancel.clicked.connect(self.close)
48
                              self.button_cancel.setToolTip('Cancel this definition<br><b>(Ctrl + Q)</b>')
49
50
                              QtWidgets.QShortcut(QtGui.QKeySequence('Ctrl+Q'), self).activated.connect(self.button_cancel.click)
51
52
                              self.element_tl = QtWidgets.QLineEdit(self)
53
                              self.element_tl.textChanged.connect(self.update_confirm_button)
54
55
                              self.element_tr = QtWidgets.QLineEdit(self)
                              self.element_tr.textChanged.connect(self.update_confirm_button)
56
57
58
                              self.element_bl = QtWidgets.QLineEdit(self)
59
                              self.element_bl.textChanged.connect(self.update_confirm_button)
60
61
                              self.element br = QtWidgets.QLineEdit(self)
62
                              \verb|self.element_br.textChanged.connect(self.update\_confirm\_button)|\\
63
64
                              self.matrix_elements = (self.element_tl, self.element_tr, self.element_bl, self.element_br)
65
66
                              self.letter_combo_box = QtWidgets.QComboBox(self)
67
                              # Everything except I, because that's the identity
68
69
                              for letter in ALPHABET_NO_I:
70
                                     self.letter_combo_box.addItem(letter)
71
                              \verb|self.letter_combo_box.activated.connect(self.load_matrix)|\\
72
73
74
                              # === Arrange the widgets
75
76
                              self.setContentsMargins(10, 10, 10, 10)
77
78
                              self.grid_matrix = QGridLayout()
```

Centre number: 123456

```
79
                 self.grid_matrix.setSpacing(20)
80
                 self.grid_matrix.addWidget(self.element_tl, 0, 0)
81
                 self.grid_matrix.addWidget(self.element_tr, 0, 1)
82
                 self.grid_matrix.addWidget(self.element_bl, 1, 0)
83
                 self.grid_matrix.addWidget(self.element_br, 1, 1)
84
                 self.hlay_buttons = QHBoxLayout()
 85
86
                 self.hlay buttons.setSpacing(20)
87
                 self.hlay_buttons.addWidget(self.button_cancel)
 88
                 self.hlay_buttons.addWidget(self.button_confirm)
89
                 self.vlay_right = QVBoxLayout()
 90
 91
                 self.vlay_right.setSpacing(20)
92
                 self.vlay_right.addLayout(self.grid_matrix)
93
                 self.vlay_right.addLayout(self.hlay_buttons)
94
95
                 self.hlay_all = QHBoxLayout()
 96
                 self.hlay_all.setSpacing(20)
                 self.hlay_all.addWidget(self.letter_combo_box)
97
98
                 self.hlay_all.addLayout(self.vlay_right)
99
                 self.setLayout(self.hlay_all)
100
101
                 # Finally, we load the default matrix A into the boxes
102
103
                 self.load_matrix(0)
104
             def update_confirm_button(self) -> None:
105
106
                 """Enable the confirm button if there are numbers in every box."""
                 for elem in self.matrix_elements:
107
                     if elem.text() == '' or not is_float(elem.text()):
108
109
                         # If they're not all numbers, then we can't confirm it
                         self.button_confirm.setEnabled(False)
110
111
                         return
112
                 # If we didn't find anything invalid
113
114
                 \verb|self.button_confirm.setEnabled(True)|\\
115
             def load_matrix(self, index: int) -> None:
116
117
                 """If the selected matrix is defined, load it into the boxes."""
                 matrix = self.matrix_wrapper[ALPHABET_N0_I[index]]
118
119
120
                 if matrix is None:
                     for elem in self.matrix_elements:
121
122
                         elem.setText('')
123
124
                 else:
125
                     self.element_tl.setText(str(matrix[0][0]))
126
                     self.element tr.setText(str(matrix[0][1]))
127
                     self.element_bl.setText(str(matrix[1][0]))
128
                     self.element_br.setText(str(matrix[1][1]))
129
130
                 self.update_confirm_button()
131
132
             def confirm_matrix(self) -> None:
133
                 """Confirm the inputted matrix and assign it to the name."""
                 letter = self.letter_combo_box.currentText()
134
135
                 matrix = array([
                     [float(self.element_tl.text()), float(self.element_tr.text())],
136
137
                     [float(self.element_bl.text()), float(self.element_br.text())]
138
                 1)
139
```

self.matrix\_wrapper[letter] = matrix

self.close()

140141

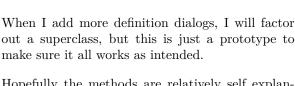




Figure 6: The first version of the numerical definition dialog

Hopefully the methods are relatively self explanatory, but they're just utility methods to update the GUI when things are changed. We connect the QLineEdit widgets to the update\_confirm\_button() slot to make sure the confirm button is always up to date.

Centre number: 123456

The confirm\_matrix() method just updates the instance's matrix wrapper with the new matrix. We pass a reference to the LintransMainWindow instance's matrix wrapper when we open the dialog, so we're just updating the referenced object directly.

In the LintransMainWindow class, we're just connecting a lambda slot to the button so that it opens the dialog, as seen here:

```
# cedbd3ed126a1183f197c27adf6dabb4e5d301c7
# src/lintrans/gui/main_window.py

66 self.button_define_numerically.clicked.connect(
67 lambda: DefineNumericallyDialog(self.matrix_wrapper, self).exec()
68 )
```

#### 3.2.3 More definition dialogs

# 5d04fb7233a03d0cd8fa0768f6387c6678da9df3

I then factored out the constructor into a DefineDialog superclass so that I could easily create other definition dialogs.

```
# src/lintrans/gui/dialogs/define_new_matrix.py
22
        class DefineDialog(QDialog):
23
             """A superclass for definitions dialogs."""
24
            def __init__(self, matrix_wrapper: MatrixWrapper, *args, **kwargs):
                 """Create the dialog, but don't run it yet.
26
27
28
                 :param matrix_wrapper: The MatrixWrapper that this dialog will mutate
29
                :type matrix_wrapper: MatrixWrapper
30
31
                super().__init__(*args, **kwargs)
33
                self.matrix_wrapper = matrix_wrapper
34
                self.setWindowTitle('Define a matrix')
35
36
                # === Create the widgets
37
                self.button_confirm = QtWidgets.QPushButton(self)
38
39
                self.button confirm.setText('Confirm')
40
                self.button_confirm.setEnabled(False)
41
                self.button_confirm.clicked.connect(self.confirm_matrix)
42
                self.button confirm.setToolTip('Confirm this as the new matrix<br/>br><b/>(Ctrl + Enter)</br/>/b>')
43
                QShortcut(QKeySequence('Ctrl+Return'), self).activated.connect(self.button_confirm.click)
45
                self.button_cancel = QtWidgets.QPushButton(self)
46
                self.button_cancel.setText('Cancel')
47
                self.button cancel.clicked.connect(self.close)
                self.button\_cancel.setToolTip('Cancel this definition < br >< b>(Ctrl + Q) < / b>')
48
49
                QShortcut(QKeySequence('Ctrl+Q'), self).activated.connect(self.button_cancel.click)
50
51
                self.label_equals = QtWidgets.QLabel()
```

# 0d534c35c6a4451e317d41a0d2b3ecb17827b45f

This superclass just has a constructor that subclasses can use. When I added the <code>DefineAsARotationDialog</code> class, I also moved the cancel and confirm buttons into the constructor and added abstract methods that all dialog subclasses must implement.

```
# src/lintrans/gui/dialogs/define_new_matrix.py
61
                # === Arrange the widgets
62
63
                self.setContentsMargins(10, 10, 10, 10)
64
                self.horizontal_spacer = QSpacerItem(50, 5, hPolicy=QSizePolicy.Expanding, vPolicy=QSizePolicy.Minimum)
65
66
67
                self.hlay_buttons = QHBoxLayout()
68
                self.hlay_buttons.setSpacing(20)
                self.hlay_buttons.addItem(self.horizontal_spacer)
69
70
                self.hlav buttons.addWidget(self.button cancel)
71
                self.hlay_buttons.addWidget(self.button_confirm)
72
73
            @property
74
            def selected_letter(self) -> str:
75
                 """The letter currently selected in the combo box."""
76
                return self.letter_combo_box.currentText()
77
78
            @abc.abstractmethod
79
            def update_confirm_button(self) -> None:
80
                """Enable the confirm button if it should be enabled."""
81
82
83
            @abc.abstractmethod
            def confirm matrix(self) -> None:
84
                """Confirm the inputted matrix and assign it.
85
86
87
                This should mutate self.matrix_wrapper and then call self.accept().
                0.00
88
89
```

I then added the class for the rotation definition dialog.

```
# 0d534c35c6a4451e317d41a0d2b3ecb17827b45f
         # src/lintrans/gui/dialogs/define_new_matrix.py
182
         class DefineAsARotationDialog(DefineDialog):
             """The dialog that allows the user to define a new matrix as a rotation."""
183
184
185
             def __init__(self, matrix_wrapper: MatrixWrapper, *args, **kwargs):
                 """Create the dialog, but don't run it yet."""
186
187
                 super().__init__(matrix_wrapper, *args, **kwargs)
188
189
                 # === Create the widgets
190
191
                 self.label_equals.setText('= rot(')
192
193
                 self.text_angle = QtWidgets.QLineEdit(self)
194
                 self.text_angle.setPlaceholderText('angle')
                 self.text_angle.textChanged.connect(self.update_confirm_button)
195
196
197
                 self.label_close_paren = QtWidgets.QLabel(self)
```

```
198
                 self.label_close_paren.setText(')')
199
                 self.checkbox radians = OtWidgets.OCheckBox(self)
200
201
                 self.checkbox_radians.setText('Radians')
202
203
                 # === Arrange the widgets
204
                 self.hlay\_checkbox\_and\_buttons = QHBoxLayout()
205
206
                 self.hlay_checkbox_and_buttons.setSpacing(20)
207
                 self.hlay_checkbox_and_buttons.addWidget(self.checkbox_radians)
208
                 self.hlav checkbox and buttons.addItem(self.horizontal spacer)
209
                 self.hlay_checkbox_and_buttons.addLayout(self.hlay_buttons)
210
211
                 self.hlay_definition = QHBoxLayout()
212
                 self.hlay_definition.addWidget(self.letter_combo_box)
                 self.hlay definition.addWidget(self.label equals)
214
                 self.hlay_definition.addWidget(self.text_angle)
215
                 self.hlay_definition.addWidget(self.label_close_paren)
216
217
                 self.vlay_all = QVBoxLayout()
218
                 self.vlay all.setSpacing(20)
219
                 self.vlay_all.addLayout(self.hlay_definition)
220
                 self.vlay_all.addLayout(self.hlay_checkbox_and_buttons)
221
222
                 self.setLayout(self.vlay_all)
223
224
             def update confirm button(self) -> None:
225
                 """Enable the confirm button if there is a valid float in the angle box."""
                 self.button_confirm.setEnabled(is_float(self.text_angle.text()))
226
             def confirm_matrix(self) -> None:
228
                   "Confirm the inputted matrix and assign it."""
229
230
                 self.matrix_wrapper[self.selected_letter] = create_rotation_matrix(
231
                     float(self.text_angle.text()),
232
                     degrees=not self.checkbox_radians.isChecked()
233
234
                 self.accept()
```

This dialog class just overrides the abstract methods of the superclass with its own implementations. This will be the pattern that all of the definition dialogs will follow.

It has a checkbox for radians, since this is supported in <code>create\_rotation\_matrix()</code>, but the textbox only supports numbers, so the user would have to calculate some multiple of  $\pi$  and paste in several decimal places. I expect people to only use degrees, because these are easier to use.



Figure 7: The first version of the rotation definition dialog

I also then implemented a simple <code>DefineAsAnExpressionDialog</code>, which evaluates a given expression in the current <code>MatrixWrapper</code> context and assigns the result to the given matrix name.

```
# d5f930e15c3c8798d4990486532da46e926a6cb9
         # src/lintrans/gui/dialogs/define_new_matrix.py
241
         class DefineAsAnExpressionDialog(DefineDialog):
242
             """The dialog that allows the user to define a matrix as an expression."""
243
244
                  _init__(self, matrix_wrapper: MatrixWrapper, *args, **kwargs):
245
                  """Create the dialog, but don't run it yet."'
246
                 super().__init__(matrix_wrapper, *args, **kwargs)
247
248
                 self.setMinimumWidth(450)
249
250
                 # === Create the widgets
251
252
                 self.text_box_expression = QtWidgets.QLineEdit(self)
```

```
253
                 self.text_box_expression.setPlaceholderText('Enter matrix expression...')
254
                 self.text_box_expression.textChanged.connect(self.update_confirm_button)
255
256
                 # === Arrange the widgets
257
258
                 self.hlay_definition.addWidget(self.text_box_expression)
259
                 self.vlay_all = QVBoxLayout()
260
261
                 self.vlay_all.setSpacing(20)
262
                 self.vlay_all.addLayout(self.hlay_definition)
263
                 self.vlav all.addLavout(self.hlav buttons)
264
265
                 self.setLayout(self.vlay all)
266
267
             def update confirm button(self) -> None:
268
                   ""Enable the confirm button if the expression is valid."""
269
                 self.button_confirm.setEnabled(
270
                     self.matrix wrapper.is valid expression(self.text box expression.text())
271
272
273
             def confirm matrix(self) -> None:
                  """Evaluate the matrix expression and assign its value to the chosen matrix."""
274
275
                 self.matrix_wrapper[self.selected_letter] = \
276
                     \verb|self.matrix_wrapper.evaluate_expression(self.text_box_expression.text())|\\
277
                 self.accept()
```

My next dialog that I wanted to implement was a visual definition dialog, which would allow the user to drag around the basis vectors to define a transformation. However, I would first need to create the lintrans.gui.plots package to allow for actually visualizing matrices and transformations.

## 3.3 Visualizing matrices

### 3.3.1 Asking strangers on the internet for help

After creating most of the GUI skeleton, I wanted to build the viewport. Unfortunately, I had no idea what I was doing.

While looking through the PyQt5 docs, I found a pretty comprehensive explanation of the Qt5 'Graphics View Framework'[13], which seemed pretty good, but not really what I was looking for. I wanted a way to easily draw lots of straight, parallel lines. This framework seemed more focussed on manipulating objects on a canvas, almost like sprites. I knew of a different Python library called matplotlib, which has various backends available. I learned that it could be embedded in a standard PyQt5 GUI, so I started doing some research.

I didn't get very far with matplotlib. I hadn't used it much before and it's designed for visualizing data. It can draw manually defined straight lines on a canvas, but that's not what it's designed for and it's not very good at it. Thankfully, my horrific matplotlib code has been lost to time. I used the Qt5Agg backend from matplotlib to create a custom PyQt5 widget for the GUI and I could graph randomly generated data with it after following a tutorial[14].

I realised that I wasn't going to get very far with matplotlib, but I didn't know what else to do. I couldn't find any relevant examples on the internet, so I decided to post a question on a forum myself. I'd had experience with StackOverflow and its unfriendly community before, so I decided to ask the r/learnpython subreddit[15].

I only got one response, but it was incredibly helpful. The person told me that if I couldn't find an easy way to do what I wanted, I could write a custom PyQt5 widget. I knew this was possible with a class that just inherited from Qwidget, but had no idea how to actually make something useful. Thankfully, this person provided a link to a GitLab repository of theirs, where they had multiple examples of custom widgets with PyQt5[16].

When looking through this repo, I found out how to draw on a widget like a simple canvas. All I have

to do is override the paintEvent() method and use a QPainter object to draw on the widget. I used this knowledge to start creating the actual viewport for the GUI, starting with the background axes.

#### 3.3.2 Creating the plots package

Initially, the lintrans.gui.plots package just has some classes for widgets. TransformationPlotWidget acts as a base class and then ViewTransformationWidget acts as a wrapper. I will expand this class in the future

```
# 4af63072b383dc9cef9adbb8900323aa007e7f26
        # src/lintrans/gui/plots/plot_widget.py
        """This module provides the basic classes for plotting transformations."""
 3
        from __future__ import annotations
        from PyQt5.QtCore import Qt
        from PyQt5.QtGui import QColor, QPainter, QPaintEvent, QPen
        from PyQt5.QtWidgets import QWidget
 8
 a
10
        class TransformationPlotWidget(QWidget):
11
            """An abstract superclass for plot widgets.
13
            This class provides a background (untransformed) plane, and all the backend
14
            details for a Qt application, but does not provide useful functionality. To
15
            be useful, this class must be subclassed and behaviour must be implemented
16
            by the subclass.
17
18
            .. warning:: This class should never be directly instantiated, only subclassed.
19
21
              I would make this class have ``metaclass=abc.ABCMeta``, but I can't because it subclasses ``QWidget``,
               and a every superclass of a class must have the same metaclass, and ``QWidget`` is not an abstract class.
22
23
24
25
                 _init__(self, *args, **kwargs):
                """Create the widget, passing ``*args`` and ``**kwargs`` to the superclass constructor (``QWidget``)."""
26
27
                super().__init__(*args, **kwargs)
28
29
                self.setAutoFillBackground(True)
30
31
                # Set the background to white
                palette = self.palette()
32
33
                palette.setColor(self.backgroundRole(), Qt.white)
34
                self.setPalette(palette)
35
                # Set the gird colour to grey and the axes colour to black
37
                self.grid colour = QColor(128, 128, 128)
38
                self.axes_colour = QColor(0, 0, 0)
39
                self.grid\_spacing: int = 50
40
41
                self.line_width: float = 0.4
43
            @property
            def w(self) -> int:
44
45
                """Return the width of the widget."""
46
                return self.size().width()
48
            @property
49
            def h(self) -> int:
50
                """Return the height of the widget."""
51
                return self.size().height()
53
            def paintEvent(self, e: QPaintEvent):
                 """Handle a ``QPaintEvent`` by drawing the widget."""
54
                gp = OPainter()
56
                ap.begin(self)
57
                self.draw_widget(qp)
```

```
58
59
60
61
62
63
64
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66
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68
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70
71
73
74
75
76
77
78
79
80
81
82
83
84
85
86
87
```

89

45

46

47

```
qp.end()
    def draw_widget(self, qp: QPainter):
        """Draw the grid and axes in the widget."""
        qp.setRenderHint(QPainter.Antialiasing)
        qp.setBrush(Qt.NoBrush)
        # Draw the grid
        qp.setPen(QPen(self.grid_colour, self.line_width))
        # We draw the background grid, centered in the middle
        # We deliberately exclude the axes - these are drawn separately
        for x in range(self.w // 2 + self.grid_spacing, self.w, self.grid_spacing):
            qp.drawLine(x, 0, x, self.h)
            qp.drawLine(self.w - x, 0, self.w - x, self.h)
        for y in range(self.h // 2 + self.grid_spacing, self.h, self.grid_spacing):
            qp.drawLine(0, y, self.w, y)
            qp.drawLine(0, self.h - y, self.w, self.h - y)
        # Now draw the axes
        qp.setPen(QPen(self.axes_colour, self.line_width))
        qp.drawLine(self.w // 2, 0, self.w // 2, self.h)
        qp.drawLine(0, self.h // 2, self.w, self.h // 2)
class ViewTransformationWidget(TransformationPlotWidget):
    """This class is used to visualise matrices as transformations."""
    def __init__(self, *args, **kwargs):
        """Create the widget, passing ``*args`` and ``**kwargs`` to the superclass constructor."""
        super().__init__(*args, **kwargs)
```

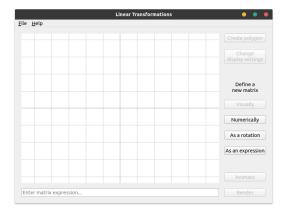


Figure 8: The GUI with background axes

The meat of this class is the <code>draw\_widget()</code> method. Right now, this method only draws the background axes. My next step is to implement basis vector attributes and draw them in <code>draw\_widget()</code>. After changing the the plot attribute in <code>LintransMainWindow</code> to an instance of <code>ViewTransformationWidget</code>, the plot was visible in the GUI.

I then refactored the code slightly to rename draw\_widget() to draw\_background() and then call it from the paintEvent() method in ViewTransformationWidget.

## 3.3.3 Implementing basis vectors

My first step in implementing basis vectors was to add some utility methods to convert between coordinate systems. The matrices are using Cartesian coordinates with (0,0) in the middle, positive x going to the right, and positive y going up. However, Qt5 is using standard computer graphics coordinates, with (0,0) in the top left, positive x going to the right, and positive y going down. I needed a way to convert Cartesian 'grid' coordinates to Qt5 'canvas' coordinates, so I wrote some little utility methods.

```
# 1fa7e1c61d61cb6aeff773b9698541f82fee39ea
# src/lintrans/gui/plots/plot_widget.py

@property
def origin(self) -> tuple[int, int]:
    """Return the canvas coords of the origin."""
```

Candidate name: D. Dyson Candidate number: 123456 Centre number: 123456

```
48
                return self.width() // 2, self.height() // 2
49
50
            def trans_x(self, x: float) -> int:
51
                """Transform an x coordinate from grid coords to canvas coords."""
52
                return int(self.origin[0] + x * self.grid_spacing)
53
54
            def trans_y(self, y: float) -> int:
55
                 """Transform a y coordinate from grid coords to canvas coords."""
56
                return int(self.origin[1] - y * self.grid_spacing)
57
            def trans_coords(self, x: float, y: float) -> tuple[int, int]:
58
                """Transform a coordinate in grid coords to canvas coords."""
59
60
                return self.trans_x(x), self.trans_y(y)
```

# 37e7c208a33d7cbbc8e0bb6c94cd889e2918c605

Once I had a way to convert coordinates, I could add the basis vectors themselves. I did this by creating attributes for the points in the constructor and creating a transform\_by\_matrix() method to change these point attributes accordingly.

```
# src/lintrans/gui/plots/plot_widget.py
92
         class ViewTransformationWidget(TransformationPlotWidget):
 93
             """This class is used to visualise matrices as transformations."""
94
95
             def __init__(self, *args, **kwargs):
                 """Create the widget, passing ``*args`` and ``**kwargs`` to the superclass constructor."""
 96
97
                 super().__init__(*args, **kwargs)
98
                 self.point_i: tuple[float, float] = (1., 0.)
99
100
                 self.point_j: tuple[float, float] = (0., 1.)
101
                 self.colour_i = QColor(37, 244, 15)
102
                 self.colour_j = QColor(8, 8, 216)
103
104
105
                 self.width_vector_line = 1
106
                 self.width_transformed_grid = 0.6
107
108
             def transform_by_matrix(self, matrix: MatrixType) -> None:
                 """Transform the plane by the given matrix.""
110
                 self.point_i = (matrix[0][0], matrix[1][0])
111
                 self.point_j = (matrix[0][1], matrix[1][1])
112
                 self.update()
```

I also created a draw\_transformed\_grid() method which gets called in paintEvent().

```
# 37e7c208a33d7cbbc8e0bb6c94cd889e2918c605
         # src/lintrans/gui/plots/plot_widget.py
122
             def draw_transformed_grid(self, painter: QPainter) -> None:
                 """Draw the transformed version of the grid, given by the unit vectors."""
123
124
                 # Draw the unit vectors
                 painter.setPen(QPen(self.colour_i, self.width_vector_line))
125
126
                 painter.drawLine(*self.origin, *self.trans_coords(*self.point_i))
127
                 painter.setPen(QPen(self.colour_j, self.width_vector_line))
128
                 painter.drawLine(*self.origin, *self.trans_coords(*self.point_j))
```

 $I then \ changed \ the \ render\_expression (\ ) \ method \ in \ Lintrans Main Window \ to \ call \ this \ new \ transform\_by\_matrix (\ ) \ method.$ 

Testing this new code shows that it works well.

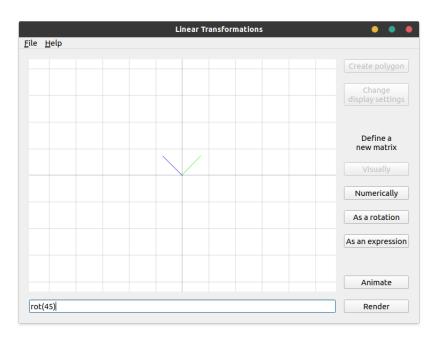


Figure 9: Basis vectors drawn for a 45° rotation

### 3.3.4 Drawing the transformed grid

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65

66

After drawing the basis vectors, I wanted to draw the transformed version of the grid. I first created a <code>grid\_corner()</code> utility method to return the grid coordinates+ of the top right corner of the canvas. This allows me to find the bounding box in which to draw the grid lines.

```
# 2ade98ac28d1c3f6691e4afa819142a3ab8e9fd9
# src/lintrans/gui/plots/plot_widget.py

def grid_corner(self) -> tuple[float, float]:
    """Return the grid coords of the top right corner."""
    return self.width() / (2 * self.grid_spacing), self.height() / (2 * self.grid_spacing)
```

I then created a <code>draw\_parallel\_lines()</code> method that would fill the bounding box with a set of lines parallel to a given vector with spacing defined by the intersection with a given point.

