

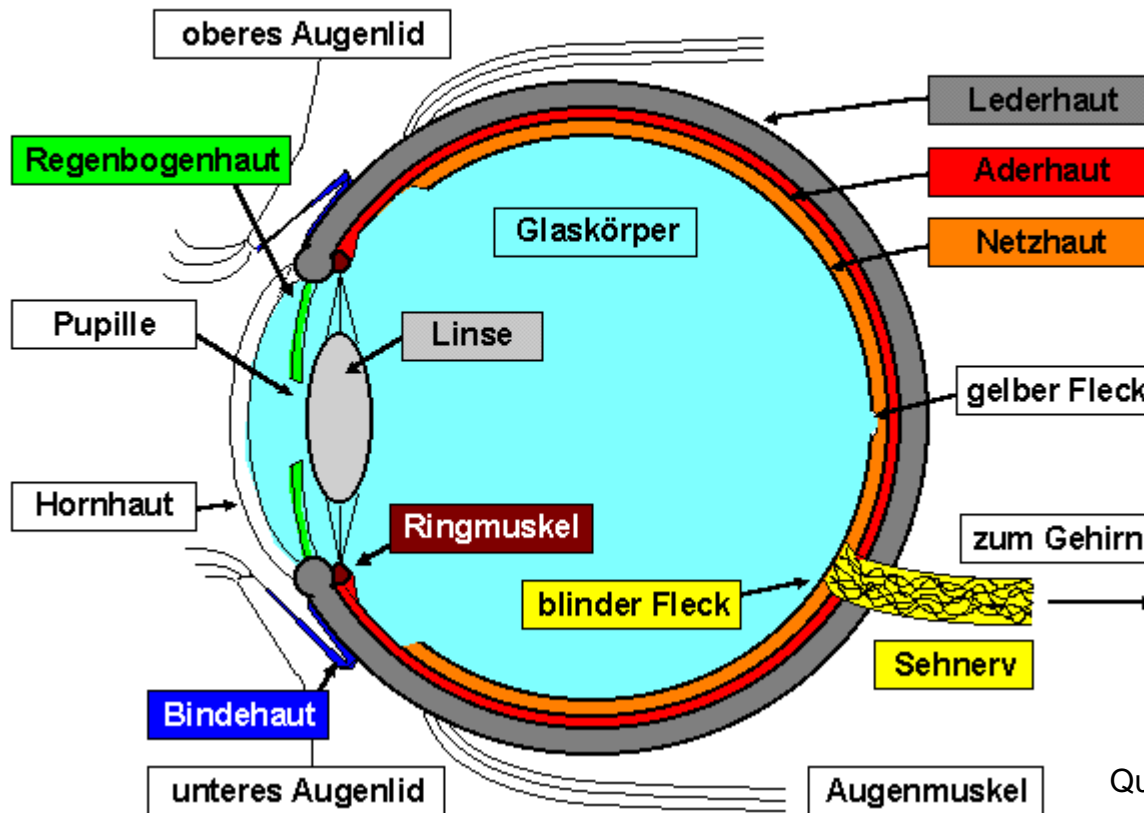
# Course on Virtual Reality

## 3-D Vision

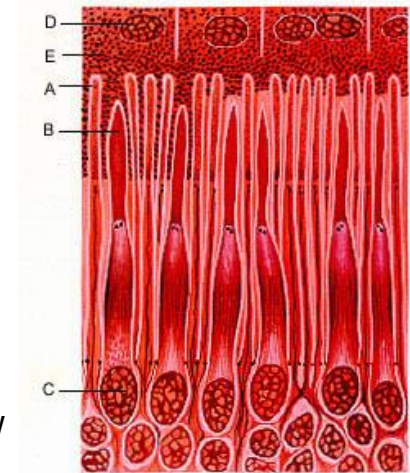
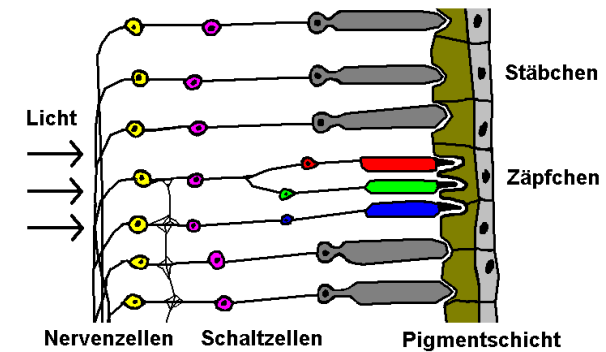
# Exact correspondence of visual perception in the real world and in the virtual world

