# Sparse Linear System Solvers Comparison

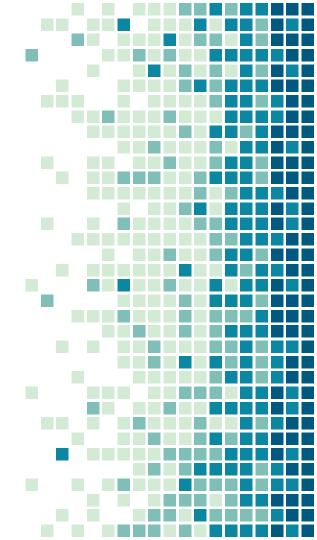
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Università degli Studi di Milano-Bicocca

Course: *Methods of Scientific Calculus* 



1. PROBLEM



## WHICH IS THE BEST TOOL TO SOLVE SPARSE LINEAR PROBLEMS WITH CHOLESKY DECOMPOSITION?

#### Windows or Linux?

We'll test both.



## WHICH IS THE BEST TOOL TO SOLVE SPARSE LINEAR PROBLEMS WITH CHOLESKY DECOMPOSITION?

**MATLAB** or some other open source software? We'll try out:

- C++
- Pythor



2.
CHOLESKY
AVAILABLE LIBRARIES



### **MATLAB**

MATLAB has built-in capabilities to solve sparse linear problems using the Cholesky method.

As you can find <u>here</u>, whenever you do  $x = A \setminus B$  (where A and B are matrices of equal number of rows), MATLAB internally operates a <u>resolution</u> <u>choice</u> based on matrices shapes and symmetries, that always gives the optimal solver, thus the minimum computation time.







## **PYTHON**



## 3. COMPARISON TESTS



## SAMPLES

All tests you can find in this presentation are made solving the equation Ax = b, where b is chosen for having the exact solution composed as  $xe = [1 \ 1 \ 1 \ 1 ]$ . In other words, b = A \* xe.



## SAMPLES

All input sample are positive-definite and symmetric matrices that come from the <u>SuiteSparse Matrix Collection</u>.

In particular, the following matrices have been used:

ex15
shallow\_water1
cfd1
cfd2
parabolic\_fem

apache2 StocF-1465 Flan\_1565 G3\_circuit



## PERFORMANCES

In order to declare the best library and operating system that fit your needs, we have developed some scripts you can find in this GitHub repository.

For each library, we'll consider three performances:

- **Resolution Time**
- Used Memory
- **Relative Error**



## **ENVIRONMENTS**

We'll soon present the results of our study. We ran our tests on Azure Virtual Machines.

The following are both the Windows and Linux virtual machines technical specifications:

- 8 VCPUs
- 56 GB of RAM



We used Ubuntu 18.04 and Windows 10 Pro 1803.



4. RESULTS



## SOME NOTES

We ran MATLAB and Eigen scripts both on Windows and Linux, while Scikit-Sparse was only tested on Linux, because of the impossibility of installing it on Windows. Specifically, we had problem obtaining SuiteSparse library and compiling cholmod.h to run it with Python.

Also, you will notice that some value are missing for the two largest matrices with C++ Eigen library.



