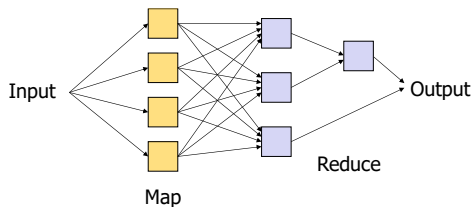
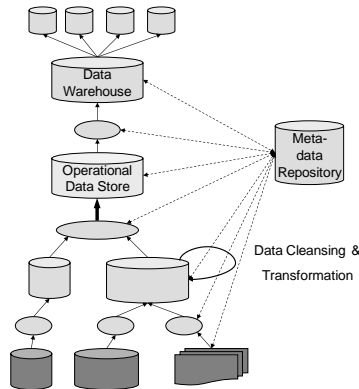
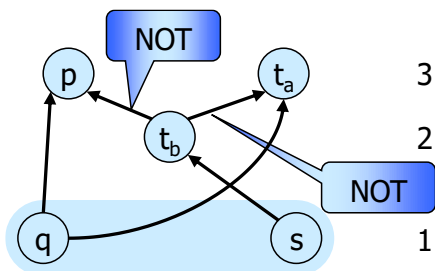


Chapter 5

Advanced Query Processing



?-
:-



5.1 Query Processing in Big Data Systems

5.2 Query Processing in Deductive Database Systems

5.3 Queries in Data Integration Systems

Literature

Karau H. & Warren, R.: High Performance Spark. O'Reilly, 2017.

Ré, C., & Salihoglu, S.: Topics in DBMS. Course at Stanford University, <https://web.stanford.edu/class/cs345d-01/>

Bauer, A. & Günzel, H. (ed.) Data-Warehouse-Systeme: Architektur, Entwicklung, Anwendung dpunkt-Verlag, 2001

Ceri, S.; Gottlob, G. & Tanca, L. Logic programming and databases Springer Publishing Company, Incorporated, 2012

Quix, C. Metadata Management for quality-oriented Information Logistics in Data Warehouse Systems (in German) RWTH Aachen University, 2003

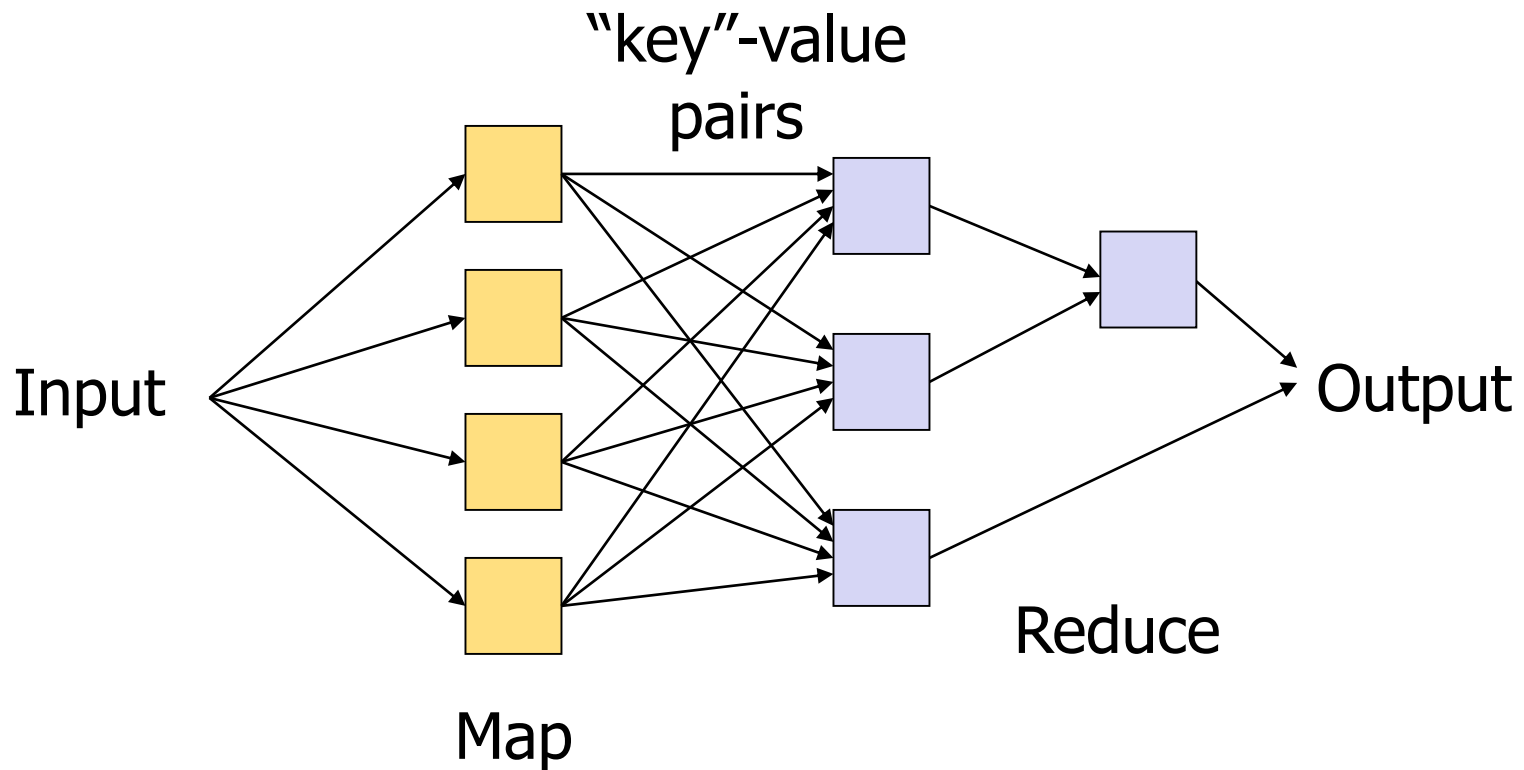
- Huge amount of data to be processed
 - For example: Google in 2003
 - 20 billion web pages → 400 TB of data
 - Requires ~4 months to read data (using a disk with ~30 MB/sec)
 - Requires ~1000 disks
 - This for just storing and reading the data, but you want to process the data, e.g.,
 - Process crawled documents
 - Process web request logs
 - Compute page rank
 - Build inverted indexes
 - ...
- Cannot be done on a single machine, needs massive parallel distributed system

1. Scalable
2. Fault-Tolerant
3. Easy To Program
4. Applicable To Many Problems

- Lots of programming work
 - communication and coordination
 - work partitioning
 - status reporting
 - optimization
 - locality
- Needs to be repeated for every problem you want to solve
- Needs to be fault-tolerant
 - One server may stay up three years (1,000 days)
 - If you have 10,000 servers, expect to lose 10 a day

- Programming pattern for parallel computation in distributed system
- Defined by two functions:
 - $\text{Map}(\text{data}) \rightarrow (\text{key}, \text{value})$
 - Reads input data and emits key-value pairs
 - Keys are not necessarily unique in emitted pairs
 - $\text{Reduce}(\text{key}, \text{values}) \rightarrow (\text{key}, \text{values})$
 - Gets input from Map function, a set of values for a single key
 - Input and output structure should be the same (some implementations require that output is a single value)
 - Reduce can be called multiple times for the same key
- Map and Reduce jobs can run on different nodes

Map-Reduce



Simple Example for Map-Reduce

(in MongoDB syntax)

Query: Sum of items in customers' shopping carts, grouped by product ID

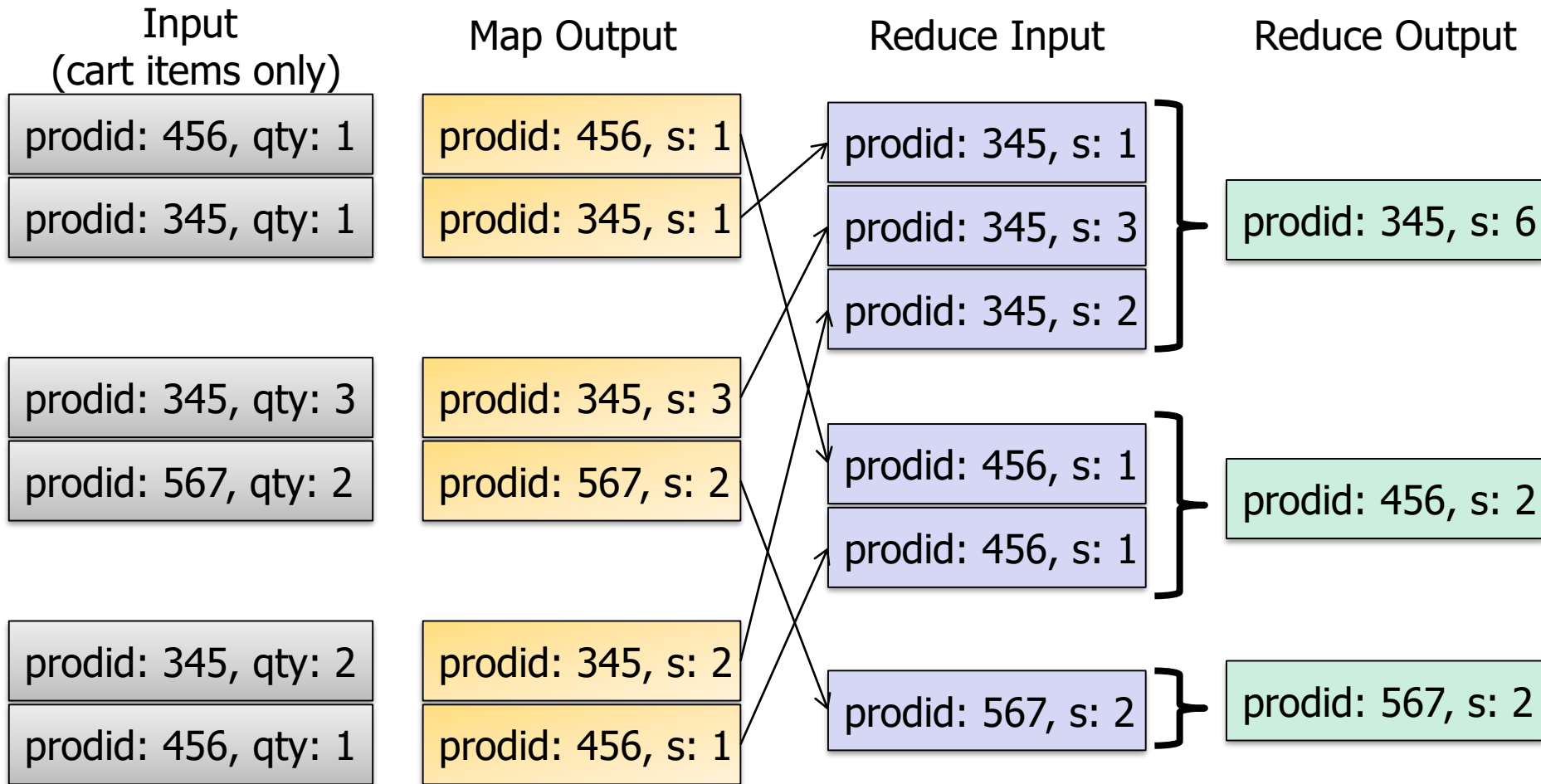
Input: Customer collection

```
{
  firstname: "John",
  lastname: "Doe",
  address: { ... },
  cart: [ { prodid: 3456,
            qty: 2},
          { prodid: 6789,
            qty: 1} ]
}
```

```
map=function() {
  if(this.cart!=null) {
    this.cart.forEach(function(item) {
      emit(item.prodid, { sum: item.qty });
    });
  }
}
```

```
reduce=function(key, values) {
  var s=0;
  values.forEach(function(value) {
    s+=value.sum;
  });
  return ( { sum: s} );
}
```