# The Human Eye

## Das Auge



## Bau der Netzhaut



Quelle: WWW

# Physiological & Psychological Clues

## Traditional CG:

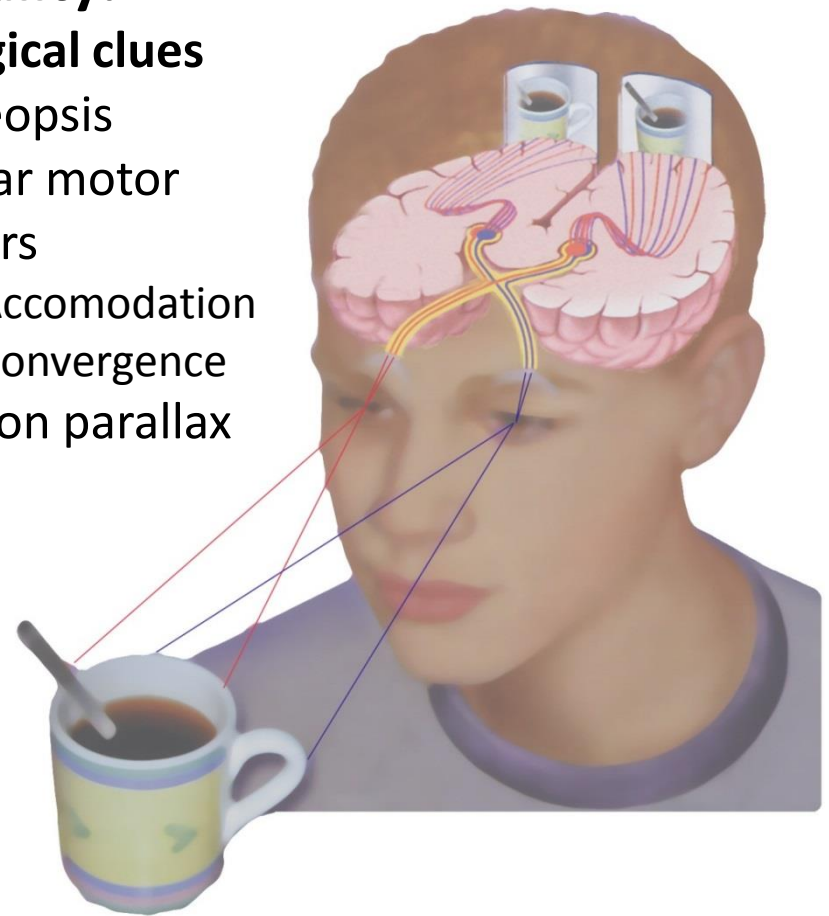
- **Psychological clues**

- Perspective shortening
- Occlusion of objects
- Light and shadows
- Texture gradients
- Atmospheric perspective