```
# 2ade98ac28d1c3f6691e4afa819142a3ab8e9fd9
         # src/lintrans/gui/plots/plot_widget.py
             def draw_parallel_lines(self, painter: QPainter, vector: tuple[float, float], point: tuple[float, float]) ->
126
             \hookrightarrow None:
                 """Draw a set of grid lines parallel to ``vector`` intersecting ``point``."""
                 max_x, max_y = self.grid_corner()
128
129
                 vector_x, vector_y = vector
130
                 point_x, point_y = point
131
132
                 if vector_x == 0:
133
                     painter.drawLine(self.trans_x(0), 0, self.trans_x(0), self.height())
134
```

```
135
                      for i in range(int(max_x / point_x)):
136
                         painter.drawLine(
137
                              self.trans_x((i + 1) * point_x),
138
                              self.trans_x((i + 1) * point_x),
139
140
                              self.height()
141
                          painter.drawLine(
142
143
                              self.trans_x(-1 * (i + 1) * point_x),
144
                              self.trans_x(-1 * (i + 1) * point_x),
145
146
                              self.height()
147
                          )
148
149
                 elif vector_y == 0:
150
                      painter.drawLine(0, self.trans\_y(0), self.width(), self.trans\_y(0))
151
152
                      for i in range(int(max_y / point_y)):
                          painter.drawLine(
153
154
155
                              self.trans_y((i + 1) * point_y),
156
                              self.width(),
157
                              self.trans_y((i + 1) * point_y)
158
159
                          painter.drawLine(
160
                              0,
                              self.trans_y(-1 * (i + 1) * point_y),
161
162
                              self.width(),
                              self.trans_y(-1 * (i + 1) * point_y)
163
164
                          )
```

I then called this method from draw\_transformed\_grid().

```
# 2ade98ac28d1c3f6691e4afa819142a3ab8e9fd9
         # src/lintrans/gui/plots/plot_widget.py
166
             def draw_transformed_grid(self, painter: QPainter) -> None:
                 """Draw the transformed version of the grid, given by the unit vectors."""
167
168
                 # Draw the unit vectors
169
                 painter.setPen(QPen(self.colour_i, self.width_vector_line))
                 painter.drawLine(*self.origin, *self.trans_coords(*self.point_i))
170
171
                 painter.setPen(QPen(self.colour_j, self.width_vector_line))
172
                 painter.drawLine(*self.origin, *self.trans_coords(*self.point_j))
173
                 # Draw all the parallel lines
174
175
                 painter.setPen(QPen(self.colour_i, self.width_transformed_grid))
176
                 self.draw_parallel_lines(painter, self.point_i, self.point_j)
177
                 painter.setPen(QPen(self.colour\_j, self.width\_transformed\_grid))
                 self.draw_parallel_lines(painter, self.point_j, self.point_i)
178
```

This worked quite well when the matrix involved no rotation, as seen in Figure 10, but this didn't work with rotation. When trying rot(45) for example, it looked the same as in Figure 9.

Also, the vectors aren't particularly clear. They'd be much better with arrowheads on their tips, but this is just a prototype. The arrowheads will come later.

My next step was to make the transformed grid lines work with rotations.

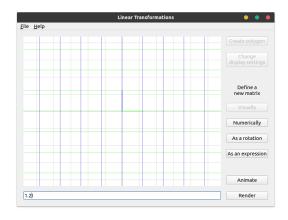


Figure 10: Parallel lines being drawn for matrix  $1.2\mathbf{I}$ 

ii: int = 1

while True:

 $y1 = m * max_x + ii * c$ 

 $y2 = -1 * m * max_x + ii * c$ 

192193

194

```
196
197
                       if y1 < max_y or y2 < max_y:</pre>
198
                           multiples_of_c += 1
199
                           ii += 1
200
201
                       else:
202
203
204
                  # Once we know how many lines we can draw, we just draw them all
205
                  for i in range(1, multiples_of_c + 1):
                       painter.drawLine(
206
207
                           *self.trans_coords(
208
                               -1 * max x,
209
                               m \star -1 \star max_x + i \star c
210
211
                           *self.trans_coords(
212
213
                               m * max_x + i * c
214
215
216
                       painter.drawLine(
                           *self.trans_coords(
218
                                -1 * max_x,
219
                               m * -1 * max x - i * c
220
221
                           *self.trans_coords(
222
                               \max_{x}
223
                               m * max_x - i * c
224
                           )
225
                       )
```

This code checks if x or y is zero<sup>10</sup> and if they're not, then we have to use the standard straight line equation y = mx + c to create parallel lines. We find our value of m and then iterate through all the values of c that keep the line within the bounding box.

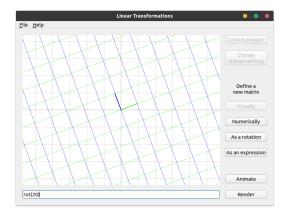


Figure 11: An example of a 20° rotation

There are some serious logical errors in this code. It works fine for things like 3rot(45) or 0.5rot(20), but something like rot(115) will leave the program hanging indefinitely.

In fact, this code only works for rotations between  $0^{\circ}$  and  $90^{\circ}$ , and will hang forever when given a matrix like  $\begin{pmatrix} 12 & 4 \\ -2 & 3 \end{pmatrix}$ , because it's just not very good.

I will fix these issues in the future, but it works somewhat decently, so I decided to do animation next, because that sounded more fun.

## 3.3.5 Implementing animation

238

239

Now that I had a very crude renderer, I could create a method to animate a matrix. Eventually I want to be able to apply a given matrix to the currently rendered scene and animate between them. However, I wanted to start simple by animating from the identity to the given matrix.

```
# 829a130af5aee9819bf0269c03ecfb20bec1a108
# src/lintrans/gui/main_window.py

def animate_expression(self) -> None:
    """Animate the expression in the input box, and then clear the box."""
```

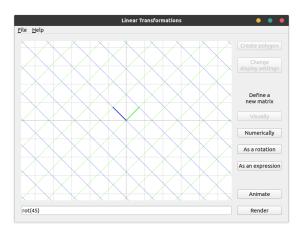
 $<sup>^{10}</sup>$ We actually check if they're less than  $10^{-12}$  to allow for floating point errors

```
240
                 self.button_render.setEnabled(False)
241
                 self.button_animate.setEnabled(False)
242
                 matrix = self.matrix_wrapper.evaluate_expression(self.lineedit_expression_box.text())
243
244
                 matrix move = matrix - self.matrix wrapper['I']
245
                 steps: int = 100
246
247
                 for i in range(0, steps + 1):
248
                      self.plot.visualize_matrix_transformation(
249
                          self.matrix_wrapper['I'] + (i / steps) * matrix_move
250
251
252
                      self.update()
253
                      self.repaint()
254
255
                      time.sleep(0.01)
256
257
                 self.button_render.setEnabled(False)
                 self.button_animate.setEnabled(False)
258
```

This code creates the matrix\_move variable and adds scaled versions of it to the identity matrix and renders that each frame. It's simple, but it works well for this simple use case. Unfortunately, it's very hard to show off an animation in a PDF, since all these images are static. The git commit hashes are included in the code snippets if you want to clone the repo[11], checkout this commit, and run it yourself if you want.

#### 3.3.6 Preserving determinants

Ignoring the obvious flaw with not being able to render transformations with a more than 90° rotation, the animations don't respect determinants. When rotating 90°, the determinant changes during the animation, even though we're going from a determinant 1 matrix (the identity) to another determinant 1 matrix. This is because we're just moving each vector to its new position in a straight line. I want to animate in a way that smoothly transitions the determinant.



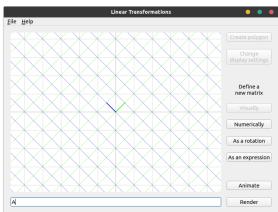


Figure 12: What we would expect halfway through a 90° rotation

Figure 13: What we actually get halfway through a 90° rotation

In order to smoothly animate the determinant, I had to do some maths. I first defined the matrix **A** to be equivalent to the matrix\_move variable from before - the target matrix minus the identity, scaled by the proportion. I then wanted to normalize **A** so that it had a determinant of 1 so that I could scale it up with the proportion variable through the animation.

I think I first tried just multiplying **A** by  $\frac{1}{\det(\mathbf{A})}$  but that didn't work, so I googled it. I found a post[17] on ResearchGate about the topic, and thanks to a very helpful comment from Jeffrey L Stuart, I learned that for a  $2 \times 2$  matrix **A** and a scalar c,  $\det(c\mathbf{A}) = c^2 \det(\mathbf{A})$ .

# 6ff49450d8438ea2b2e7d2a97125dc518e648bc5

I wanted a c such that  $\det(c\mathbf{A}) = 1$ . Therefore  $c = \frac{1}{\sqrt{|\det(\mathbf{A})|}}$ . I then defined matrix  $\mathbf{B}$  to be  $c\mathbf{A}$ .

Then I wanted to scale this normalized matrix **B** to have the same determinant as the target matrix **T** using some scalar d. We know that  $\det(d\mathbf{B}) = d^2 \det(\mathbf{B}) = \det(\mathbf{T})$ . We can just rearrange to find d and get  $d = \sqrt{\left|\frac{\det(\mathbf{T})}{\det(\mathbf{B})}\right|}$ . But **B** is defined so that  $\det(\mathbf{B}) = 1$ , so we can get  $d = \sqrt{|\det(\mathbf{T})|}$ .

However, we want to scale this over time with our proportion variable p, so our final scalar  $s = 1 + p\left(\sqrt{|\det(\mathbf{T})|} - 1\right)$ . We define a matrix  $\mathbf{C} = s\mathbf{B}$  and render  $\mathbf{C}$  each frame. When in code form, this is the following:

```
# src/lintrans/gui/main_window.py
245
                  # Get the target matrix and it's determinant
246
                  matrix target = self.matrix wrapper.evaluate expression(self.lineedit expression box.text())
247
                  det_target = linalg.det(matrix_target)
248
249
                  identity = self.matrix wrapper['I']
250
                  steps: int = 100
251
252
                  for i in range(0, steps + 1):
253
                      # This proportion is how far we are through the loop
254
                      proportion = i / steps
255
256
                      # matrix_a is the identity plus some part of the target, scaled by the proportion
257
                      # If we just used matrix a, then things would animate, but the determinants would be weird
258
                      matrix_a = identity + proportion * (matrix_target - identity)
259
260
                      # So to fix the determinant problem, we get the determinant of matrix_a and use it to normalise
261
                      det_a = linalg.det(matrix_a)
262
263
                      # For a 2x2 matrix A and a scalar c, we know that det(cA) = c^2 det(A)
                      # We want B = cA such that det(B) = 1, so then we can scale it with the animation
264
265
                      # So we get c^2 \det(A) = 1 \Rightarrow c = \operatorname{sgrt}(1 / \operatorname{abs}(\det(A)))
266
                      # Then we scale A down to get a determinant of 1, and call that matrix_b
                      if det_a == 0:
267
268
                          c = 0
269
                      else:
270
                          c = np.sgrt(1 / abs(det a))
271
272
                      matrix_b = c * matrix_a
273
274
                      # matrix_c is the final matrix that we transform by
275
                      # It's B, but we scale it up over time to have the target determinant
276
277
                      # We want some C = dB such that det(C) is some target determinant T
278
                      \# \det(dB) = d^2 \det(B) = T \Rightarrow d = \operatorname{sqrt}(\operatorname{abs}(T / \det(B)))
279
                      # But we defined B to have det 1, so we can ignore it there
280
281
                      # We're also subtracting 1 and multiplying by the proportion and then adding one
282
                      # This just scales the determinant along with the animation
283
                      scalar = 1 + proportion * (np.sqrt(abs(det_target)) - 1)
284
285
                      matrix_c = scalar * matrix_b
286
287
                      self.plot.visualize_matrix_transformation(matrix_c)
288
289
                      self.repaint()
290
                      time.sleep(0.01)
```

Unfortunately, the system I use to render matrices is still quite bad at its job. This makes it hard to test properly. But, transformations like 2rot(90) work exactly as expected, which is very good.

# Candidate name: D. Dyson

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# A Project code

## A.1 \_\_main\_\_.py

```
#!/usr/bin/env python
 2
 3
        # lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
 6
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 8
        """This module provides a :func:`main` function to interpret command line arguments and run the program."""
10
11
12
        from argparse import ArgumentParser
        from textwrap import dedent
13
14
15
        from lintrans import version
16
        from lintrans.gui import main_window
17
18
19
        def main(args: list[str]) -> None:
20
            """Interpret program-specific command line arguments and run the main window in most cases.
21
22
            If the user supplies --help or --version, then we simply respond to that and then return.
23
            If they don't supply either of these, then we run :func:`lintrans.gui.main_window.main`.
24
25
            :param list[str] args: The full argument list (including program name)
26
27
            parser = ArgumentParser(add_help=False)
28
29
            parser.add_argument(
30
                '-h',
31
                '--help',
32
                default=False.
                action='store_true'
34
35
36
            parser.add_argument(
37
                '-V',
38
                '--version',
39
                default=False,
40
                action='store_true'
41
42
43
            parsed_args, unparsed_args = parser.parse_known_args()
45
            if parsed_args.help:
46
                print(dedent('''
47
                Usage: lintrans [option]
48
49
50
                                     Display this help text and exit
                    -h. --help
51
                    -V. --version
                                     Display the version information and exit
52
                Any other options will get passed to the QApplication constructor.
53
54
                If you don't know what that means, then don't provide any arguments and just the run the program.'''[1:]))
55
                return
56
57
            if parsed_args.version:
58
                print(dedent(f''
59
                lintrans (version {__version__})
60
                The linear transformation visualizer
61
62
                Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
63
                This program is licensed under GNU GPLv3, available here:
64
65
                <https://www.gnu.org/licenses/gpl-3.0.html>'''[1:]))
66
                return
```

```
68
            for arg in unparsed_args:
                print(f'Passing "{arg}" to QApplication. See --help for recognised args')
69
70
71
            main_window.main(args[:1] + unparsed_args)
72
73
        if __name__ == '__main__':
74
75
            main(sys.argv)
        A.2 __init__.py
        # lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
 3
        # This program is licensed under GNU GPLv3, available here:
 5
        # <https://www.gnu.org/licenses/gpl-3.0.html>
6
        """This is the top-level ``lintrans`` package, which contains all the subpackages of the project."""
8
9
        from . import gui, matrices, typing_
10
        __version__ = '0.2.2-alpha'
11
12
        __all__ = ['gui', 'matrices', 'typing_', '__version__']
13
        A.3 gui/settings.py
        # lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
 5
        # <https://www.gnu.org/licenses/gpl-3.0.html>
6
        """This module contains the :class:`DisplaySettings` class, which holds configuration for display."""
8
a
        from __future__ import annotations
10
11
        from dataclasses import dataclass
12
13
14
        @dataclass
15
        class DisplaySettings:
            """This class simply holds some attributes to configure display."""
16
17
18
            # === Basic stuff
19
20
            draw_background_grid: bool = True
21
            """This controls whether we want to draw the background grid.
22
            The background axes will always be drawn. This makes it easy to identify the center of the space.
23
24
25
26
            draw_transformed_grid: bool = True
27
            """This controls whether we want to draw the transformed grid. Vectors are handled separately."""
28
29
            draw basis vectors: bool = True
30
            """This controls whether we want to draw the transformed basis vectors."""
31
32
            # === Animations
33
34
            smoothen_determinant: bool = True
            """This controls whether we want the determinant to change smoothly during the animation.
35
36
37
              Even if this is True, it will be ignored if we're animating from a positive det matrix to
38
               a negative det matrix, or vice versa, because if we try to smoothly animate that determinant,
39
               things blow up and the app often crashes.
40
```

```
42
43
             applicative_animation: bool = True
44
              ""There are two types of simple animation, transitional and applicative.
45
46
             Let ``C`` be the matrix representing the currently displayed transformation, and let ``T`` be the target matrix.
             Transitional animation means that we animate directly from ``C`` from ``T``, and applicative animation means that we animate from ``C`` to ``TC``, so we apply ``T`` to ``C``.
47
48
49
50
51
             animation_pause_length: int = 400
             """This is the number of milliseconds that we wait between animations when using comma syntax."""
52
53
54
             # === Matrix info
55
56
             draw_determinant_parallelogram: bool = False
57
             """This controls whether or not we should shade the parallelogram representing the determinant of the matrix."""
58
59
             show_determinant_value: bool = True
             """This controls whether we should write the text value of the determinant inside the parallelogram.
60
61
62
             The text only gets draw if :attr:`draw determinant parallelogram` is also True.
63
64
65
             draw_eigenvectors: bool = False
66
             """This controls whether we should draw the eigenvectors of the transformation."""
67
68
             draw eigenlines: bool = False
69
             """This controls whether we should draw the eigenlines of the transformation."""
```

## A.4 gui/validate.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
 4
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 7
        """This simple module provides a :class:`MatrixExpressionValidator` class to validate matrix expression input."""
 8
 9
        from __future__ import annotations
10
        import re
11
12
13
        from PyQt5.QtGui import QValidator
14
15
        from lintrans.matrices import parse
16
17
18
        class MatrixExpressionValidator(QValidator):
            """This class validates matrix expressions in a Qt input box."""
19
20
21
            def validate(self, text: str, pos: int) -> tuple[QValidator.State, str, int]:
22
                 """Validate the given text according to the rules defined in the :mod:`lintrans.matrices` module."""
                clean_text = re.sub(parse.NAIVE_CHARACTER_CLASS[:-1] + ',]', '', text)
23
24
25
                if clean_text == '':
26
                    if parse.validate_matrix_expression(clean_text):
27
                        return QValidator.Acceptable, text, pos
28
                    else:
29
                        return QValidator.Intermediate, text, pos
30
31
                return QValidator.Invalid, text, pos
```