Example



A More Complex Example (1)

Join between customers and products

Input: Customers + products collection

```
{
  firstname: "John",
  lastname: "Doe",
  address: { ... },
  cart: [ { prodid: 3456,
            qty: 2},
          { prodid: 6789,
            qty: 1} ]
}
{
  prodid: 3456,
  price: 34
}
{
  prodid: 6789,
  price: 23
}
```

Query: The sum of items and their value in all shopping carts, grouped by product ID

```
map=function() {
  if(this.cart!=null) {
    this.cart.forEach(function(item) {
      emit(item.prodid, { qty: item.qty,
                        price: null,
                        total: null });
    });
  }
  if(this.prodid!=null) {
    emit(this.prodid, {qty: 0,
                      price: this.price,
                      total: 0 });
  }
}
```

A More Complex Example (2)

Join between customers and products

Input: Customers + products collection

```
{
  firstname: "John",
  lastname: "Doe",
  address: { ... },
  cart: [ { prodid: 3456,
            qty: 2},
          { prodid: 6789,
            qty: 1} ]
}
{
  prodid: 3456,
  price: 34
}
{
  prodid: 6789,
  price: 23
}
```

Query: The sum of items and their value in all shopping carts, grouped by product ID

```
map=function() {
  reduce=function(key, values) {
    var res = { qty : 0, price: null, total: null };
    values.forEach(function(value) {
      res.qty+=value.qty;

      if(res.price!=null) {
        res.total+=res.price*value.qty;
      }

      if(res.price==null && value.price!=null) {
        res.price=value.price;
        res.total=res.price * res.qty;
      }
    });
    return res;
  }
}
```

A More Complex Example (3)

Join between customers and products

Map Output

id: 456, qty: 1, price: null, total: null
id: 345, qty: 1, price: null, total: null
id: 345, qty: 3, price: null, total: null
id: 567, qty: 2, price: null, total: null
id: 345, qty: 2, price: null, total: null
id: 456, qty: 1, price: null, total: null
id: 345, price: 34, qty: 0, total: 0
id: 456, price: 45, qty: 0, total: 0
id: 567, price: 56, qty: 0, total: 0

Reduce Input

id: 345, qty: 1, ...
id: 345, qty: 3, ...
id: 345, qty: 2, ...
id: 345, price: 34, ...
id: 456, qty: 1, ...
id: 456, qty: 1, ...
id: 456, price: 45, ...
id: 567, qty: 2, ...
id: 567, price: 56, ...

Reduce Output

id: 345, qty: 6, price: 34, total: 204
--

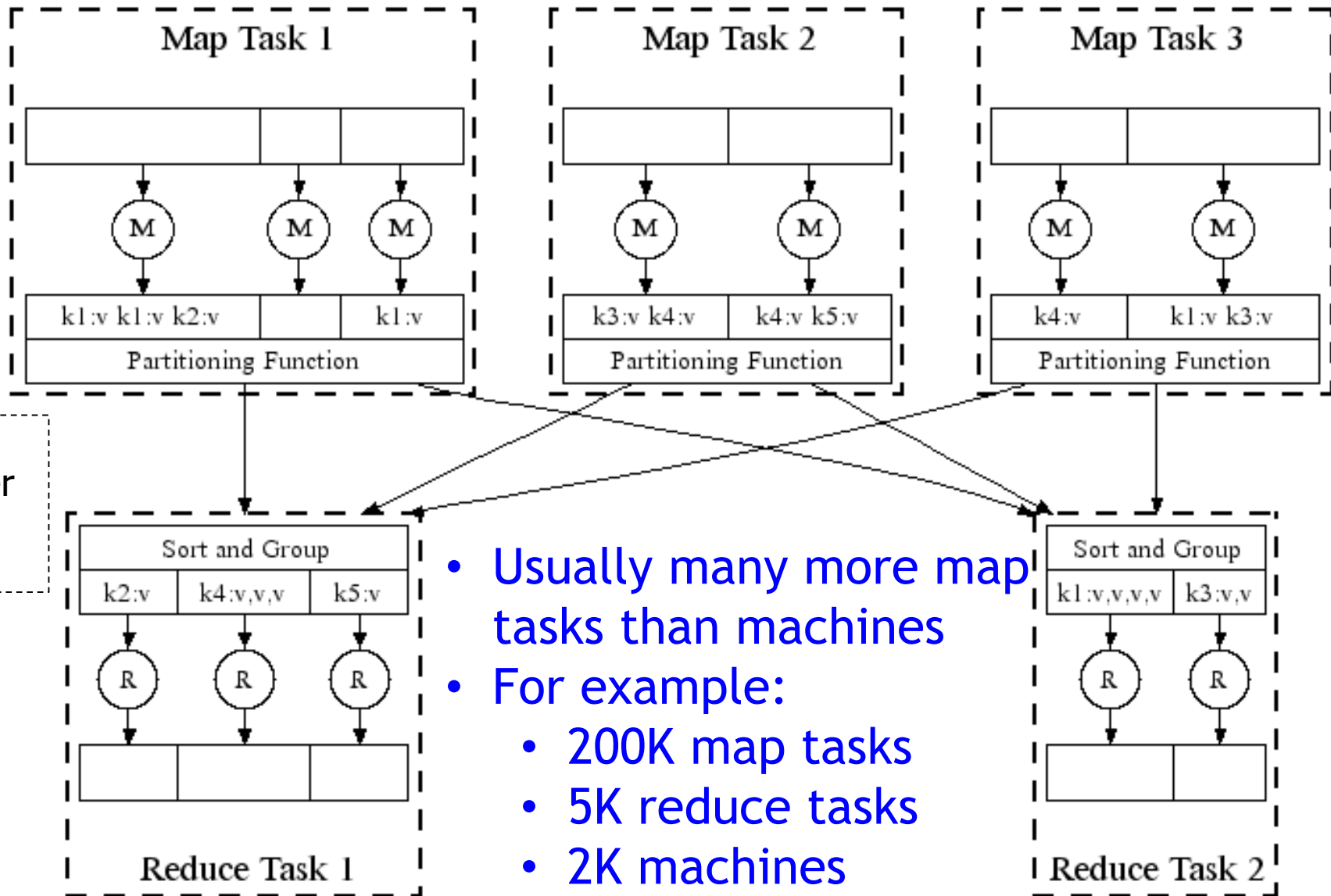
id: 456, qty: 2, price: 45, total: 90

id: 567, qty: 2, price: 56, total: 112
--

Key Points of Map-Reduce

- Map-Reduce: pattern enabling parallel query processing over a cluster
- Many implementations, e.g., in Hadoop with distributed file system or NoSQL systems with database query processing
- No coordination is required between individual map and reduce jobs
- Sharding & replication fits nicely into Map-Reduce pattern
 - Parallelism is increased: Map tasks can be distributed to different shards or their replicas
 - Availability is increased: if a node is not available, replica can take over the job
- Mapping of input data is important
 - Key determines grouping
 - Data structure of value is output

MapReduce Execution



- Usually many more map tasks than machines
- For example:
 - 200K map tasks
 - 5K reduce tasks
 - 2K machines

- On worker failure
 - Detect failure via periodic heartbeats
 - Re-execute completed and in-progress map tasks
 - Re-execute in progress reduce tasks
 - Task completion committed through master
- Master failure
 - Is much more rare
 - Fail-over to secondary master nodes (e.g., name node, resource manager)

Map Reduce Limitations

- Many queries/computations need multiple MR jobs
- 2-stage computation too rigid
- Example: Find the top 10 most visited pages in each category

Visits

User	Url	Time
Amy	cnn.com	8:00
Amy	bbc.com	10:00
Amy	flickr.com	10:05
Fred	cnn.com	12:00

UrlInfo

Url	Category	PageRank
cnn.com	News	0.9
bbc.com	News	0.8
flickr.com	Photos	0.7
espn.com	Sports	0.9

Example:

Top 10 most visited pages in each category

Visits(User, Url, Time)

UrlInfo(Url, Category, PageRank)

MR Job 1: group
by url + count

UrlCount(Url, Count)

MR Job 2: join

UrlCategoryCount(Url, Category, Count)

MR Job 3: group by
category + count

TopTenUrlPerCategory(Url, Category, Count)

Common Operations
are coded manually:
join, selects,
projection,
aggregates, sorting,
distinct

Map Reduce is not a good model for data processing

- Required
 - Support for algebra operations: join, selection, projection, group by, ...
 - More abstract language to implement data transformations and queries
- ➔ High-level languages that are compiled into Map-Reduce jobs
 - ➔ Apache Pig (Pig Latin)
 - ➔ Apache Hive (HiveQL)



- High-level language for analyzing large data sets
- Apache project since 2007, mainly supported by Twitter and Hortonworks
- Pig Latin: Procedural language with algebra-like operations (join, selection, projection, ...)
- Workflows can be defined as step-by-step procedural scripts
- Pig Latin can be compiled to jobs on
 - Hadoop
 - Tez
 - Spark

Based on: Christopher Olston, Benjamin Reed, Utkarsh Srivastava, Ravi Kumar, Andrew Tomkins:
Pig latin: a not-so-foreign language for data processing. SIGMOD Conference 2008: 1099-1110

Pig Latin Example

```
visits          = load '/data/visits' as (user, url, time);
gVisits        = group visits by url;
urlCounts      = foreach gVisits generate url, count(visits);

urlInfo        = load '/data/urlInfo' as (url, category, pRank);
urlCategoryCount = join urlCounts by url, urlInfo by url;

gCategories    = group urlCategoryCount by category;
topUrls        = foreach gCategories generate top(urlCounts,10);

store topUrls into '/data/topUrls';
```

Pig Latin Example

```
visits = load '/data/visits' as (user, url, time);
```

```
gVisits = group visits by url;
```

```
urlCounts = foreach gVisits generate url, count(visits);
```

```
urlInfo = load '/data/urlInfo' as (url, category, pRank);
```

```
urlCategoryCount = join urlCounts by url, urlInfo by url;
```

```
gCategories = Operates directly over files category;
```

```
topUrls = foreach gCategories generate url, urlCategoryCount, 10);
```

```
store topUrls into '/data/topUrls';
```

Pig Latin Example

```
visits          = load '/data/visits' as (user, url, time);
gVisits        = group visits by url;
urlCounts = foreach gVisits generate url, count(visits);
```

```
urlInfo        = load '/data/urlInfo' as (url, category, pRank);
urlCategoryCount = join urlCounts by url, urlInfo by url;
```

```
gCategories    = group urlCategoryCount by category;
topUrls = foreach gCategories generate url, count(urlCounts,10);
```

```
store topUrls into '/data/topUrls';
```

Schemas optional;
Can be assigned dynamically
→ Schema-on-Read

Pig Latin Example

User-defined functions (UDFs)
can be used in every construct

- Load, Store
- Group, Filter, Foreach

```
visits
gVisits
urlCount = group visits by url, time;

urlInfo = group urlCount by url, category, pRank);
urlCategoryCount = join urlCounts by url, urlInfo by url;

gCategories = group urlCategoryCount by category;
topUrls = foreach gCategories generate top(urlCounts,10);

store topUrls into '/data/topUrls';
```

Pig Latin Example

```
visits = load '/data/visits' as (user, url, time);
```

```
gVisits = group visits by url;
```

MR Job 1

```
urlCounts = foreach gVisits generate url, count(visits);
```

```
urlInfo = load '/data/urlInfo' as (url, category, pRank);
```

```
urlCategoryCount = join urlCounts by url, urlInfo by
```