## Virtual Reality:

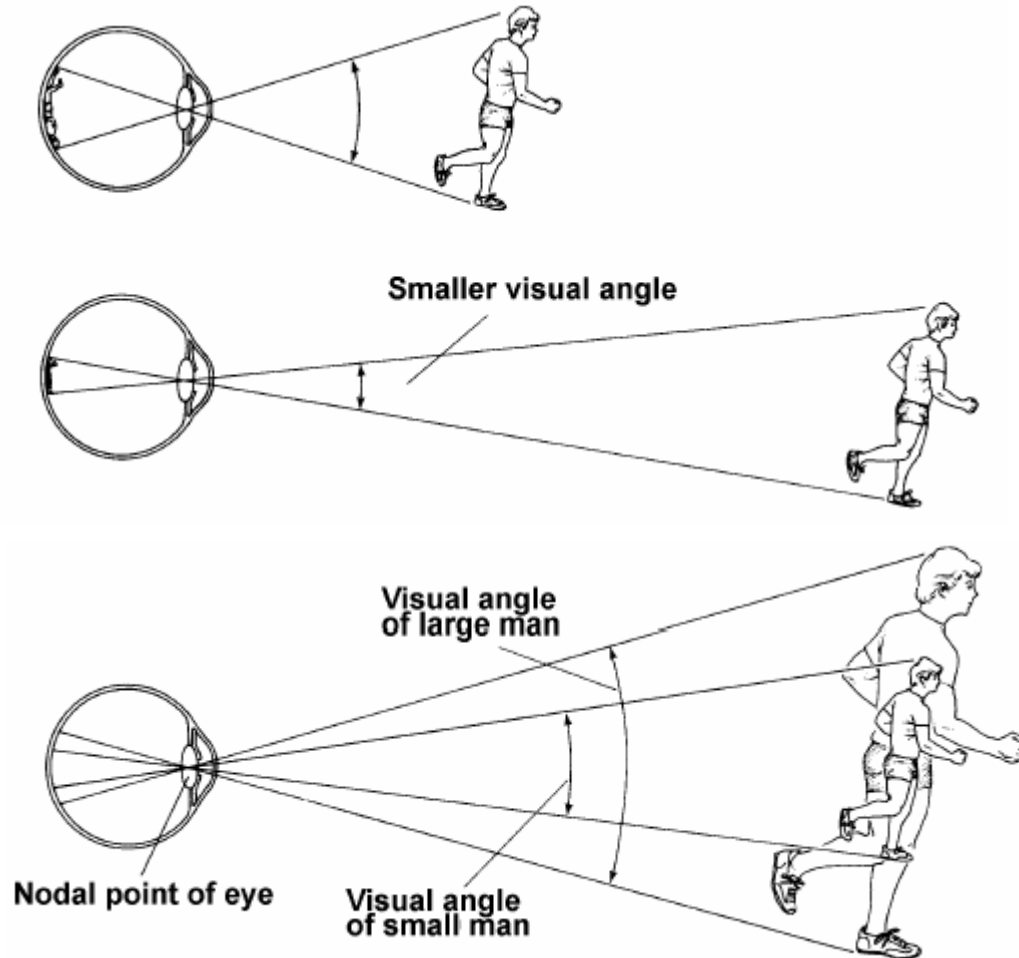
- **Physiological clues**

- Stereopsis
- Ocular motor factors
  - Accommodation
  - Convergence
- Motion parallax



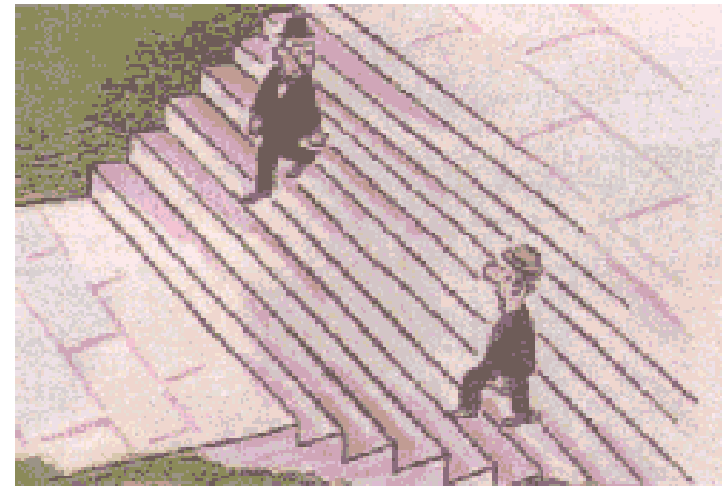
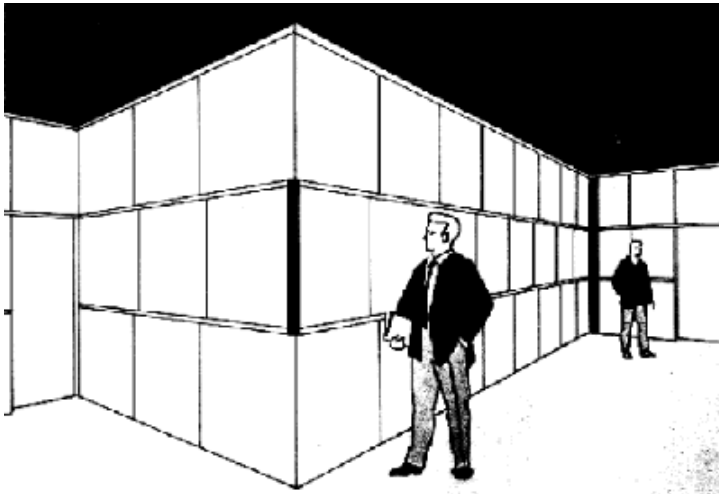
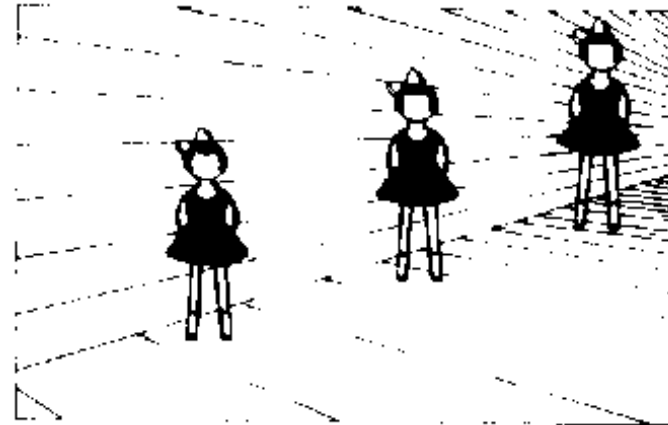
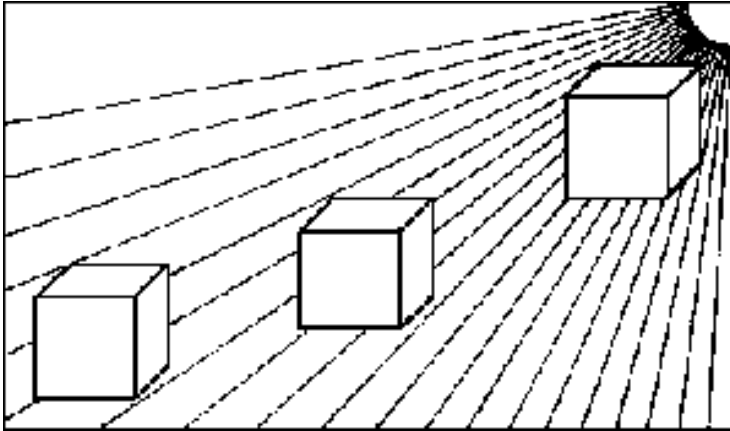
# Perspective