## A.5 gui/main\_window.py

```
# lintrans - The linear transformation visualizer
Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
```

```
# This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 6
        """This module provides the :class:`LintransMainWindow` class, which provides the main window for the GUI."""
 8
 9
        from __future__ import annotations
10
11
        import sys
12
        import webbrowser
13
        from copy import deepcopy
14
        from typing import Type
15
16
        import numpy as np
17
        from numpy import linalg
18
        from numpy.linalg import LinAlgError
19
        from PyQt5 import QtWidgets
20
        from PyQt5.QtCore import pyqtSlot, QThread
21
        from PyQt5.QtGui import QKeySequence
        from PyQt5.QtWidgets import (QApplication, QHBoxLayout, QMainWindow, QMessageBox,
22
23
                                      QShortcut, QSizePolicy, QSpacerItem, QVBoxLayout)
24
25
        from lintrans.matrices import MatrixWrapper
26
        from lintrans.matrices.parse import validate_matrix_expression
27
        from lintrans.typing_ import MatrixType
28
        from . import dialogs
29
        from .dialogs import DefineAsAnExpressionDialog, DefineDialog, DefineNumericallyDialog, DefineVisuallyDialog
30
        from .dialogs.settings import DisplaySettingsDialog
31
        from .plots import VisualizeTransformationWidget
32
        from .settings import DisplaySettings
        from .validate import MatrixExpressionValidator
34
35
36
        class LintransMainWindow(QMainWindow):
37
            """This class provides a main window for the GUI using the Qt framework.
38
39
            This class should not be used directly, instead call :func:`lintrans.gui.main_window.main` to create the GUI.
40
41
42
            def __init__(self):
                 """Create the main window object, and create and arrange every widget in it.
43
44
45
                This doesn't show the window, it just constructs it. Use :func:`lintrans.gui.main_window.main` to show the
        \hookrightarrow GUI.
46
47
                super().__init__()
48
49
                self.matrix_wrapper = MatrixWrapper()
50
51
                self.setWindowTitle('lintrans')
52
                self.setMinimumSize(1000, 750)
53
54
                self.animating: bool = False
55
                self.animating_sequence: bool = False
56
57
                # === Create menubar
58
59
                self.menubar = QtWidgets.QMenuBar(self)
60
61
                self.menu file = OtWidgets.OMenu(self.menubar)
62
                self.menu_file.setTitle('&File')
63
                self.menu help = OtWidgets.OMenu(self.menubar)
64
                self.menu_help.setTitle('&Help')
65
66
67
                self.action_new = QtWidgets.QAction(self)
68
                self.action_new.setText('&New')
                self.action_new.setShortcut('Ctrl+N')
69
70
                self.action_new.triggered.connect(lambda: print('new'))
71
                self.action_open = QtWidgets.QAction(self)
73
                self.action_open.setText('&Open')
74
                self.action_open.setShortcut('Ctrl+0')
75
                self.action_open.triggered.connect(lambda: print('open'))
```

```
76
 77
                 self.action_save = QtWidgets.QAction(self)
 78
                 self.action_save.setText('&Save')
                 self.action_save.setShortcut('Ctrl+S')
 79
 80
                 self.action_save.triggered.connect(lambda: print('save'))
81
                 self.action_save_as = QtWidgets.QAction(self)
 82
83
                 self.action save as.setText('Save as...')
84
                 self.action_save_as.triggered.connect(lambda: print('save as'))
 85
                 self.action tutorial = OtWidgets.OAction(self)
86
                 self.action_tutorial.setText('&Tutorial')
87
88
                 self.action tutorial.setShortcut('F1')
89
                 self.action_tutorial.triggered.connect(lambda: print('tutorial'))
 90
 91
                 self.action_docs = QtWidgets.QAction(self)
92
                 self.action_docs.setText('&Docs')
 93
                 self.action_docs.triggered.connect(
                     lambda: webbrowser.open_new_tab('https://doctordalek1963.github.io/lintrans/docs/index.html')
94
 95
96
97
                 self.action_about = QtWidgets.QAction(self)
98
                 self.action_about.setText('&About')
99
                 self.action_about.triggered.connect(lambda: dialogs.AboutDialog(self).open())
100
101
                 # TODO: Implement these actions and enable them
                 self.action new.setEnabled(False)
102
                 self.action_open.setEnabled(False)
103
104
                 self.action save.setEnabled(False)
105
                 {\tt self.action\_save\_as.setEnabled(False)}
106
                 self.action_tutorial.setEnabled(False)
107
108
                 self.menu_file.addAction(self.action_new)
109
                 self.menu_file.addAction(self.action_open)
110
                 self.menu_file.addSeparator()
                 self.menu_file.addAction(self.action_save)
111
112
                 self.menu_file.addAction(self.action_save_as)
113
114
                 self.menu_help.addAction(self.action_tutorial)
                 self.menu_help.addAction(self.action_docs)
115
116
                 self.menu_help.addSeparator()
117
                 self.menu_help.addAction(self.action_about)
118
119
                 self.menubar.addAction(self.menu_file.menuAction())
120
                 self.menubar.addAction(self.menu_help.menuAction())
121
                 self.setMenuBar(self.menubar)
122
123
124
                 # === Create widgets
125
                 # Left layout: the plot and input box
126
127
128
                 self.plot = VisualizeTransformationWidget(self, display_settings=DisplaySettings())
129
130
                 self.lineedit_expression_box = QtWidgets.QLineEdit(self)
131
                 self.lineedit expression box.setPlaceholderText('Enter matrix expression...')
132
                 \verb|self.lineedit_expression_box.setValidator(MatrixExpressionValidator(self))| \\
133
                 \verb|self.lineedit_expression_box.textChanged.connect(self.update_render_buttons)|\\
134
135
                 # Right layout: all the buttons
136
                 # Misc buttons
137
138
139
                 self.button_create_polygon = QtWidgets.QPushButton(self)
140
                 self.button_create_polygon.setText('Create polygon')
141
                 # self.button_create_polygon.clicked.connect(self.create_polygon)
                 self.button_create_polygon.setToolTip('Define a new polygon to view the transformation of')
142
143
144
                 # TODO: Implement this and enable button
                 self.button_create_polygon.setEnabled(False)
145
146
147
                 self.button_change_display_settings = QtWidgets.QPushButton(self)
148
                 {\tt self.button\_change\_display\_settings.setText('Change \verb| ndisplay settings')}
```

```
149
                 self.button_change_display_settings.clicked.connect(self.dialog_change_display_settings)
150
                 self.button_change_display_settings.setToolTip(
                      "Change which things are rendered and how they're rendered<br><bc/>ctrl + D)</br>
151
152
153
                 QShortcut(QKeySequence('Ctrl+D'), self).activated.connect(self.button\_change\_display\_settings.click) \\
154
155
                 self.button_reset_zoom = QtWidgets.QPushButton(self)
156
                 self.button reset zoom.setText('Reset zoom')
157
                 self.button_reset_zoom.clicked.connect(self.reset_zoom)
158
                 self.button_reset_zoom.setToolTip('Reset the zoom level back to normal<br><br/><br/>to normal<br/><br/>b')
                 QShortcut(QKeySequence('Ctrl+Shift+R'), self).activated.connect(self.button_reset_zoom.click)
159
160
161
                 # Define new matrix buttons and their groupbox
162
163
                 self.button_define_visually = QtWidgets.QPushButton(self)
                 self.button_define_visually.setText('Visually')
164
165
                 self.button_define_visually.setToolTip('Drag the basis vectors<br><b>(Alt + 1)</b>')
166
                 self.button_define_visually.clicked.connect(lambda: self.dialog_define_matrix(DefineVisuallyDialog))
167
                 QShortcut(QKeySequence('Alt+1'), self).activated.connect(self.button_define_visually.click)
168
                 self.button_define_numerically = QtWidgets.QPushButton(self)
169
170
                 self.button_define_numerically.setText('Numerically')
171
                 self.button_define_numerically.setToolTip('Define a matrix just with numbers<br/>drs-<br/>db')
172
                 self.button define numerically.clicked.connect(lambda: self.dialog define matrix(DefineNumericallyDialog))
173
                 QShortcut(QKeySequence('Alt+2'), self).activated.connect(self.button_define_numerically.click)
174
175
                 self.button_define_as_expression = QtWidgets.QPushButton(self)
                 self.button_define_as_expression.setText('As an expression')
176
177
                 self.button_define_as_expression.setToolTip('Define a matrix in terms of other matrices<br/>d>(Alt +
                 \hookrightarrow 3)</b>')
178
                 \verb|self.button_define_as_expression.clicked.connect(| \verb|lambda:||

    self.dialog_define_matrix(DefineAsAnExpressionDialog))

179
                 QShortcut(QKeySequence('Alt+3'), self).activated.connect(self.button_define_as_expression.click)
180
181
                 self.vlay_define_new_matrix = QVBoxLayout()
182
                 self.vlay_define_new_matrix.setSpacing(20)
183
                 self.vlay define new matrix.addWidget(self.button define visually)
184
                 self.vlay_define_new_matrix.addWidget(self.button_define_numerically)
185
                 \verb|self.vlay_define_new_matrix.addWidget(self.button_define_as_expression)| \\
186
187
                 self.groupbox_define_new_matrix = QtWidgets.QGroupBox('Define a new matrix', self)
188
                 {\tt self.groupbox\_define\_new\_matrix.setLayout(self.vlay\_define\_new\_matrix)}
189
190
                 # Render buttons
191
                 self.button_reset = QtWidgets.QPushButton(self)
192
                 self.button_reset.setText('Reset')
193
194
                 self.button reset.clicked.connect(self.reset transformation)
195
                 self.button_reset.setToolTip('Reset the visualized transformation back to the identity<br><br/>c(trl +
                 QShortcut(QKeySequence('Ctrl+R'), self).activated.connect(self.button_reset.click)
196
197
198
                 self.button_render = QtWidgets.QPushButton(self)
199
                 self.button_render.setText('Render')
200
                 self.button_render.setEnabled(False)
201
                 self.button render.clicked.connect(self.render expression)
202
                 self.button\_render.setToolTip('Render the expression < br > < b < (Ctrl + Enter) < / b > ')
203
                 QShortcut(QKeySequence('Ctrl+Return'), self).activated.connect(self.button_render.click)
204
205
                 self.button_animate = QtWidgets.QPushButton(self)
206
                 self.button_animate.setText('Animate')
207
                 self.button_animate.setEnabled(False)
                 self.button_animate.clicked.connect(self.animate_expression)
208
209
                 self.button animate.setToolTip('Animate the expression<br><b/><br/>Ctrl + Shift + Enter)')
210
                 QShortcut(QKeySequence('Ctrl+Shift+Return'), self). activated.connect(self.button\_animate.click)
211
212
                 # === Arrange widgets
213
214
                 self.vlay_left = QVBoxLayout()
                 self.vlay_left.addWidget(self.plot)
216
                 self.vlay_left.addWidget(self.lineedit_expression_box)
217
218
                 self.vlay_misc_buttons = QVBoxLayout()
```

```
219
                 self.vlay_misc_buttons.setSpacing(20)
220
                 self.vlay_misc_buttons.addWidget(self.button_create_polygon)
221
                 self.vlay_misc_buttons.addWidget(self.button_change_display_settings)
222
                 self.vlay_misc_buttons.addWidget(self.button_reset_zoom)
223
224
                 self.vlay_render = QVBoxLayout()
225
                 self.vlay_render.setSpacing(20)
226
                 self.vlay render.addWidget(self.button reset)
227
                 self.vlay_render.addWidget(self.button_animate)
228
                 self.vlay_render.addWidget(self.button_render)
229
230
                 self.vlay_right = QVBoxLayout()
231
                 self.vlay right.setSpacing(50)
232
                 {\tt self.vlay\_right.addLayout(self.vlay\_misc\_buttons)}
                 \verb|self.vlay_right.addItem(QSpacerItem(100, 2, hPolicy=QSizePolicy.Minimum, vPolicy=QSizePolicy.Expanding)|| \\
233
                 \verb|self.vlay_right.addWidget(self.groupbox_define_new_matrix)|\\
234
235
                 self.vlay_right.addItem(QSpacerItem(100, 2, hPolicy=QSizePolicy.Minimum, vPolicy=QSizePolicy.Expanding))
236
                 self.vlay_right.addLayout(self.vlay_render)
237
238
                 self.hlay_all = QHBoxLayout()
239
                 self.hlay_all.setSpacing(15)
240
                 self.hlay_all.addLayout(self.vlay_left)
241
                 self.hlay_all.addLayout(self.vlay_right)
242
243
                 self.central_widget = QtWidgets.QWidget()
244
                 self.central_widget.setLayout(self.hlay_all)
245
                 self.central_widget.setContentsMargins(10, 10, 10, 10)
246
247
                 self.setCentralWidget(self.central_widget)
248
249
             def update_render_buttons(self) -> None:
250
                   ""Enable or disable the render and animate buttons according to whether the matrix expression is valid."""
251
                 text = self.lineedit_expression_box.text()
252
253
                 # Let's say that the user defines a non-singular matrix A, then defines B as A^-1
254
                 # If they then redefine A and make it singular, then we get a LinAlgError when
255
                 # trying to evaluate an expression with B in it
256
                 \# To fix this, we just do naive validation rather than aware validation
257
                 if ',' in text:
258
                     self.button_render.setEnabled(False)
259
260
261
                         valid = all(self.matrix_wrapper.is_valid_expression(x) for x in text.split(','))
262
                     except LinAlgError:
263
                         valid = all(validate_matrix_expression(x) for x in text.split(','))
264
265
                     self.button_animate.setEnabled(valid)
266
267
                 else:
268
                     try:
269
                         valid = self.matrix_wrapper.is_valid_expression(text)
270
                     except LinAlgError:
271
                         valid = validate_matrix_expression(text)
272
273
                     self.button_render.setEnabled(valid)
274
                     self.button_animate.setEnabled(valid)
275
276
             @pyqtSlot()
277
             def reset zoom(self) -> None:
278
                 """Reset the zoom level back to normal."""
279
                 self.plot.grid_spacing = self.plot.default_grid_spacing
280
                 self.plot.update()
281
282
             @pygtSlot()
283
             def reset_transformation(self) -> None:
284
                 """Reset the visualized transformation back to the identity."""
285
                 self.plot.visualize_matrix_transformation(self.matrix_wrapper['I'])
286
                 self.animating = False
287
                 self.animating_sequence = False
                 self.plot.update()
288
289
290
             @pygtSlot()
291
             def render_expression(self) -> None:
```

```
292
                 """Render the transformation given by the expression in the input box."""
293
                 try:
294
                     matrix = self.matrix wrapper.evaluate expression(self.lineedit expression box.text())
295
296
                 except LinAlgError:
                     self.show_error_message('Singular matrix', 'Cannot take inverse of singular matrix')
297
298
                     return
299
300
                 if self.is_matrix_too_big(matrix):
301
                     self.show_error_message('Matrix too big', "This matrix doesn't fit on the canvas")
302
                     return
303
304
                 self.plot.visualize matrix transformation(matrix)
305
                 self.plot.update()
306
307
             @nvatSlot()
308
             def animate_expression(self) -> None:
309
                  """Animate from the current matrix to the matrix in the expression box."""
310
                 self.button_render.setEnabled(False)
311
                 \verb|self.button_animate.setEnabled(False)|\\
312
313
                 matrix_start: MatrixType = np.array([
                     [self.plot.point_i[0], self.plot.point_j[0]],
314
315
                     [self.plot.point_i[1], self.plot.point_j[1]]
316
                 1)
317
318
                 text = self.lineedit_expression_box.text()
319
320
                 # If there's commas in the expression, then we want to animate each part at a time
                 if '.' in text:
321
322
                     current_matrix = matrix_start
323
                     self.animating sequence = True
324
325
                     # For each expression in the list, right multiply it by the current matrix,
326
                     # and animate from the current matrix to that new matrix
327
                     for expr in text.split(',')[::-1]:
328
                          try:
                             new\_matrix = self.matrix\_wrapper.evaluate\_expression(expr) \ @ \ current\_matrix
329
330
                          except LinAlgError:
                              self.show_error_message('Singular matrix', 'Cannot take inverse of singular matrix')
331
332
                              return
333
334
                          if not self.animating_sequence:
335
                              break
336
                          self.animate_between_matrices(current_matrix, new_matrix)
337
338
                         current_matrix = new_matrix
339
340
                         # Here we just redraw and allow for other events to be handled while we pause
341
                         self.plot.update()
342
                          QApplication.processEvents()
343
                          QThread.msleep(self.plot.display\_settings.animation\_pause\_length)
344
345
                     self.animating_sequence = False
346
347
                 # If there's no commas, then just animate directly from the start to the target
348
                 else:
                     # Get the target matrix and it's determinant
349
350
                     try:
351
                          matrix_target = self.matrix_wrapper.evaluate_expression(text)
352
353
                     except LinAlgError:
354
                          self.show_error_message('Singular matrix', 'Cannot take inverse of singular matrix')
355
                         return
356
357
                     # The concept of applicative animation is explained in /gui/settings.py
358
                     if self.plot.display_settings.applicative_animation:
359
                          matrix_target = matrix_target @ matrix_start
360
                     # If we want a transitional animation and we're animating the same matrix, then restart the animation
361
362
                     # We use this check rather than equality because of small floating point errors
363
                     elif (abs(matrix_start - matrix_target) < 1e-12).all():</pre>
364
                          matrix_start = self.matrix_wrapper['I']
```

```
365
366
                           # We pause here for 200 ms to make the animation look a bit nicer
367
                           self.plot.visualize_matrix_transformation(matrix_start)
368
                           self.plot.update()
369
                           QApplication.processEvents()
370
                           QThread.msleep(200)
371
                       {\tt self.animate\_between\_matrices(matrix\_start,\ matrix\_target)}
372
373
374
                  self.update_render_buttons()
375
              def animate_between_matrices(self, matrix_start: MatrixType, matrix_target: MatrixType, steps: int = 100) ->
376
              \hookrightarrow None:
                   """Animate from the start matrix to the target matrix."""
377
378
                  det_target = linalg.det(matrix_target)
379
                  det_start = linalg.det(matrix_start)
380
381
                  self.animating = True
382
383
                  for i in range(0, steps + 1):
384
                       if not self.animating:
385
                           break
386
387
                       # This proportion is how far we are through the loop
388
                       proportion = i / steps
389
                       # matrix_a is the start matrix plus some part of the target, scaled by the proportion
390
391
                       # If we just used matrix_a, then things would animate, but the determinants would be weird
                       matrix_a = matrix_start + proportion * (matrix_target - matrix_start)
392
393
394
                       \textbf{if} \ \ \text{self.plot.display\_settings.smoothen\_determinant} \ \ \textbf{and} \ \ \text{det\_start} \ \ \star \ \ \text{det\_target} \ > \ \emptyset \text{:}
395
                           # To fix the determinant problem, we get the determinant of matrix_a and use it to normalize
396
                           det_a = linalg.det(matrix_a)
397
398
                           # For a 2x2 matrix A and a scalar c, we know that det(cA) = c^2 det(A)
399
                           # We want B = cA such that det(B) = det(S), where S is the start matrix,
400
                           # so then we can scale it with the animation, so we get
401
                           \# \det(cA) = c^2 \det(A) = \det(S) \Rightarrow c = \operatorname{sqrt}(\operatorname{abs}(\det(S) / \det(A)))
402
                           # Then we scale A to get the determinant we want, and call that matrix_b
403
                           if det a == 0:
404
                                c = 0
405
                           else:
406
                               c = np.sqrt(abs(det_start / det_a))
407
408
                           matrix_b = c * matrix_a
409
                           det_b = linalg.det(matrix_b)
410
411
                           # matrix to render is the final matrix that we then render for this frame
412
                           # It's B, but we scale it over time to have the target determinant
413
                           # We want some C = dB such that det(C) is some target determinant T
414
415
                           \# \det(dB) = d^2 \det(B) = T \Rightarrow d = \operatorname{sqrt}(\operatorname{abs}(T / \det(B)))
416
417
                           # We're also subtracting 1 and multiplying by the proportion and then adding one
418
                           # This just scales the determinant along with the animation
419
420
                           # That is all of course, if we can do that
421
                            # We'll crash if we try to do this with det(B) == 0
422
                           if det b != 0:
423
                                scalar = 1 + proportion * (np.sqrt(abs(det_target / det_b)) - 1)
424
                                matrix_to_render = scalar * matrix_b
425
426
                           else:
427
                                matrix\_to\_render = matrix\_a
428
429
430
                           matrix_to_render = matrix_a
431
432
                       if self.is_matrix_too_big(matrix_to_render):
                           self.show_error_message('Matrix too big', "This matrix doesn't fit on the canvas")
433
434
435
436
                       \verb|self.plot.visualize_matrix_transformation(matrix_to_render)|\\
```

```
437
438
                     # We schedule the plot to be updated, tell the event loop to
439
                     # process events, and asynchronously sleep for 10ms
                     # This allows for other events to be processed while animating, like zooming in and out
440
441
                     self.plot.update()
442
                     QApplication.processEvents()
                     QThread.msleep(1000 // steps)
443
444
445
                 self.animating = False
446
447
             @pvgtSlot(DefineDialog)
             def dialog_define_matrix(self, dialog_class: Type[DefineDialog]) -> None:
448
449
                  """Open a generic definition dialog to define a new matrix.
450
451
                 The class for the desired dialog is passed as an argument. We create an
452
                 instance of this class and the dialog is opened asynchronously and modally
453
                 (meaning it blocks interaction with the main window) with the proper method
454
                 connected to the :meth: `QDialog.accepted` signal.
455
456
                 .. note:: ``dialog_class`` must subclass :class:`lintrans.gui.dialogs.define_new_matrix.DefineDialog`.
457
458
                 :param dialog_class: The dialog class to instantiate
459
                 :type dialog_class: Type[lintrans.gui.dialogs.define_new_matrix.DefineDialog]
460
461
                 # We create a dialog with a deepcopy of the current matrix_wrapper
462
                 # This avoids the dialog mutating this one
463
                 dialog: DefineDialog
464
465
                 if dialog_class == DefineVisuallyDialog:
466
                     dialog = DefineVisuallyDialog(
467
                         self,
468
                         matrix wrapper=deepcopy(self.matrix wrapper),
469
                         display_settings=self.plot.display_settings
470
471
                 else:
472
                     dialog = dialog_class(self, matrix_wrapper=deepcopy(self.matrix_wrapper))
473
474
                 # .open() is asynchronous and doesn't spawn a new event loop, but the dialog is still modal (blocking)
475
                 dialog.open()
476
477
                 # So we have to use the accepted signal to call a method when the user accepts the dialog
478
                 dialog.accepted.connect(self.assign_matrix_wrapper)
479
480
             @pyqtSlot()
481
             def assign matrix wrapper(self) -> None:
                  """Assign a new value to ``self.matrix_wrapper`` and give the expression box focus."""
482
483
                 self.matrix_wrapper = self.sender().matrix_wrapper
484
                 self.lineedit expression box.setFocus()
485
                 self.update_render_buttons()
486
487
             @pvqtSlot()
488
             def dialog_change_display_settings(self) -> None:
                  """Open the dialog to change the display settings."""
489
490
                 dialog = DisplaySettingsDialog(self, display_settings=self.plot.display_settings)
491
492
                 dialog.accepted.connect(lambda: self.assign_display_settings(dialog.display_settings))
493
494
             @pyqtSlot(DisplaySettings)
             def assign_display_settings(self, display_settings: DisplaySettings) -> None:
495
496
                  """Assign a new value to ``self.plot.display_settings`` and give the expression box focus."""
497
                 self.plot.display settings = display settings
498
                 self.plot.update()
499
                 self.lineedit_expression_box.setFocus()
500
                 self.update_render_buttons()
501
502
             def show_error_message(self, title: str, text: str, info: str | None = None) -> None:
503
                   "Show an error message in a dialog box.
504
505
                 :param str title: The window title of the dialog box
506
                 :param str text: The simple error message
507
                 :param info: The more informative error message
508
                 :type info: Optional[str]
509
```

```
dialog = QMessageBox(self)
511
                 dialog.setIcon(QMessageBox.Critical)
                 dialog.setWindowTitle(title)
512
513
                 dialog.setText(text)
514
515
                 if info is not None:
                      dialog.setInformativeText(info)
516
517
518
                 dialog.open()
519
                 # This is `finished` rather than `accepted` because we want to update the buttons no matter what
520
521
                 dialog.finished.connect(self.update_render_buttons)
522
             def is_matrix_too_big(self, matrix: MatrixType) -> bool:
523
524
                 """Check if the given matrix will actually fit onto the canvas.
525
526
                 Convert the elements of the matrix to canvas coords and make sure they fit within Qt's 32-bit integer limit.
527
                 :param MatrixType matrix: The matrix to check
528
529
                 :returns bool: Whether the matrix fits on the canvas
530
                 coords: \ list[tuple[int, \ int]] = [self.plot.canvas\_coords(*vector) \ \textit{for} \ vector \ \textit{in} \ matrix.T]
531
532
533
                 for x, y in coords:
                      if not (-2147483648 \leq x \leq 2147483647 and -2147483648 \leq y \leq 2147483647):
534
535
                          return True
536
537
                 return False
538
539
540
         def main(args: list[str]) -> None:
541
              """Run the GUI by creating and showing an instance of :class:`LintransMainWindow`.
542
543
              :param list[str] args: The args to pass to :class:`QApplication`
544
545
             app = QApplication(args)
546
             window = LintransMainWindow()
547
             window.show()
548
             sys.exit(app.exec_())
         A.6 gui/__init__.py
         # lintrans - The linear transformation visualizer
  1
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
  4
         # <https://www.gnu.org/licenses/gpl-3.0.html>
  6
         \hbox{\tt """} \textit{This package supplies the main GUI and associated dialogs for visualization.} \\ \hbox{\tt """}
  8
  9
         from . import dialogs, plots, settings, validate
 10
         from .main_window import main
 11
         __all__ = ['dialogs', 'main', 'plots', 'settings', 'validate']
 12
         A.7
                 gui/dialogs/settings.py
         # lintrans - The linear transformation visualizer
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
  5
         # <https://www.gnu.org/licenses/gpl-3.0.html>
         """This module provides dialogs to edit settings within the app."""
  8
  9
         from __future__ import annotations
 10
 11
         import abc
```

self.display\_settings = display\_settings
self.setWindowTitle('Change display settings')

self.dict\_checkboxes: dict[str, QCheckBox] = dict()