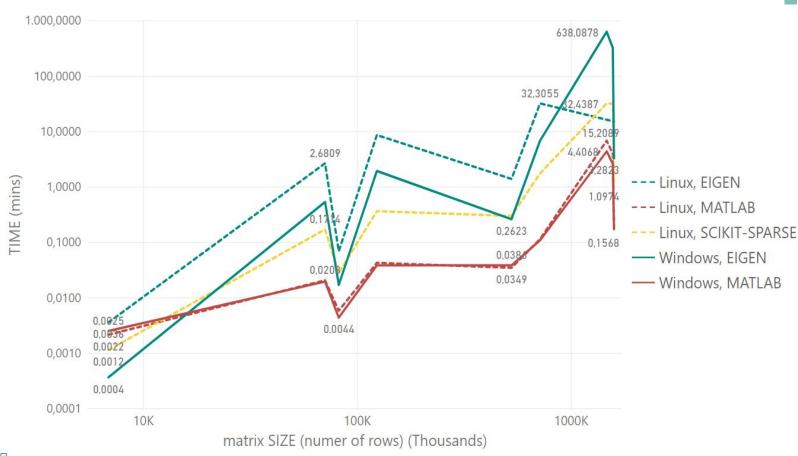
## SOME NOTES

Although the first idea of plotting some matrices resolution result charts could be to put the matrix size on the X-axis, the most natural way to present this type of data for **sparse matrices** is to consider, for the abscissa, the number of non-zero elements that appear in each matrix.

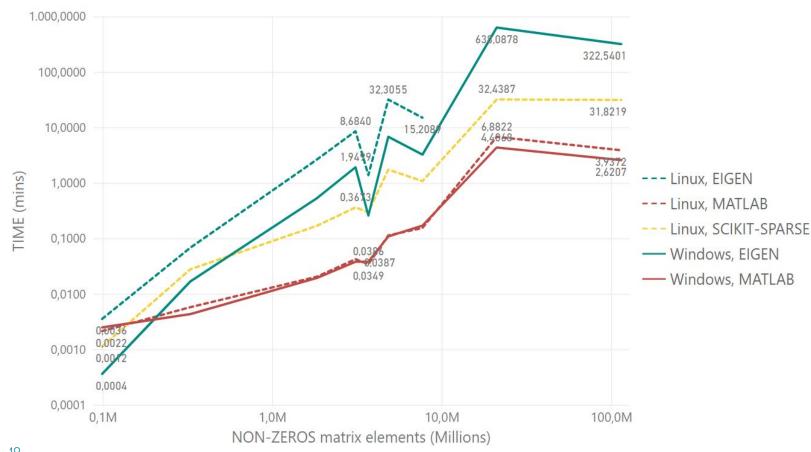
However, we'll show you both size and non-zeros based charts.