Drawing: Goldstein (WWW)



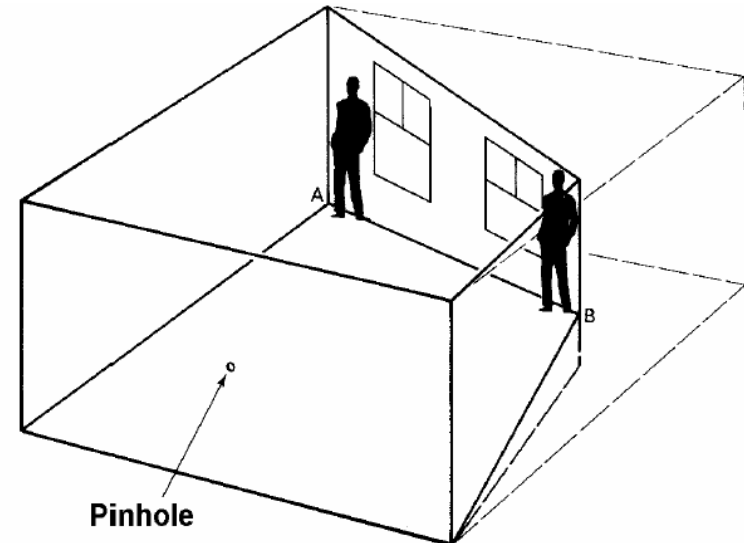
# Optical Illusion based on Perspective

Drawing: Anonymous (WWW)