79 80

81 82

```
85
                 # === Create the widgets
86
                 # Basic stuff
87
 88
89
                 self.checkbox_draw_background_grid = QCheckBox(self)
90
                 self.checkbox_draw_background_grid.setText('Draw &background grid')
 91
                 self.checkbox_draw_background_grid.setToolTip(
92
                      'Draw the background grid (axes are always drawn)'
93
 94
                 self.dict_checkboxes['b'] = self.checkbox_draw_background_grid
95
                 self.checkbox_draw_transformed_grid = QCheckBox(self)
 96
97
                 self.checkbox draw transformed grid.setText('Draw t&ransformed grid')
98
                 {\tt self.checkbox\_draw\_transformed\_grid.setToolTip(}
99
                      'Draw the transformed grid (vectors are handled separately)'
100
101
                 self.dict_checkboxes['r'] = self.checkbox_draw_transformed_grid
102
                 self.checkbox_draw_basis_vectors = QCheckBox(self)
103
104
                 self.checkbox_draw_basis_vectors.setText('Draw basis &vectors')
105
                 self.checkbox_draw_basis_vectors.setToolTip(
106
                      'Draw the transformed basis vectors'
107
                 self.dict_checkboxes['v'] = self.checkbox_draw_basis_vectors
108
109
110
                 # Animations
111
                 self.checkbox_smoothen_determinant = QCheckBox(self)
112
113
                 self.checkbox_smoothen_determinant.setText('&Smoothen determinant')
114
                 {\tt self.checkbox\_smoothen\_determinant.setToolTip(}
115
                      'Smoothly animate the determinant transition during animation (if possible)'
116
117
                 self.dict_checkboxes['s'] = self.checkbox_smoothen_determinant
118
119
                 self.checkbox\_applicative\_animation = QCheckBox(self)
                 self.checkbox_applicative_animation.setText('&Applicative animation')
120
121
                 self.checkbox applicative animation.setToolTip(
122
                      'Animate the new transformation applied to the current one, \n'
123
                      'rather than just that transformation on its own
124
125
                 self.dict_checkboxes['a'] = self.checkbox_applicative_animation
126
                 self.label_animation_pause_length = QtWidgets.QLabel(self)
127
128
                 self.label_animation_pause_length.setText('Animation pause length (ms)')
129
                 self.label animation pause length.setToolTip(
130
                      'How many milliseconds to pause for in comma-separated animations'
131
132
133
                 self.lineedit_animation_pause_length = QtWidgets.QLineEdit(self)
134
                 self.lineedit_animation_pause_length.setValidator(QIntValidator(1, 999, self))
135
136
                 # Matrix info
137
138
                 {\tt self.checkbox\_draw\_determinant\_parallelogram} \ = \ {\tt QCheckBox(self)}
139
                 self.checkbox_draw_determinant_parallelogram.setText('Draw &determinant parallelogram')
140
                 self.checkbox draw determinant parallelogram.setToolTip(
141
                      'Shade the parallelogram representing the determinant of the matrix'
142
143
                 self.checkbox_draw_determinant_parallelogram.clicked.connect(self.update_gui)
144
                 \verb|self.dict_checkboxes['d']| = \verb|self.checkbox_draw_determinant_parallelogram||
145
                 {\tt self.checkbox\_show\_determinant\_value} \ = \ {\tt QCheckBox(self)}
146
                 self.checkbox_show_determinant_value.setText('Show de&terminant value')
147
148
                 self.checkbox show determinant value.setToolTip(
149
                      'Show the value of the determinant inside the parallelogram'
150
                 self.dict_checkboxes['t'] = self.checkbox_show_determinant_value
151
152
                 self.checkbox_draw_eigenvectors = QCheckBox(self)
153
                 {\tt self.checkbox\_draw\_eigenvectors.setText('Draw~\&eigenvectors')}
154
155
                 self.checkbox_draw_eigenvectors.setToolTip('Draw the eigenvectors of the transformations')
                 self.dict_checkboxes['e'] = self.checkbox_draw_eigenvectors
156
157
```

```
158
                  self.checkbox_draw_eigenlines = QCheckBox(self)
159
                  self.checkbox_draw_eigenlines.setText('Draw eigen&lines')
                  self.checkbox_draw_eigenlines.setToolTip('Draw the eigenlines (invariant lines) of the transformations')
160
161
                  self.dict_checkboxes['l'] = self.checkbox_draw_eigenlines
162
163
                  # === Arrange the widgets in QGroupBoxes
164
165
                  # Basic stuff
166
167
                  self.vlay_groupbox_basic_stuff = QVBoxLayout()
168
                  self.vlav groupbox basic stuff.setSpacing(20)
                  self.vlay_groupbox_basic_stuff.addWidget(self.checkbox_draw_background_grid)
169
170
                  self.vlay groupbox basic stuff.addWidget(self.checkbox draw transformed grid)
171
                  \verb|self.vlay_groupbox_basic_stuff.addWidget(self.checkbox_draw_basis_vectors)|\\
172
                  self.groupbox_basic_stuff = QGroupBox('Basic stuff', self)
173
174
                  self.groupbox_basic_stuff.setLayout(self.vlay_groupbox_basic_stuff)
175
                  # Animations
176
177
178
                  self.hlay_animation_pause_length = QHBoxLayout()
179
                  \verb|self.hlay_animation_pause_length.addWidget(self.label_animation_pause_length)| \\
180
                  {\tt self.hlay\_animation\_pause\_length.addWidget(self.lineedit\_animation\_pause\_length)}
181
182
                  self.vlay_groupbox_animations = QVBoxLayout()
183
                  self.vlay_groupbox_animations.setSpacing(20)
184
                  self.vlay_groupbox_animations.addWidget(self.checkbox_smoothen_determinant)
                  \verb|self.vlay_groupbox_animations.addWidget(self.checkbox_applicative_animation)|\\
185
186
                  \verb|self.vlay_groupbox_animations.addLayout(self.hlay_animation_pause_length)|\\
187
                  self.groupbox_animations = QGroupBox('Animations', self)
188
189
                  self.groupbox animations.setLayout(self.vlay groupbox animations)
190
191
                  # Matrix info
192
                  self.vlay_groupbox_matrix_info = QVBoxLayout()
193
194
                  self.vlay groupbox matrix info.setSpacing(20)
195
                  \verb|self.vlay_groupbox_matrix_info.addWidget(self.checkbox_draw_determinant_parallelogram)| \\
196
                  \verb|self.vlay_groupbox_matrix_info.addWidget(self.checkbox_show_determinant_value)| \\
                  self.vlay_groupbox_matrix_info.addWidget(self.checkbox_draw_eigenvectors)
197
198
                  self.vlay_groupbox_matrix_info.addWidget(self.checkbox_draw_eigenlines)
199
200
                  self.groupbox matrix info = OGroupBox('Matrix info', self)
201
                  \verb|self.groupbox_matrix_info.setLayout(self.vlay_groupbox_matrix_info)| \\
202
203
                  # Now arrange the groupboxes
                  self.vlay_options.addWidget(self.groupbox_basic_stuff)
204
                  self.vlay_options.addWidget(self.groupbox_animations)
205
206
                  self.vlay_options.addWidget(self.groupbox_matrix_info)
207
                  # Finally, we load the current settings and update the GUI
208
209
                  self.load_settings()
210
                  self.update_gui()
211
212
              def load_settings(self) -> None:
                  """Load the current display settings into the widgets."""
213
214
                  # Basic stuff
215
                  \verb|self.checkbox_draw_background_grid.setChecked(self.display_settings.draw_background_grid)| \\
216
                  self.checkbox_draw_transformed_grid.setChecked(self.display_settings.draw_transformed_grid)
217
                  \verb|self.checkbox_draw_basis_vectors.setChecked(self.display_settings.draw_basis_vectors)| \\
218
219
                  # Animations
                  \verb|self.checkbox_smoothen_determinant.setChecked(self.display_settings.smoothen_determinant)| \\
220
221
                  self.checkbox applicative animation.setChecked(self.display settings.applicative animation)
222
                  \verb|self.lineedit_animation_pause_length.setText(str(self.display_settings.animation_pause_length))| \\
223
224
                  # Matrix info
225
                  self.checkbox_draw_determinant_parallelogram.setChecked( |
                  \ \hookrightarrow \ \ \text{self.display\_settings.draw\_determinant\_parallelogram)}
                  \verb|self.checkbox_show_determinant_value.setChecked(self.display_settings.show_determinant_value)| \\
226
                  self.checkbox draw eigenvectors.setChecked(self.display settings.draw eigenvectors)
228
                  {\tt self.checkbox\_draw\_eigenlines.setChecked(self.display\_settings.draw\_eigenlines)}
229
```

```
230
             def confirm_settings(self) -> None:
231
                  """Build a :class:`lintrans.gui.settings.DisplaySettings` object and assign it."""
                  # Basic stuff
233
                  self.display_settings.draw_background_grid = self.checkbox_draw_background_grid.isChecked()
234
                  self.display_settings.draw_transformed_grid = self.checkbox_draw_transformed_grid.isChecked()
235
                  \verb|self.display_settings.draw_basis_vectors| = \verb|self.checkbox_draw_basis_vectors.isChecked()| \\
236
                  # Animations
238
                  \verb|self.display_settings.smoothen_determinant| = \verb|self.checkbox_smoothen_determinant.isChecked(|)|
239
                  self.display_settings.applicative_animation = self.checkbox_applicative_animation.isChecked()
240
                  self.display_settings.animation_pause_length = int(self.lineedit_animation_pause_length.text())
241
242
                  # Matrix info
243
                  {\tt self.display\_settings.draw\_determinant\_parallelogram} \ = \\
                  \ \hookrightarrow \ \ \text{self.checkbox\_draw\_determinant\_parallelogram.isChecked()}
244
                  {\tt self.display\_settings.show\_determinant\_value} \ = \ {\tt self.checkbox\_show\_determinant\_value.isChecked()}
245
                  {\tt self.display\_settings.draw\_eigenvectors} \ = \ {\tt self.checkbox\_draw\_eigenvectors.isChecked()}
246
                  self.display_settings.draw_eigenlines = self.checkbox_draw_eigenlines.isChecked()
247
248
                  self.accept()
249
250
             def update_gui(self) -> None:
251
                  """Update the GUI according to other widgets in the GUI.
252
253
                  For example, this method updates which checkboxes are enabled based on the values of other checkboxes.
254
255
                  \verb|self.checkbox_show_determinant_value.setEnabled(self.checkbox_draw_determinant_parallelogram.isChecked())| \\
256
257
             def keyPressEvent(self, event: QKeyEvent) -> None:
258
                  """Handle a :class:`QKeyEvent` by manually activating toggling checkboxes.
259
                  Qt handles these shortcuts automatically and allows the user to do ``Alt + Key``
260
                  to activate a simple shortcut defined with ``&``. However, I like to be able to
261
                  just hit ``Key`` and have the shortcut activate.
262
263
264
                  letter = event.text().lower()
265
                  key = event.key()
266
267
                  if letter in self.dict_checkboxes:
268
                      self.dict checkboxes[letter].animateClick()
269
270
                  # Return or keypad enter
271
                  elif kev == 0x010000004 or kev == 0x01000005:
272
                      self.button_confirm.click()
273
274
                  # Escape
275
                  elif key == 0x01000000:
276
                      self.button_cancel.click()
277
278
279
                      event.ianore()
         A.8
                  gui/dialogs/define_new_matrix.py
         # lintrans - The linear transformation visualizer
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
  5
         # <https://www.gnu.org/licenses/gpl-3.0.html>
         """This module provides an abstract :class:`DefineDialog` class and subclasses, allowing definition of new
  7

    matrices."""
```

```
8
9
        from __future__ import annotations
10
11
        import abc
12
13
        from numpy import array
        from PyQt5 import QtWidgets
14
15
        from PyQt5.QtCore import pyqtSlot
```

```
16
        from PyQt5.QtGui import QDoubleValidator, QKeySequence
17
        from PyQt5.QtWidgets import QGridLayout, QHBoxLayout, QShortcut, QSizePolicy, QSpacerItem, QVBoxLayout
18
19
        from lintrans.gui.dialogs.misc import FixedSizeDialog
20
        from lintrans.gui.plots import DefineVisuallyWidget
21
        from lintrans.gui.settings import DisplaySettings
        from lintrans.gui.validate import MatrixExpressionValidator
23
        from lintrans.matrices import MatrixWrapper
24
        from lintrans.typing_ import MatrixType
25
        ALPHABET_NO_I = 'ABCDEFGHJKLMNOPQRSTUVWXYZ'
26
27
28
        def is_valid_float(string: str) -> bool:
29
30
            """Check if the string is a valid float (or anything that can be cast to a float, such as an int).
31
            This function simply checks that ``float(string)`` doesn't raise an error.
32
33
            .. note:: An empty string is not a valid float, so will return False.
34
35
36
            :param str string: The string to check
37
            :returns bool: Whether the string is a valid float
38
39
            try:
40
                float(string)
41
                return True
            except ValueError:
42
43
                return False
44
45
46
        def round_float(num: float, precision: int = 5) -> str:
47
             """Round a floating point number to a given number of decimal places for pretty printing.
48
49
            :param float num: The number to round
50
            :param int precision: The number of decimal places to round to
51
            :returns str: The rounded number for pretty printing
52
            # Round to ``precision`` number of decimal places
53
54
            string = str(round(num, precision))
55
56
            # Cut off the potential final zero
57
            if string.endswith('.0'):
58
                return string[:-2]
59
60
            elif 'e' in string: # Scientific notation
61
                split = string.split('e')
                # The leading 0 only happens when the exponent is negative, so we know there'll be a minus sign
62
                return split[0] + 'e-' + split[1][1:].lstrip('0')
63
64
65
66
                return string
67
68
        class DefineDialog(FixedSizeDialog):
69
70
            """An abstract superclass for definitions dialogs.
71
72
            \dots \ \textit{warning::} \ \textit{This class should never be directly instantiated, only subclassed.}
73
74
            .. note::
75
               I would make this class have ``metaclass=abc.ABCMeta``, but I can't because it subclasses :class:`QDialog`,
76
               and every superclass of a class must have the same metaclass, and :class:`QDialog` is not an abstract class.
77
78
79
            def __init__(self, *args, matrix_wrapper: MatrixWrapper, **kwargs):
                 """Create the widgets and layout of the dialog.
80
                .. note:: ``*args`` and ``**kwargs`` are passed to the super constructor (:class:`QDialog`).
82
83
84
                :param MatrixWrapper matrix_wrapper: The MatrixWrapper that this dialog will mutate
85
86
                super().__init__(*args, **kwargs)
87
88
                self.matrix_wrapper = matrix_wrapper
```

```
89
                 self.setWindowTitle('Define a matrix')
 90
91
                 # === Create the widgets
92
93
                 self.button_confirm = QtWidgets.QPushButton(self)
94
                 self.button_confirm.setText('Confirm')
95
                 self.button_confirm.setEnabled(False)
96
                 self.button confirm.clicked.connect(self.confirm matrix)
97
                 self.button_confirm.setToolTip('Confirm this as the new matrix<br><b>(Ctrl + Enter)</b>')
 98
                 QShortcut(QKeySequence('Ctrl+Return'), self).activated.connect(self.button_confirm.click)
99
                 self.button_cancel = QtWidgets.QPushButton(self)
100
101
                 self.button cancel.setText('Cancel')
102
                 self.button_cancel.clicked.connect(self.reject)
                 self.button_cancel.setToolTip('Cancel this definition<br><<br/>b>')
103
104
105
                 self.label_equals = QtWidgets.QLabel()
106
                 self.label_equals.setText('=')
107
108
                 self.combobox_letter = QtWidgets.QComboBox(self)
109
110
                 for letter in ALPHABET_NO_I:
111
                     self.combobox_letter.addItem(letter)
112
113
                 self.combobox_letter.activated.connect(self.load_matrix)
114
                 # === Arrange the widgets
115
116
117
                 self.setContentsMargins(10, 10, 10, 10)
118
                 self.hlay_buttons = QHBoxLayout()
119
120
                 self.hlay buttons.setSpacing(20)
121
                 self.hlay_buttons.addItem(QSpacerItem(50, 5, hPolicy=QSizePolicy.Expanding, vPolicy=QSizePolicy.Minimum))
122
                 self.hlay_buttons.addWidget(self.button_cancel)
123
                 self.hlay_buttons.addWidget(self.button_confirm)
124
                 self.hlay_definition = QHBoxLayout()
125
126
                 self.hlay_definition.setSpacing(20)
127
                 self.hlay_definition.addWidget(self.combobox_letter)
128
                 self.hlay definition.addWidget(self.label equals)
129
130
                 self.vlay_all = QVBoxLayout()
131
                 self.vlay_all.setSpacing(20)
132
133
                 self.setLayout(self.vlay all)
134
135
             @property
136
             def selected letter(self) -> str:
                 """Return the letter currently selected in the combo box."""
137
138
                 return str(self.combobox_letter.currentText())
139
140
             @abc.abstractmethod
141
             @pygtSlot()
142
             def update_confirm_button(self) -> None:
143
                  """Enable the confirm button if it should be enabled, else, disable it."""
144
145
             @pyqtSlot(int)
146
             def load_matrix(self, index: int) -> None:
                  """Load the selected matrix into the dialog.
147
148
149
                 This method is optionally able to be overridden. If it is not overridden,
150
                 then no matrix is loaded when selecting a name.
151
152
                 We have this method in the superclass so that we can define it as the slot
153
                 for \ the \ : meth: `QComboBox.activated` \ signal \ in \ this \ constructor, \ rather \ than
154
                 having to define that in the constructor of every subclass.
155
156
157
             @abc.abstractmethod
158
             @pvatSlot()
159
             def confirm_matrix(self) -> None:
160
                 """Confirm the inputted matrix and assign it.
161
```

```
162
                  .. note:: When subclassing, this method should mutate ``self.matrix_wrapper`` and then call
             ``self.accept()``.
163
164
165
         class DefineVisuallyDialog(DefineDialog):
166
             """The dialog class that allows the user to define a matrix visually."""
167
168
             def __init__(self, *args, matrix_wrapper: MatrixWrapper, display_settings: DisplaySettings, **kwargs):
169
170
                  """Create the widgets and layout of the dialog.
171
172
                 :param MatrixWrapper matrix_wrapper: The MatrixWrapper that this dialog will mutate
173
174
                 super().__init__(*args, matrix_wrapper=matrix_wrapper, **kwargs)
175
176
                 self.setMinimumSize(700, 550)
177
178
                 # === Create the widgets
179
180
                 self.plot = DefineVisuallyWidget(self, display_settings=display_settings)
181
182
                 # === Arrange the widgets
183
                 self.hlay_definition.addWidget(self.plot)
184
185
                 self.hlay_definition.setStretchFactor(self.plot, 1)
186
                 self.vlay_all.addLayout(self.hlay_definition)
187
188
                 self.vlay_all.addLayout(self.hlay_buttons)
189
                 # We load the default matrix A into the plot
190
191
                 self.load matrix(0)
192
193
                 # We also enable the confirm button, because any visually defined matrix is valid
194
                 self.button_confirm.setEnabled(True)
195
196
197
             def update_confirm_button(self) -> None:
                 """Enable the confirm button.
198
199
200
                 .. note::
201
                    The confirm button is always enabled in this dialog and this method is never actually used,
202
                    so it's got an empty body. It's only here because we need to implement the abstract method.
203
204
205
             @pyqtSlot(int)
206
             def load_matrix(self, index: int) -> None:
207
                 """Show the selected matrix on the plot. If the matrix is None, show the identity."""
208
                 matrix = self.matrix_wrapper[self.selected_letter]
209
210
                 if matrix is None:
                     matrix = self.matrix_wrapper['I']
211
212
213
                 self.plot.visualize_matrix_transformation(matrix)
214
                 self.plot.update()
215
216
             @pygtSlot()
217
             def confirm_matrix(self) -> None:
218
                 """Confirm the matrix that's been defined visually."""
219
                 matrix: MatrixType = array([
220
                     [self.plot.point_i[0], self.plot.point_j[0]],
                     [self.plot.point_i[1], self.plot.point_j[1]]
221
222
                 1)
223
224
                 self.matrix wrapper[self.selected letter] = matrix
225
                 self.accept()
226
227
228
         class DefineNumericallyDialog(DefineDialog):
229
             """The dialog class that allows the user to define a new matrix numerically."""
230
231
             def __init__(self, *args, matrix_wrapper: MatrixWrapper, **kwargs):
232
                 """Create the widgets and layout of the dialog.
233
```

```
234
                  : param\ Matrix \textit{Wrapper}\ matrix\_\textit{wrapper}:\ The\ \textit{MatrixWrapper}\ that\ this\ dialog\ will\ \textit{mutate}
235
236
                 super().__init__(*args, matrix_wrapper=matrix_wrapper, **kwargs)
237
238
                 # === Create the widgets
239
240
                 # tl = top left, br = bottom right, etc.
241
                 self.element_tl = QtWidgets.QLineEdit(self)
242
                 self.element_tl.textChanged.connect(self.update_confirm_button)
243
                 self.element_tl.setValidator(QDoubleValidator())
244
245
                 self.element_tr = QtWidgets.QLineEdit(self)
246
                 self.element tr.textChanged.connect(self.update confirm button)
247
                 self.element_tr.setValidator(QDoubleValidator())
248
249
                 self.element bl = QtWidgets.QLineEdit(self)
250
                 self.element_bl.textChanged.connect(self.update_confirm_button)
251
                 self.element_bl.setValidator(QDoubleValidator())
252
253
                 self.element_br = QtWidgets.QLineEdit(self)
254
                 self.element br.textChanged.connect(self.update confirm button)
255
                 self.element_br.setValidator(QDoubleValidator())
256
257
                 self.matrix_elements = (self.element_tl, self.element_tr, self.element_bl, self.element_br)
258
259
                 # === Arrange the widgets
260
261
                 self.grid_matrix = QGridLayout()
262
                 self.grid matrix.setSpacing(20)
263
                 self.grid_matrix.addWidget(self.element_tl, 0, 0)
264
                 self.grid_matrix.addWidget(self.element_tr, 0, 1)
265
                 self.grid matrix.addWidget(self.element bl. 1, 0)
266
                 self.grid_matrix.addWidget(self.element_br, 1, 1)
267
                 self.hlay_definition.addLayout(self.grid_matrix)
268
269
270
                 self.vlay_all.addLayout(self.hlay_definition)
271
                 self.vlay_all.addLayout(self.hlay_buttons)
272
273
                 # We load the default matrix A into the boxes
274
                 self.load_matrix(0)
275
276
                 self.element_tl.setFocus()
277
278
             @pyqtSlot()
             def update_confirm_button(self) -> None:
279
280
                  """Enable the confirm button if there are valid floats in every box."""
281
                 for elem in self.matrix elements:
282
                      if not is_valid_float(elem.text()):
283
                          # If they're not all numbers, then we can't confirm it
                          {\tt self.button\_confirm.setEnabled(\textbf{False})}
284
285
                          return
286
                 # If we didn't find anything invalid
287
288
                 self.button_confirm.setEnabled(True)
289
290
             @pyqtSlot(int)
291
             def load_matrix(self, index: int) -> None:
                  """If the selected matrix is defined, load its values into the boxes."""
292
293
                 matrix = self.matrix_wrapper[self.selected_letter]
294
295
                 if matrix is None:
296
                      for elem in self.matrix_elements:
297
                         elem.setText('')
298
299
                      self.element_tl.setText(round_float(matrix[0][0]))
300
301
                      self.element_tr.setText(round_float(matrix[0][1]))
302
                      self.element_bl.setText(round_float(matrix[1][0]))
                      self.element_br.setText(round_float(matrix[1][1]))
303
304
305
                 self.update confirm button()
306
```

```
307
             @pyqtSlot()
308
             def confirm_matrix(self) -> None:
309
                  ""Confirm the matrix in the boxes and assign it to the name in the combo box."""
310
                 matrix: MatrixType = array([
311
                     [float(self.element_tl.text()), float(self.element_tr.text())],
312
                     [float(self.element_bl.text()), float(self.element_br.text())]
                 ])
313
314
315
                 self.matrix_wrapper[self.selected_letter] = matrix
316
                 self.accept()
317
318
         class DefineAsAnExpressionDialog(DefineDialog):
319
             """The dialog class that allows the user to define a matrix as an expression of other matrices."""
320
321
322
             def __init__(self, *args, matrix_wrapper: MatrixWrapper, **kwargs):
323
                   ""Create the widgets and layout of the dialog.
324
                 :param MatrixWrapper matrix_wrapper: The MatrixWrapper that this dialog will mutate
325
326
327
                 super().__init__(*args, matrix_wrapper=matrix_wrapper, **kwargs)
328
329
                 self.setMinimumWidth(450)
330
331
                 # === Create the widgets
332
333
                 self.lineedit_expression_box = QtWidgets.QLineEdit(self)
334
                 \verb|self.lineedit_expression_box.setPlaceholderText('Enter matrix expression...')| \\
335
                 self.lineedit expression box.textChanged.connect(self.update confirm button)
336
                 {\tt self.lineedit\_expression\_box.setValidator(MatrixExpressionValidator())}
337
338
                 # === Arrange the widgets
339
340
                 self.hlay_definition.addWidget(self.lineedit_expression_box)
341
342
                 self.vlay_all.addLayout(self.hlay_definition)
343
                 self.vlay all.addLayout(self.hlay buttons)
344
345
                 # Load the matrix if it's defined as an expression
346
                 self.load matrix(0)
347
348
                 self.lineedit_expression_box.setFocus()
349
350
             @pyqtSlot()
351
             def update_confirm_button(self) -> None:
                   ""Enable the confirm button if the matrix expression is valid in the wrapper."""
352
353
                 text = self.lineedit_expression_box.text()
354
                 valid_expression = self.matrix_wrapper.is_valid_expression(text)
355
356
                 self.button_confirm.setEnabled(valid_expression and self.selected_letter not in text)
357
358
             @pyqtSlot(int)
359
             def load_matrix(self, index: int) -> None:
                  ""If the selected matrix is defined an expression, load that expression into the box."""
360
361
                 if (expr := self.matrix_wrapper.get_expression(self.selected_letter)) is not None:
362
                     self.lineedit expression box.setText(expr)
363
                 else:
364
                     self.lineedit_expression_box.setText('')
365
366
             @pyqtSlot()
367
             def confirm matrix(self) -> None:
                  """Evaluate the matrix expression and assign its value to the name in the combo box."""
368
369
                 self.matrix_wrapper[self.selected_letter] = self.lineedit_expression_box.text()
370
                 self.accept()
```

## A.9 gui/dialogs/misc.py

```
1  # lintrans - The linear transformation visualizer
2  # Copyright (C) 2022 D. Dyson (DoctorDalek1963)
```

```
# This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
6
 7
        """This module provides miscellaneous dialog classes like :class:`AboutDialog`."""
8
9
        from __future__ import annotations
10
11
        import platform
12
13
        from PyQt5 import QtWidgets
        from Pv0t5.0tCore import Ot
14
        from PyQt5.QtWidgets import QDialog, QVBoxLayout
15
16
17
        import lintrans
18
19
20
        class FixedSizeDialog(QDialog):
21
            """A simple superclass to create modal dialog boxes with fixed size.
22
23
            We override the :meth:`open` method to set the fixed size as soon as the dialog is opened modally.
24
25
26
            def open(self) -> None:
27
                 """Override :meth:`QDialog.open` to set the dialog to a fixed size."""
28
                super().open()
29
                self.setFixedSize(self.size())
30
31
32
        class AboutDialog(FixedSizeDialog):
33
            """A simple dialog class to display information about the app to the user.
34
35
            It only has an :meth:`__init__` method because it only has label widgets, so no other methods are necessary
        \hookrightarrow here.
36
            0.00
37
38
                 _init__(self, *args, **kwargs):
                """Create an :class:`AboutDialog` object with all the label widgets."""
39
40
                super().__init__(*args, **kwargs)
41
42
                self.setWindowTitle('About lintrans')
43
44
                # === Create the widgets
45
46
                label_title = QtWidgets.QLabel(self)
47
                label_title.setText(f'lintrans (version {lintrans.__version__})')
48
                label_title.setAlignment(Qt.AlignCenter)
49
50
                font_title = label_title.font()
51
                font_title.setPointSize(font_title.pointSize() * 2)
52
                label_title.setFont(font_title)
53
54
                label_version_info = QtWidgets.QLabel(self)
55
                label version info.setText(
                    56
57
                    f'Running on {platform.platform()}
58
59
                label\_version\_info.setAlignment(Qt.AlignCenter)
60
                label_info = QtWidgets.QLabel(self)
61
62
                label_info.setText(
63
                     'lintrans is a program designed to help visualise<br>'
                    '2D linear transformations represented with matrices.<br>
64
65
                    "It's designed for teachers and students and any feedback<br>"
66
                    'is greatly appreciated at <a href="https://github.com/DoctorDalek1963/lintrans" '
67
                    'style="color: black;">my GitHub page</a><br>or via email '
68
                    '(<a href="mailto:dyson.dyson@icloud.com" style="color: black;">dyson.dyson@icloud.com</a>).'
69
70
                label_info.setAlignment(Qt.AlignCenter)
71
                label_info.setTextFormat(Qt.RichText)
                label_info.setOpenExternalLinks(True)
73
74
                label_copyright = QtWidgets.QLabel(self)
75
                {\tt label\_copyright.setText} (
```

```
'This program is free software.<br/>copyright 2021-2022 D. Dyson (DoctorDalek1963).<br/>dr>'
77
                    'This program is licensed under GPLv3, which can be found
78
                    '<a href="https://www.gnu.org/licenses/gpl-3.0.html" style="color: black;">here</a>.'
79
80
                label_copyright.setAlignment(Qt.AlignCenter)
                label_copyright.setTextFormat(Qt.RichText)
81
                label\_copyright.setOpenExternalLinks(\textbf{True})
82
83
84
                # === Arrange the widgets
85
                self.setContentsMargins(10, 10, 10, 10)
86
87
88
                vlay = QVBoxLayout()
                vlay.setSpacing(20)
89
                vlay.addWidget(label_title)
90
                vlay.addWidget(label_version_info)
91
92
                vlay.addWidget(label_info)
93
                vlay.addWidget(label_copyright)
94
95
                self.setLayout(vlay)
        A.10
                  gui/dialogs/__init__.py
        # lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
 4
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 7
        """This package provides separate dialogs for the main GUI.
 8
 9
        These dialogs are for defining new matrices in different ways and editing settings.
10
        from .define_new_matrix import DefineAsAnExpressionDialog, DefineDialog, DefineNumericallyDialog,
12

→ DefineVisuallyDialog

13
        from .misc import AboutDialog
        from .settings import DisplaySettingsDialog
14
        __all__ = ['DefineAsAnExpressionDialog', 'DefineDialog', 'DefineNumericallyDialog', 'DefineVisuallyDialog',
16
                   'AboutDialog', 'DisplaySettingsDialog']
17
```