MR Job 2

```
gCategories = group urlCategoryCount by category
```

MR Job 3

```
topUrls = foreach gCategories generate top(urlCounts,10);
```

```
store topUrls into '/data/topUrls';
```


Execution of Pig Latin Example: Compiles also to Map-Reduce jobs

Visits(User, Url, Time)

UrlInfo(Url, Category, PageRank)

MR Job 1: group
by url + count

UrlCount(Url, Count)

MR Job 2: join

UrlCategoryCount(Url, Category, Count)

MR Job 3: group by
category + count

TopTenUrlPerCategory(Url, Category, Count)

```
visits = load
'/data/visits' as (user, url,
time);
gVisits = group visits by
url;
visitCounts = foreach gVisits
generate url, count(visits);
```

```
urlInfo = load
'/data/urlInfo' as (url,
category, pRank);
visitCounts = join
visitCounts by url, urlInfo by
url;
```

```
gCategories = group
visitCounts by category;
topUrls = foreach
gCategories generate
top(visitCounts,10);
```

```
store topUrls into
'/data/topUrls';
```



- Data warehouse software for large datasets in distributed storage
- Hive-QL: SQL-like declarative language
 - e.g., SELECT *, INSERT INTO, GROUP BY, SORT BY
- Compiles to
 - Hadoop
 - Tez
 - Spark

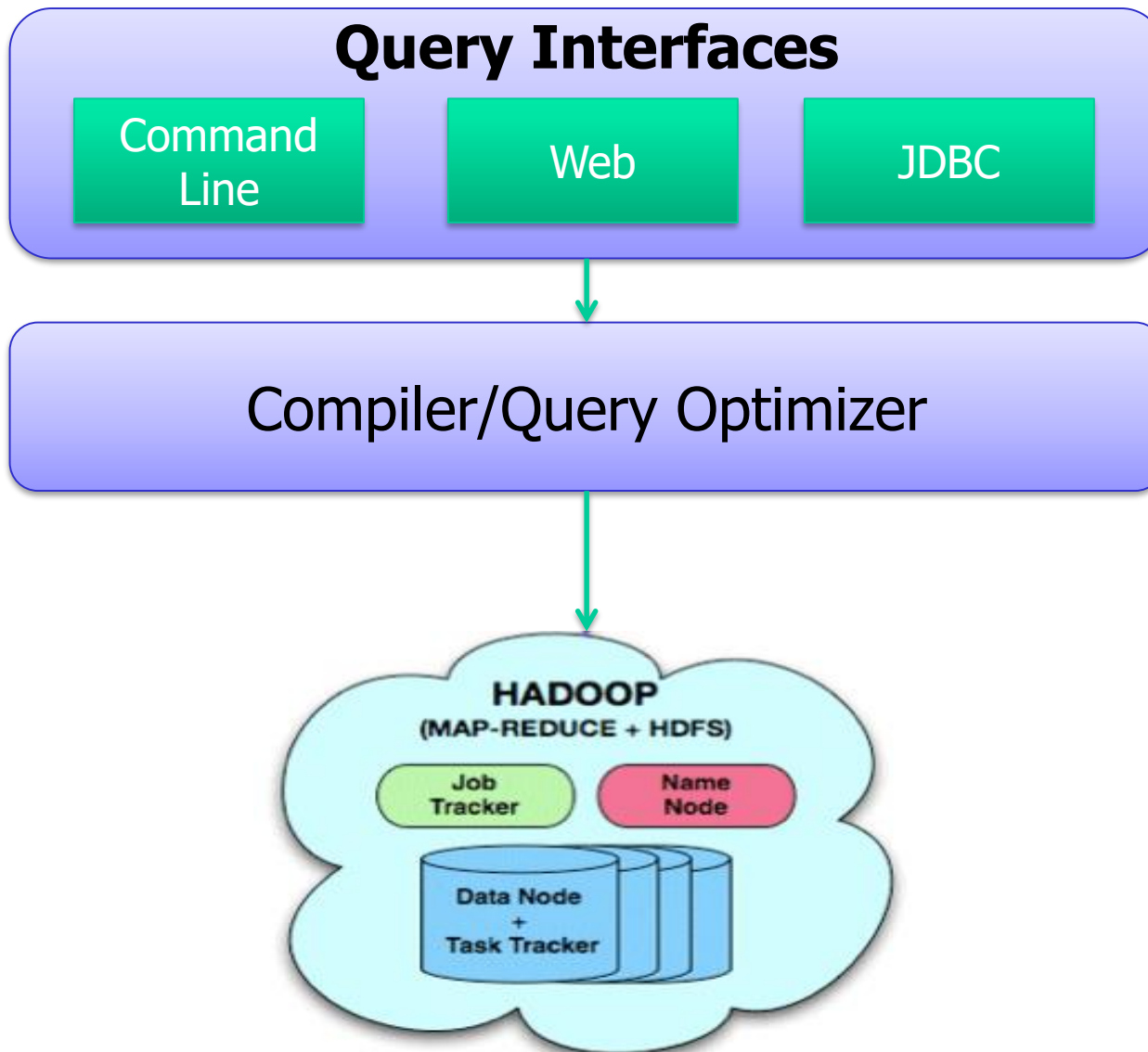
Based on: Ashish Thusoo, Joydeep Sen Sarma, Namit Jain, Zheng Shao, Prasad Chakka, Suresh Anthony, Hao Liu, Pete Wyckoff, Raghotham Murthy: Hive - A Warehousing Solution Over a Map-Reduce Framework. PVLDB 2(2): 1626-1629 (2009)

```
INSERT TABLE UrlCounts  
(SELECT url, count(*) AS count  
FROM Visits  
GROUP BY url)
```

```
INSERT TABLE UrlCategoryCount  
(SELECT url, count, category  
FROM UrlCounts JOIN UrlInfo ON (UrlCounts.url = UrlInfo  
.url))
```

```
SELECT category, topTen(*)  
FROM UrlCategoryCount  
GROUP BY category
```

Apache Hive Architecture



Hive Execution Example: Compiles also to Map-Reduce jobs

Visits(User, Url, Time)

UrlInfo(Url, Category, PageRank)

MR Job 1: group
by url + count

UrlCount(Url, Count)

```
INSERT TABLE UrlCounts
(SELECT url, count(*) AS count
FROM Visits
GROUP BY url)
```

MR Job 2: join

```
INSERT TABLE UrlCategoryCount
(SELECT url, count, category
FROM UrlCounts JOIN UrlInfo ON
(UrlCounts.url = UrlInfo.url))
```

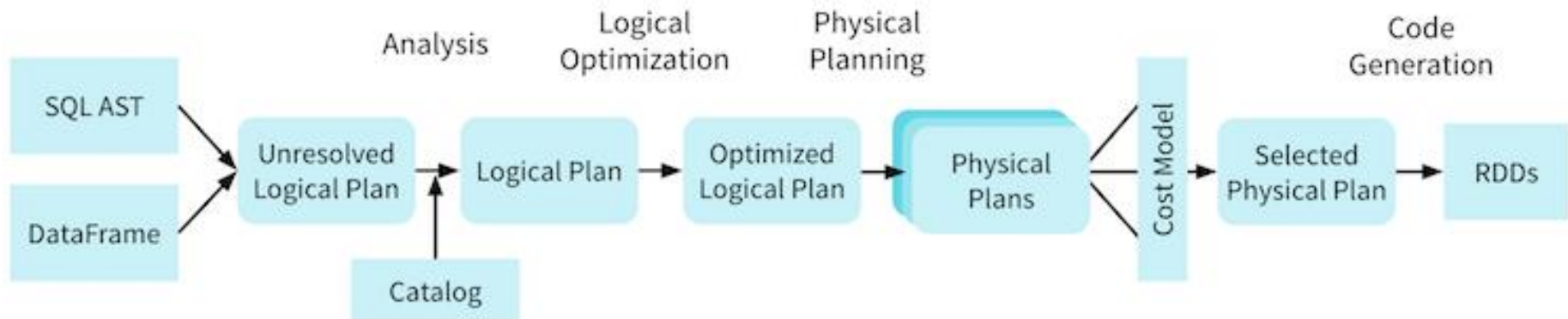
UrlCategoryCount(Url, Category, Count)

```
SELECT category, topTen(*)
FROM UrlCategoryCount
GROUP BY category
```

MR Job 3: group by
category + count

TopTenUrlPerCategory(Url, Category, Count)

- See also chapter 4.2.2
- Queries can be also specified in Spark SQL (SQL dialect of Apache Spark)
- DataFrames represent relational tables, implemented as RDDs
- Query processing are transformations & actions on RDDs/DataFrames



Apache Spark Example

```
var visits=spark.read.format („com.databricks.spark.csv“)
    .option („header“, “true“).load („visits.csv“)
var urlinfo=spark.read.format („com.databricks.spark.csv“)
    .option („header“, “true“).load („urlinfo.csv“)
```

```
visits.createOrReplaceTempView („visits“)
urlinfo.createOrReplaceTempView („urlinfo“)
```

Create tables for
SQL queries

```
val q=spark.sql („SELECT v.url, u.category, count (*)
    FROM visits v, urlinfo u
    WHERE v.url=u.url
    GROUP BY v.url, u.category“)
```

```
q.explain()
```

Show query plan

Filtering of top 10 URLs by
category has to be done
separately

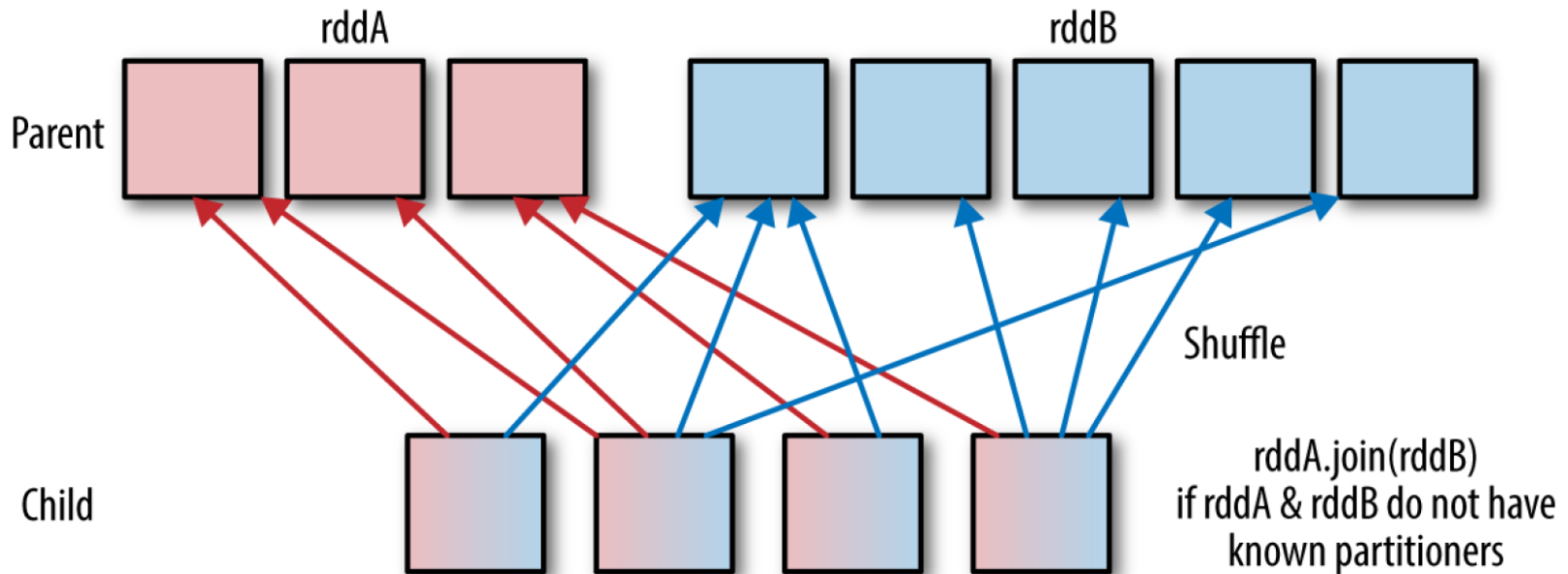
```
scala> q.explain()
== Physical Plan ==
*HashAggregate(keys=[url#13, category#40], functions=[count(1)])
+- Exchange hashpartitioning(url#13, category#40, 200)
   +- *HashAggregate(keys=[url#13, category#40], functions=[partial_count(1)])
      +- *Project [url#13, category#40]
         +- *BroadcastHashJoin [url#13], [url#39], Inner, BuildRight
            :- *Project [url#13]
               : +- *Filter isnotnull(url#13)
               :    +- *FileScan csv [url#13] Batched: false, Format: CSV, Location: InMemoryFileIndex
[file:/home/scala/visits.csv], PartitionFilters: [], PushedFilters: [IsNotNull(url)], ReadSchema: st
ruct<url:string>
            +- BroadcastExchange HashedRelationBroadcastMode(List(input[0, string, true]))
               +- *Project [url#39, category#40]
                  +- *Filter isnotnull(url#39)
                     +- *FileScan csv [url#39,category#40] Batched: false, Format: CSV, Location: In
MemoryFileIndex[file:/home/scala/urlinfo.csv], PartitionFilters: [], PushedFilters: [IsNotNull(url)]
, ReadSchema: struct<url:string,category:string>

scala> _
```