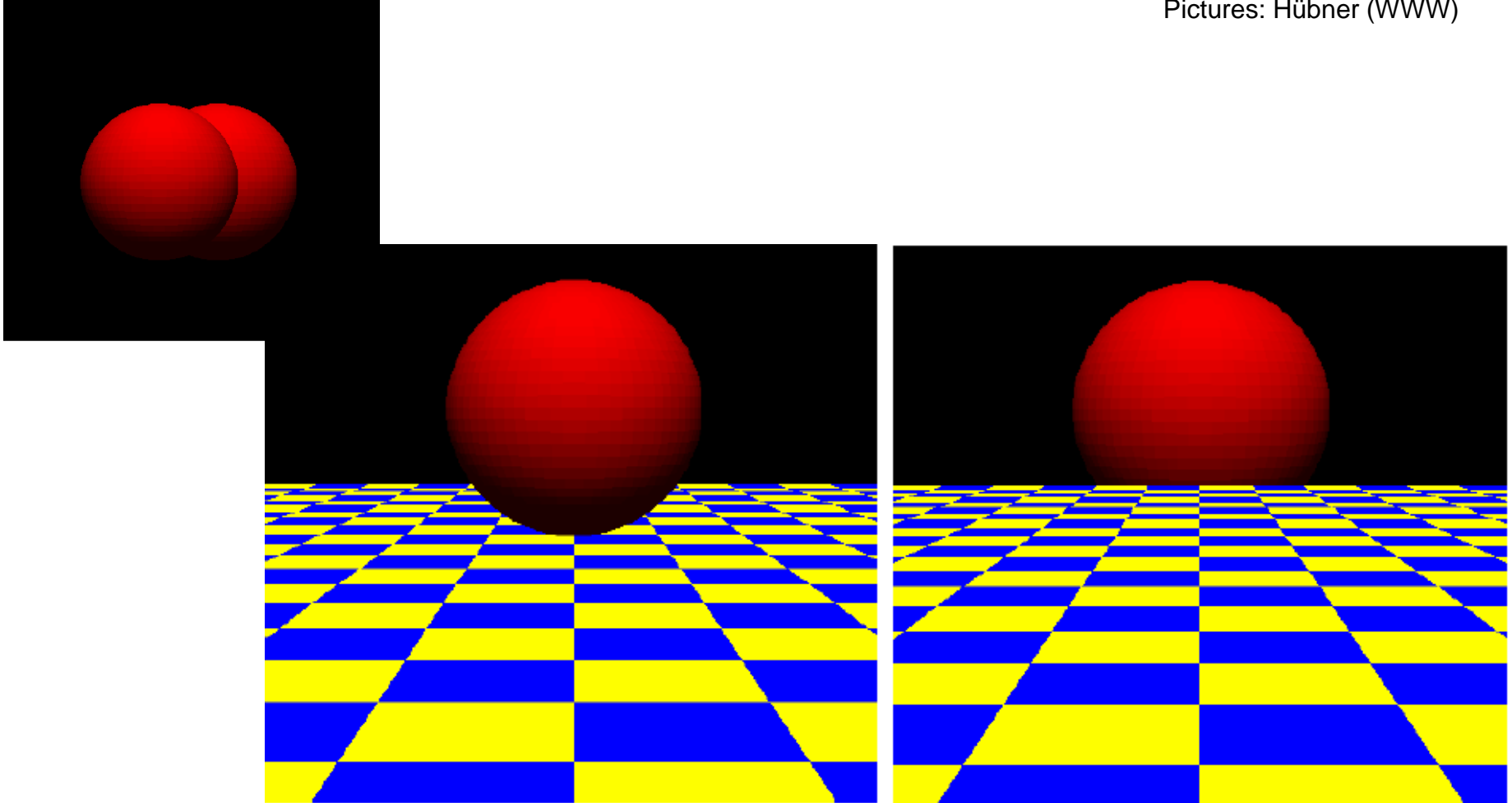
# The Ames Room

Pictures: Goldstein, Levine & Shefner (WWW)