## A.11 gui/plots/classes.py

```
# lintrans - The linear transformation visualizer
 2
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 7
        """This module provides superclasses for plotting transformations."""
 8
        from __future__ import annotations
10
11
        from abc import abstractmethod
12
        from typing import Iterable
13
14
        import numpy as np
        from nptyping import Float, NDArray
15
16
        from PyQt5.QtCore import QPoint, QRectF, Qt
        from PyQt5.QtGui import QBrush, QColor, QPainter, QPainterPath, QPaintEvent, QPen, QWheelEvent
17
        from PyQt5.QtWidgets import QWidget
18
19
        from lintrans.typing_ import MatrixType
20
21
23
        class BackgroundPlot(OWidget):
24
            """This class provides a background for plotting, as well as setup for a Qt widget.
```

```
26
            This class provides a background (untransformed) plane, and all the backend
27
            details for a Qt application, but does not provide useful functionality. To
28
            be useful, this class must be subclassed and behaviour must be implemented
29
            by the subclass.
30
            .. warning:: This class should never be directly instantiated, only subclassed.
31
32
33
            .. note::
               I would make this class have ``metaclass=abc.ABCMeta``, but I can't because it subclasses :class:`QWidget`,
34
               and every superclass of a class must have the same metaclass, and :class: `QWidget` is not an abstract class.
35
36
37
38
            default\_grid\_spacing: int = 85
39
            minimum_grid_spacing: int = 5
40
41
            def __init__(self, *args, **kwargs):
                """Create the widget and setup backend stuff for rendering.
43
44
                \dots note:: ``*args`` and ``**kwargs`` are passed the superclass constructor (:class:`QWidget`).
45
46
                super().__init__(*args, **kwargs)
47
48
                self.setAutoFillBackground(True)
49
50
                # Set the background to white
51
                palette = self.palette()
                palette.setColor(self.backgroundRole(), Qt.white)
52
53
                self.setPalette(palette)
54
55
                # Set the grid colour to grey and the axes colour to black
56
                self.colour background grid = QColor('#808080')
57
                self.colour_background_axes = QColor('#000000')
58
                self.grid_spacing = BackgroundPlot.default_grid_spacing
59
                self.width\_background\_grid: float = 0.3
60
61
62
            @property
63
            def canvas_origin(self) -> tuple[int, int]:
64
                 """Return the canvas coords of the grid origin.
65
66
                The return value is intended to be unpacked and passed to a :meth:`QPainter.drawLine:iiii` call.
67
68
                See :meth:`canvas_coords`.
69
                :returns: The canvas coordinates of the grid origin
70
71
                :rtype: tuple[int, int]
72
73
                return self.width() // 2, self.height() // 2
74
75
            def canvas_x(self, x: float) -> int:
76
                 """Convert an x coordinate from grid coords to canvas coords."""
77
                return int(self.canvas_origin[0] + x * self.grid_spacing)
78
79
            def canvas_y(self, y: float) -> int:
                 """Convert a y coordinate from grid coords to canvas coords."""
80
81
                return int(self.canvas_origin[1] - y * self.grid_spacing)
82
            def canvas_coords(self, x: float, y: float) -> tuple[int, int]:
83
84
                 """Convert a coordinate from grid coords to canvas coords.
85
                This method is intended to be used like
86
87
88
                .. code::
89
90
                   painter.drawLine(*self.canvas_coords(x1, y1), *self.canvas_coords(x2, y2))
91
92
                or like
93
94
                .. code::
95
96
                   painter.drawLine(*self.canvas origin, *self.canvas coords(x, y))
97
```

```
98
                 See :attr:`canvas_origin`.
99
100
                 :param float x: The x component of the grid coordinate
                  :param float y: The y component of the grid coordinate
101
102
                 :returns: The resultant canvas coordinates
103
                 :rtype: tuple[int, int]
104
105
                 return self.canvas_x(x), self.canvas_y(y)
106
107
             def grid_corner(self) -> tuple[float, float]:
                   ""Return the grid coords of the top right corner."""
108
                 return self.width() / (2 * self.grid_spacing), self.height() / (2 * self.grid_spacing)
109
110
111
             def grid_coords(self, x: int, y: int) -> tuple[float, float]:
112
                  """Convert a coordinate from canvas coords to grid coords.
113
114
                  :param int x: The x component of the canvas coordinate
115
                 :param int y: The y component of the canvas coordinate
116
                 :returns: The resultant grid coordinates
117
                  :rtype: tuple[float, float]
118
119
                 # We get the maximum grid coords and convert them into canvas coords
                  \textbf{return} \ (\textbf{x} - \texttt{self.canvas\_origin[0]}) \ / \ \texttt{self.grid\_spacing}, \ (-\textbf{y} + \texttt{self.canvas\_origin[1]}) \ / \ \texttt{self.grid\_spacing} 
120
121
122
             @abstractmethod
123
             def paintEvent(self, event: QPaintEvent) -> None:
                  """Handle a :class:`QPaintEvent`.
124
125
126
                  .. note:: This method is abstract and must be overridden by all subclasses.
127
128
129
             def draw_background(self, painter: QPainter, draw_grid: bool) -> None:
130
                  """Draw the background grid.
131
                 .. note:: This method is just a utility method for subclasses to use to render the background grid.
132
133
134
                 :param QPainter painter: The painter to draw the background with
135
                 :param bool draw_grid: Whether to draw the grid lines
136
                 if draw grid:
137
138
                      painter.setPen(QPen(self.colour_background_grid, self.width_background_grid))
139
140
                      # Draw equally spaced vertical lines, starting in the middle and going out
141
                      # We loop up to half of the width. This is because we draw a line on each side in each iteration
142
                      for x in range(self.width() // 2 + self.grid_spacing, self.width(), self.grid_spacing):
143
                          painter.drawLine(x, 0, x, self.height())
144
                          painter.drawLine(self.width() - x, 0, self.width() - x, self.height())
145
146
                      # Same with the horizontal lines
                      for y in range(self.height() // 2 + self.grid_spacing, self.height(), self.grid_spacing):
147
148
                          painter.drawLine(0, y, self.width(), y)\\
149
                          painter.drawLine(0, self.height() - y, self.width(), self.height() - y)
150
                 # Now draw the axes
151
                 painter.setPen(QPen(self.colour_background_axes, self.width_background_grid))
152
153
                 painter.drawLine(self.width() // 2, 0, self.width() // 2, self.height())
154
                 painter.drawLine(0, self.height() \ // \ 2, self.width(), self.height() \ // \ 2)
155
156
             def wheelEvent(self, event: OWheelEvent) -> None:
157
                  """Handle a :class:`QWheelEvent` by zooming in or our of the grid."""
158
                 # angleDelta() returns a number of units equal to 8 times the number of degrees rotated
159
                 degrees = event.angleDelta() / 8
160
161
                 if degrees is not None:
162
                      new_spacing = max(1, self.grid_spacing + degrees.y())
163
                      if new_spacing >= self.minimum_grid_spacing:
164
165
                          self.grid_spacing = new_spacing
166
                 event.accent()
167
168
                 self.update()
169
```

```
171
         class VectorGridPlot(BackgroundPlot):
172
             """This class represents a background plot, with vectors and their grid drawn on top.
173
174
             This class should be subclassed to be used for visualization and matrix definition widgets.
175
             All useful behaviour should be implemented by any subclass.
176
177
             .. warning:: This class should never be directly instantiated, only subclassed.
178
179
             def __init__(self, *args, **kwargs):
    """Create the widget with ``point_i`` and ``point_j`` attributes.
180
181
182
183
                 .. note:: ``*args`` and ``**kwargs`` are passed to the superclass constructor (:class:`BackgroundPlot`).
184
185
                 super().__init__(*args, **kwargs)
186
187
                 self.point_i: tuple[float, float] = (1., 0.)
188
                 self.point_j: tuple[float, float] = (0., 1.)
189
190
                 self.colour_i = QColor('#0808d8')
191
                 self.colour_j = QColor('#e90000')
192
                 self.colour_eigen = QColor('#13cf00')
                 self.colour_text = QColor('#000000')
193
194
195
                 self.width_vector_line = 1.8
196
                 self.width_transformed_grid = 0.8
197
198
                 self.arrowhead\_length = 0.15
199
                 self.max_parallel_lines = 150
200
201
202
             @property
203
             def matrix(self) -> MatrixType:
204
                 """Return the assembled matrix of the basis vectors."""
205
                 return np.array([
206
                      [self.point_i[0], self.point_j[0]],
207
                      [self.point_i[1], self.point_j[1]]
208
                 1)
209
210
             @property
211
             def det(self) -> float:
                  """Return the determinant of the assembled matrix."""
212
213
                 return float(np.linalg.det(self.matrix))
214
215
             @property
             def eigs(self) -> Iterable[tuple[float, NDArray[(1, 2), Float]]]:
216
217
                 """Return the eigenvalues and eigenvectors zipped together to be iterated over.
218
219
                 :rtype: Iterable[tuple[float, NDArray[(1, 2), Float]]]
220
221
                 values, vectors = np.linalg.eig(self.matrix)
222
                 return zip(values, vectors.T)
223
224
             @abstractmethod
225
             def paintEvent(self, event: QPaintEvent) -> None:
226
                  """Handle a :class:`QPaintEvent`.
227
228
                 .. note:: This method is abstract and must be overridden by all subclasses.
229
230
231
             def draw_parallel_lines(self, painter: QPainter, vector: tuple[float, float], point: tuple[float, float]) ->

→ None:

232
                 """Draw a set of evenly spaced grid lines parallel to ``vector`` intersecting ``point``.
233
234
                 :param QPainter painter: The painter to draw the lines with
235
                 :param vector: The vector to draw the grid lines parallel to
236
                 :type vector: tuple[float, float]
237
                 :param point: The point for the lines to intersect with
                 :type point: tuple[float, float]
238
239
240
                 max_x, max_y = self.grid_corner()
241
                 vector_x, vector_y = vector
242
                 point_x, point_y = point
```

```
244
                  # If the determinant is 0
245
                  if abs(vector_x * point_y - vector_y * point_x) < 1e-12:</pre>
246
                      rank = np.linalg.matrix_rank(
247
                          np.array([
248
                              [vector_x, point_x],
249
                              [vector_y, point_y]
250
                          ])
251
                      )
252
253
                      # If the matrix is rank 1, then we can draw the column space line
254
                      if rank == 1:
255
                          if abs(vector x) < 1e-12:
                              painter.drawLine(self.width() // 2, 0, self.width() // 2, self.height())
256
257
                          elif abs(vector_y) < 1e-12:</pre>
                              painter.drawLine(0, self.height() // 2, self.width(), self.height() // 2)
258
259
                          else:
260
                              self.draw_oblique_line(painter, vector_y / vector_x, 0)
261
262
                      # If the rank is 0, then we don't draw any lines
263
                      else:
264
                          return
265
266
                  elif abs(vector_x) < 1e-12 and abs(vector_y) < 1e-12:</pre>
267
                      # If both components of the vector are practically 0, then we can't render any grid lines
268
269
270
                  # Draw vertical lines
271
                  elif abs(vector_x) < 1e-12:</pre>
272
                      painter.drawLine(self.canvas\_x(\emptyset),\ \emptyset,\ self.canvas\_x(\emptyset),\ self.height())
273
274
                      for i in range(max(abs(int(max x / point x)), self.max parallel lines)):
275
                          painter.drawLine(
276
                              self.canvas_x((i + 1) * point_x),
277
                              0.
278
                              self.canvas_x((i + 1) * point_x),
279
                              self.height()
280
                          )
281
                          painter.drawLine(
                              self.canvas_x(-1 * (i + 1) * point_x),
282
283
                              0.
284
                              self.canvas_x(-1 * (i + 1) * point_x),
285
                              self.height()
286
                          )
287
                  # Draw horizontal lines
288
289
                  elif abs(vector_y) < 1e-12:</pre>
                      painter.drawLine(0, self.canvas\_y(0), self.width(), self.canvas\_y(0))
290
291
292
                      for i in range(max(abs(int(max_y / point_y)), self.max_parallel_lines)):
293
                          painter.drawLine(
294
                              0,
295
                              self.canvas_y((i + 1) * point_y),
296
                              self.width().
297
                              self.canvas_y((i + 1) * point_y)
298
299
                          painter.drawLine(
300
                              0,
301
                              self.canvas_y(-1 * (i + 1) * point_y),
302
                              self.width(),
303
                              self.canvas_y(-1 * (i + 1) * point_y)
304
305
306
                  # If the line is oblique, then we can use y = mx + c
307
                  else:
308
                      m = vector_y / vector_x
309
                      c = point_y - m * point_x
310
311
                      self.draw_oblique_line(painter, m, 0)
312
313
                      # We don't want to overshoot the max number of parallel lines,
314
                      # but we should also stop looping as soon as we can't draw any more lines
315
                      for i in range(1, self.max_parallel_lines + 1):
```

```
316
                          if not self.draw_pair_of_oblique_lines(painter, m, i * c):
317
                              break
318
319
             def draw_pair_of_oblique_lines(self, painter: QPainter, m: float, c: float) -> bool:
320
                  """Draw a pair of oblique lines, using the equation y = mx + c.
321
                 This method just calls :meth:`draw_oblique_line` with ``c`` and ``-c``,
323
                 and returns True if either call returned True.
324
325
                 :param QPainter painter: The painter to draw the vectors and grid lines with
326
                 :param float m: The gradient of the lines to draw
327
                 :param float c: The y-intercept of the lines to draw. We use the positive and negative versions
328
                 :returns bool: Whether we were able to draw any lines on the canvas
329
330
                 return any([
331
                     self.draw_oblique_line(painter, m, c),
332
                     self.draw_oblique_line(painter, m, -c)
333
                 1)
334
335
             def draw_oblique_line(self, painter: QPainter, m: float, c: float) -> bool:
336
                  """Draw an oblique line, using the equation y = mx + c.
337
                 We only draw the part of the line that fits within the canvas, returning True if
338
339
                 we were able to draw a line within the boundaries, and False if we couldn't draw a line
340
341
                 :param QPainter painter: The painter to draw the vectors and grid lines with
                 :param float m: The gradient of the line to draw
342
343
                 :param float c: The y-intercept of the line to draw
344
                 :returns bool: Whether we were able to draw a line on the canvas
345
346
                 max_x, max_y = self.grid_corner()
347
348
                 # These variable names are shortened for convenience
349
                 # myi is max_y_intersection, mmyi is minus_max_y_intersection, etc.
350
                 myi = (max_y - c) / m
351
                 mmyi = (-max_y - c) / m
352
                 mxi = max_x * m + c
353
                 mmxi = -max\_x \ * \ m \ + \ c
354
355
                 # The inner list here is a list of coords, or None
356
                 # If an intersection fits within the bounds, then we keep its coord,
357
                 # else it is None, and then gets discarded from the points list
358
                 # By the end, points is a list of two coords, or an empty list
359
                 points: list[tuple[float, float]] = [
360
                     x for x in [
                         (myi, max_y) if -max_x < myi < max_x else None,
361
362
                          (mmyi, -max_y) if -max_x < mmyi < max_x else None,
363
                          (max_x, mxi) if -max_y < mxi < max_y else None,</pre>
364
                          (-max_x, mmxi) if -max_y < mmxi < max_y else None
365
                     ] if x is not None
                 1
366
367
368
                 # If no intersections fit on the canvas
369
                 if len(points) < 2:</pre>
370
                     return False
371
372
                 # If we can, then draw the line
373
                 else:
374
                     painter.drawLine(
375
                          *self.canvas_coords(*points[0]),
376
                          *self.canvas_coords(*points[1])
377
                     )
378
                     return True
379
380
             def draw_transformed_grid(self, painter: QPainter) -> None:
381
                  """Draw the transformed version of the grid, given by the basis vectors.
382
383
                 .. note:: This method draws the grid, but not the basis vectors. Use :meth:`draw_basis_vectors` to draw
         \hookrightarrow them.
384
385
                 :param QPainter painter: The painter to draw the grid lines with
386
387
                 # Draw all the parallel lines
```

```
388
                 painter.setPen(QPen(self.colour_i, self.width_transformed_grid))
389
                 self.draw_parallel_lines(painter, self.point_i, self.point_j)
                 painter.setPen(QPen(self.colour_j, self.width_transformed_grid))
390
391
                 self.draw_parallel_lines(painter, self.point_j, self.point_i)
392
393
             def draw_arrowhead_away_from_origin(self, painter: QPainter, point: tuple[float, float]) -> None:
394
                  """Draw an arrowhead at ``point``, pointing away from the origin.
395
396
                 :param QPainter painter: The painter to draw the arrowhead with
397
                 :param point: The point to draw the arrowhead at, given in grid coords
398
                 :type point: tuple[float, float]
399
400
                 # This algorithm was adapted from a C# algorithm found at
401
                 # http://csharphelper.com/blog/2014/12/draw-lines-with-arrowheads-in-c/
402
403
                 \# Get the x and y coords of the point, and then normalize them
404
                 # We have to normalize them, or else the size of the arrowhead will
405
                 # scale with the distance of the point from the origin
406
                 x, y = point
407
                 vector_length = np.sqrt(x * x + y * y)
408
409
                 if vector_length < 1e-12:</pre>
410
                      return
411
412
                 nx = x / vector_length
413
                 ny = y / vector_length
414
                 \# We choose a length and find the steps in the x and y directions
415
416
                 length = min(
                     {\tt self.arrowhead\_length} \ * \ {\tt self.default\_grid\_spacing} \ / \ {\tt self.grid\_spacing},
417
418
                      vector_length
419
420
                 dx = length * (-nx - ny)
421
                 dy = length * (nx - ny)
422
423
                 # Then we just plot those lines
424
                 painter.drawLine(*self.canvas\_coords(x, y), *self.canvas\_coords(x + dx, y + dy))
425
                 painter.drawLine(*self.canvas\_coords(x, y), *self.canvas\_coords(x - dy, y + dx))
426
427
             def draw_position_vector(self, painter: QPainter, point: tuple[float, float], colour: QColor) -> None:
428
                  """Draw a vector from the origin to the given point.
429
430
                 :param QPainter painter: The painter to draw the position vector with
431
                 :param point: The tip of the position vector in grid coords
432
                 :type point: tuple[float, float]
433
                 :param QColor colour: The colour to draw the position vector in
434
435
                 painter.setPen(QPen(colour, self.width vector line))
436
                 painter.drawLine(*self.canvas_origin, *self.canvas_coords(*point))
437
                 self.draw_arrowhead_away_from_origin(painter, point)
438
439
             def draw_basis_vectors(self, painter: QPainter) -> None:
440
                  """Draw arrowheads at the tips of the basis vectors.
441
                 :param QPainter painter: The painter to draw the basis vectors with
442
443
444
                 self.draw_position_vector(painter, self.point_i, self.colour_i)
445
                 self.draw_position_vector(painter, self.point_j, self.colour_j)
446
447
             def draw_determinant_parallelogram(self, painter: QPainter) -> None:
448
                  """Draw the parallelogram of the determinant of the matrix.
449
450
                  :param QPainter painter: The painter to draw the parallelogram with
451
452
                 if self.det == 0:
453
                     return
454
455
                 path = QPainterPath()
456
                 path.moveTo(*self.canvas origin)
                 path.lineTo(*self.canvas_coords(*self.point_i))
457
458
                 path.lineTo(*self.canvas\_coords(self.point\_i[0] + self.point\_j[0], self.point\_i[1] + self.point\_j[1]))
459
                 path.lineTo(*self.canvas_coords(*self.point_j))
460
```

```
461
                 color = (16, 235, 253) if self.det > 0 else (253, 34, 16)
462
                 brush = QBrush(QColor(*color, alpha=128), Qt.SolidPattern)
463
464
                 painter.fillPath(path, brush)
465
466
             def draw_determinant_text(self, painter: QPainter) -> None:
467
                  """Write the string value of the determinant in the middle of the parallelogram.
468
469
                 :param QPainter painter: The painter to draw the determinant text with
470
471
                 painter.setPen(QPen(self.colour_text, self.width_vector_line))
472
473
                 # We're building a QRect that encloses the determinant parallelogram
474
                 # Then we can center the text in this QRect
475
                 coords: list[tuple[float, float]] = [
476
                     (0, 0),
477
                     self.point_i,
478
                     self.point_j,
479
                     (
480
                          self.point_i[0] + self.point_j[0],
481
                         self.point_i[1] + self.point_j[1]
482
                      )
483
                 ]
484
485
                 xs = [t[0] for t in coords]
486
                 ys = [t[1] for t in coords]
487
488
                 top_left = QPoint(*self.canvas_coords(min(xs), max(ys)))
                 bottom_right = QPoint(*self.canvas_coords(max(xs), min(ys)))
489
490
491
                 rect = QRectF(top_left, bottom_right)
492
493
                 painter.drawText(
494
                     rect,
495
                      Qt.AlignHCenter | Qt.AlignVCenter,
496
                      f'{self.det:.2f}'
497
498
499
             def draw_eigenvectors(self, painter: QPainter) -> None:
500
                  """Draw the eigenvectors of the displayed matrix transformation.
501
502
                 :param QPainter painter: The painter to draw the eigenvectors with
503
504
                 for value, vector in self.eigs:
505
                     x = value * vector[0]
                     y = value * vector[1]
506
507
508
                      if x.imag != 0 or y.imag != 0:
509
                          continue
510
                      self.draw_position_vector(painter, (x, y), self.colour_eigen)
511
512
513
                     # Now we need to draw the eigenvalue at the tip of the eigenvector
514
515
                      offset = 3
516
                      top left: QPoint
517
                      bottom_right: QPoint
518
                      alignment_flags: int
519
520
                      if x >= 0 and y >= 0: # Q1
521
                          top_left = QPoint(self.canvas_x(x) + offset, 0)
                         bottom_right = QPoint(self.width(), self.canvas_y(y) - offset)
522
523
                          alignment\_flags = Qt.AlignLeft \ | \ Qt.AlignBottom
524
525
                      elif x < 0 and y >= 0: # Q2
526
                          top_left = QPoint(0, 0)
527
                          bottom_right = QPoint(self.canvas_x(x) - offset, self.canvas_y(y) - offset)
528
                          alignment\_flags = Qt.AlignRight \ | \ Qt.AlignBottom
529
                      elif x < 0 and y < 0: # Q3
530
531
                          top_left = QPoint(0, self.canvas_y(y) + offset)
532
                         bottom_right = QPoint(self.canvas_x(x) - offset, self.height())
533
                          alignment\_flags = Qt.AlignRight \mid Qt.AlignTop
```

```
534
535
                     else: # Q4
                         top_left = QPoint(self.canvas_x(x) + offset, self.canvas_y(y) + offset)
536
537
                         bottom_right = QPoint(self.width(), self.height())
538
                         alignment_flags = Qt.AlignLeft | Qt.AlignTop
539
540
                     painter.setPen(QPen(self.colour_text, self.width_vector_line))
541
                     painter.drawText(QRectF(top_left, bottom_right), alignment_flags, f'{value:.2f}')
542
543
             def draw_eigenlines(self, painter: QPainter) -> None:
                  """Draw the eigenlines (invariant lines).
544
545
546
                 :param OPainter painter: The painter to draw the eigenlines with
547
548
                 painter.setPen(QPen(self.colour_eigen, self.width_transformed_grid))
549
550
                 for value, vector in self.eigs:
551
                     if value.imag != 0:
                         continue
552
553
554
                     x, y = vector
555
556
                     if x == 0:
557
                         x mid = int(self.width() / 2)
558
                         painter.drawLine(x_mid, 0, x_mid, self.height())
559
560
                     elif y == 0:
561
                         y_mid = int(self.height() / 2)
                         painter.drawLine(0, y\_mid, self.width(), y\_mid)
562
563
564
565
                         self.draw_oblique_line(painter, y / x, 0)
         A.12
                   gui/plots/__init__.py
         # lintrans - The linear transformation visualizer
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
         # <https://www.gnu.org/licenses/gpl-3.0.html>
  6
         """This package provides widgets for the visualization plot in the main window and the visual definition dialog."""
  8
  9
         from . import classes
 10
         from .widgets import DefineVisuallyWidget, VisualizeTransformationWidget
 11
         __all__ = ['classes', 'DefineVisuallyWidget', 'VisualizeTransformationWidget']
         A.13
                   gui/plots/widgets.py
         # lintrans - The linear transformation visualizer
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
         # <https://www.gnu.org/licenses/gpl-3.0.html>
  6
         """This module provides the actual widgets that can be used to visualize transformations in the GUI."""
  9
         from future import annotations
 10
 11
         from PyQt5.QtCore import Qt
         \textbf{from } \textbf{PyQt5.QtGui import} \textbf{ QMouseEvent, QPainter, QPaintEvent}
 12
 13
 14
         from .classes import VectorGridPlot
 15
         from lintrans.typing_ import MatrixType
```

from lintrans.gui.settings import DisplaySettings

```
19
        class VisualizeTransformationWidget(VectorGridPlot):
20
            """This class is the widget that is used in the main window to visualize transformations.
21
            It handles all the rendering itself, and the only method that the user needs to
22
23
            worry about is :meth:`visualize_matrix_transformation`, which allows you to visualize
24
            the given matrix transformation.
26
27
            def __init__(self, *args, display_settings: DisplaySettings, **kwargs):
                 """Create the widget and assign its display settings, passing ``*args`` and ``**kwargs`` to super."""
28
                super().__init__(*args, **kwargs)
29
30
31
                self.display_settings = display_settings
32
            def visualize_matrix_transformation(self, matrix: MatrixType) -> None:
34
                 """Transform the grid by the given matrix.
35
                .. warning:: This method does not call ``update()``. This must be done by the caller.
36
37
38
39
                   This method transforms the background grid, not the basis vectors. This
40
                   means that it cannot be used to compose transformations. Compositions
41
                    should be done by the user.
42
43
                :param MatrixType matrix: The matrix to transform by
45
                self.point_i = (matrix[0][0], matrix[1][0])
46
                self.point_j = (matrix[0][1], matrix[1][1])
47
48
            def paintEvent(self, event: QPaintEvent) -> None:
                 """Handle a :class:`\mathtt{QPaintEvent}` by drawing the background grid and the transformed grid.
49
50
51
                The transformed grid is defined by the basis vectors i and j, which can
52
                be controlled with the :meth:`visualize_matrix_transformation` method.
53
54
                painter = QPainter()
55
                painter.begin(self)
56
57
                painter.setRenderHint(QPainter.Antialiasing)
58
                painter.setBrush(Ot.NoBrush)
59
60
                self.draw_background(painter, self.display_settings.draw_background_grid)
61
62
                if self.display_settings.draw_eigenlines:
63
                    self.draw_eigenlines(painter)
64
                if self.display_settings.draw_eigenvectors:
65
66
                    self.draw_eigenvectors(painter)
67
68
                \textbf{if} \ \texttt{self.display\_settings.draw\_determinant\_parallelogram:}
69
                    self.draw_determinant_parallelogram(painter)
70
71
                     if self.display_settings.show_determinant_value:
                         self.draw_determinant_text(painter)
73
74
                if self.display_settings.draw_transformed_grid:
75
                     self.draw_transformed_grid(painter)
                if self.display_settings.draw_basis_vectors:
77
78
                     self.draw_basis_vectors(painter)
79
80
                nainter.end()
                event.accept()
81
82
83
84
        class DefineVisuallyWidget(VisualizeTransformationWidget):
85
             """This class is the widget that allows the user to visually define a matrix.
86
87
            This is just the widget itself. If you want the dialog, use
            : class: \verb|`lintrans.gui.dialogs.define_new_matrix.DefineVisuallyDialog\verb|`|.
88
89
90
91
            def __init__(self, *args, display_settings: DisplaySettings, **kwargs):
```

```
"""Create the widget and enable mouse tracking. ``*args`` and ``**kwargs`` are passed to ``super()``."""
93
                 super().__init__(*args, display_settings=display_settings, **kwargs)
94
95
                 self.dragged_point: tuple[float, float] | None = None
96
                 \# This is the distance that the cursor needs to be from the point to drag it
97
98
                 self.epsilon: int = 5
99
100
             def mousePressEvent(self, event: QMouseEvent) -> None:
                  """Handle a QMouseEvent when the user pressed a button."""
101
                 mx = event.x()
102
103
                 my = event.y()
104
                 button = event.button()
105
106
                 if button != Qt.LeftButton:
107
                     event.ignore()
                     return
108
109
                 for point in (self.point_i, self.point_j):
110
111
                     px, py = self.canvas_coords(*point)
                     if abs(px - mx) <= self.epsilon and abs(py - my) <= self.epsilon:</pre>
112
                         self.dragged_point = point[0], point[1]
113
114
115
                 event.accept()
116
117
             def mouseReleaseEvent(self, event: QMouseEvent) -> None:
                  """Handle a QMouseEvent when the user release a button."""
118
119
                 if event.button() == Qt.LeftButton:
120
                     self.dragged_point = None
121
                     event.accept()
122
123
                     event.ignore()
124
             def mouseMoveEvent(self, event: QMouseEvent) -> None:
125
                  """Handle the mouse moving on the canvas.""'
126
127
                 mx = event.x()
128
                 my = event.y()
129
130
                 if self.dragged_point is not None:
131
                     x, y = self.grid_coords(mx, my)
132
                     if self.dragged_point == self.point_i:
133
134
                         self.point_i = x, y
135
136
                     elif self.dragged_point == self.point_j:
137
                         self.point_j = x, y
138
139
                     self.dragged_point = x, y
140
                     self.update()
141
142
143
                     event.accept()
144
145
                 event.ignore()
```

