



机器学习及其MATLAB实现—从基础到实践 第7课

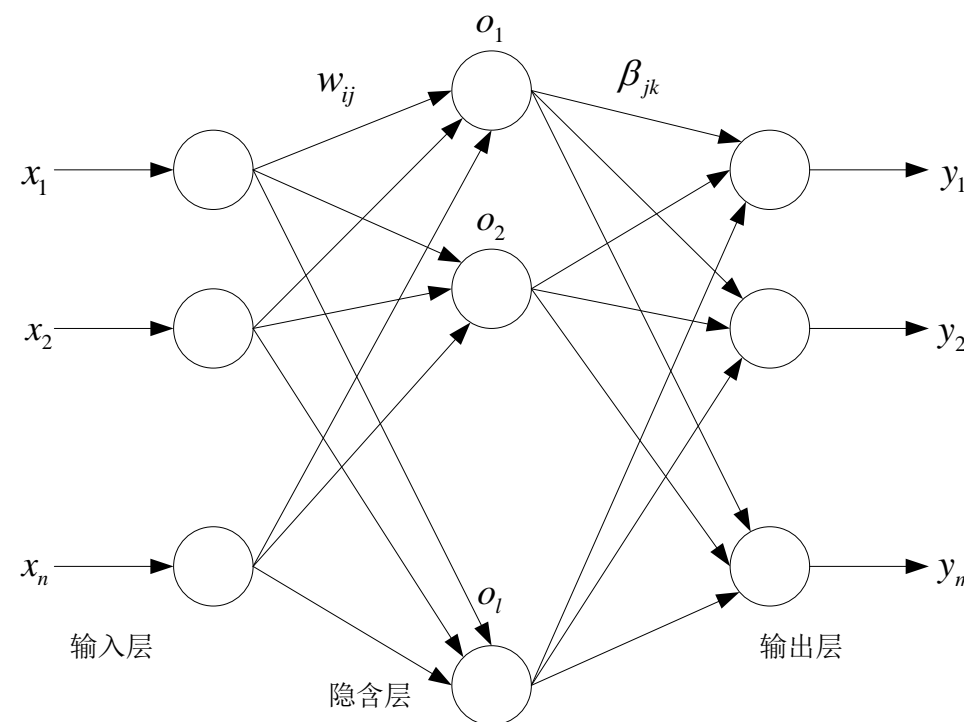
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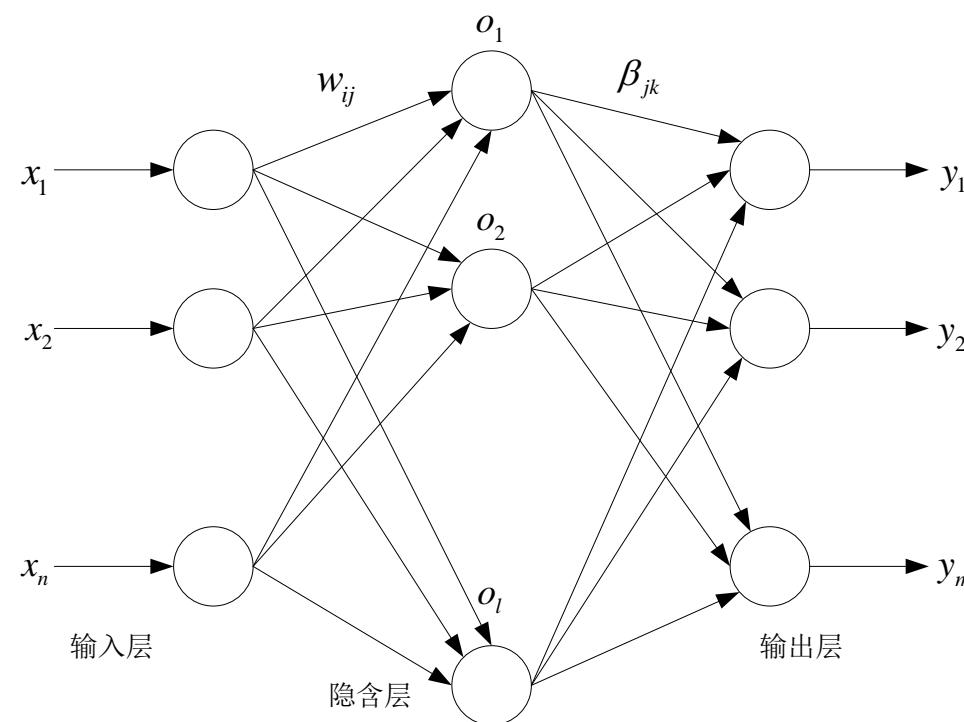
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- 第一课 MATLAB入门基础
- 第二课 MATLAB进阶与提高
- 第三课 BP神经网络
- 第四课 RBF、GRNN和PNN神经网络
- 第五课 竞争神经网络与SOM神经网络
- 第六课 支持向量机 (Support Vector Machine, SVM)
- **第七课 极限学习机 (Extreme Learning Machine, ELM)**
- 第八课 决策树与随机森林
- 第九课 遗传算法 (Genetic Algorithm, GA)
- 第十课 粒子群优化 (Particle Swarm Optimization, PSO) 算法
- 第十一课 蚁群算法 (Ant Colony Algorithm, ACA)
- 第十二课 模拟退火算法 (Simulated Annealing, SA)
- 第十三课 降维与特征选择

