

Distributions

Quick Guide to the test application

1. Model expression:

- The arguments for the formula are the distributions that are specified in the right-hand part in the distributions list;
- Arguments can consist of letters only (the restriction will be removed later);

Example:

A1+B2 is incorrect, **A+B** is correct;

- It is prohibited to set two operators in a row, even if it follows the generally accepted logic:

Example:

A^-B is incorrect, **A^(-B)** is correct;

- Parenthesis operators are also supported:

Examples:

(A+5)/(B+3)

-(A*B)^(C/3);

- Supported operators. Note that all of the binary operators can be executed with method of random algebra:

| Operator | Description | Example |
|--------------------|---|---------|
| + | Addition | A+5 |
| - | Substitution | A-5 |
| * | Multiplication | A*5 |
| / | Division | A/5 |
| ^ | Rising to the power | A^5 |
| _ | Logarithm to base | A_5 |
| sqrt() | Square root | sqrt(A) |
| abs() | Absolute value | abs(A) |
| ln(), lg() | Natural/common logarithm | ln(A) |
| sin(), cos(), tg() | Sine / cosine / tangent of value in radians, not implemented for method of random algebra | sin(A) |

- When calculating by the method of algebra of random variables, it is prohibited to use the same parameter in the formula twice. In case it is impossible to rewrite the expression, it is necessary to use the Monte Carlo method.

Examples:

A+A*2+B – incorrect, should rewrite to **A*3+B**

$A*(A+5)$ – incorrect, Monte-Carlo only

2. Distribution settings

A table consists of three columns, an argument, a type of distribution, and distribution settings.

- An argument must be the formula parameter;
- Distribution type is selected from the drop-down list, the list of available distribution types will be updated;
- In order to change the distribution settings, double-click the corresponding cell in the distribution settings column with the left mouse button.
- For multidimensional normal distribution parameters are set as variance-covariance matrix and vector of means, the resulting distribution is calculated by the formula:

$$c_1 \cdot D_1 + c_2 \cdot D_2 + \dots + c_n \cdot D_n,$$

where n – number of dimensions, D – normal distributions, c – scale coefficients from the coefficients table.

3. Calculations

After the model and distributions settings have been defined in accordance with the previous sections, it is necessary to set the calculation parameters.

For the method of random variable algebra, the most important parameter is the number of **samples**, this parameter indicates the number of samples with which the probability density will be sampled to perform subsequent operations.

Remarks:

- The greater the number of samples, the more accurate, but slower the parameters of the resulting distribution will be calculated;
- In the case of an additive measurement model, convolution is performed by the fast Fourier transform method, its complexity is $O(N \log(N))$. In case, if the number of samples is up to 100,000, it will take less than 1 second to perform convolution of two random variables. For other cases, for example, the product of two random variables, numerical integration will be performed, its complexity is $O(N^2)$, then less than 1 second will be spent for 10,000 samples, and about a minute (depending on processor speed) for 100,000 samples;
- Recommended values: 1,000 samples for regular measurements and 10,000 for precision;
- If only analytical conversions are performed, this parameter is irrelevant.

For the Monte-Carlo method, the main parameter is the **number of experiments**. The recommended by GUM value is 10^6 . The larger the value, the greater the accuracy, but the dependency is back-root, which means that in order to achieve an accuracy of 10 times more, we will need to perform 100 times more experiments.

Remarks:

- The number of **pockets** only affects plotting;
- **Probability** used when finding quantiles.

After all the parameters are set, you should click the **evaluate** button. After that, charts of probability density and distribution functions will be constructed and moments and quantiles in the “results” block will be determined.

4. Results

| Parameter | Description |
|------------|---|
| t, ms | Time spent on performing calculations |
| μ | Expected value |
| σ | Standard deviation |
| σ^2 | Dispersion |
| U^+ | The upper bound of the coverage interval for a given probability p. |
| U^- | The lower bound of the coverage interval for a given probability p. |
| γ | Skewness |
| U_{\pm} | $(U^+ - U^-)/2$. If the skewness tends to 0, this value can be used to express the expanded uncertainty $Y = \mu \pm U$, otherwise suggested entry $Y \in [U^-, U^+]$. |