## A.14 matrices/parse.py

```
# lintrans - The linear transformation visualizer
# Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)

# This program is licensed under GNU GPLv3, available here:
# <a href="https://www.gnu.org/licenses/gpl-3.0.html">https://www.gnu.org/licenses/gpl-3.0.html</a>

"""This module provides functions to parse and validate matrix expressions."""

from __future__ import annotations

import re
from dataclasses import dataclass
from typing import Pattern
```

```
15
        from lintrans.typing_ import MatrixParseList
16
17
        NAIVE_CHARACTER_CLASS = r'[-+\sA-Z0-9.rot()^{}]'
18
19
20
        class MatrixParseError(Exception):
21
            """A simple exception to be raised when an error is found when parsing."""
22
23
24
        def compile_naive_expression_pattern() -> Pattern[str]:
25
            """Compile the single RegEx pattern that will match a valid matrix expression."""
26
            digit_no_zero = '[123456789]'
            digits = ' \d+'
27
28
            integer_no_zero = digit_no_zero + '(' + digits + ')?'
            real\_number = f'(\{integer\_no\_zero\}(\\.\{digits\})?|0\\.\{digits\})'
29
30
31
            index_content = f'(-?{integer_no_zero}|T)'
32
            index = f'(\\^{{{index_content}}}|\\^{index_content})'
33
            matrix\_identifier = f'([A-Z]|rot\(-?\{real\_number\}\))|\(\{NAIVE\_CHARACTER\_CLASS\}+\))'
34
            matrix = '(' + real_number + '?' + matrix_identifier + index + '?)'
            expression = f'^-?{matrix}+(()+-?|-){matrix}+)*
35
36
37
            return re.compile(expression)
38
39
        # This is an expensive pattern to compile, so we compile it when this module is initialized
40
41
        naive_expression_pattern = compile_naive_expression_pattern()
42
43
44
        def find_sub_expressions(expression: str) -> list[str]:
45
             """Find all the sub-expressions in the given expression.
46
            This function only goes one level deep, so may return strings like ``'A(BC)D'``.
47
48
49
            : raises \ \textit{MatrixParseError} : \textit{If there are unbalanced parentheses}
50
            sub_expressions: list[str] = []
51
52
            string =
53
            paren_depth = 0
54
            pointer = 0
55
56
            while True:
57
                char = expression[pointer]
58
                if char == '(' and expression[pointer - 3:pointer] != 'rot':
59
60
                    paren_depth += 1
61
62
                     # This is a bit of a manual bodge, but it eliminates extraneous parens
63
                     if paren_depth == 1:
                        pointer += 1
64
65
                         continue
66
                elif char == ')' and re.match(f'{NAIVE_CHARACTER_CLASS}*?rot\\([-\\d.]+$', expression[:pointer]) is None:
67
68
                     paren_depth -= 1
69
70
                if paren_depth > 0:
71
                    string += char
72
73
                if paren_depth == 0 and string:
74
                    sub_expressions.append(string)
75
                     string = '
76
77
                pointer += 1
78
79
                if pointer >= len(expression):
80
                    break
81
82
            if paren_depth != 0:
                raise MatrixParseError('Unbalanced parentheses in expression')
83
84
85
            return sub expressions
86
```

```
88
         def validate_matrix_expression(expression: str) -> bool:
89
              """Validate the given matrix expression.
90
91
             This function simply checks the expression against the BNF schema documented in
92
             :ref:`expression-syntax-docs`. It is not aware of which matrices are actually defined
93
             in a wrapper. For an aware version of this function, use the
94
             :meth:`lintrans.matrices.wrapper.MatrixWrapper.is valid expression` method.
95
96
             :param str expression: The expression to be validated
97
             :returns bool: Whether the expression is valid according to the schema
98
99
             # Remove all whitespace
             expression = re.sub(r'\s', '', expression)
100
101
102
             match = naive_expression_pattern.match(expression)
103
104
             if match is None:
105
                 return False
106
107
             # Check that the whole expression was matched against
108
             if expression != match.group(0):
109
                 return False
110
111
112
                 sub_expressions = find_sub_expressions(expression)
             except MatrixParseError:
113
114
                 return False
115
             if not sub_expressions:
116
117
                 return True
118
119
             return all(validate_matrix_expression(m) for m in sub_expressions)
120
121
122
         @dataclass
123
         class MatrixToken:
             """A simple dataclass to hold information about a matrix token being parsed."""
124
125
             multiplier: str = ''
126
             identifier: str = ''
127
             exponent: str = ''
128
129
130
             @property
131
             def tuple(self) -> tuple[str, str, str]:
                  """Create a tuple of the token for parsing."""
132
133
                 return self.multiplier, self.identifier, self.exponent
134
135
         class ExpressionParser:
136
             """A class to hold state during parsing."""
137
138
139
             def init (self, expression: str):
                 """Create an instance of the parser with the given expression."""
140
141
                 # Remove all whitespace
                 expression = re.sub(r'\s', '', expression)
142
143
                 # Check if it's valid
144
145
                 if not validate_matrix_expression(expression):
146
                     raise MatrixParseError('Invalid expression')
147
                 # Wrap all exponents and transposition powers with {}
148
149
                 expression = re.sub(r'(?<=\^)(-?\d+|T)(?=[^\}]|$)', r'{\g<0>}', expression)
150
151
                 # Remove any standalone minuses
152
                 expression = re.sub(r'-(?=[A-Z])', '-1', expression)
153
154
                 # Replace subtractions with additions
155
                 expression = re.sub(r'-(?=\d+\.?\d*([A-Z]|rot))', '+-', expression)
156
157
                 # Get rid of a potential leading + introduced by the last step
158
                 expression = re.sub(r'^\+', '', expression)
159
```

```
160
                 self.expression = expression
161
                 self.pointer: int = 0
162
                 self.current_token: MatrixToken = MatrixToken()
163
164
                 self.current_group: list[tuple[str, str, str]] = []
165
                 self.final_list: MatrixParseList = []
166
167
168
             def __repr__(self) -> str:
169
                  """Return a simple repr."""
                 return f'{self.__class__.__module__}.{self.__class__.__name__}("{self.expression}")'
170
171
172
             @property
173
             def char(self) -> str:
174
                 """Return the char pointed to by the pointer."""
175
                 return self.expression[self.pointer]
176
177
             def parse(self) -> MatrixParseList:
                   ""Parse the instance's matrix expression and return the MatrixParseList.
178
179
180
                 :returns MatrixParseList: The parsed expression
181
                 self._parse_multiplication_group()
182
183
184
                 while self.pointer < len(self.expression):</pre>
185
                     if self.expression[self.pointer] != '+':
                         raise MatrixParseError('Expected "+" between multiplication groups')
186
187
188
                     self.pointer += 1
189
                     self._parse_multiplication_group()
190
                 return self.final_list
191
192
193
             def _parse_multiplication_group(self) -> None:
                   "Parse a group of matrices to be multiplied.
194
195
196
                 :returns bool: Success or failure
197
198
                 while self._parse_matrix():
                     if self.pointer >= len(self.expression) or self.char == '+':
199
200
                          self.final_list.append(self.current_group)
201
                          self.current_group = []
202
                         self.pointer += 1
203
204
             def _parse_matrix(self) -> bool:
                  """Parse a full matrix using :meth:`_parse_matrix_part`.
205
206
207
                 :returns bool: Success or failure
208
209
                 self.current_token = MatrixToken()
210
211
                 while self._parse_matrix_part():
212
                     pass # The actual execution is taken care of in the loop condition
214
                 if self.current_token.identifier == '':
215
                     return False
216
217
                 self.current_group.append(self.current_token.tuple)
218
                 return True
219
220
             def _parse_matrix_part(self) -> bool:
221
                  """Parse part of a matrix (multiplier, identifier, or exponent) from the expression and pointer.
222
                 .. note:: This method mutates ``self.current_token``.
223
224
225
                 :returns bool: Success or failure
226
                 :raises MatrixParseError: If we fail to parse this part of the token
227
228
                 if self.pointer >= len(self.expression):
                     return False
229
230
231
                 if self.char.isdigit() or self.char == '-':
                     if self.current_token.multiplier != '' \
232
```

```
233
                              or (self.current_token.multiplier == '' and self.current_token.identifier != ''):
234
                         return False
235
236
                     self._parse_multiplier()
237
238
                 elif self.char.isalpha() and self.char.isupper():
239
                     if self.current_token.identifier != '':
                         return False
240
241
242
                     self.current_token.identifier = self.char
243
                     self.pointer += 1
244
245
                 elif self.char == 'r':
                     if self.current_token.identifier != '':
246
247
                         return False
248
249
                     self._parse_rot_identifier()
250
                 elif self.char == '(':
251
252
                     if self.current_token.identifier != '':
253
                         return False
254
255
                     self._parse_sub_expression()
256
                 elif self.char == '^':
257
258
                     if self.current_token.exponent != '':
259
                         return False
260
261
                     self. parse exponent()
262
263
                 elif self.char == '+':
264
                     return False
265
266
                     raise MatrixParseError(f'Unrecognised character "{self.char}" in matrix expression')
267
268
269
                 return True
270
271
             def _parse_multiplier(self) -> None:
272
                  """Parse a multiplier from the expression and pointer.
273
274
                 .. note:: This method mutates ``self.current_token.multiplier``.
275
276
                 :raises MatrixParseError: If we fail to parse this part of the token
277
                 multiplier = ''
278
279
280
                 while self.char.isdigit() or self.char in ('.', '-'):
281
                     multiplier += self.char
282
                     self.pointer += 1
283
284
                 # There can only be one dot in the multiplier
285
                 if len(multiplier.split('.')) > 2:
                     raise MatrixParseError(f'Multiplier "{multiplier}" has more than one dot')
286
287
                 if '-' in multiplier and '-' in multiplier[1:]:
288
                     raise MatrixParseError('Character "-" can only occur at the start of a multiplier')
289
290
291
                 self.current_token.multiplier = multiplier
292
293
             def _parse_rot_identifier(self) -> None:
                  """Parse a ``rot()``-style identifier from the expression and pointer.
294
295
296
                 .. note:: this method mutates ``self.current_token.identifier``.
297
298
                 :raises MatrixParseError: If we fail to parse this part of the token
299
300
                 if match := re.match(r'rot)([^()]+), self.expression[self.pointer:]):
301
                     self.current_token.identifier = match.group(0)
                     self.pointer += len(match.group(0))
302
303
                 else:
304
                     raise MatrixParseError(f'Invalid rot-identifier "{self.expression[self.pointer:self.pointer + 15] |
         }...")
```

```
305
306
             def _parse_sub_expression(self) -> None:
307
                   ""Parse a parenthesized sub-expression as the identifier, from the expression and pointer.
308
309
                 .. note:: this method mutates ``self.current_token.identifier``.
310
                 :raises MatrixParseError: If we fail to parse this part of the token
311
312
313
                 if self.char != '(':
314
                     raise MatrixParseError('Sub-expression must start with "("')
315
                 self.pointer += 1
316
317
                 paren depth = 1
                 identifier = ''
318
319
320
                 while paren_depth > 0:
321
                     if self.char == '(':
322
                         paren_depth += 1
                     elif self.char == ')':
323
324
                         paren_depth -= 1
325
326
                     if paren_depth == 0:
327
                         self.pointer += 1
328
                         break
329
330
                     identifier += self.char
331
                     self.pointer += 1
332
333
                 self.current_token.identifier = identifier
334
335
             def _parse_exponent(self) -> None:
336
                   ""Parse a matrix exponent from the expression and pointer.
337
                 .. note:: this method mutates ``self.current_token.exponent``.
338
339
340
                 :raises MatrixParseError: If we fail to parse this part of the token
341
                 if match := re.match(r'\^\{(-?\d+|T)\)', self.expression[self.pointer:]):
342
343
                     self.current_token.exponent = match.group(1)
344
                     self.pointer += len(match.group(0))
345
                 else:
                     raise MatrixParseError(f'Invalid exponent "{self.expression[self.pointer:self.pointer + 10]}..."')
346
347
348
349
         def parse_matrix_expression(expression: str) -> MatrixParseList:
350
              \hbox{\tt ""Parse the matrix expression and return a : data: `lintrans.typing\_.MatrixParseList`.}
351
352
             :Example:
353
354
             >>> parse_matrix_expression('A')
             [[('', 'A', '')]]
355
356
             >>> parse_matrix_expression('-3M^2')
357
             [[('-3', 'M', '2')]]
             >>> parse\_matrix\_expression('1.2rot(12)^{3}2B^T')
358
359
             [[('1.2', 'rot(12)', '3'), ('2', 'B', 'T')]]
             >>> parse_matrix_expression('A^2 + 3B')
360
             [[('', 'A', '2')], [('3', 'B', '')]]
361
             >>> parse_matrix_expression('-3A^{-1}3B^T - 45M^2')
362
             [[('-3', 'A', '-1'), ('3', 'B', 'T')], [('-45', 'M', '2')]]
363
364
             >>> parse\_matrix\_expression('5.3A^{4} 2.6B^{-2} + 4.6D^T 8.9E^{-1}')
             [[('5.3', 'A', '4'), ('2.6', 'B', '-2')], [('4.6', 'D', 'T'), ('8.9', 'E', '-1')]]
365
366
             >>> parse_matrix_expression('2(A+B^TC)^2D')
367
             [[('2', 'A+B^{T}C', '2'), ('', 'D', '')]]
368
369
             :param str expression: The expression to be parsed
370
             :returns: A list of parsed components
371
             :rtype: :data:`lintrans.typing_.MatrixParseList`
372
373
             return ExpressionParser(expression).parse()
```

#### A.15 matrices/\_\_init\_\_.py

```
# lintrans - The linear transformation visualizer
Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)

# This program is licensed under GNU GPLv3, available here:
# <https://www.gnu.org/licenses/gpl-3.0.html>

"""This package supplies classes and functions to parse, evaluate, and wrap matrices."""

from . import parse
from .wrapper import create_rotation_matrix, MatrixWrapper

__all__ = ['create_rotation_matrix', 'MatrixWrapper', 'parse']
```

#### A.16 matrices/wrapper.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
 4
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 5
 6
        """This module contains the main :class:`MatrixWrapper` class and a function to create a matrix from an angle."""
 8
 9
        from __future__ import annotations
10
11
        import re
12
        from copy import copy
13
        from functools import reduce
14
        from operator import add, matmul
15
        from typing import Any, Optional, Union
16
17
        import numpy as np
18
19
        from .parse import parse_matrix_expression, validate_matrix_expression
20
        from lintrans.typing_ import is_matrix_type, MatrixType
21
22
23
        class MatrixWrapper:
24
            """A wrapper class to hold all possible matrices and allow access to them.
25
26
            .. note::
               When defining a custom matrix, its name must be a capital letter and cannot be ``I``.
27
28
29
            The contained matrices can be accessed and assigned to using square bracket notation.
30
31
            :Example:
32
33
            >>> wrapper = MatrixWrapper()
34
            >>> wrapper['I']
35
            array([[1., 0.],
36
                  [0., 1.]])
37
            >>> wrapper['M'] # Returns None
            >>> wrapper['M'] = np.array([[1, 2], [3, 4]])
38
            >>> wrapper['M']
39
40
            array([[1., 2.],
41
                  [3., 4.]])
43
44
            def __init__(self):
                """Initialize a :class:`MatrixWrapper` object with a dictionary of matrices which can be accessed."""
45
                self._matrices: dict[str, Optional[Union[MatrixType, str]]] = {
46
47
                     'A': None, 'B': None, 'C': None, 'D': None,
48
                    'E': None, 'F': None, 'G': None, 'H': None,
49
                    'I': np.eye(2), # I is always defined as the identity matrix
                    'J': None, 'K': None, 'L': None, 'M': None,
                    'N': None, '0': None, 'P': None, 'Q': None,
51
                    'R': None, 'S': None, 'T': None, 'U': None,
52
```

Centre number: 123456

```
53
                     'V': None, 'W': None, 'X': None, 'Y': None,
54
                     'Z': None
55
                 }
 56
57
             def repr (self) -> str:
                  """Return a nice string repr of the :class:`MatrixWrapper` for debugging."""
58
                 defined_matrices = ''.join([k for k, v in self._matrices.items() if v is not None])
59
60
                 return f'<{self.__class__.__module__}.{self.__class__.__name__} object with ' \</pre>
61
                        f"{len(defined_matrices)} defined matrices: '{defined_matrices}'>"
62
63
             def __eq__(self, other: Any) -> bool:
                 """Check for equality in wrappers by comparing dictionaries.
64
65
66
                 :param Any other: The object to compare this wrapper to
67
68
                 if not isinstance(other, self.__class__):
69
                     return NotImplemented
 70
                 # We loop over every matrix and check if every value is equal in each
 71
 72
                 for name in self._matrices:
 73
                     s_matrix = self[name]
 74
                     o_matrix = other[name]
 75
 76
                     if s matrix is None and o matrix is None:
 77
                         continue
 78
 79
                     elif (s matrix is None and o matrix is not None) or \
80
                          (s_matrix is not None and o_matrix is None):
81
                         return False
82
                     # This is mainly to satisfy mypy, because we know these must be matrices
83
84
                     elif not is_matrix_type(s_matrix) or not is_matrix_type(o_matrix):
85
                         return False
86
                     # Now we know they're both NumPy arrays
87
88
                     elif np.array_equal(s_matrix, o_matrix):
89
                         continue
90
91
92
                         return False
93
94
                 return True
95
96
                 __hash__(self) -> int:
97
                  """Return the hash of the matrices dictionary."""
98
                 return hash(self._matrices)
99
100
             def __getitem__(self, name: str) -> Optional[MatrixType]:
101
                   ""Get the matrix with the given name.
102
                 If it is a simple name, it will just be fetched from the dictionary. If the name is ``rot(x)``, with
103
104
                 a given angle in degrees, then we return a new matrix representing a rotation by that angle.
105
106
                 .. note::
107
                    If the named matrix is defined as an expression, then this method will return its evaluation.
108
                    If you want the expression itself, use :meth: 'get expression'.
109
                 :param str name: The name of the matrix to get
110
111
                 :returns Optional[MatrixType]: The value of the matrix (could be None)
112
113
                 :raises NameError: If there is no matrix with the given name
114
                 # Return a new rotation matrix
115
                 if (match := re.match(r'rot\((-?\d^*\.?\d^*)\)', name)) is not None:
116
117
                     return create_rotation_matrix(float(match.group(1)))
118
                 if name not in self._matrices:
119
120
                     if validate_matrix_expression(name):
121
                         return self.evaluate_expression(name)
122
123
                     raise NameError(f'Unrecognised matrix name "{name}"')
124
125
                 # We copy the matrix before we return it so the user can't accidentally mutate the matrix
```

```
126
                 matrix = copy(self._matrices[name])
127
128
                 if isinstance(matrix, str):
129
                     return self.evaluate_expression(matrix)
130
131
                 return matrix
132
             def __setitem__(self, name: str, new_matrix: Optional[Union[MatrixType, str]]) -> None:
133
134
                  ""Set the value of matrix ``name`` with the new_matrix.
135
                 The new matrix may be a simple 2x2 NumPy array, or it could be a string, representing an
136
                 expression in terms of other, previously defined matrices.
137
138
                 :param str name: The name of the matrix to set the value of
139
                 :param Optional[Union[MatrixType, str]] new_matrix: The value of the new matrix (could be None)
140
141
142
                 :raises NameError: If the name isn't a legal matrix name
143
                 :raises TypeError: If the matrix isn't a valid 2x2 NumPy array or expression in terms of other defined

    matrices

144
                 :raises ValueError: If you attempt to define a matrix in terms of itself
145
                 if not (name in self._matrices and name != 'I'):
146
                     raise NameError('Matrix name is illegal')
147
148
149
                 if new matrix is None:
150
                     self._matrices[name] = None
151
                     return
152
153
                 if isinstance(new matrix, str):
154
                     if self.is_valid_expression(new_matrix):
                         if name not in new_matrix:
155
156
                             self. matrices[name] = new matrix
157
                             return
158
                             raise ValueError('Cannot define a matrix recursively')
159
160
161
                 if not is matrix type(new matrix):
                     raise TypeError('Matrix must be a 2x2 NumPy array')
162
163
                 # All matrices must have float entries
164
165
                 a = float(new_matrix[0][0])
166
                 b = float(new_matrix[0][1])
167
                 c = float(new matrix[1][0])
168
                 d = float(new_matrix[1][1])
169
                 self._matrices[name] = np.array([[a, b], [c, d]])
170
171
172
             def get expression(self. name: str) -> Optional[str]:
173
                   ""If the named matrix is defined as an expression, return that expression, else return None.
174
                 :param str name: The name of the matrix
175
176
                 :returns Optional[str]: The expression that the matrix is defined as, or None
177
178
                 :raises NameError: If the name is invalid
179
180
                 if name not in self. matrices:
181
                     raise NameError('Matrix must have a legal name')
182
183
                 matrix = self. matrices[name]
184
                 if isinstance(matrix, str):
185
                     return matrix
186
187
                 return None
188
189
             def is_valid_expression(self, expression: str) -> bool:
190
                 """Check if the given expression is valid, using the context of the wrapper.
191
192
                 This method calls :func:`lintrans.matrices.parse.validate_matrix_expression`, but also
193
                 ensures that all the matrices in the expression are defined in the wrapper.
194
195
                 :param str expression: The expression to validate
196
                 :returns bool: Whether the expression is valid in this wrapper
197
```