- The learning speed of feedforward neural networks is in general **far slower than required** and it has been a **major bottleneck** in their applications for past decades.
- Two key reasons behind may be:
 - 1) the slow **gradient-based** learning algorithms are extensively used to train neural networks.
 - 2) all the parameters of the networks are **tuned iteratively** by using such learning algorithms.

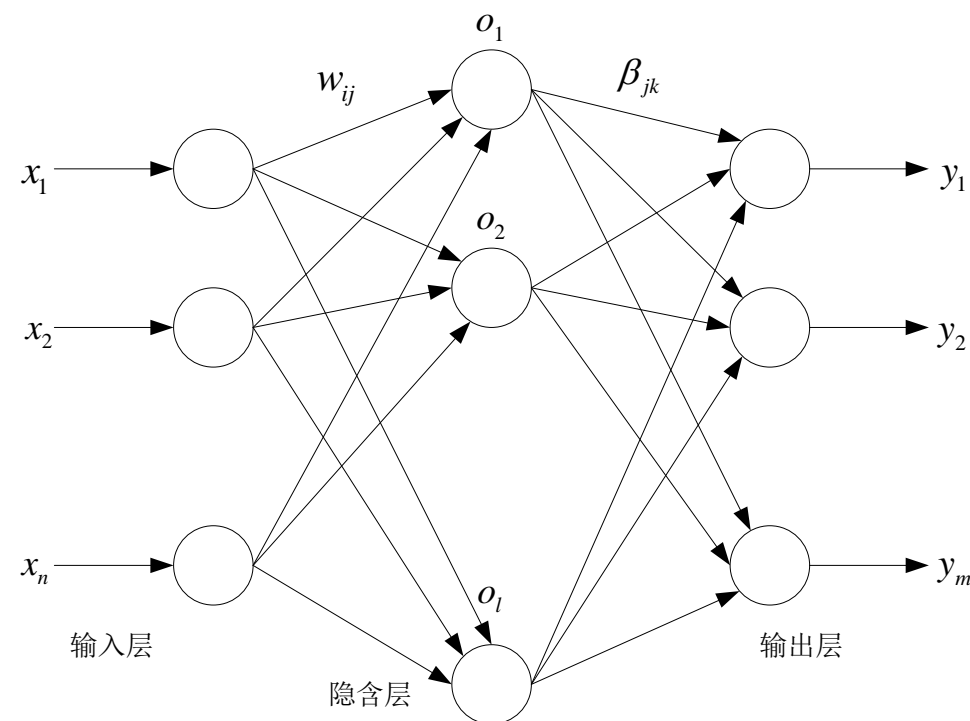


- Unlike these traditional implementations, **Extreme Learning Machine (ELM)** which **randomly** all the hidden nodes parameters of generalized **Single-hidden Layer Feedforward Networks (SLFNs)** and **analytically** determines the output weights of SLFNs.
- All the hidden node parameters are **independent** from the target functions or the training datasets. **All the parameters of ELMs can be analytically determined instead of being tuned.**
- In theory, this algorithm tends to provide the **good generalization performance** at extremely **fast learning speed**.



