

Biotech Beer Brewing

Final report

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Abstract—Bla blub

I. INTRODUCTION

Alcohol fermentation in beer or wine production is a highly complex process as the quality of the product plays a major role in defining its price. On the other hand the process itself underlies strict laws which guarantee transparency for the customers [2] [3]. Additionally the growing organic food market calls for products with even more strict processing standards [4]. Compared to other sectors in the food industry where alcohol fermentation is applied all these constraints increases the effort dramatically of finding optimal ways of controlling product quality. As experimental development in laboratories is very costly and not affordable by smaller breweries, simulation methods are gaining popularity.

A well established group of methods uses Genome-Scale Models (GEM) to model metabolic fluxes in bacteria [18]. GEMs are created by analysing the information in the genome of a bacteria about its enzymatical processes and extrapolating a network of metabolites and metabolite reactions which represents the internal fluxes of this bacteria. Based on this model possible flux distributions can be predicted using linear optimization methods, known as flux balance analysis (FBA) [1].

In its basic form describes FBA the behavior of only one bacteria in a constant environment. Zomorri et al. summarizes some approaches to extend FBA to multispecies simulations (*steady-state models*) in time variant environments (*dynamic models*) and even considering spacial variations (*spatio-temporal models*) [18].

The simulation of co-cultures using GEMs is still an emerging field. Every approach has its strengths and weaknesses and must be chosen dependent on the application. In *Steady-state models* like compartmentalized community-level metabolic modeling a common objective function for all involved species must be formulated. This approach has a relatively low computational effort but shows drawbacks in competitive co-cultures where a common objective can not easily be formulated. The spacial dimension of *Spatio-temporal models* results in very high computational effort and it has to be evaluated if this enhances the accuracy of the estimated behavior in that case.

The class of *dynamic models* described by Zomorrodi et al. uses a system of ordinary differential equations (ODE) to extend the static simulation approach of FBA with external system dynamics like the exchange of metabolites and bacteria growth and is called dynamic flux balance analysis (DFBA) [18].

Mehadevan et al. describes two basic categories of DFBA approaches: *dynamic optimization approach* (DOA) and *static optimization approach* (SOA) [13].

In DOA the linear programming (LP) problem to predict the behavior of the bacteria and the differential equations are reformulated to a non-linear programming problem (NLP). This approach has a very high computational effort [9] compared to SOA and has only been used for relatively small GEMs with up to 13 modeled fluxes and 8 metabolites [12] [11].

In SOA the simulation time is discretised by a defined time interval and a FBA is executed for each time point. The results are used to iteratively solve the discretised differential equations to update the environmental conditions at each time point. The described integration method in SOA is similar to Euler-Cauchy. In this approach it is assumed that the cell internal dynamics are much faster than the external dynamics.

Höffner et al. basically generalizes SOA to arbitrary integration methods for solving the system of ODEs by using a third-party solver and names it *direct approach* (DA) [9].

Henson et al. introduces a further method which shows similarities to SOA and DA but enhances the efficiency of the algorithm [9] by reformulating the LP and ODE to a differential-algebraic equation system [8].

The DA described by Höffner et al. has been successfully applied to simulate alcohol fermentation in a wine approximating setup [15] [14] and to predict growth of bacteria in a co-culture [7]. Zhuang et al. implemented the method in the *Dynamic Multispecies Metabolic Modeling* (DMMM) framework which is publicly accessible and written for Matlab [16]. The method developed by Henson et al. compared to DMMM has the potential to increase the accuracy by fixed calculation runtime but since the implementation of DMMM is publicly accessible and relatively simple to implement, this method shall be used in this work.

II. METHODS

A. Genome-Scale Models

B. Flux Balance Analysis

C. Simulation Algorithm

As described by Zhuang et al. in [17] the algorithm uses a ODE solver with embedded FBA. A FBA is solved for each GEM in the model and for each time step in the discretised simulation time interval considering the changed metabolite and bacteria densities in the shared environment. The results of the FBAs are used by the ODE solver to solve the differential equations