```
198
                 :raises LinAlgError: If a matrix is defined in terms of the inverse of a singular matrix
199
                 # Get rid of the transposes to check all capital letters
200
201
                 new_expression = expression.replace('^T', '').replace('^{T}', '')
202
203
                 # Make sure all the referenced matrices are defined
204
                 for matrix in [x for x in new_expression if re.match('[A-Z]', x)]:
                     if self[matrix] is None:
205
206
                         return False
207
                     if (expr := self.get_expression(matrix)) is not None:
208
209
                         if not self.is_valid_expression(expr):
210
                             return False
211
212
                 return validate_matrix_expression(expression)
214
             def evaluate_expression(self, expression: str) -> MatrixType:
215
                 """Evaluate a given expression and return the matrix evaluation.
216
217
                 :param str expression: The expression to be parsed
218
                 :returns MatrixType: The matrix result of the expression
219
220
                 :raises ValueError: If the expression is invalid
221
222
                 if not self.is_valid_expression(expression):
223
                     raise ValueError('The expression is invalid')
224
225
                 parsed_result = parse_matrix_expression(expression)
                 final_groups: list[list[MatrixType]] = []
226
228
                 for group in parsed_result:
229
                     f_group: list[MatrixType] = []
230
231
                     for multiplier, identifier, index in group:
232
                         if index == 'T':
233
                             m = self[identifier]
234
235
                             # This assertion is just so mypy doesn't complain
236
                             # We know this won't be None, because we know that this matrix is defined in this wrapper
237
                             assert m is not None
238
                             matrix_value = m.T
239
240
                         else:
241
                             matrix_value = np.linalg.matrix_power(self[identifier], 1 if index == '' else int(index))
242
                         matrix_value *= 1 if multiplier == '' else float(multiplier)
243
244
                         f_group.append(matrix_value)
245
246
                     final_groups.append(f_group)
247
248
                 return reduce(add, [reduce(matmul, group) for group in final_groups])
249
250
251
         def create_rotation_matrix(angle: float, *, degrees: bool = True) -> MatrixType:
252
             """Create a matrix representing a rotation (anticlockwise) by the given angle.
253
254
             :Example:
255
             >>> create_rotation_matrix(30)
256
257
             array([[ 0.8660254, -0.5
258
                    [ 0.5
                              , 0.8660254]])
259
             >>> create_rotation_matrix(45)
260
             array([[ 0.70710678, -0.70710678],
261
                   [ 0.70710678, 0.70710678]])
262
             >>> create_rotation_matrix(np.pi / 3, degrees=False)
263
             array([[ 0.5
                              , -0.8660254],
                    [ 0.8660254, 0.5
264
                                           77)
265
266
             :param float angle: The angle to rotate anticlockwise by
267
             :param bool degrees: Whether to interpret the angle as degrees (True) or radians (False)
268
             :returns MatrixType: The resultant matrix
269
270
             rad = np.deg2rad(angle) if degrees else angle
```

# A.17 typing\_/\_\_init\_\_.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
        """This package supplies type aliases for linear algebra and transformations.
 8
9
        .. note::
10
          This package is called ``typing_`` and not ``typing`` to avoid name collisions with the
           builtin :mod:`typing`. I don't quite know how this collision occurs, but renaming
11
12
           this module fixed the problem.
13
14
15
        from __future__ import annotations
16
17
        from typing import Any, TypeGuard
18
        from numpy import ndarray
19
20
        from nptyping import NDArray, Float
21
22
        __all__ = ['is_matrix_type', 'MatrixType', 'MatrixParseList']
23
24
        MatrixType = NDArray[(2, 2), Float]
        """This type represents a 2x2 matrix as a NumPy array."""
25
26
27
        MatrixParseList = list[list[tuple[str, str, str]]]
        """This is a list containing lists of tuples. Each tuple represents a matrix and is ``(multiplier,
28
        matrix_identifier, index)`` where all of them are strings. These matrix-representing tuples are
29
30
        contained in lists which represent multiplication groups. Every matrix in the group should be
31
        multiplied together, in order. These multiplication group lists are contained by a top level list,
32
        which is this type. Once these multiplication group lists have been evaluated, they should be summed.
34
        In the tuples, the multiplier is a string representing a real number, the matrix identifier
        is a capital letter or ``rot(x)`` where x is a real number angle, and the index is a string
35
        representing an integer, or it's the letter ``T`` for transpose.
36
37
38
39
40
        def is_matrix_type(matrix: Any) -> TypeGuard[NDArray[(2, 2), Float]]:
41
            """Check if the given value is a valid matrix type.
42
43
            .. note::
               This function is a TypeGuard, meaning if it returns True, then the
44
               passed value must be a :attr:`lintrans.typing_.MatrixType`.
46
47
            return isinstance(matrix, ndarray) and matrix.shape == (2, 2)
```

Centre number: 123456

# B Testing code

#### B.1 gui/test\_dialog\_utility\_functions.py

```
# lintrans - The linear transformation visualizer
 2
         # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
         # This program is licensed under GNU GPLv3, available here:
         # <https://www.gnu.org/licenses/gpl-3.0.html>
         """Test the utility functions for GUI dialog boxes."""
 8
         import numpy as np
10
         import pytest
11
12
        from lintrans.gui.dialogs.define_new_matrix import is_valid_float, round_float
13
         valid_floats: list[str] = [
14
             '0', '1', '3', '-2', '123', '-208', '1.2', '-3.5', '4.252634', '-42362.352325', '164', '-2.59e3', '4.13e-6', '-5.5244e-12'
15
16
17
18
19
         invalid_floats: list[str] = [
             '', 'pi', 'e', '1.2.3', '1,2', '-', '.', 'None', 'no', 'yes', 'float'
20
21
22
23
24
        @pytest.mark.parametrize('inputs,output', [(valid_floats, True), (invalid_floats, False)])
25
         def test_is_valid_float(inputs: list[str], output: bool) -> None:
26
             """Test the is_valid_float() function."""
27
             for inp in inputs:
28
                 assert is_valid_float(inp) == output
29
30
31
        def test round float() -> None:
             """Test the round_float() function."""
32
             expected_values: list[tuple[float, int, str]] = [
                 (1.0, 4, '1'), (1e-6, 4, '0'), (1e-5, 6, '1e-5'), (6.3e-8, 5, '0'), (3.2e-8, 10, '3.2e-8'),
34
                 (np.sqrt(2) / 2, 5, '0.70711'), (-1 * np.sqrt(2) / 2, 5, '-0.70711'),
35
                 (np.pi, 1, '3.1'), (np.pi, 2, '3.14'), (np.pi, 3, '3.142'), (np.pi, 4, '3.1416'), (np.pi, 5, '3.14159'),
36
                 (1.23456789, 2, '1.23'), (1.23456789, 3, '1.235'), (1.23456789, 4, '1.2346'), (1.23456789, 5, '1.23457'), (12345.678, 1, '12345.7'), (12345.678, 2, '12345.68'), (12345.678, 3, '12345.678'),
37
38
39
             ]
40
             for num, precision, answer in expected_values:
42
                 assert round_float(num, precision) == answer
```

#### m B.2 matrices/test\_parse\_and\_validate\_expression.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
        """Test the :mod:`matrices.parse` module validation and parsing."""
8
        import pytest
10
11
        from lintrans.matrices.parse import (
12
            MatrixParseError, find_sub_expressions, parse_matrix_expression, validate_matrix_expression
13
        from lintrans.typing_ import MatrixParseList
14
15
        expected_sub_expressions: list[tuple[str, list[str]]] = [
16
           ('2(AB)^-1', ['AB']),
            ('-3(A+B)^2-C(B^TA)^-1', ['A+B', 'B^TA']),
18
19
            ('rot(45)', []),
```

Centre number: 123456

```
20
              ('()', []),
21
              ('(())', ['()']),
22
              ('2.3A^-1(AB)^-1+(BC)^2', ['AB', 'BC']),
23
              ('(2.3A^{-1}(AB)^{-1}+(BC)^{2})', ['2.3A^{-1}(AB)^{-1}+(BC)^{2}']),
24
         1
25
26
27
         def test_find_sub_expressions() -> None:
28
               """Test the :func:`lintrans.matrices.parse.find_sub_expressions` function."""
29
              for inp, output in expected_sub_expressions:
30
                   \textbf{assert} \hspace{0.1cm} \texttt{find\_sub\_expressions(inp)} \hspace{0.1cm} = \hspace{0.1cm} \texttt{output}
31
32
33
         valid_inputs: list[str] = [
               'A', 'AB', '3A', '1.2A', '-3.4A', 'A^2', 'A^-1', 'A^{-1}',
34
35
               'A^12', 'A^T', 'A^{5}', 'A^{T}', '4.3A^7', '9.2A^{18}', '0.1A'
36
37
              'rot(45)', 'rot(12.5)', '3rot(90)',
               'rot(135)^3', 'rot(51)^T', 'rot(-34)^-1',
38
39
40
               'A+B', 'A+2B', '4.3A+9B', 'A^2+B^T', '3A^7+0.8B^{16}',
               'A-B', '3A-4B', '3.2A^3-16.79B^T', '4.752A^{17}-3.32B^{36}',
41
               'A-1B', '-A', '-1A'
42
43
44
              '3A4B', 'A^TB', 'A^{T}B', '4A^6B^3',
45
               '2A^{3}4B^5', '4rot(90)^3', 'rot(45)rot(13)',
               'Arot(90)', 'AB^2', 'A^2B^2', '8.36A^T3.4B^12',
46
47
48
               '3.5A^{4}5.6rot(19.2)^T-B^{-1}4.1C^5',
49
               '(A)', '(AB)^-1', '2.3(3B^TA)^2', '-3.4(9D^{2}3F^-1)^T+C', '(AB)(C)',
50
               '3(rot(34)^-7A)^-1+B', '3A^2B+4A(B+C)^-1D^T-A(C(D+E)B)'
51
52
         1
53
54
         invalid_inputs: list[str] = [
              '', 'rot()', 'A^', 'A^1.2', 'A^{3.4}', '1,2A', 'ro(12)', '5', '12^2', '^T', '^{12}', '.1A', 'A^{13', 'A^3}', 'A^A', '^2', 'A-B', '--A', '+A', '--1A', 'A-B', 'A-1B', '.A', '1.A',
55
56
               '2.3AB)^T', '(AB+)', '-4.6(9A', '-2(3.4A^{-1}-C^)^2', '9.2)', '3A^2B+4A(B+C)^-1D^T-A(C(D+EB)',
57
58
59
               'This is 100% a valid matrix expression, I swear'
60
         1
61
62
63
         @pytest.mark.parametrize('inputs,output', [(valid_inputs, True), (invalid_inputs, False)])
64
          def test_validate_matrix_expression(inputs: list[str], output: bool) -> None:
               """Test the validate_matrix_expression() function.'
65
66
               for inp in inputs:
67
                   assert validate_matrix_expression(inp) == output
68
69
70
         expressions_and_parsed_expressions: list[tuple[str, MatrixParseList]] = [
71
               # Simple expressions
              ('A', [[('', 'A', '')]]),
('A^2', [[('', 'A', '2')]]),
('A^{2}', [[('', 'A', '2')]]),
('3A', [[('3', 'A', '')]]),
72
73
74
75
              ('1.4A^3', [[('1.4', 'A', '3')]]),
('0.1A', [[('0.1', 'A', '')]]),
76
77
              ('0.1A', [[('0.1', 'A', '')]]),
78
79
              ('A^12', [[('', 'A', '12')]]),
              ('A^234', [[('', 'A', '234')]]),
80
81
              # Multiplications
82
              ('A 0.1B', [[('', 'A', ''), ('0.1', 'B', '')]]), ('A^2 3B', [[('', 'A', '23'), ('', 'B', '')]]),
83
84
85
              ('4A^{3} 6B^2', [[('4', 'A', '3'), ('6', 'B', '2')]]),
              ('4.2A^{T} 6.1B^-1', [[('4.2', 'A', 'T'), ('6.1', 'B', '-1')]]),

('-1.2A^2 rot(45)^2', [[('-1.2', 'A', '2'), ('', 'rot(45)', '2')]]),

('3.2A^T 4.5B^{5} 9.6rot(121.3)', [[('3.2', 'A', 'T'), ('4.5', 'B', '5'), ('9.6', 'rot(121.3)', '')]]),
86
87
88
              ('-1.18A^{-2} 0.1B^{2} 9rot(-34.6)^-1', [[('-1.18', 'A', '-2'), ('0.1', 'B', '2'), ('9', 'rot(-34.6)', '-1')]]),
89
90
91
              # Additions
              ('A + B', [[('', 'A', '')], [('', 'B', '')]]),
92
```

```
('A + B - C', [[('', 'A', '')], [('', 'B', '')], [('-1', 'C', '')]]),
 93
              ('A^2 + 0.5B', [[('', 'A', '2')], [('0.5', 'B', '')]]),
 94
              ('2A^3 + 8B^T - 3C^-1', [[('2', 'A', '3')], [('8', 'B', 'T')], [('-3', 'C', '-1')]]),

('4.9A^2 - 3rot(134.2)^-1 + 7.6B^8', [[('4.9', 'A', '2')], [('-3', 'rot(134.2)', '-1')], [('7.6', 'B', '8')]]),
 95
 96
 97
 98
              # Additions with multiplication
 99
              ('2.14A^{3} 4.5rot(14.5)^-1 + 8B^T - 3C^-1', [[('2.14', 'A', '3'), ('4.5', 'rot(14.5)', '-1')],
                                                                [('8', 'B', 'T')], [('-3', 'C', '-1')]]),
100
              ('2.14A^{3} 4.5rot(14.5)^-1 + 8.5B^T 5.97C^14 - 3.14D^{-1} 6.7E^T',
101
               [[('2.14', 'A', '3'), ('4.5', 'rot(14.5)', '-1')], [('8.5', 'B', 'T'), ('5.97', 'C', '14')],
102
                [('-3.14', 'D', '-1'), ('6.7', 'E', 'T')]]),
103
104
105
              # Parenthesized expressions
              ('(AB)^-1', [[('', 'AB', '-1')]]),
106
              ('-3(A+B)^2-C(B^TA)^-1', [[('-3', 'A+B', '2')], [('-1', 'C', ''), ('', 'B^{T}A', '-1')]]),
107
              ('2.3(3B^TA)^2', [[('2.3', '3B^{T}A', '2')]]),
('-3.4(9D^{2}3F^-1)^T+C', [[('-3.4', '9D^{2}3F^{-1}', 'T')], [('', 'C', '')]]),
108
109
              ('2.39(3.1A^{-1}2.3B(CD)^{-1})^T + (AB^T)^{-1}, [[('2.39', '3.1A^{-1}2.3B(CD)^{-1}', 'T')], [('', 'AB^{T}', 'B')]
110

    '-1')]])

111
112
113
114
          def test_parse_matrix_expression() -> None:
               """Test the parse_matrix_expression() function."""
115
116
              for expression, parsed_expression in expressions_and_parsed_expressions:
117
                   # Test it with and without whitespace
                   assert parse_matrix_expression(expression) == parsed_expression
118
119
                   assert parse_matrix_expression(expression.replace(' ', '')) == parsed_expression
120
121
          def test_parse_error() -> None:
122
               """Test that parse_matrix_expression() raises a MatrixParseError."""
123
124
              for expression in invalid_inputs:
125
                   with pytest.raises(MatrixParseError):
126
                       parse_matrix_expression(expression)
```

#### B.3 matrices/test\_rotation\_matrices.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
 2
        # This program is licensed under GNU GPLv3, available here:
 5
        # <https://www.gnu.org/licenses/gpl-3.0.html>
        """Test functions for rotation matrices."""
 7
 8
        import numpy as np
10
        import pytest
11
        from lintrans.matrices import create_rotation_matrix
12
        from lintrans.typing_ import MatrixType
13
14
        angles_and_matrices: list[tuple[float, float, MatrixType]] = [
15
16
            (0, 0, np.array([[1, 0], [0, 1]])),
17
            (90, np.pi / 2, np.array([[0, -1], [1, 0]])),
18
            (180, np.pi, np.array([[-1, 0], [0, -1]])),
19
            (270, 3 * np.pi / 2, np.array([[0, 1], [-1, 0]])),
            (360, 2 * np.pi, np.array([[1, 0], [0, 1]])),
20
21
22
            (45, np.pi / 4, np.array([
                [np.sqrt(2) / 2, -1 * np.sqrt(2) / 2],
23
24
                [np.sqrt(2) / 2, np.sqrt(2) / 2]
            ])),
26
            (135, 3 * np.pi / 4, np.array([
27
                [-1 * np.sqrt(2) / 2, -1 * np.sqrt(2) / 2],
28
                [np.sqrt(2) / 2, -1 * np.sqrt(2) / 2]
29
            ])),
30
            (225, 5 * np.pi / 4, np.array([
31
                [-1 * np.sqrt(2) / 2, np.sqrt(2) / 2],
32
                [-1 * np.sqrt(2) / 2, -1 * np.sqrt(2) / 2]
```

```
33
            ])),
            (315, 7 * np.pi / 4, np.array([
34
                [np.sqrt(2) / 2, np.sqrt(2) / 2],
35
36
                [-1 * np.sqrt(2) / 2, np.sqrt(2) / 2]
37
            ])),
38
39
            (30, np.pi / 6, np.array([
                [np.sqrt(3) / 2, -1 / 2],
40
41
                [1 / 2, np.sqrt(3) / 2]
            ])),
            (60, np.pi / 3, np.array([
43
44
                [1 / 2, -1 * np.sqrt(3) / 2],
45
                [np.sqrt(3) / 2, 1 / 2]
46
            ])),
47
            (120, 2 * np.pi / 3, np.array([
                [-1 / 2, -1 * np.sqrt(3) / 2],
48
49
                [np.sqrt(3) / 2, -1 / 2]
50
            ])),
            (150, 5 * np.pi / 6, np.array([
51
52
                [-1 * np.sqrt(3) / 2, -1 / 2],
53
                [1 / 2, -1 * np.sqrt(3) / 2]
54
            ])),
55
            (210, 7 * np.pi / 6, np.array([
                [-1 * np.sqrt(3) / 2, 1 / 2],
56
57
                [-1 / 2, -1 * np.sqrt(3) / 2]
58
            ])),
            (240, 4 * np.pi / 3, np.array([
59
60
                [-1 / 2, np.sqrt(3) / 2],
61
                [-1 * np.sqrt(3) / 2, -1 / 2]
62
            1)),
            (300, 10 * np.pi / 6, np.array([
63
64
                [1 / 2, np.sqrt(3) / 2],
65
                [-1 * np.sqrt(3) / 2, 1 / 2]
66
67
            (330, 11 * np.pi / 6, np.array([
68
                [np.sqrt(3) / 2, 1 / 2],
                [-1 / 2, np.sqrt(3) / 2]
69
            ]))
70
71
        ]
72
73
74
        def test_create_rotation_matrix() -> None:
             """Test that create_rotation_matrix() works with given angles and expected matrices."""
75
76
            for degrees, radians, matrix in angles_and_matrices:
77
                assert create_rotation_matrix(degrees, degrees=True) == pytest.approx(matrix)
78
                assert create_rotation_matrix(radians, degrees=False) == pytest.approx(matrix)
79
80
                \textbf{assert} \ \ create\_rotation\_matrix(-1 \ * \ degrees= \textbf{True}) \ = \ pytest.approx(np.linalg.inv(matrix))
81
                assert create_rotation_matrix(-1 * radians, degrees=False) == pytest.approx(np.linalg.inv(matrix))
```

#### B.4 matrices/matrix\_wrapper/conftest.py

```
# lintrans - The linear transformation visualizer
 1
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
 5
        # <https://www.gnu.org/licenses/gpl-3.0.html>
        """A simple conftest.py containing some re-usable fixtures."""
 7
 8
9
        import numpy as np
10
        import pytest
11
        from lintrans.matrices import MatrixWrapper
12
13
14
        def get_test_wrapper() -> MatrixWrapper:
15
16
            """Return a new MatrixWrapper object with some preset values."""
17
            wrapper = MatrixWrapper()
```

```
19
            root_two_over_two = np.sqrt(2) / 2
20
21
            wrapper['A'] = np.array([[1, 2], [3, 4]])
22
            wrapper['B'] = np.array([[6, 4], [12, 9]])
23
            wrapper['C'] = np.array([[-1, -3], [4, -12]])
24
            wrapper['D'] = np.array([[13.2, 9.4], [-3.4, -1.8]])
25
            wrapper['E'] = np.array([
                [root_two_over_two, -1 * root_two_over_two],
26
27
                [root_two_over_two, root_two_over_two]
28
            ])
29
            wrapper['F'] = np.array([[-1, 0], [0, 1]])
30
            wrapper['G'] = np.array([[np.pi, np.e], [1729, 743.631]])
31
32
            return wrapper
33
34
35
        @pytest.fixture
36
        def test_wrapper() -> MatrixWrapper:
             """Return a new MatrixWrapper object with some preset values."""
37
38
            return get_test_wrapper()
39
40
41
        @pytest.fixture
42
        def new_wrapper() -> MatrixWrapper:
43
            """Return a new MatrixWrapper with no initialized values."""
44
            return MatrixWrapper()
```

# B.5 matrices/matrix\_wrapper/test\_misc.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
        # <https://www.gnu.org/licenses/gpl-3.0.html>
 6
        """Test the miscellaneous methods of the MatrixWrapper class."""
 8
 9
        from lintrans.matrices import MatrixWrapper
10
11
        def test_get_expression(test_wrapper: MatrixWrapper) -> None:
             """Test the get_expression method of the MatrixWrapper class."""
13
            test_wrapper['N'] = 'A^2'
14
            test_wrapper['0'] = '4B'
15
            test_wrapper['P'] = 'A+C'
16
17
18
            test_wrapper['Q'] = 'N^-1'
            test_wrapper['R'] = 'P-40'
19
20
            test_wrapper['S'] = 'NOP'
21
22
            assert test_wrapper.get_expression('A') is None
23
            assert test_wrapper.get_expression('B') is None
24
            assert test_wrapper.get_expression('C') is None
25
            {\bf assert} \ {\tt test\_wrapper.get\_expression('D')} \ {\bf is} \ {\bf None}
26
            assert test_wrapper.get_expression('E') is None
            assert test_wrapper.get_expression('F') is None
27
28
            assert test_wrapper.get_expression('G') is None
29
            assert test_wrapper.get_expression('N') == 'A^2'
30
            assert test_wrapper.get_expression('0') == '4B'
31
            assert test_wrapper.get_expression('P') == 'A+C'
32
33
            assert test_wrapper.get_expression('Q') == 'N^-1'
35
            assert test_wrapper.get_expression('R') == 'P-40'
36
            assert test_wrapper.get_expression('S') == 'NOP'
```

#### B.6 matrices/matrix\_wrapper/test\_setitem\_and\_getitem.py

```
# lintrans - The linear transformation visualizer
        # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
        # This program is licensed under GNU GPLv3, available here:
 5
        # <https://www.gnu.org/licenses/gpl-3.0.html>
        """Test the MatrixWrapper __setitem__() and __getitem__() methods."""
 8
        import numpy as np
10
        from numpy import linalg as la
11
        import pytest
12
        from typing import Any
13
14
        from lintrans.matrices import MatrixWrapper
15
        from lintrans.typing_ import MatrixType
16
17
        valid_matrix_names = 'ABCDEFGHJKLMNOPQRSTUVWXYZ'
        invalid_matrix_names = ['bad name', '123456', 'Th15 Is an 1nV@l1D n@m3', 'abc', 'a']
18
19
20
        test_matrix: MatrixType = np.array([[1, 2], [4, 3]])
21
22
23
        def test_basic_get_matrix(new_wrapper: MatrixWrapper) -> None:
24
            """Test MatrixWrapper().__getitem__()."""
25
            for name in valid_matrix_names:
26
                assert new wrapper[name] is None
27
28
            assert (new_wrapper['I'] == np.array([[1, 0], [0, 1]])).all()
29
30
31
        def test_get_name_error(new_wrapper: MatrixWrapper) -> None:
            """Test that MatrixWrapper().__getitem__() raises a NameError if called with an invalid name."""
32
            for name in invalid_matrix_names:
                with pytest.raises(NameError):
34
35
                    _ = new_wrapper[name]
36
37
38
        def test_basic_set_matrix(new_wrapper: MatrixWrapper) -> None:
39
            """Test MatrixWrapper().__setitem__()."""
            for name in valid_matrix_names:
40
41
                new_wrapper[name] = test_matrix
42
                assert (new_wrapper[name] == test_matrix).all()
43
44
                new_wrapper[name] = None
45
                assert new_wrapper[name] is None
46
        def test_set_expression(test_wrapper: MatrixWrapper) -> None:
48
49
            """Test that MatrixWrapper.__setitem__() can accept a valid expression."""
50
            test_wrapper['N'] = 'A^2'
            test_wrapper['0'] = 'BA+2C'
51
            test_wrapper['P'] = 'E^T'
52
53
            test_wrapper['Q'] = 'C^-1B'
54
            test_wrapper['R'] = 'A^{2}3B'
            test_wrapper['S'] = 'N^-1'
55
            test_wrapper['T'] = 'PQP^-1'
56
57
58
            with pytest.raises(TypeError):
59
                test_wrapper['U'] = 'A+1'
60
61
            with pytest.raises(TypeError):
62
                test_wrapper['V'] = 'K'
63
            with pytest.raises(TypeError):
64
65
                test_wrapper['W'] = 'L^2'
66
67
            with pytest.raises(TypeError):
68
                test_wrapper['X'] = 'M^-1'
69
70
```