- Broadcast operations
 - ➔ Shuffle data between nodes in cluster

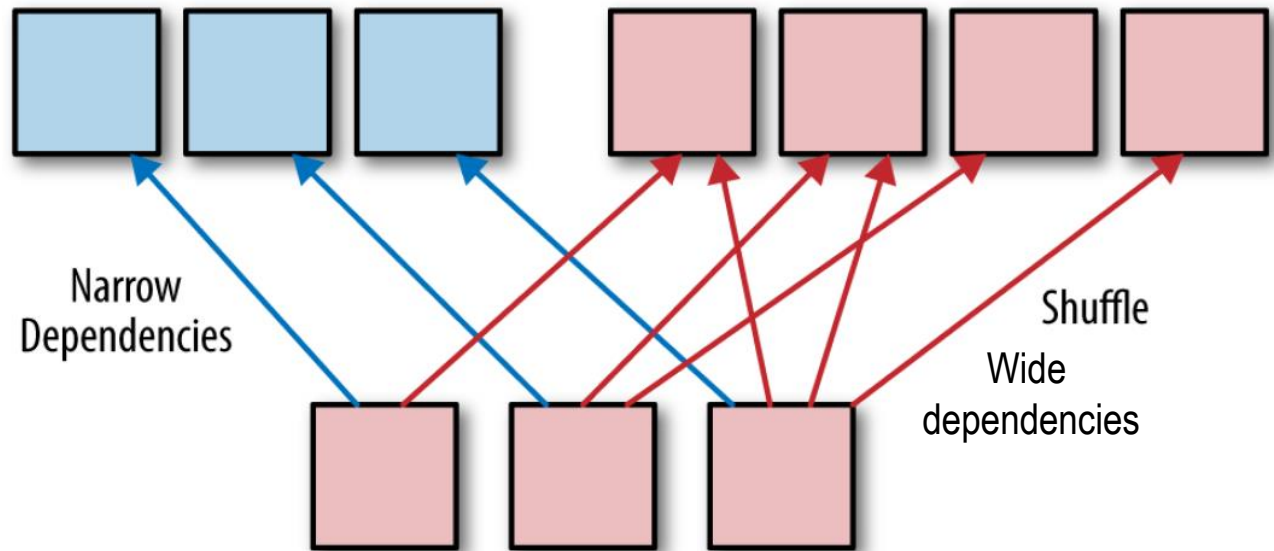
Default Join Method: Shuffle Join

- Remember: Partitioning method assigns a partition to a data object
 - Hash, range, or custom partitioners can be chosen in Spark
- If both RDDs use different custom partitioners (semantics is unknown for Spark), data has to be shuffled with a common partitioner



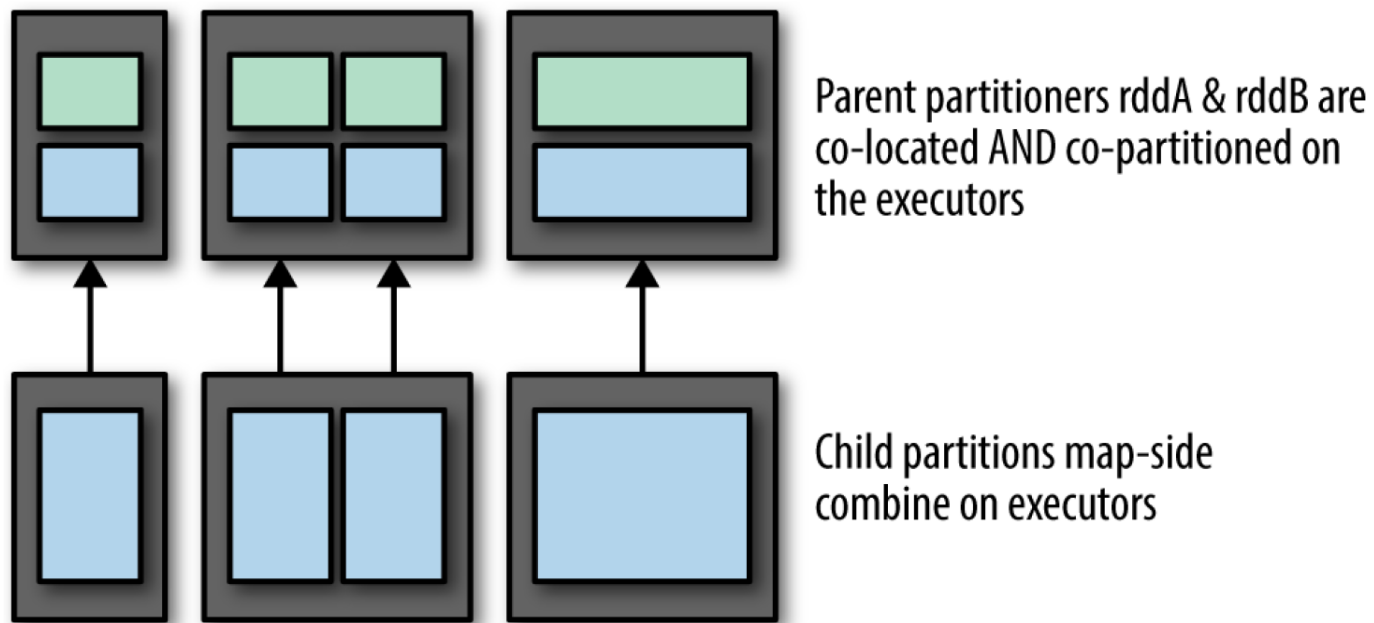
Join with Shuffle for only one RDD

- If RDD A has a known partitioner, RDD B does not, then only RDD B needs to be shuffled with the partitioner of RDD A
- Narrow dependencies: a partition depends only on one or two „parent“ partitions
- Wide dependencies: a partition depends on multiple parent partitions



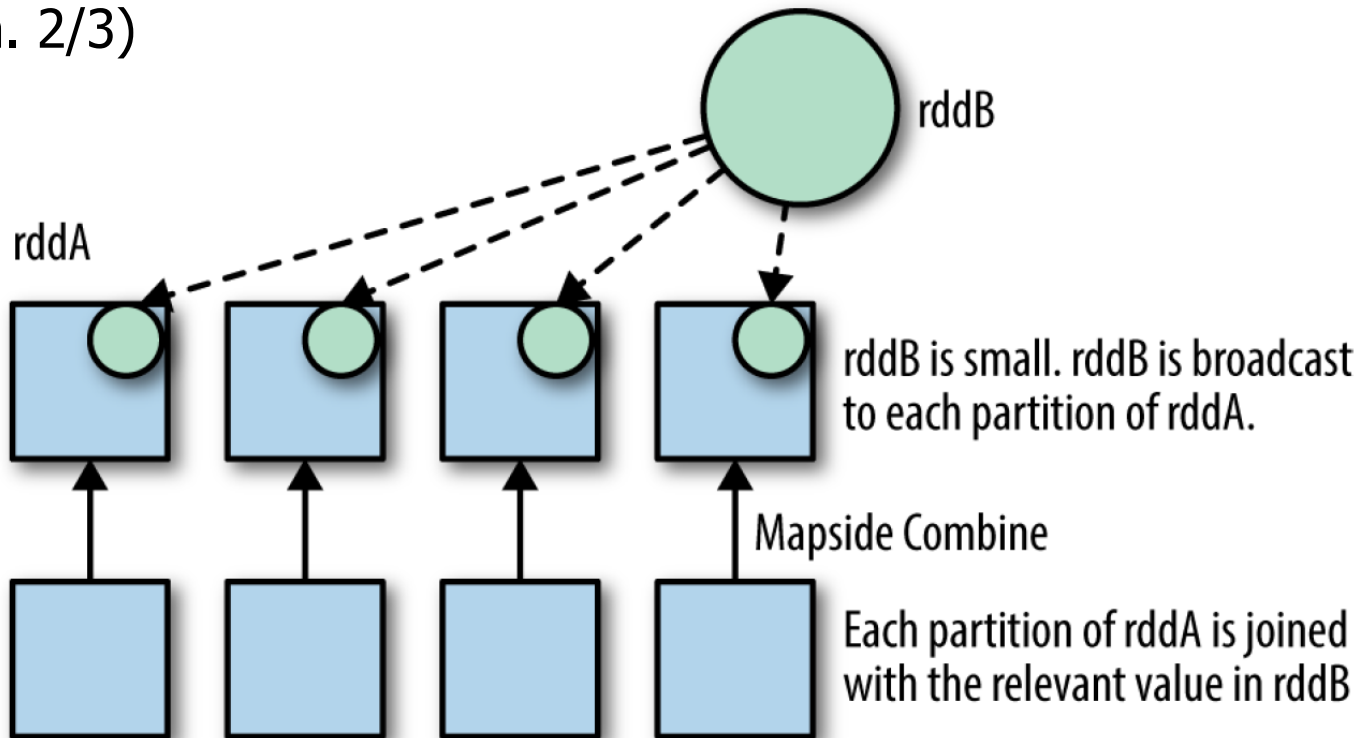
Co-located Join

- If both RDDs have the same partitioner, then the partitions to be joined are on the same node → join is executed on these nodes



Broadcast Hash Join

- No common partitioner for RDDs
- Smaller RDD is sent to each worker node
- In the best case, this RDD fits into memory
 - Retain only those columns of the RDD which are necessary for the join (like semi-join, index-only query, optimized nested loop join → Ch. 2/3)



Motivation (1)

- Some queries cannot be expressed in SQL or relational algebra
 - Give me a list of all parts that are required to build the component X.
 - Give me a list of all known ancestors of „John Doe“.
- Recursion is required to express such queries
- Datalog is a language that allows recursion
 - Note: SQL-99 also includes recursion, but it has not been adopted to all DB systems
- Deductive DBs and their languages are the foundation for database theory