TABLE I: Overview of implemented features compared to DMMM

| Feature | DMMM | This project |
|--|-------------------------|--------------|
| Model | | |
| arbitrary many GEMs | yes | yes |
| arbitrary many metabolites in environment | yes | yes |
| mortality of bacteria | yes (in output flux) | yes |
| input/output flux of bacteria and metabolites | yes | no |
| parameterized initial state of environment composition | yes | yes |
| Michaelis-Menten kinetics | yes | yes |
| Algorithm | | |
| ODE solver | yes | yes |
| different ODE solvers | yes | no |
| analytical solver | yes | no |

$$\frac{dx_j}{dt} = \mu_j x_j \quad (1)$$

$$\frac{ds_i}{dt} = \sum_{j=1}^N v_{i,j} x_j \quad (2)$$

which models the dynamics of the bacteria's environment [16] where $i = 1 \dots N$ is the index of metabolites in the shared environment and $j = 1 \dots M$ is the index of bacteria. The bacteria density is modeled in x_j with $[x_j] = \frac{g}{l}$ and μ_j is the bacteria's growth rate with $[\mu_j] = \frac{mmol}{g_{DW}h}$. Input and output fluxes of the bacteria's models are modeled in $v_{i,j}$ with $[v_{i,j}] = \frac{mmol}{g_{DW}h}$, the densities of metabolites in the shared environment in s_i with $[s_i] = \frac{mmol}{l}$.

In each time step each bacteria's metabolite intake must be changed dependent on the densities of the metabolites in the shared environment. To model saturation of metabolite intake for high metabolite densities Zhuang et al. implemented Michaelis-Menten kinetics [10]

$$v_{max,i,j} = \frac{v_{mm,i,j} s_i}{s_i + k_{mm,i,j}} \quad (3)$$

This formula describes the upper bound of the input flux $v_{max,i,j}$ for metabolite i of bacteria j dependent on the metabolite density s_i . The formula is characterized by to constants $[v_{mm,i,j}] = \frac{mmol}{g_{DW}h}$ and $[k_{mm,i,j}] = \frac{mmol}{l}$ for each bacteria and metabolite.

Mortality is considered using a constant $[\mu_{mort,j}] = \frac{mmol}{g_{DW}h}$ for each bacteria j in this implementation while Zhuang et al. modeled this using the output flux of bacteria out of the system.

Algorithm 1 shows a basic implementation of the differential equations solved by an ODE solver during the simulation similar to DMMM [17].

The algorithm expects a list of bacteria models consisting of

- GEM of this bacteria: A , v_{min} , v_{max} , w_{growth}
- v_{mm} (Michaelis-Menten V_{max}) for each exchange metabolite and species
- k_{mm} (Michaelis-Menten K) for each exchange metabolite and species

- mortality μ_{mort}

Furthermore a list of all exchange metabolites in the environment, the bacteria and metabolite densities.

Algorithm 1: Differential equation with embedded FBA

1 function step($model_1 \dots model_M, m_1 \dots m_N, x_1 \dots M, s_1 \dots s_N$);

Input : bacteria models $model_j$, exchange metabolites m_i in environment, bacteria densities x_j , metabolite densities s_i