极限学习机原理概述

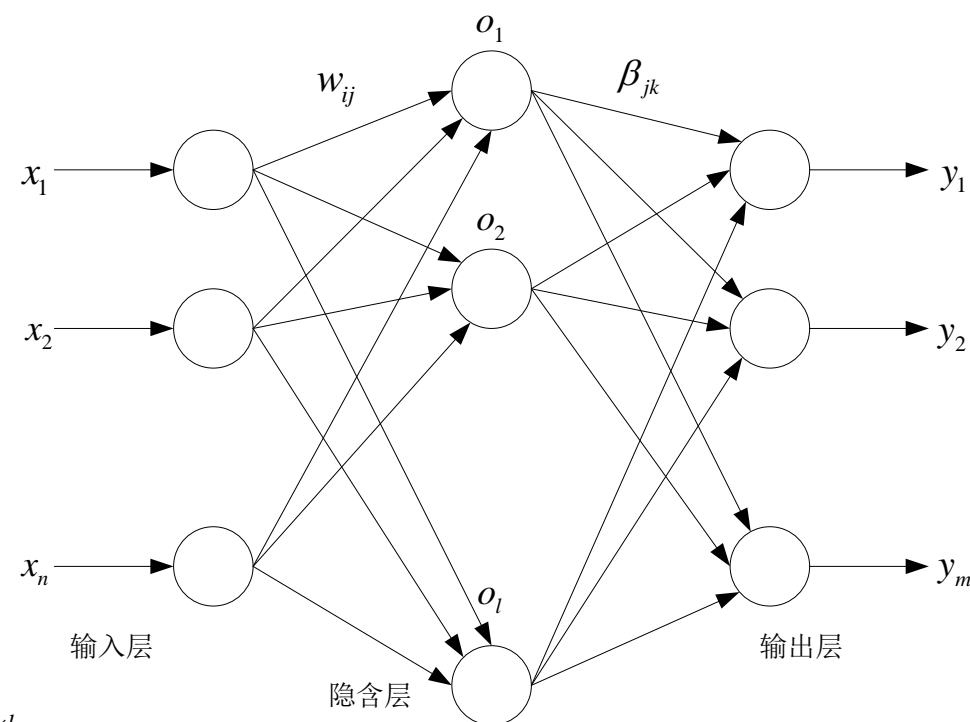
$$W = \begin{bmatrix} w_{11} & w_{12} & \dots & w_{1n} \\ w_{21} & w_{22} & \dots & w_{2n} \\ \dots & \dots & \dots & \dots \\ w_{l1} & w_{l2} & \dots & w_{ln} \end{bmatrix}_{l \times n}$$
$$\beta = \begin{bmatrix} \beta_{11} & \beta_{12} & \dots & \beta_{1m} \\ \beta_{21} & \beta_{22} & \dots & \beta_{2m} \\ \dots & \dots & \dots & \dots \\ \beta_{l1} & \beta_{l2} & \dots & \beta_{lm} \end{bmatrix}_{l \times m}$$
$$b = \begin{bmatrix} b_1 \\ b_2 \\ \dots \\ b_l \end{bmatrix}_{l \times 1}$$
$$X = \begin{bmatrix} x_{11} & x_{12} & \dots & x_{1Q} \\ x_{21} & x_{22} & \dots & x_{2Q} \\ \dots & \dots & \dots & \dots \\ x_{n1} & x_{n2} & \dots & x_{nQ} \end{bmatrix}_{n \times Q}$$
$$Y = \begin{bmatrix} y_{11} & y_{12} & \dots & y_{1Q} \\ y_{21} & y_{22} & \dots & y_{2Q} \\ \dots & \dots & \dots & \dots \\ y_{m1} & y_{m2} & \dots & y_{mQ} \end{bmatrix}_{m \times Q}$$
$$T = [t_1, t_2, \dots, t_Q]_{m \times Q}, t_j = \begin{bmatrix} t_{1j} \\ t_{2j} \\ \dots \\ t_{mj} \end{bmatrix}_{m \times 1} = \begin{bmatrix} \sum_{i=1}^l \beta_{i1} g(w_i x_j + b_i) \\ \sum_{i=1}^l \beta_{i2} g(w_i x_j + b_i) \\ \dots \\ \sum_{i=1}^l \beta_{im} g(w_i x_j + b_i) \end{bmatrix}_{m \times 1} \quad (j = 1, 2, \dots, Q)$$



$$T = [t_1, t_2, \dots, t_Q]_{m \times Q}, t_j = \begin{bmatrix} t_{1j} \\ t_{2j} \\ \dots \\ t_{mj} \end{bmatrix}_{m \times 1} = \begin{bmatrix} \sum_{i=1}^l \beta_{i1} g(w_i x_j + b_i) \\ \sum_{i=1}^l \beta_{i2} g(w_i x_j + b_i) \\ \dots \\ \sum_{i=1}^l \beta_{im} g(w_i x_j + b_i) \end{bmatrix}_{m \times 1} \quad (j = 1, 2, \dots, Q)$$