#### RESOLUTION TIME BY MATRIX SIZE



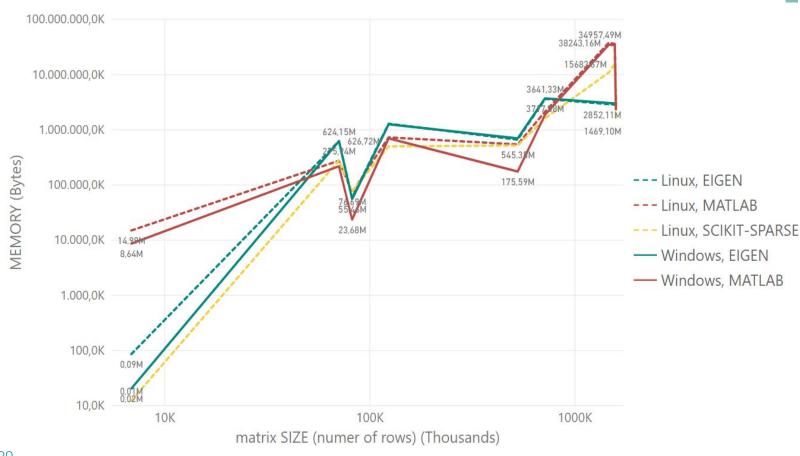
#### RESOLUTION TIME BY MATRIX NON-ZEROS ELEMENTS



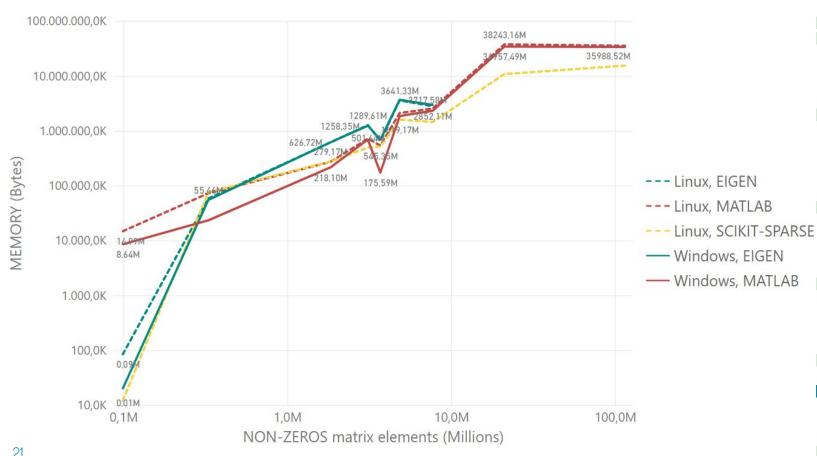
#### RESOLUTION TIME CONSIDERATIONS



#### MEMORY BY MATRIX SIZE



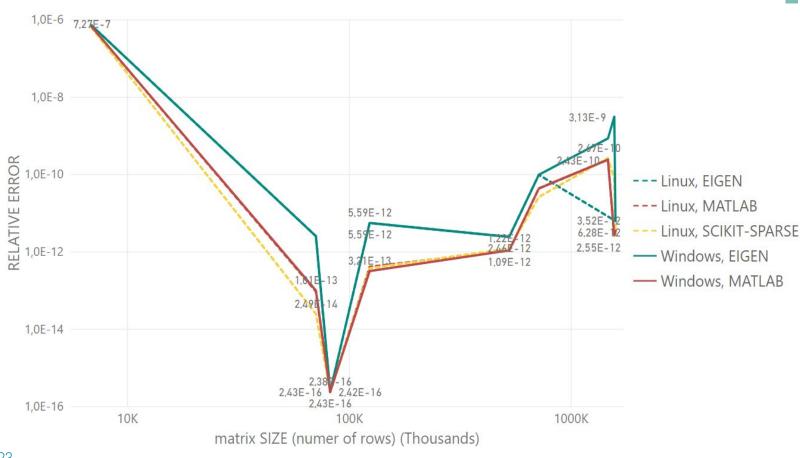
#### MEMORY BY MATRIX NON-ZEROS ELEMENTS



### MEMORY CONSIDERATIONS

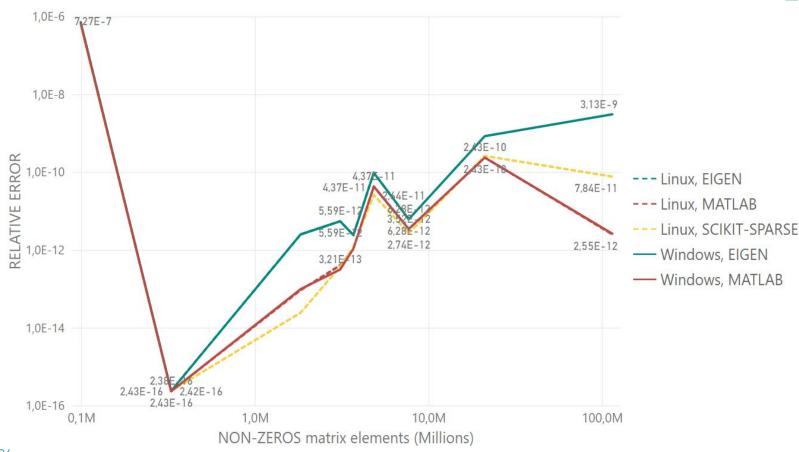


#### RELATIVE ERROR BY MATRIX SIZE





#### RELATIVE ERROR BY MATRIX NON-ZEROS ELEMENTS



#### RELATIVE ERROR CONSIDERATIONS



## 5. CONCLUSIONS



## CONCLUSIONS

Lorem ipsum dolor sit amet.