Output: slope of bacteria and metabolite densities \dot{x}_j, \dot{s}_i

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2 for  $j := 1$  to  $M$  do
3   for  $i := 1$  to  $M$  do
4      $model_j :=$ 
        $update\_intake\_bounds(model_j, s_j, m_i)$ 
5   end
6 end
7 for  $j := 1$  to  $M$  do
8    $\mu_j, v_j := FBA(model_j, w_{growth})$ 
9 end
10  $\mu := \mu - \mu_{mort}$ 
11  $\dot{x} := diag(\mu) x$ 
12 for  $j := 1$  to  $M$  do
13   for  $i := 1$  to  $N$  do
14      $\dot{s}[m_i] := \dot{s}[m_i] + v_j[m_i] x_j$ 
15   end
16 end
17 return  $\dot{x}, \dot{s}$ 

```

In a first step the upper bounds of the intake fluxes are updated for each bacteria j and exchange metabolite i . The function $update_intake_bounds(model_j, s_j, m_i)$ calculates the upper bounds using the formula 3 if the metabolite m_i is contained in $model_j$ as a exchange metabolite and updates this value in the model.

In a next step the GEMs are optimized for growth using FBA, the results are used as growth rate μ_j and actual input and output fluxes v_j of bacteria j in this time step.

The mortality is considered by subtracting the constants μ from the growth rates μ .

At last step the slopes \dot{x} and \dot{s} are calculated according to 1 and 2 and returned to the ODE solver.

D. Simulation Setup

The goal of the simulation is to validate the basic functionality of the simulator using a simplified setup of a realistic future simulation scenario. As defined in our project goals, this simulation scenario is the dynamic flux balance analysis (DFBA) of a co-culture of *Saccharomyces cerevisiae* and *Lactobacillus plantarum*.

As genome-scale models a model of *Lactobacillus plantarum* published by Teusink et al. [?]. A decision about a yeast model is not made yet.

The simulation will consider two input metabolites: oxygen and glucose. Table II and table III contain all values needed to define the initial metabolite conditions and kinetics.

TABLE II: Model constants used in the simulation setup

| Constant | <i>S. cerevisiae</i> | <i>L. plantarum</i> |
|--|----------------------|---------------------|
| Maximum glucose uptake rate (mmol/g/h) | 18.5 | ? |
| Maximum oxygen uptake rate (mmol/g/h) | 2.5 | ? |
| Glucose uptake saturation constant (g/l) | 0.5 | ? |
| Oxygen uptake saturation constant (mM) | 0.005 | ? |

TABLE III: Simulation parameters used in the simulation setup

| Parameter | value | reference |
|----------------------------------|--------------------|----------------------|
| Initial glucose density (mmol/l) | 272.9 ... 1230.755 | equation 6, table IV |
| Initial oxygen density (mmol/l) | 0.5039 | equation 7, table IV |

To verify the basic functionality of the simulator the resulting bacteria densities and metabolite densities of ethanol, d- and l-lactate, oxygen and glucose will be compared to existing data.

III. RESULTS

IV. CONCLUSIONS

APPENDIX A

The following approximation is used to convert °C (“degree plato”) to a density measure (g/l) [6].

$$d_{total} = 4.13 \frac{g}{l} \frac{1}{^{\circ}P} p + 997 \frac{g}{l} \quad (4)$$

As the simulation framework expects metabolite densities relative to the total volume of the solution (mmol of metabolite per liter solution, mmol/l) the total density d_{total} must to converted to a density s_{glc} . It is assumed that $V_{total} = V_{glc} + V_w$.

$$\begin{aligned} d_{total} &= \frac{m_{total}}{V_{total}} \\ d_{total} &= \frac{m_{glc} + m_w}{V_{total}} \\ d_{total} &= \frac{m_{glc} + d_w V_w}{V_{total}} \\ d_{total} &= \frac{m_{glc} + d_w (V_{total} - V_{glc})}{V_{total}} \\ d_{total} &= \frac{m_{glc} + d_w \left(V_{total} - \frac{m_{glc}}{d_{glc}} \right)}{V_{total}} \\ s_{glc} &= \frac{m_{glc}}{V_{total}} = \frac{d_{total} - d_w}{1 - \frac{d_w}{d_{glc}}} \end{aligned} \quad (5)$$

Combining equation 4 and 5, including all constants and converting it to mmol/l leads to:

$$s_{glc} = \left(63.857 \frac{1}{^{\circ}P} p - 46.385 \right) \frac{mmol}{l} \quad (6)$$

TABLE IV: Constants used in this document

| Constant | symbol | value | reference |
|--|-----------|---------|-----------|
| Oxygen saturation of water at 20°C (mg/l) | - | 9.077 | [1] |
| Molar mass of water (g/mol) | - | 18.015 | [5] |
| Molar mass of glucose (g/mol) | - | 180.156 | [5] |
| Density of water (g/l) | d_w | 1.00 | [5] |
| Density of glucose (g/l) | d_{glc} | 1.56 | [5] |
| Typical glucose/water solution density to brew beer (°P) | - | 5...20 | - |

To calculate the initial oxygen density in the solution it is assumed that the solution is at 20 °C and fully saturated with oxygen:

$$s_{init,ox} = 9.077 \frac{mg}{l} = 9.077 \cdot 10^{-3} \frac{g}{l} = \frac{9.077 \cdot 10^{-3} \frac{g}{l}}{18.015 \cdot 10^{-3} \frac{g}{mmol}} = 0,5039 \frac{mmol}{l} \quad (7)$$

APPENDIX B

TABLE V: Rating of considered DFBA methods

| Method | comp. effort | impl. complexity | flexibility |
|---|--------------|------------------|-------------|
| dynamic optimization approach (DOA) | high | medium-high | ? |
| static optimization approach (SOA) | low | low | low |
| direct approach (DA) | medium | low | medium |
| reformulation to a differential-algebraic equation system | low-medium | high | ? |

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