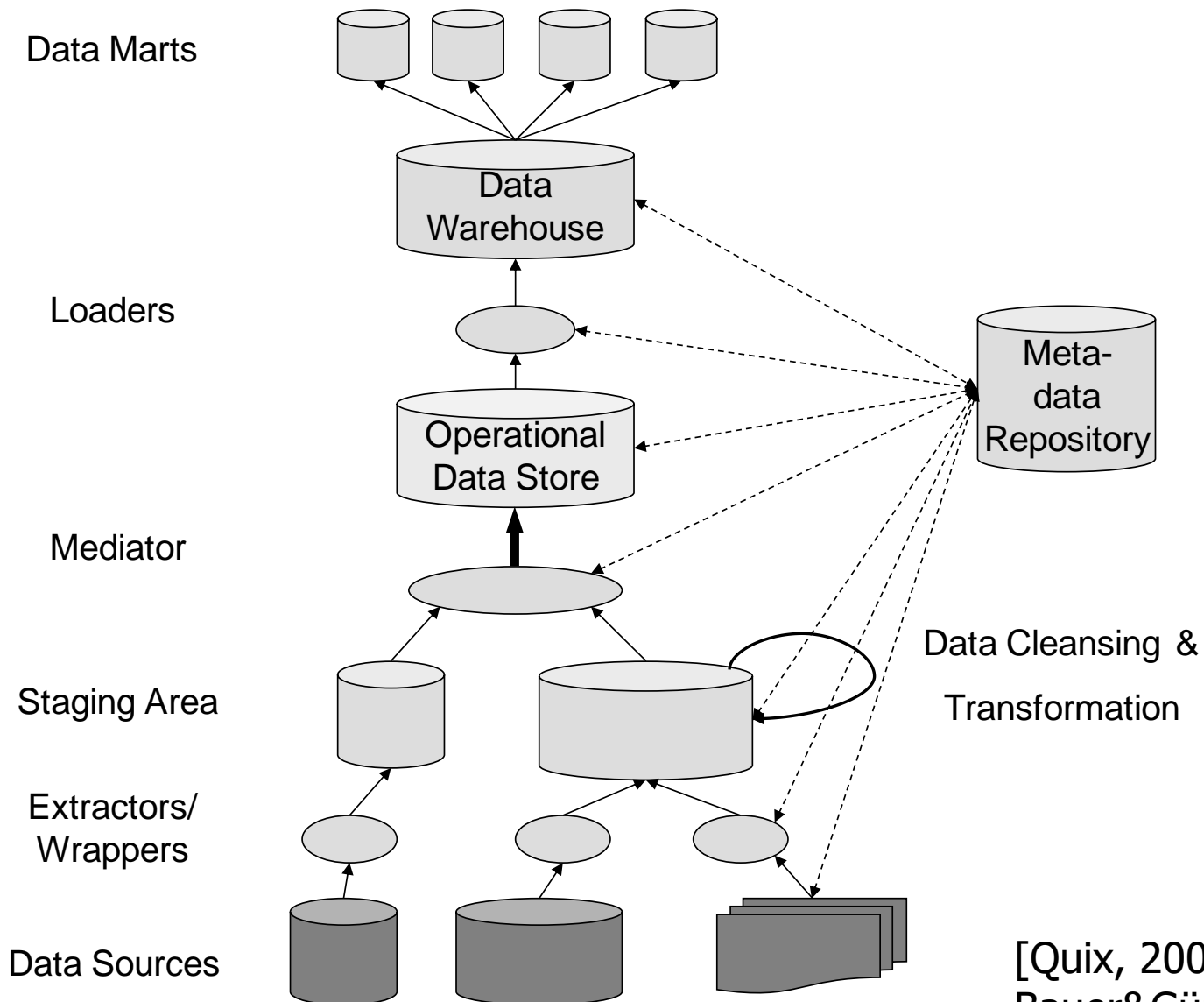
- Organizations use DWHs to analyze current and historical data to identify useful patterns and support business strategies
- Emphasis is on complex, interactive, exploratory analysis of very large datasets created by integrating data from across all parts of an enterprise; data is fairly static



Data Warehouses

- Historical data for Decision Support
- Long-running transactions
- **Huge** amount of data, integrated from various sources
- Focus on queries rather than updates
- Mappings between data sources and data warehouse can be expressed as logical rules

Data Warehouse Architecture



[Quix, 2003;
Bauer&Günzel, 2013]

Remember: Domain Relational Calculus

(see Chapter 2.1.4)

- Atomic formulas are $r(X_1, \dots, X_k)$ with r being a k -ary relation and X_1, \dots, X_k being variables or constants
- A database can be represented in the same way
 - A database is a set of *facts*
 - A *fact* is an atomic relation predicate only with constants representing one tuple of a relation, e.g.

empl(122, 'Miller', 'single', 35.000, 4)
 empl(101, 'Meyer', 'married', 55.000, 4)
 dept(4, 'computer', 101)
 office(2, 6232, 122)
 ...

DB Schema:

EMPL(eno, name, marstat, salary, dno)
 DEPT(dno, dname, mgr)

Integrity constraints:

EMPL[dno] \subseteq DEPT[dno]
 DEPT[mgr] \subseteq EMPL[eno]

- Rules: Horn clauses

$$p :- r_1 \wedge r_2 \wedge \dots \wedge r_k$$

where p and r_i are relation predicates. e.g.

$p(X,Y) :- r_1(X,Z) \wedge r_2(Z,Y)$
 $\text{manager}(\text{SSN},N) :- \text{empl}(\text{SSN},N,M,S,D) \wedge \text{dept}(D,DN,\text{SSN})$

Semantics: $p(X,Y)$ is true if there exist some X,Y,Z such that every r_i is true

- Queries

– Pure form with "?-", e.g.

$?- \text{empl}(\text{SSN},N,_,_,D) \wedge \text{dept}(D,\text{'computer'},_).$

– Usually, use of special query predicate, e.g.

$q(X,Y) :- r_1(X,Z) \wedge r_2(Z,Y)$

- Constraints

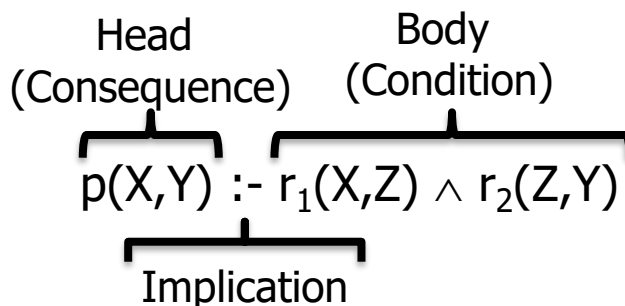
– Rules without head that must be always false, e.g.

$:- \text{empl}(S,N,M,\text{Salary},D) \wedge \text{Salary} < 10.000$

More expressive constraints than PKs and FKs are possible, similar to Assertions in SQL

- Syntactic conventions
 - Predicate names start with a lower case character
 - Variable names start with an upper case character
 - String atoms are enclosed in 'single quotes'

- Terminology



- *Distinguished variables*: appear in head and body, e.g. X and Y (\forall)
 - *Non-distinguished (existential) variables*: appear only in body, e.g. Z (\exists)
 - *Anonymous variable*: _
- Datalog vs. Prolog
 - Prolog allows function symbols as arguments of a predicate, Datalog does not



- Define rules for the Tax50 from chapter 3:

```
CREATE VIEW TAX50 AS SELECT e.* FROM EMPL e  
WHERE (e.marstat='single' AND e.salary<40.000)  
OR (e.marstat='married' AND e.salary<80.000);
```

- Constraint: an employee must not earn more than his/her manager

Model-theoretic approach

- Theory: schema (S) + integrity constraints (IC)
- Interpretation: database state
- Queries search through the interpretation
- Modifications must take the theory into consideration

Proof-theoretic approach

- Theory: Facts and deduction rules (T) + integrity constraints (IC)
- Queries are theories, which must be proved by using the axioms T.
- A modification adopts a new theory (e.g., T') and it should not violate the integrity constraints, i.e.

$$T' \models IC$$

Example

T: empl(12, 'jim', 50000, 2).
 empl(11, 'jones', 60000, 2).
 dept(2, 'R&D', 11).

works_dir_for(X,Y) :- empl(_,X,_,D), dept(D,_,M), empl(M,Y,_,_).

works_for(X,Y) :- works_dir_for(X,Y).
 works_for(X,Y) :- works_dir_for(X,Z), works_for(Z,Y).

same_manager(X,Y) :- works_for(X,M), works_for(Y,M), X<>Y.

IC: :- empl(X,_,S,_), S<10000 .
 :- empl(X,_,S,_), S>90000 .

Query: ? - works_for(X, jones).

DB Schema:

EMPL(eno, name, salary, dno)

DEPT(dno, dname, mgr)

Integrity constraints:

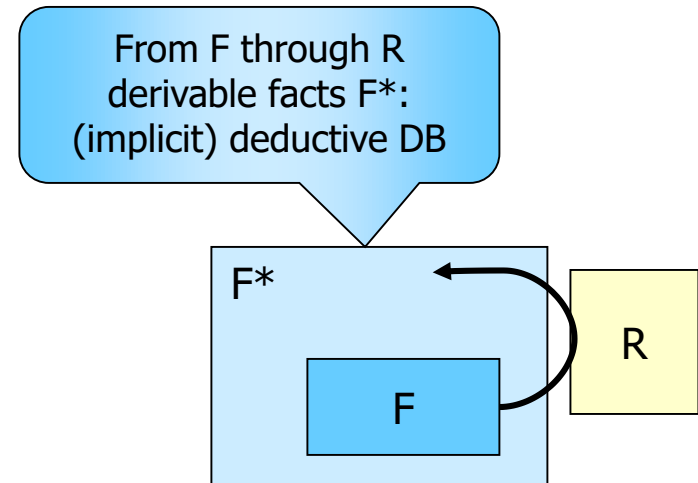
EMPL[dno] \subseteq DEPT[dno]

DEPT[mgr] \subseteq EMPL[eno]

Definition 5.1:

A *deductive database* consists of a set F of facts, a set R of deduction rules, a set IC of integrity constraints and the set F^* of all explicit and derived (implicit) facts.

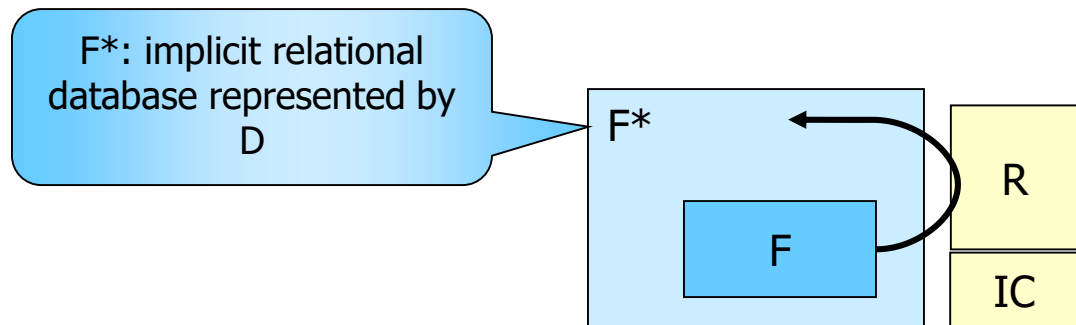
- EDB: extensional DB
 - Relations defined as a set of facts in F
 - Base relations
 - Set of facts
- IDB: intensional DB
 - Relations defined by rules in R
 - Derived relations



Datalog and its variations

- Datalog \neg : Negation is allowed
- NR-Datalog: Recursion is not allowed

Deductive database $D=(F, R, IC)$



Question:

- What is the formal definition of F^* ?
- Is F^* uniquely determinable?
- What is the meaning of "derivable"?