## THANKS!

## Any questions?

You can find us at: m.ferri17@campus.unimib.it n.habbash@campus.unimib.it

https://github.com/dodicin/slss-comparison-test



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## HELLO!

### I am Jayden Smith

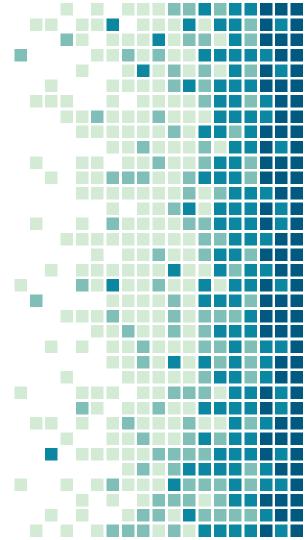
I am here because I love to give presentations.

You can find me at @username

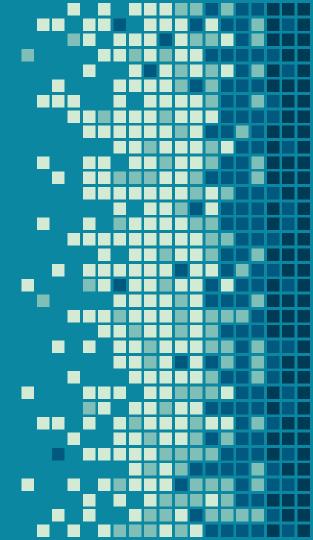


## 1. TRANSITION HEADLINE

Let's start with the first set of slides



Quotations are commonly printed as a means of inspiration and to invoke philosophical thoughts from the reader.

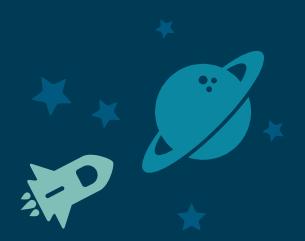


### THIS IS A SLIDE TITLE

- Here you have a list of items
- And some text
- But remember not to overload your slides with content

Your audience will listen to you or read the content, but won't do both.





## BIG CONCEPT

Bring the attention of your audience over a key concept using icons or illustrations



## YOU CAN ALSO SPLIT YOUR CONTENT

#### White

Is the color of milk and fresh snow, the color produced by the combination of all the colors of the visible spectrum.

#### Black

Is the color of coal, ebony, and of outer space. It is the darkest color, the result of the absence of or complete absorption of light.



## IN TWO OR THREE COLUMNS

#### Yellow

Is the color of gold, butter and ripe lemons. In the spectrum of visible light, yellow is found between green and orange.

#### Blue

Is the colour of the clear sky and the deep sea. It is located between violet and green on the optical spectrum.

#### Red

Is the color of blood, and because of this it has historically been associated with sacrifice, danger and courage.



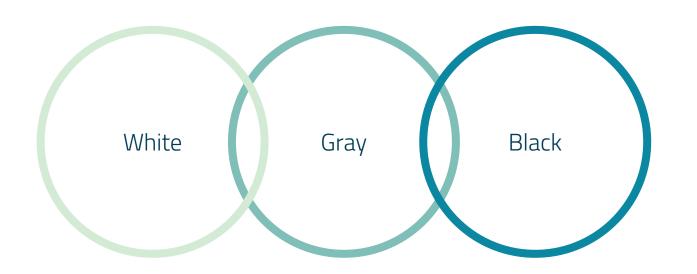


# A PICTURE IS WORTH A THOUSAND WORDS

A complex idea can be conveyed with just a single still image, namely making it possible to absorb large amounts of data quickly.



## USE CHARTS TO EXPLAIN YOUR IDEAS





## AND TABLES TO COMPARE DATA

	А	В	С
Yellow	10	20	7
Blue	30	15	10
Orange	5	24	16



## MAPS



# 89,526,124

Whoa! That's a big number, aren't you proud?



## 89,526,124\$

That's a lot of money

185,244 users

And a lot of users

100%

Total success!