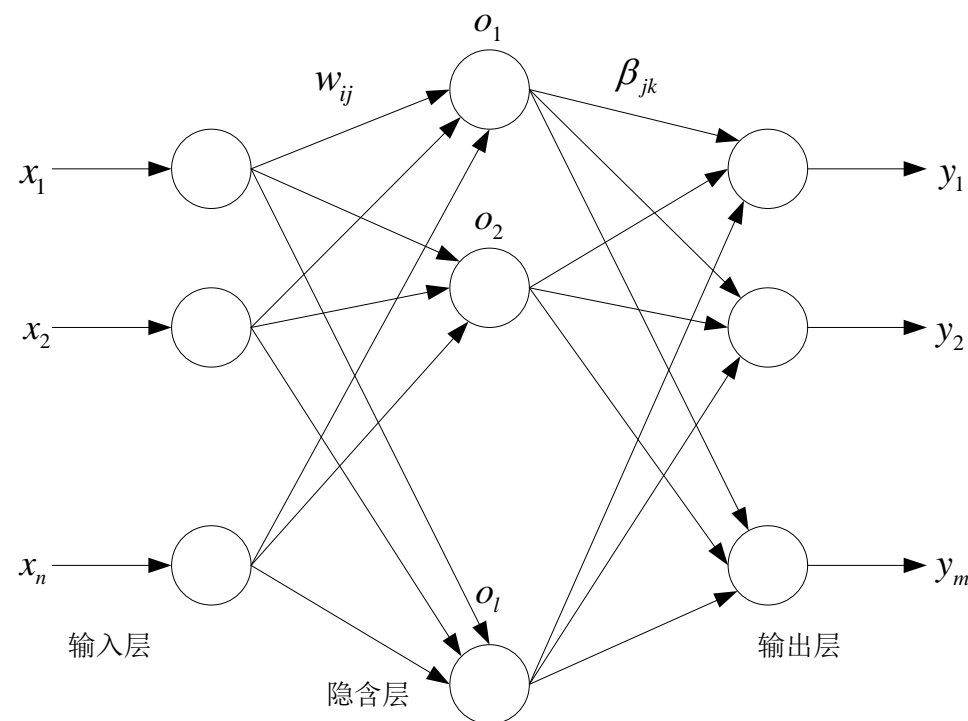
$$H\beta = T'$$

$$H(w_1, w_2, \dots, w_l, b_1, b_2, \dots, b_l, x_1, x_2, \dots, x_Q) = \begin{bmatrix} g(w_1 \cdot x_1 + b_1) & g(w_2 \cdot x_1 + b_2) & g(w_l \cdot x_1 + b_l) \\ g(w_1 \cdot x_2 + b_1) & g(w_2 \cdot x_2 + b_2) & g(w_l \cdot x_2 + b_l) \\ \dots & \dots & \dots \\ g(w_1 \cdot x_Q + b_1) & g(w_2 \cdot x_Q + b_2) & g(w_l \cdot x_Q + b_l) \end{bmatrix}_{Q \times l}$$



Theorem 2.1. Given a standard SLFN with N hidden nodes and activation function $g: \mathbf{R} \rightarrow \mathbf{R}$ which is infinitely differentiable in any interval, for N arbitrary distinct samples $(\mathbf{x}_i, \mathbf{t}_i)$, where $\mathbf{x}_i \in \mathbf{R}^n$ and $\mathbf{t}_i \in \mathbf{R}^m$, for any \mathbf{w}_i and b_i randomly chosen from any intervals of \mathbf{R}^n and \mathbf{R} , respectively, according to any continuous probability distribution, then with probability one, the hidden layer output matrix \mathbf{H} of the SLFN is invertible and $\|\mathbf{H}\boldsymbol{\beta} - \mathbf{T}\| = 0$.