Problems are caused by negation and recursion, therefore the classes NR-DATALOG, $NR-DATALOG^-$ and $DATALOG^-$ have to be considered separately.

F^* is formally defined as the minimal *Herbrand model* of D .

Definition 5.2 (Herbrand Base of D):

All positive ground literals are constructable from predicates in D and constants in D .

Definition 5.3 (Herbrand Model of D):

A *Herbrand Model* is every subset M of the Herbrand Base of D , such that:

Every fact from F is contained in M . For every ground instance of a rule in D over constants in D , if M contains all literals in the body, then M contains the head as well.

A minimal model does not properly contain any other model.

Example: NR-DATALOG

F: $q(a,b)$ $t(b)$ R: $p(X) \leftarrow q(X,Y), t(Y)$
 $q(b,a)$

- The Herbrand base is

$q(a,a)$	$q(a,b)$	$p(a)$	$t(a)$
$q(b,a)$	$q(b,b)$	$p(b)$	$t(b)$

- The Herbrand models M_i are consequently

Minimal M_1 : $q(a,b)$ $t(b)$ and M_2 : $q(a,b)$ $t(b)$ $p(a)$
 $q(b,a)$ $p(a)$ $q(b,a)$ $p(b)$
 $q(b,b)$

- The ground instances of the rule are thus (blue = contained in M_i)

$p(a)$	\leftarrow	$q(a,a), t(a)$	and	$p(a)$	\leftarrow	$q(a,a), t(a)$
$p(a)$	\leftarrow	$q(a,b), t(b)$		$p(a)$	\leftarrow	$q(a,b), t(b)$
$p(b)$	\leftarrow	$q(b,a), t(a)$		$p(b)$	\leftarrow	$q(b,a), t(a)$
$p(b)$	\leftarrow	$q(b,b), t(b)$		$p(b)$	\leftarrow	$q(b,b), t(b)$

Least Fixpoint for NR-Datalog

F^* is created by the repeated (finite) application of the immediate consequence operator T_D (naive evaluation strategies) starting from F results in derivation of implicit facts from F :

$$T_D(T_D(\dots(T_D(F))\dots))$$

Definition 5.4:

For a subset S of a Herbrand Base the application of T_D to S is defined as:

$$T_D(S) := \{ H : (H \leftarrow B) \text{ is a ground instance of a rule such that } S \text{ contains all literals in } B \}$$

Start by F

Add $T_D(F_0)$

$$F_0 \cup T_D(F_0)$$

(= F_0)

Add $T_D(F_1)$

$$F_1 \cup T_D(F_1)$$

(= F_1)

(= F_2)



F^*

Operator correspond to this construction

$$T_D^*(S) = S \cup T_D(S)$$

Least fixpoint of this operator:
minimal solution is $X = T_D^*(X)$

Theorem 5.1: (v. Emden, Kowalski 1976)

The uniquely determined least fix point of T_D^* is the minimal Herbrand Model of D

Compute the least fixpoint!



$q(X) \text{ :- } r(X,Y), \text{ NOT } b(X).$

$c(1,2).$

$b(3).$

$r(X,Y) \text{ :- } c(X,Y), b(Y).$

$c(2,3).$

$b(4).$

$r(X,Y) \text{ :- } c(X,Z), r(Z,Y).$

$c(1,4).$

Problem: If negation occurs in the body of a rule, then there may be no unique minimal Herbrand model any more. Which one is the “natural model” of D, and thus represents the intended semantics of D?

Example:

F: $q(a,b)$ R: $p(X) \leftarrow q(X,Y), \text{ NOT } t(Y)$
 $q(b,a)$ $t(b)$

- The minimal Herbrand models are

$M_1: F \cup \{p(b)\}$
 $M_2: F \cup \{t(a)\}$

$p(b)$ is derivable from F, M_1 is the “natural” model of D

No reason why $t(a)$ should be true.

- Ground instances of the rules (in M_1 , in M_2 , in M_1 and M_2):

$p(a) \leftarrow q(a,a), \text{ NOT } t(a)$
 $p(a) \leftarrow q(a,b), \text{ NOT } t(b)$
 $p(b) \leftarrow q(b,a), \text{ NOT } t(a)$
 $p(b) \leftarrow q(b,b), \text{ NOT } t(b)$

- Main problem in presence of negation: characterization of the “natural” model of D (representing the intended semantics of D).

Example (NR-DATALOG[¬])

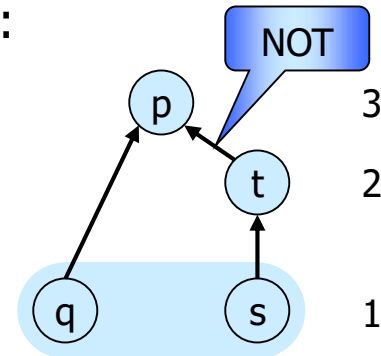
Least fixpoint characterization cannot be directly adopted

F: $q(a,b) \quad s(b)$
 $q(b,a)$

R: $p(X) \leftarrow q(X,Y), \text{ NOT } t(Y)$
 $t(Y) \leftarrow s(Y)$

- First application of T_D :
 - No t-fact in F \Rightarrow $p(a)$ and $p(b)$ are derivable
 - $s(b)$ in F \Rightarrow $t(b)$ is derivable
- Second application of T_D :
 - No new fact derivable \Rightarrow fixpoint reached
- It follows therefore:
 least fixpoint of T_D^* : $F \cup \{t(b), p(a), p(b)\} \neq$
 “natural” Herbrand model: $F \cup \{t(b), p(b)\}$
- Reason (intuitively): “ $t(b)$ arrives too late for preventing derivation of $p(a)$.”

Predicates “call” each other in a hierarchical order:



- ⇒ Predicates can be *layered* (or: *stratified*); no two predicates in a layer (*stratum*) depend negatively on each other. If a predicate p depends on a negative predicate r , then r is in a lower layer.
- If application of T_D is done layer by layer, the least fixpoint of D is consequently the *natural* Herbrand model.
- It follows therefore:
 1. layer: F
 2. layer: $F \cup \{t(b)\}$
 3. layer: $F \cup \{t(b)\} \cup \{p(b)\}$

Least Fixpoint for Recursive Stratified DATALOG⁻ Programs

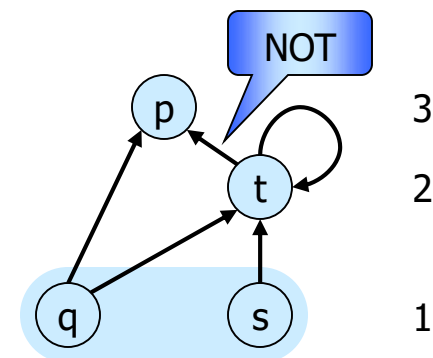
Problem: The recursion leads possibly to more than one application of T_D per layer. If negations do not occur in the recursion cycle, there will be no problem.

Example:

F:	$q(b,c)$	$s(c)$	R:	$p(X)$	$\leftarrow q(X,Y), \text{NOT } t(Y)$
	$q(b,a)$			$t(Y)$	$\leftarrow q(Y,Z), t(Z)$
				$t(Y)$	$\leftarrow s(Y)$

- From this it follows:
 1. layer: F
 2. layer: $F \cup \{t(c)\}$
 $F \cup \{t(c)\} \cup \{t(b)\}$
 3. layer: $F \cup \{t(c)\} \cup \{t(b)\} \cup \{p(b)\}$

.....



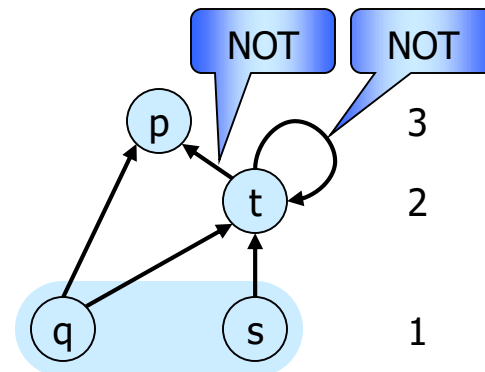
Problem: Negation in the recursion cycle violates the stratification condition.

Example:

F:	q(a,b)	s(c)	R:	p(X)	← q(X,Y), NOT t(Y)
	q(b,a)			t(Y)	← q(Y,Z), NOT t(Z)
				t(Y)	← s(Y)

- Even when applying T_D for t-rules only results in „anomalies“:

- t(a) is generated, as t(b) is initially missing
- t(b) is generated, as t(a) is initially missing



- Do t(a) and t(b) belong to the “natural” Herbrand model now? Is there any reasonable “natural” Herbrand model at all?

Example (cont.)

- $t(a)$ and $t(b)$ are not “natural” consequences of $R \cup F$:

$t(a) \quad \leftarrow q(a, Z), \text{ NOT } t(Z)$
 $\quad \quad \quad b \quad \quad \quad b$

$t(b) \quad \leftarrow q(b, Z), \text{ NOT } t(Z)$
 $\quad \quad \quad a \quad \quad \quad a$

- Consequently it results in two exclusive cases:

either $\text{NOT } t(b)$, consequently $t(a)$
 or $\text{NOT } t(a)$, consequently $t(b)$.

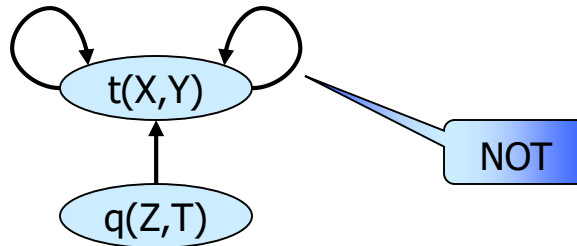
- So that it yields also two different models:

$F \cup \{p(a), t(a)\} \quad , \text{ also NOT } t(b)$
 or $F \cup \{p(b), t(b)\} \quad , \text{ also NOT } t(a)$.

Example DATALOG⁻ [cont.]:

F:	q(a,b) q(b,c)	R:	t(X,Y) \leftarrow q(X,Y), NOT t(Y,X) t(X,Y) \leftarrow t(X,Z), t(Z,Y), NOT t(Y,X)
----	------------------	----	--

R is not stratified, but "locally stratified":



"Reachable" instances of R:

t(a,b)	\leftarrow q(a,b), NOT t(b,a)
t(b,c)	\leftarrow q(b,c), NOT t(c,b)
t(a,c)	\leftarrow t(a,b), t(b,c), NOT t(c,a)

- No recursion cycle involves negation among "reachable" instances.
- Test for local stratification expensive, but can be computed "on the fly", i.e., during evaluation of the rules without computing the (local) stratification [Bry, 1989]

Are these programs stratified?



Program 1

$q(X) \quad :- \text{ NOT } p(X), t(X).$
 $p(X) \quad :- s(X,X), \text{ NOT } r(X).$
 $s(X,Y) \quad :- s(Y,X), t(Y).$
 $r(X) \quad :- t(X), \text{ NOT } s(X,X).$

Program 2

$p(X) \quad :- q(X,Y), \text{ NOT } t(Y).$
 $t(Y) \quad :- q(Y,Z), \text{ NOT } t(Z).$
 $t(Y) \quad :- s(Y).$

- **Bottom-Up (Forward Chaining):**

- Generation of implicit facts at evaluation-time
- Evaluation of the query against temporarily materialized implicit databases.
(direct implementation of least fixpoint computation)
- **Drawback:** when materializing F^* , the particular query Q is not considered \rightarrow many irrelevant answers and intermediate results may be generated.