```
71
         def test_simple_dynamic_evaluation(test_wrapper: MatrixWrapper) -> None:
             """Test that expression-defined matrices are evaluated dynamically."""
 72
 73
             test_wrapper['N'] = 'A^2'
             test_wrapper['0'] = '4B'
 74
 75
             test_wrapper['P'] = 'A+C'
 76
 77
             assert (test_wrapper['N'] == test_wrapper.evaluate_expression('A^2')).all()
 78
             assert (test_wrapper['0'] == test_wrapper.evaluate_expression('4B')).all()
 79
             assert (test_wrapper['P'] == test_wrapper.evaluate_expression('A+C')).all()
 80
             assert (test_wrapper.evaluate_expression('N^2 + 30') ==
81
                     la.matrix_power(test_wrapper.evaluate_expression('A^2'), 2) +
82
83
                     3 * test_wrapper.evaluate_expression('4B')
84
                     ).all()
             assert (test_wrapper.evaluate_expression('P^-1 - 3N0^2') ==
 85
86
                     la.inv(test_wrapper.evaluate_expression('A+C')) -
87
                     (3 * test_wrapper.evaluate_expression('A^2')) @
88
                     la.matrix_power(test_wrapper.evaluate_expression('4B'), 2)
89
                     ).all()
 90
91
             test_wrapper['A'] = np.array([
92
                 [19, -21.5],
93
                 [84, 96.572]
94
             1)
95
             test_wrapper['B'] = np.array([
 96
                 [-0.993, 2.52],
97
                 [1e10, 0]
98
             ])
99
             test_wrapper['C'] = np.array([
100
                 [0, 19512].
                 [1.414, 19]
101
             1)
102
103
104
             assert (test_wrapper['N'] == test_wrapper.evaluate_expression('A^2')).all()
             assert (test_wrapper['0'] == test_wrapper.evaluate_expression('4B')).all()
105
106
             assert (test_wrapper['P'] == test_wrapper.evaluate_expression('A+C')).all()
107
             assert (test_wrapper.evaluate_expression('N^2 + 30') ==
108
109
                     la.matrix_power(test_wrapper.evaluate_expression('A^2'), 2) +
                     3 * test_wrapper.evaluate_expression('4B')
110
111
                     ).all()
112
             assert (test_wrapper.evaluate_expression('P^-1 - 3N0^2') ==
113
                     la.inv(test_wrapper.evaluate_expression('A+C')) -
114
                     (3 * test_wrapper.evaluate_expression('A^2')) @
115
                     la.matrix power(test wrapper.evaluate expression('4B'), 2)
116
                     ).all()
117
118
119
         def test_recursive_dynamic_evaluation(test_wrapper: MatrixWrapper) -> None:
120
             """Test that dynamic evaluation works recursively.""
             test wrapper['N'] = 'A^2'
121
122
             test_wrapper['0'] = '4B'
123
             test_wrapper['P'] = 'A+C'
124
125
             test_wrapper['Q'] = 'N^-1'
             test wrapper['R'] = 'P-40'
126
127
             test_wrapper['S'] = 'NOP'
128
129
             assert test_wrapper['Q'] == pytest.approx(test_wrapper.evaluate_expression('A^-2'))
130
             assert test_wrapper['R'] == pytest.approx(test_wrapper.evaluate_expression('A + C - 16B'))
131
             assert test_wrapper['S'] == pytest.approx(test_wrapper.evaluate_expression('A^{2}4BA + A^{2}4BC'))
132
133
134
         def test set identity error(new wrapper: MatrixWrapper) -> None:
             """Test that MatrixWrapper().__setitem__() raises a NameError when trying to assign to the identity matrix."""
135
136
             with pytest.raises(NameError):
137
                 new_wrapper['I'] = test_matrix
138
139
         def test_set_name_error(new_wrapper: MatrixWrapper) -> None:
140
141
             """Test that MatrixWrapper().__setitem__() raises a NameError when trying to assign to an invalid name."""
142
             for name in invalid matrix names:
143
                 with pytest.raises(NameError):
```

```
144
                     new_wrapper[name] = test_matrix
145
146
147
         def test_set_type_error(new_wrapper: MatrixWrapper) -> None:
148
             """Test that MatrixWrapper().__setitem__() raises a TypeError when trying to set a non-matrix."""
149
             invalid_values: list[Any] = [
150
                                           [1, 2, 3, 4, 5],
151
152
                                           [[1, 2], [3, 4]],
153
                                           True,
                                           24.3222.
154
                                           'This is totally a matrix, I swear',
155
156
                                           MatrixWrapper,
157
                                           MatrixWrapper(),
                                           np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]]),
158
159
                                           np.eye(100)
160
161
             for value in invalid values:
162
163
                 with pytest.raises(TypeError):
                     new_wrapper['M'] = value
164
```

## B.7 matrices/matrix\_wrapper/test\_evaluate\_expression.py

```
# lintrans - The linear transformation visualizer
               # Copyright (C) 2021-2022 D. Dyson (DoctorDalek1963)
               # This program is licensed under GNU GPLv3, available here:
  5
               # <https://www.gnu.org/licenses/gpl-3.0.html>
  6
               """Test the MatrixWrapper evaluate_expression() method."""
 8
 9
               import numpy as np
               from numpy import linalg as la
10
11
               import pytest
12
               from pytest import approx
13
14
               from lintrans.matrices import MatrixWrapper, create_rotation_matrix
15
               from lintrans.typing_ import MatrixType
16
17
               from conftest import get test wrapper
18
19
20
               def test_simple_matrix_addition(test_wrapper: MatrixWrapper) -> None:
                        """Test simple addition and subtraction of two matrices.""
21
22
23
                       # NOTE: We assert that all of these values are not None just to stop mypy complaining
                       # These values will never actually be None because they're set in the wrapper() fixture
24
25
                       # There's probably a better way do this, because this method is a bit of a bodge, but this works for now
26
                       assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
27
                                     test\_wrapper['D'] \ is \ not \ None \ and \ test\_wrapper['E'] \ is \ not \ None \ and \ test\_wrapper['F'] \ is \ not \ None \ and \ \\
28
                                     test_wrapper['G'] is not None
29
30
                       assert (test_wrapper.evaluate_expression('A+B') == test_wrapper['A'] + test_wrapper['B']).all()
                       assert (test_wrapper.evaluate_expression('E+F') == test_wrapper['E'] + test_wrapper['F']).all()
31
                       assert \ (test\_wrapper.evaluate\_expression('G+D') == test\_wrapper['G'] + test\_wrapper['D']).all(') == test\_wrapper['D
32
33
                       assert (test_wrapper.evaluate_expression('C+C') == test_wrapper['C'] + test_wrapper['C']).all()
34
                       assert (test_wrapper.evaluate_expression('D+A') == test_wrapper['D'] + test_wrapper['A']).all()
                       assert (test_wrapper.evaluate_expression('B+C') == test_wrapper['B'] + test_wrapper['C']).all()
35
36
37
                       assert test_wrapper == get_test_wrapper()
38
39
40
               def test_simple_two_matrix_multiplication(test_wrapper: MatrixWrapper) -> None:
41
                       """Test simple multiplication of two matrices.""
42
                       assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
                                     test\_wrapper['D'] \ is \ not \ None \ and \ test\_wrapper['E'] \ is \ not \ None \ and \ test\_wrapper['F'] \ is \ not \ None \ and \ \\
43
44
                                     test_wrapper['G'] is not None
45
46
                       assert (test_wrapper.evaluate_expression('AB') == test_wrapper['A'] @ test_wrapper['B']).all()
```

```
47
                   assert (test_wrapper.evaluate_expression('BA') == test_wrapper['B'] @ test_wrapper['A']).all()
 48
                  assert (test_wrapper.evaluate_expression('AC') == test_wrapper['A'] @ test_wrapper['C']).all()
 49
                   assert (test_wrapper.evaluate_expression('DA') == test_wrapper['D'] @ test_wrapper['A']).all()
                   assert (test_wrapper.evaluate_expression('ED') == test_wrapper['E'] @ test_wrapper['D']).all()
 50
 51
                  assert (test_wrapper.evaluate_expression('FD') == test_wrapper['F'] @ test_wrapper['D']).all()
 52
                  assert (test_wrapper.evaluate_expression('GA') == test_wrapper['G'] @ test_wrapper['A']).all()
                  assert (test_wrapper.evaluate_expression('CF') == test_wrapper['C'] @ test_wrapper['F']).all()
 53
 54
                  assert (test_wrapper.evaluate_expression('AG') == test_wrapper['A'] @ test_wrapper['G']).all()
 55
 56
                  assert test_wrapper.evaluate_expression('A2B') == approx(test_wrapper['A'] @ (2 * test_wrapper['B']))
                  assert test_wrapper.evaluate_expression('2AB') == approx((2 * test_wrapper['A']) @ test_wrapper['B'])
 57
                   assert test_wrapper.evaluate_expression('C3D') == approx(test_wrapper['C'] @ (3 * test_wrapper['D']))
 58
 59
                  assert test_wrapper.evaluate_expression('4.2E1.2A') == approx((4.2 * test_wrapper['E']) @ (1.2 *

    test_wrapper['A']))

 60
 61
                  assert test wrapper == get test wrapper()
 62
 63
 64
             def test_identity_multiplication(test_wrapper: MatrixWrapper) -> None:
 65
                   """Test that multiplying by the identity doesn't change the value of a matrix."""
 66
                  assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
 67
                             test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
 68
                             test wrapper['G'] is not None
 69
 70
                  assert (test_wrapper.evaluate_expression('I') == test_wrapper['I']).all()
 71
                  assert (test_wrapper.evaluate_expression('AI') == test_wrapper['A']).all()
                  assert (test_wrapper.evaluate_expression('IA') == test_wrapper['A']).all()
 72
 73
                   assert (test_wrapper.evaluate_expression('GI') == test_wrapper['G']).all()
 74
                  assert (test_wrapper.evaluate_expression('IG') == test_wrapper['G']).all()
 75
                  assert (test_wrapper.evaluate_expression('EID') == test_wrapper['E'] @ test_wrapper['D']).all()
 76
                  assert \ (test\_wrapper.evaluate\_expression('IED'') == test\_wrapper['E''] \ @ \ test\_wrapper['D'']).all()
 77
 78
                  assert (test_wrapper.evaluate_expression('EDI') == test_wrapper['E'] @ test_wrapper['D']).all()
                  assert (test_wrapper.evaluate_expression('IEIDI') == test_wrapper['E'] @ test_wrapper['D']).all()
 79
 80
                  assert (test_wrapper.evaluate_expression('EI^3D') == test_wrapper['E'] @ test_wrapper['D']).all()
 81
 82
                  assert test wrapper == get test wrapper()
 83
 84
            def test_simple_three_matrix_multiplication(test_wrapper: MatrixWrapper) -> None:
 85
 86
                   """Test simple multiplication of two matrices.""
                   assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
 87
                            test\_wrapper['D'] is \ not \ None \ and \ test\_wrapper['E'] is \ not \ None \ and \ test\_wrapper['F'] is \ not \ None \ and \ None \ 
 88
 89
                             test_wrapper['G'] is not None
 90
 91
                  assert (test_wrapper.evaluate_expression('ABC') == test_wrapper['A'] @ test_wrapper['B'] @

    test_wrapper['C']).all()

                  assert (test_wrapper.evaluate_expression('ACB') == test_wrapper['A'] @ test_wrapper['C'] @
 92

    test_wrapper['B']).all()

 93
                  assert (test_wrapper.evaluate_expression('BAC') == test_wrapper['B'] @ test_wrapper['A'] @

    test wrapper['C']).all()

 94
                  assert (test_wrapper.evaluate_expression('EFG') == test_wrapper['E'] @ test_wrapper['F'] @

    test_wrapper['G']).all()

                  assert (test_wrapper.evaluate_expression('DAC') == test_wrapper['D'] @ test_wrapper['A'] @
 95

→ test wrapper['C']).all()

                  assert (test_wrapper.evaluate_expression('GAE') == test_wrapper['G'] @ test_wrapper['A'] @
 96

    test_wrapper['E']).all()

 97
                  assert (test_wrapper.evaluate_expression('FAG') == test_wrapper['F'] @ test_wrapper['A'] @

    test wrapper['G']).all()

                  assert (test_wrapper.evaluate_expression('GAF') == test_wrapper['G'] @ test_wrapper['A'] @
 98

    test_wrapper['F']).all()

 99
100
                  assert test_wrapper == get_test_wrapper()
101
102
103
             def test_matrix_inverses(test_wrapper: MatrixWrapper) -> None:
104
                   """Test the inverses of single matrices.""
105
                   assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
106
                            test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
                            test wrapper['G'] is not None
107
108
109
                  assert (test_wrapper.evaluate_expression('A^{-1}') == la.inv(test_wrapper['A'])).all()
110
                  assert (test_wrapper.evaluate_expression('B^{-1}') == la.inv(test_wrapper['B'])).all()
```

```
111
             assert \ (test\_wrapper.evaluate\_expression('C^{-1}') == la.inv(test\_wrapper['C'])).all()
112
             assert (test_wrapper.evaluate_expression('D^{-1}') == la.inv(test_wrapper['D'])).all()
             assert \ (test\_wrapper.evaluate\_expression('E^{-1}') == la.inv(test\_wrapper['E'])).all()
113
             assert (test_wrapper.evaluate_expression('F^{-1}') == la.inv(test_wrapper['F'])).all()
114
115
             assert (test_wrapper.evaluate_expression('G^{-1}') == la.inv(test_wrapper['G'])).all()
116
117
             assert (test_wrapper.evaluate_expression('A^-1') == la.inv(test_wrapper['A'])).all()
             assert (test_wrapper.evaluate_expression('B^-1') == la.inv(test_wrapper['B'])).all()
118
119
             assert (test_wrapper.evaluate_expression('C^-1') == la.inv(test_wrapper['C'])).all()
120
             assert (test_wrapper.evaluate_expression('D^-1') == la.inv(test_wrapper['D'])).all()
             assert (test_wrapper.evaluate_expression('E^-1') == la.inv(test_wrapper['E'])).all()
121
             assert (test_wrapper.evaluate_expression('F^-1') == la.inv(test_wrapper['F'])).all()
122
123
             assert (test_wrapper.evaluate_expression('G^-1') == la.inv(test_wrapper['G'])).all()
124
125
             assert test_wrapper == get_test_wrapper()
126
127
128
         def test_matrix_powers(test_wrapper: MatrixWrapper) -> None:
129
              ""Test that matrices can be raised to integer powers."
130
             assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
131
                    test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
132
                    test_wrapper['G'] is not None
133
             assert (test_wrapper.evaluate_expression('A^2') == la.matrix_power(test_wrapper['A'], 2)).all()
134
135
             assert (test_wrapper.evaluate_expression('B^4') == la.matrix_power(test_wrapper['B'], 4)).all()
136
             assert (test_wrapper.evaluate_expression('C^{12}') == la.matrix_power(test_wrapper['C'], 12)).all()
             assert (test_wrapper.evaluate_expression('D^12') == la.matrix_power(test_wrapper['D'], 12)).all()
137
             assert \ (test\_wrapper.evaluate\_expression('E^8') == la.matrix\_power(test\_wrapper['E'], \ 8)).all()
138
139
             assert (test_wrapper.evaluate_expression('F^{-6}') == la.matrix_power(test_wrapper['F'], -6)).all()
140
             assert \ (test\_wrapper.evaluate\_expression('G^-2') == la.matrix\_power(test\_wrapper['G'], -2)).all()
141
             \textbf{assert} \hspace{0.1in} \texttt{test\_wrapper} \hspace{0.1in} = \hspace{0.1in} \texttt{get\_test\_wrapper()}
142
143
144
145
         def test_matrix_transpose(test_wrapper: MatrixWrapper) -> None:
146
             """Test matrix transpositions.""
147
             assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
148
                    test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
149
                    test wrapper['G'] is not None
150
151
             assert \ (test\_wrapper.evaluate\_expression('A^{T}') == test\_wrapper['A'].T).all()
152
             assert (test_wrapper.evaluate_expression('B^{T}') == test_wrapper['B'].T).all()
             assert (test_wrapper.evaluate_expression('C^{T}') == test_wrapper['C'].T).all()
153
154
             assert \ (test\_wrapper.evaluate\_expression('D^{T}') == test\_wrapper['D'].T).all()
155
             assert (test_wrapper.evaluate_expression('E^{T}') == test_wrapper['E'].T).all()
             assert (test_wrapper.evaluate_expression('F^{T}') == test_wrapper['F'].T).all()
156
157
             assert (test_wrapper.evaluate_expression('G^{T}') == test_wrapper['G'].T).all()
158
159
             assert (test_wrapper.evaluate_expression('A^T') == test_wrapper['A'].T).all()
             assert (test_wrapper.evaluate_expression('B^T') == test_wrapper['B'].T).all()
160
             assert (test_wrapper.evaluate_expression('C^T') == test_wrapper['C'].T).all()
161
162
             assert (test_wrapper.evaluate_expression('D^T') == test_wrapper['D'].T).all()
             assert (test_wrapper.evaluate_expression('E^T') == test_wrapper['E'].T).all()
163
             assert (test_wrapper.evaluate_expression('F^T') == test_wrapper['F'].T).all()
164
             assert (test_wrapper.evaluate_expression('G^T') == test_wrapper['G'].T).all()
165
166
167
             assert test_wrapper == get_test_wrapper()
168
169
170
         def test_rotation_matrices(test_wrapper: MatrixWrapper) -> None:
171
             """Test that 'rot(angle)' can be used in an expression.""
             assert (test_wrapper.evaluate_expression('rot(90)') == create_rotation_matrix(90)).all()
172
173
             assert (test_wrapper.evaluate_expression('rot(180)') == create_rotation_matrix(180)).all()
174
             assert (test_wrapper.evaluate_expression('rot(270)') == create_rotation_matrix(270)).all()
175
             assert (test_wrapper.evaluate_expression('rot(360)') == create_rotation_matrix(360)).all()
176
             assert (test_wrapper.evaluate_expression('rot(45)') == create_rotation_matrix(45)).all()
177
             assert (test_wrapper.evaluate_expression('rot(30)') == create_rotation_matrix(30)).all()
178
179
             assert (test_wrapper.evaluate_expression('rot(13.43)') == create_rotation_matrix(13.43)).all()
             assert (test_wrapper.evaluate_expression('rot(49.4)') == create_rotation_matrix(49.4)).all()
180
181
             assert (test_wrapper.evaluate_expression('rot(-123.456)') == create_rotation_matrix(-123.456)).all()
             assert (test_wrapper.evaluate_expression('rot(963.245)') == create_rotation_matrix(963.245)).all()
182
183
             assert (test_wrapper.evaluate_expression('rot(-235.24)') == create_rotation_matrix(-235.24)).all()
```

184

Centre number: 123456

```
185
             assert test wrapper == get test wrapper()
186
187
188
         def test multiplication and addition(test wrapper: MatrixWrapper) -> None:
189
             """Test multiplication and addition of matrices together.
             assert test_wrapper['A'] is not None and test_wrapper['B'] is not None and test_wrapper['C'] is not None and \
190
191
                    test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
192
                    test_wrapper['G'] is not None
193
             assert (test_wrapper.evaluate_expression('AB+C') ==
194
                     test_wrapper['A'] @ test_wrapper['B'] + test_wrapper['C']).all()
195
196
             assert (test_wrapper.evaluate_expression('DE-D') ==
                     test_wrapper['D'] @ test_wrapper['E'] - test_wrapper['D']).all()
197
             assert (test_wrapper.evaluate_expression('FD+AB') ==
198
                     test\_wrapper['F'] \ @ \ test\_wrapper['D'] \ + \ test\_wrapper['A'] \ @ \ test\_wrapper['B']).all()
199
200
             assert (test_wrapper.evaluate_expression('BA-DE') ==
201
                     test_wrapper['B'] @ test_wrapper['A'] - test_wrapper['D'] @ test_wrapper['E']).all()
202
203
             assert (test_wrapper.evaluate_expression('2AB+3C') ==
204
                     (2 * test_wrapper['A']) @ test_wrapper['B'] + (3 * test_wrapper['C'])).all()
205
             assert (test_wrapper.evaluate_expression('4D7.9E-1.2A') ==
206
                     (4 * test_wrapper['D']) @ (7.9 * test_wrapper['E']) - (1.2 * test_wrapper['A'])).all()
207
208
             assert test_wrapper == get_test_wrapper()
209
210
211
         def test_complicated_expressions(test_wrapper: MatrixWrapper) -> None:
212
             """Test evaluation of complicated expressions.""
             assert\ test\_wrapper['A']\ is\ not\ None\ and\ test\_wrapper['B']\ is\ not\ None\ and\ test\_wrapper['C']\ is\ not\ None\ and\ \\
                    test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
214
                    test_wrapper['G'] is not None
215
216
             assert (test_wrapper.evaluate_expression('-3.2A^T 4B^{-1} 6C^{-1} + 8.1D^{2} 3.2E^4') ==
217
                     (-3.2 * test_wrapper['A'].T) @ (4 * la.inv(test_wrapper['B'])) @ (6 * la.inv(test_wrapper['C']))
218
219
                      + (8.1 * la.matrix_power(test_wrapper['D'], 2)) @ (3.2 * la.matrix_power(test_wrapper['E'], 4))).all()
220
             assert (test_wrapper.evaluate_expression('53.6D^{2} 3B^T - 4.9F^{2} 2D + A^3 B^-1') ==
221
222
                     (53.6 * la.matrix_power(test_wrapper['D'], 2)) @ (3 * test_wrapper['B'].T)
                     - (4.9 * la.matrix_power(test_wrapper['F'], 2)) @ (2 * test_wrapper['D'])
223
224
                     + la.matrix_power(test_wrapper['A'], 3) @ la.inv(test_wrapper['B'])).all()
225
226
             assert test_wrapper == get_test_wrapper()
227
228
229
         def test_parenthesized_expressions(test_wrapper: MatrixWrapper) -> None:
230
             """Test evaluation of parenthesized expressions."""
             assert test wrapper['A'] is not None and test wrapper['B'] is not None and test wrapper['C'] is not None and \
231
232
                    test_wrapper['D'] is not None and test_wrapper['E'] is not None and test_wrapper['F'] is not None and \
233
                    test_wrapper['G'] is not None
234
235
             assert (test_wrapper.evaluate_expression('(A^T)^2') == la.matrix_power(test_wrapper['A'].T, 2)).all()
236
             assert (test_wrapper.evaluate_expression('(B^T)^3') == la.matrix_power(test_wrapper['B'].T, 3)).all()
             assert \ (test\_wrapper.evaluate\_expression('(C^T)^4') == la.matrix\_power(test\_wrapper['C'].T, \ 4)).all()
             assert\ (test\_wrapper.evaluate\_expression('(D^T)^5') == la.matrix\_power(test\_wrapper['D'].T,\ 5)).all()
238
             assert \ (test\_wrapper.evaluate\_expression('(E^T)^6') == la.matrix\_power(test\_wrapper['E'].T, \ 6)).all()
239
             assert \ (test\_wrapper.evaluate\_expression('(F^T)^7') == la.matrix\_power(test\_wrapper['F'].T, \ 7)).all()
240
             assert\ (test\_wrapper.evaluate\_expression('(G^T)^8') == la.matrix\_power(test\_wrapper['G'].T,\ 8)).all()
241
242
243
             assert (test_wrapper.evaluate_expression('D^3(A+6.2F-0.397G^TE)^-2+A') ==
244
                     la.matrix_power(test_wrapper['D'], 3) @ la.matrix_power(
                         test\_wrapper['A'] + 6.2 * test\_wrapper['F'] - 0.397 * test\_wrapper['G'].T @ test\_wrapper['E'],
245
246
                          -2
247
                     ) + test_wrapper['A']).all()
248
249
             assert (test_wrapper.evaluate_expression('-1.2F^{3}4.9D^T(A^2(B+3E^TF)^-1)^2') ==
250
                      -1.2 * la.matrix_power(test_wrapper['F'], 3) @ (4.9 * test_wrapper['D'].T) @
251
                     la.matrix_power(
252
                          la.matrix_power(test_wrapper['A'], 2) @ la.matrix_power(
253
                              test_wrapper['B'] + 3 * test_wrapper['E'].T @ test_wrapper['F'],
254
255
                          ),
256
                         2
```

```
257
                       )).all()
258
259
260
          def test_value_errors(test_wrapper: MatrixWrapper) -> None:
              """Test that evaluate_expression() raises a ValueError for any malformed input."""
261
              invalid_expressions = ['', '+', '-', 'This is not a valid expression', '3+4', 'A+2', 'A^-', 'A^-', 'A+1', 'A^-t', '3^2']
262
263
264
265
              for expression in invalid_expressions:
266
                   with pytest.raises(ValueError):
267
                       test_wrapper.evaluate_expression(expression)
268
269
270
          def test_linalgerror() -> None:
271
              """Test that certain expressions raise np.linalg.LinAlgError."""
272
              matrix_a: MatrixType = np.array([
273
                  [0, 0],
274
                   [0, 0]
275
              ])
276
277
              matrix_b: MatrixType = np.array([
278
                   [1, 2],
279
                   [1, 2]
280
              ])
281
282
              wrapper = MatrixWrapper()
283
              wrapper['A'] = matrix_a
284
              wrapper['B'] = matrix_b
285
286
              assert (wrapper.evaluate_expression('A') == matrix_a).all()
287
              assert (wrapper.evaluate_expression('B') == matrix_b).all()
288
              \begin{tabular}{ll} \textbf{with} & pytest.raises(np.linalg.LinAlgError): \\ \end{tabular}
289
290
                  wrapper.evaluate_expression('A^-1')
291
292
              with pytest.raises(np.linalg.LinAlgError):
                  wrapper.evaluate\_expression('B^-1')
293
294
295
              assert (wrapper['A'] == matrix_a).all()
296
              assert (wrapper['B'] == matrix_b).all()
```