Theorem 2.2. Given any small positive value $\varepsilon > 0$ and activation function $g: \mathbf{R} \rightarrow \mathbf{R}$ which is infinitely differentiable in any interval, there exists $\tilde{N} \leq N$ such that for N arbitrary distinct samples $(\mathbf{x}_i, \mathbf{t}_i)$, where $\mathbf{x}_i \in \mathbf{R}^n$ and $\mathbf{t}_i \in \mathbf{R}^m$, for any \mathbf{w}_i and b_i randomly chosen from any intervals of \mathbf{R}^n and \mathbf{R} , respectively, according to any continuous probability distribution, then with probability one, $\|\mathbf{H}_{N \times \tilde{N}} \boldsymbol{\beta}_{\tilde{N} \times m} - \mathbf{T}_{N \times m}\| < \varepsilon$.



Algorithm ELM: Given a training set $\mathcal{S} = \{(\mathbf{x}_i, \mathbf{t}_i) | \mathbf{x}_i \in \mathbf{R}^n, \mathbf{t}_i \in \mathbf{R}^m, i = 1, \dots, N\}$, activation function $g(x)$, and hidden node number \tilde{N} ,

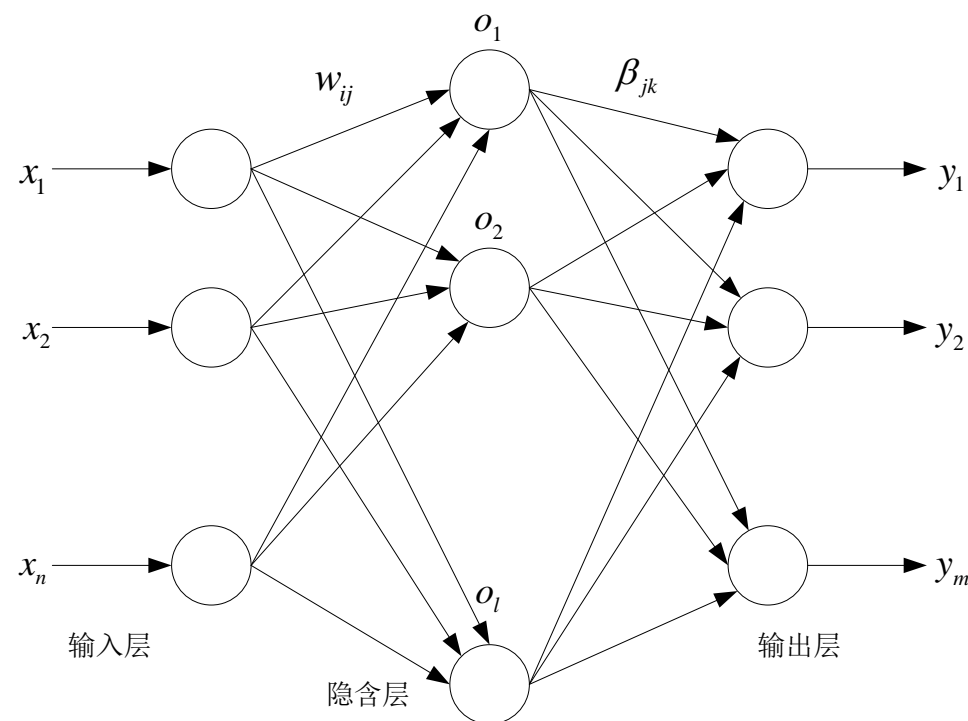
Step 1: Randomly assign input weight w_i and bias b_i , $i = 1, \dots, \tilde{N}$.

Step 2: Calculate the hidden layer output matrix \mathbf{H} .

Step 3: Calculate the output weight β

$$\beta = \mathbf{H}^\dagger \mathbf{T}, \quad (16)$$

where $\mathbf{T} = [\mathbf{t}_1, \dots, \mathbf{t}_N]^\mathbf{T}$.



- Compared BP Algorithm and SVM, ELM has several salient features:
 - **Ease of use.** No parameters need to be manually tuned except predefined network architecture.
 - **Faster learning speed.** Most training can be completed in *milliseconds*, *seconds*, and *minutes*.
 - **Higher generalization performance.** It could obtain better generalization performance than BP in most cases, and reach generalization performance similar to or better than SVM.
 - **Suitable for almost all nonlinear activation functions.** Almost all piecewise continuous (including discontinuous, differential, non-differential functions) can be used as activation functions.
 - **Suitable for fully complex activation functions.** Fully complex functions can also be used as activation functions in ELM.

- **nargin**
- **error**
- **pinv**
- **sin / hardlim**
- **elmtrain**
- **elmpredict**

汽油辛烷值预测

鸢尾花种类识别

神经网络GUI实现

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Thanks

FAQ时间