- **Top-Down (Backward Evaluation):**

- Generation of subqueries until queries to base relations are reached
- Evaluation of base subqueries against F and upward propagation of answers to the top query
- As opposed to bottom-up approach:
constants in top query and subqueries are passed downwards and provide restrictions while evaluating base queries.
- **Drawback:** Inefficient (or not terminating) for recursive queries

Example: Top-Down Evaluation

F: $q(a,b)$ $q(a,c)$ $t(d)$ R: $p(X,Y) \leftarrow q(X,Z), r(Z,Y)$
 $q(b,c)$ $q(b,d)$ $r(Z,Y) \leftarrow q(Z,Y), \text{NOT } t(Y)$
 $q(c,a)$

Q: $p(a,Y)$

Match query with head of 1st rule and generate subqueries for body:

→ $q(a,Z), r(Z,Y)$

$q(a,Z)$ can be proven with facts from F, e.g., take $q(a,c)$

→ $q(a,c), r(c,Y)$

prove $r(c,Y)$ by using second rule

→ $q(c,Y), \text{NOT } t(Y)$

$q(c,Y)$ can be proven by $q(c,a)$ in F

→ $q(c,a), \text{NOT } t(a)$

NOT $t(a)$ can be also proven by F, thus, $r(c,a)$ and $p(a,c)$ are true

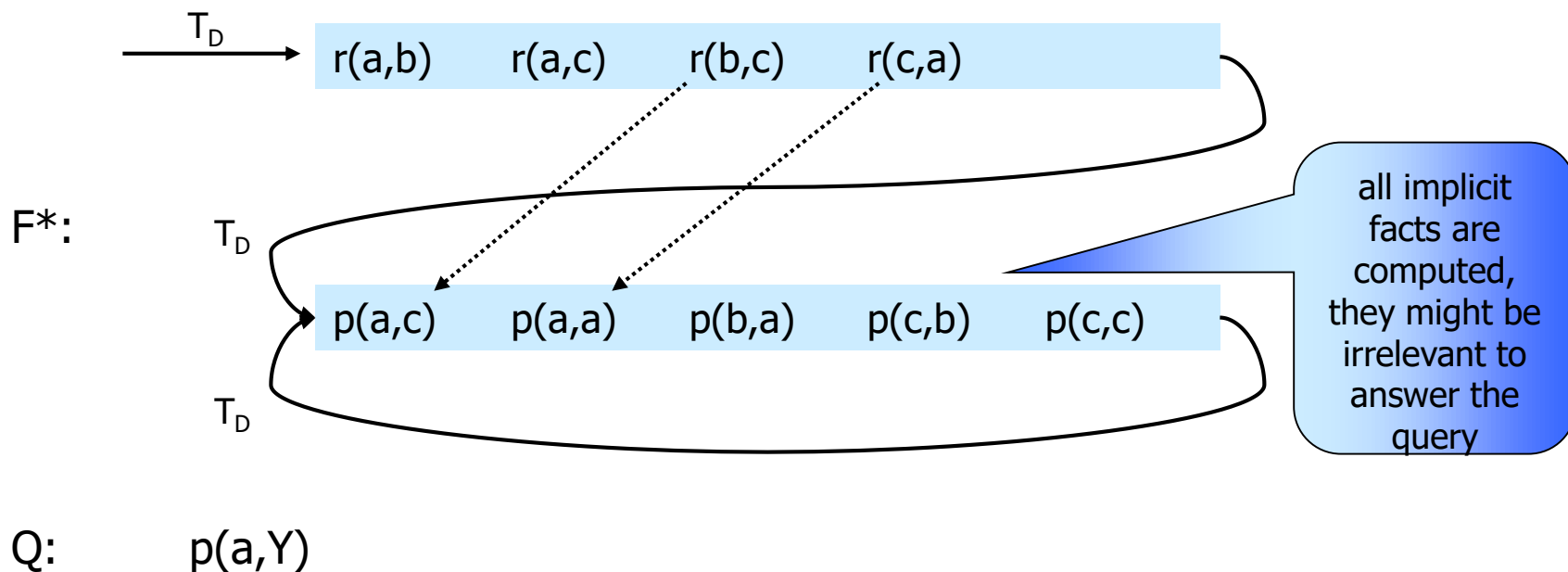
→ derivation of one result finished: $p(a,c)$

→ backtrack to choice point and generate next result (if required)

Choice
Point

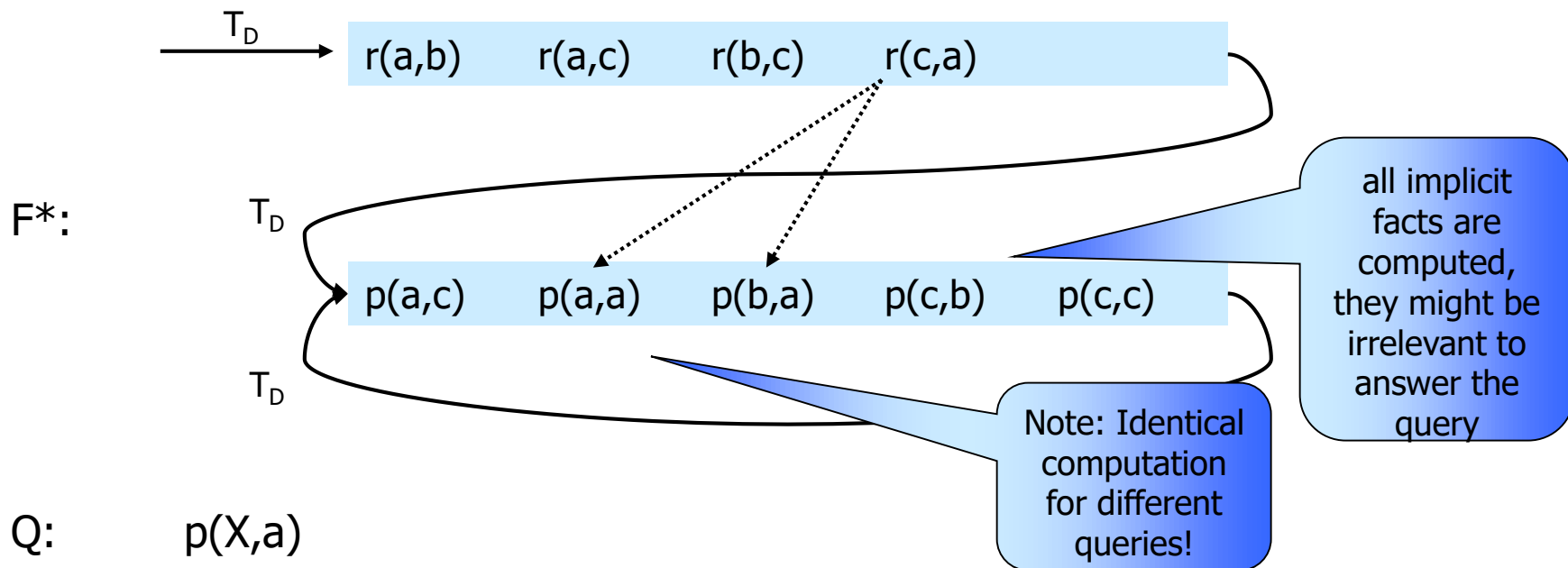
Example: Bottom-Up Evaluation

F: $q(a,b)$ $q(a,c)$ $t(d)$ R: $p(X,Y) \leftarrow q(X,Z), r(Z,Y)$
 $q(b,c)$ $q(b,d)$ $r(Z,Y) \leftarrow q(Z,Y), \text{NOT } t(Y)$
 $q(c,a)$



Example: Bottom-Up Evaluation

F: $q(a,b)$ $q(a,c)$ $t(d)$ R: $p(X,Y) \leftarrow q(X,Z), r(Z,Y)$
 $q(b,c)$ $q(b,d)$ $r(Z,Y) \leftarrow q(Z,Y), \text{NOT } t(Y)$
 $q(c,a)$



Definition 5.5:

Integrity constraints (IC) are conditions that have to be satisfied by a database at any point in time (expressing general laws which cannot be used as derivation rules) .

Definition 5.6:

Integrity-checking tests, whether a particular update is going to violate any constraint.

- **Main problem for IC-tests:**
Full evaluation of all ICs before every update would be very expensive and would decrease update performance significantly.
- **Solution:**
Determine a reduced set of **simplified ICs** for which the checking guarantees satisfaction of **all ICs**.
- This approach leads to a **specialization of constraints**.

- Integrity constraints expressed as **Datalog**[¬] rules for a meta predicate "inconsistent".
- Updates are either **atomic** insertions / deletions of facts or **general** updates (depending on a condition, which is a Datalog query to be evaluated before the update).

Example:

inconsistent \leftarrow employee(X), works_for(X,X)
 (original constraint: no employee works for himself)

insert	works_for(john, jim)
delete	employee(X) where works_for(X, john)

Input:

- Update $U = \{\text{delete } L, \text{insert } L\}$
 - Integrity constraints IC (satisfied before the update)
1. IC is affected by U , if IC contains a literal L^* that is unifiable with L (resp. $\text{NOT } L$), if U is an insertion (resp. deletion).
 2. For every such L^* , IC_σ is a relevant instance of IC with respect to U . (where σ is a most-general-unifier of L and L^*)
 3. Simplified relevant instances of IC with respect to U are obtained by deleting L^* from relevant instances.

So far, generalized updates, derivation rules and negations have not been taken into account yet.

Example: Constraint Specialization

IC: inconsistent $\leftarrow p(X,Y), \text{ NOT } s(X)$ (corresponding: $\text{FORALL } X,Y: p(X,Y) \Rightarrow s(X)$)

- insert $p(a,b)$
inconsistent $\leftarrow p(a,b), \text{ NOT } s(a)$

IC affected!
- delete $p(a,b)$
- insert $s(a)$
- delete $s(a)$
inconsistent $\leftarrow p(a,Y), \text{ NOT } s(a)$

IC affected!

Example:

IC: inconsistent $\leftarrow p(X,Y), \text{ NOT } s(X)$

- Insert $p(X,b)$ where $r(X)$
1. IC is affected by U, if IC contains a literal L^* that is unifiable with L (resp. NOT L), if U is an insertion (resp. deletion).
 2. For every such L^* IC_{σ} is a relevant instance of IC regarding U.
 3. Simplified relevant instances of IC regarding U are obtained by deleting L^* from relevant instances.