## **OUR PROCESS IS EASY**





### LET'S REVIEW SOME CONCEPTS

#### Yellow

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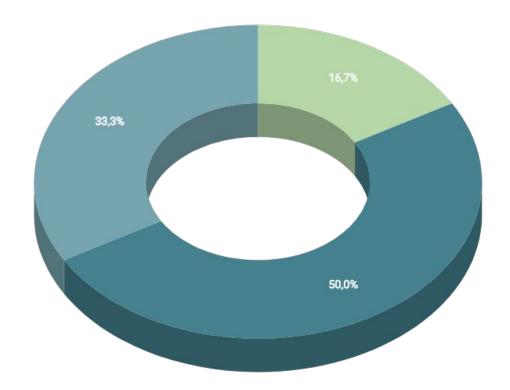
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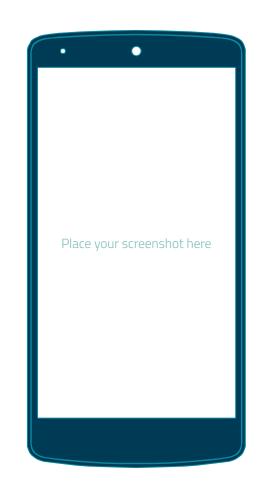
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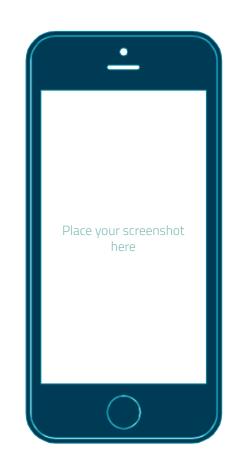


You can insert graphs from <u>Google Sheets</u>

## ANDROID PROJECT

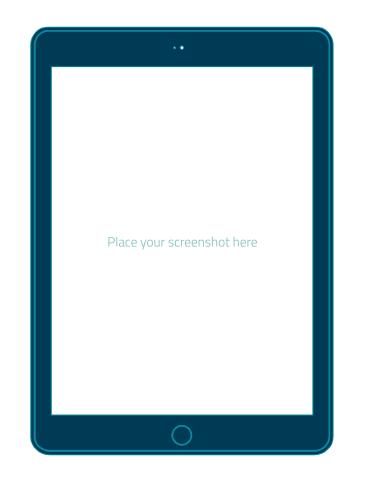


## iPHONE PROJECT

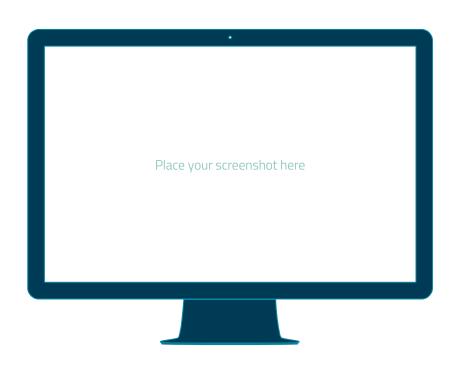




## TABLET PROJECT



## DESKTOP PROJECT





## THANKS!

## Any questions?

You can find me at:

@username user@mail.me



### CREDITS

Special thanks to all the people who made and released these awesome resources for free:

- Presentation template by <u>SlidesCarnival</u>
- Photographs by <u>Unsplash</u>



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Titles: Dosis

Body copy: Titillium Web

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Pastel green #d3ebd5 · Green #80bfb7 · Teal #0b87a1 · Navy #01597f · Dark navy #003b55

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- Resize them without losing quality.
- Change fill color and opacity.
- Change line color, width and style.

Isn't that nice?:)

Examples:









#### Now you can use any emoji as an icon!

And of course it resizes without losing quality and you can change the color.

How? Follow Google instructions <a href="https://twitter.com/googledocs/status/730087240156643328">https://twitter.com/googledocs/status/730087240156643328</a>



and many more...