Instead of a simplified relevant instance, we end up with a specialized constraint:

inconsistent $\leftarrow r(X), \text{ NOT } s(X)$

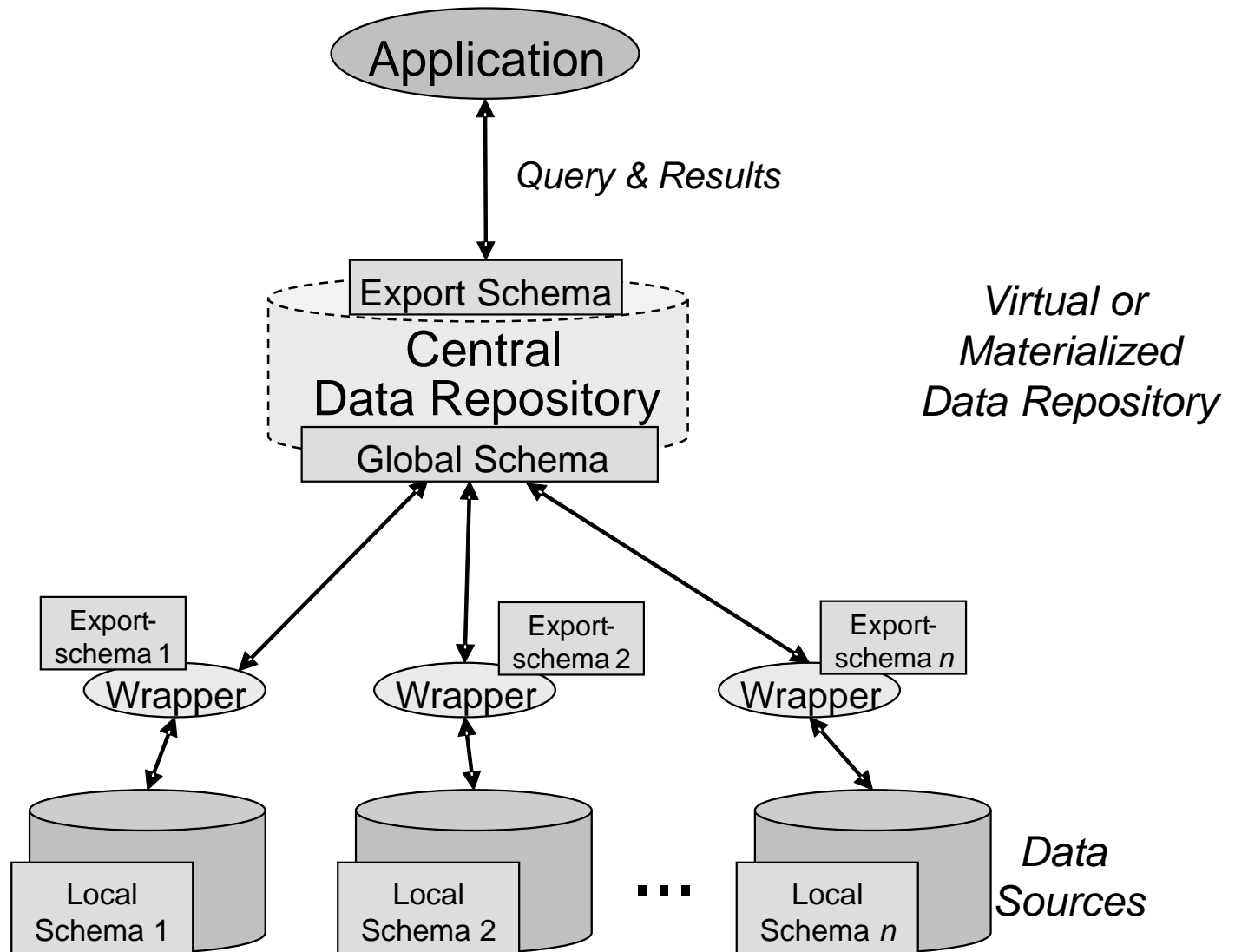
Definition 5.7:

Data integration is the problem of providing unified and transparent access to a collection of data stored in multiple, autonomous, and heterogeneous data sources

Motivations for data integration

- Company mergers
- Reorganization of companies
- Restructuring of databases in an organization
- Combination of data from several internal and external sources for data analysis (e.g. data warehousing, OLAP)

General Integration Architecture



[Quix, 2003]

- Distributed databases
 - Data sources are homogeneous DBs under central control
- Multidatabase or federated databases
 - Data sources are autonomous, heterogeneous databases
- **(Mediator-based) Data Integration**
 - Access through a global schema mapped to autonomous and heterogeneous data sources
- Data Exchange
 - Mapping between a source and a target system
 - source may specify data in target only partially
- Peer-to-peer data integration:
 - Network of autonomous systems mapped one to each other, without a global schema

- Modeling of the global schema, the sources, and **the mappings between the two**
 - Construction of the global schema
 - Discovering mappings between sources and global schema
- Legacy databases: DBs are used for many applications, structure cannot be changed.
- Heterogeneity & Conflicts
 - Data Types & Structures
 - Semantics: Meaning of terms on schema- and instance-level
- **Answering queries expressed on the global schema**
- Data extraction, cleaning, and reconciliation
- Processing of updates expressed on the global schema and/or the sources ("read/write" vs. "read-only" data integration)
- Optimization of queries across data sources

Querying Problem

- A query expressed in terms of the global schema must be reformulated in terms of (a set of) queries over the sources and/or materialized views
- The computed sub-queries are shipped to the sources, and the results are collected and assembled into the final answer
- The computed query plan should guarantee:
 - completeness of the obtained answers wrt the semantics
 - efficiency of the whole query answering process
 - efficiency in accessing sources

How to specify the mapping between the data sources and the global schema?

- **LAV (local-as-view, source-centric):**
The sources are defined in terms of the global schema (i.e. as view on the global schema)
- **GAV (global-as-view, global-schema-centric):**
The global schema is defined in terms of the sources (i.e. as view on the source schemas)
- **GLAV (combination of GAV and LAV)**

Example

- Source Schema S
 - em50(Title, Year, Director)
European movies since 1950
 - rv10(Movie, Review)
reviews since 2000
- Global Schema G
 - movie(Title, Director, Year)
 - ed(Name, Country, Dob) (*European directors*)
 - rv(Movie, Review)
- Query q

```
SELECT M.title, R.review
FROM Movie M, RV R
WHERE M.title=R.title AND M.year = 2000
```



Questions

- Can we rewrite q as a query over the source schema S ?
- Is there a unique solution?
- If not, can we characterize a best solution?
- What is the semantics of a query?
- And how do we specify the mapping between S and G ?



Problem: Expressivity

- In order to answer such questions, we have to prove that queries are equivalent or contained in each other
 - Query Equivalence
 - q and q' are equivalent if they produce the same result for all legal databases
 - Query Containment
 - q is contained in q' if the result of q is a subset of the result for q' for all legal databases
- Undecidable for many query languages
- Restriction to conjunctive queries
 - ➔ Tableau Method

- $\text{movie}(\text{Title}, \text{Year}, \text{Director}) :-$
 $\text{em50}(\text{Title}, \text{Year}, \text{Director}).$
- $\text{ed}(\text{Name}) :-$
 $\text{em50}(_, _, \text{Name}).$
- $\text{rv}(\text{Movie}, \text{Review}) :-$
 $\text{rv10}(\text{Movie}, \text{Review}).$



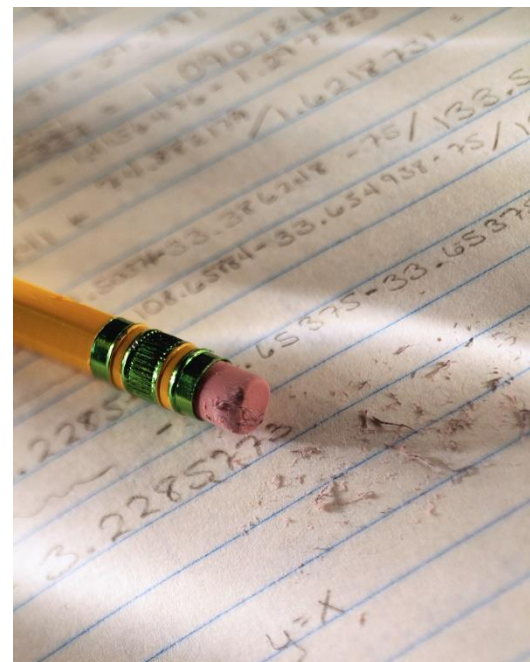
Query Rewriting in GAV

Queries over G can be rewritten as queries over S by unfolding

$q(\text{Title}, \text{Review}) :-$
 $\text{movie}(\text{Title}, 2000, _),$
 $\text{rv}(\text{Title}, \text{Review}).$



$q'(\text{Title}, \text{Review}) :-$
 $\text{em50}(\text{Title}, 2000, _),$
 $\text{rv10}(\text{Title}, \text{Review}).$



LAV Example

- `em50(Title,Year,Director) :-`
`movie(Title,Year,Director),`
`ed(Director,Country,Dob),`
`Year ≥ 1950.`
- `rv10(Movie,Review) :-`
`rv(Movie,Review),`
`movie(Movie,Year,Director),`
`Year ≥ 2000.`

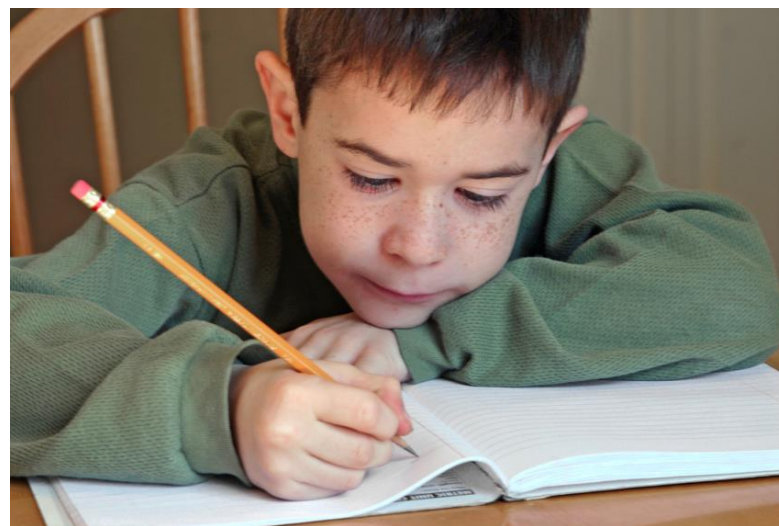


Query Rewriting in LAV

- Sources are views
- Answer queries on the basis of available data in the views
- Research area: Answering queries using views

→ **Query Optimization:** Answer a query using a materialized view!

- **Idea:** Try to cover the predicates of the query by predicates in the bodies of the source views



Query Rewriting in LAV Example

- $q(\text{Title}, \text{Review}) :-$
 $\text{movie}(\text{Title}, \text{Year}, _),$
 $\text{rv}(\text{Title}, \text{Review}),$
 $\text{Year} = 2000.$
- $\text{em50}(\text{Title}, \text{Year}, \text{Director}) :-$
 $\text{movie}(\text{Title}, \text{Year}, \text{Director}),$
 $\text{ed}(\text{Director}, \text{Country}, \text{Dob}),$
 $\text{Year} \geq 1950.$
- $\text{rv10}(\text{Movie}, \text{Review}) :-$
 $\text{rv}(\text{Movie}, \text{Review}),$
 $\text{movie}(\text{Movie}, \text{Year}, \text{Director}),$
 $\text{Year} \geq 2000.$



- Query Processing in Big Data
 - Data partitions & replications enable parallel, distributed, fault-tolerant query processing
 - Map-Reduce is a generic programming pattern for distributed computation, but often too rigid for complex data analysis
 - High-Level languages enable declarative query processing in distributed systems
- Deductive databases are the logical basis for relational databases
 - Herbrand model corresponds to least fixpoint of T_D
 - Negation and recursion require stratified computation of fixpoints
 - Integrity constraints are a special form of rules
- Application in Information Integration
 - Mappings between data sources and integrated schema can be represented as logical rules
 - Queries to integrated schema have to be rewritten into queries for data sources
 - Mappings can be specified as LAV or GAV mappings

Review Questions

- Explain the Map-Reduce programming pattern? What is done in the Map function, what is done in Reduce?
- What are the problems of the Map-Reduce programming pattern?
- What is the goal of systems like Pig Latin or Hive?
- What is a broadcast hash join in Spark?
- When do you need to do shuffling in Spark? What are narrow and wide dependencies?
- Sketch and explain the data warehouse architecture!
- What is the Herbrand Base and the Herbrand Model?
- How can you compute the minimal Herbrand Model?
- Translate a RA query into Datalog and vice versa!
- What is stratification?
- Explain top-down and bottom-up evaluation of Datalog programs!
- Show an example for a mapping between a source schema and an integrated schema using the Datalog notation.
- What is the difference of GAV and LAV mappings?

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