# Occlusion

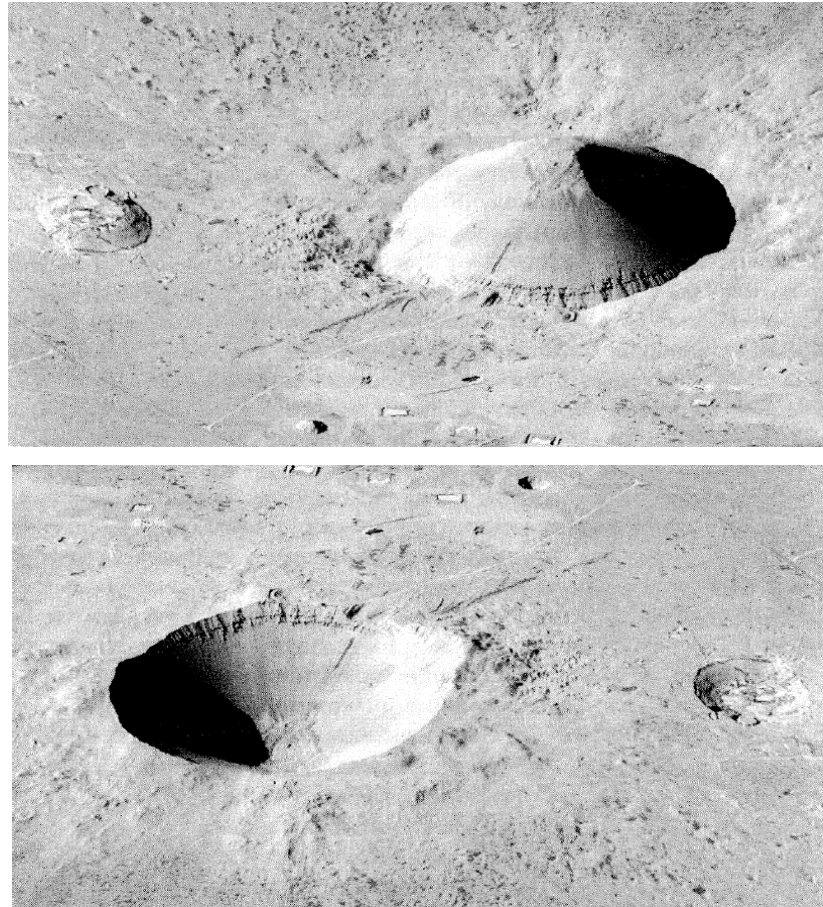
Pictures: Hübner (WWW)





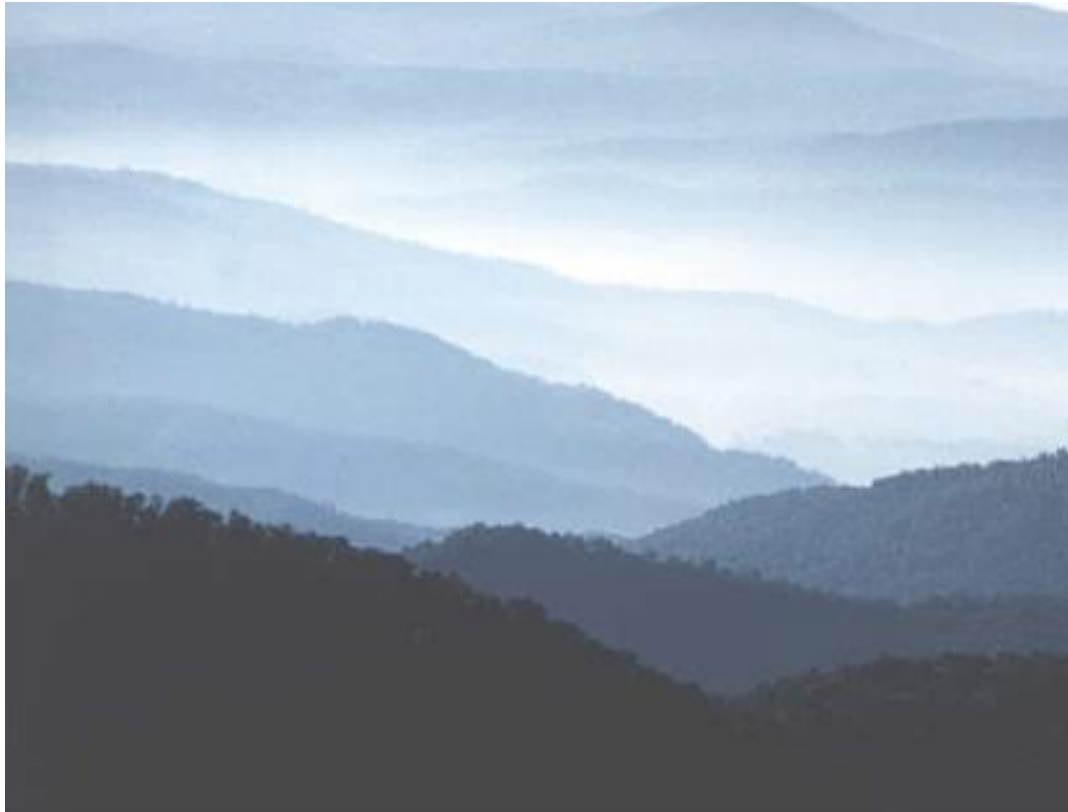
# Light & Shadows

Pictures: Levine & Shefner (WWW)



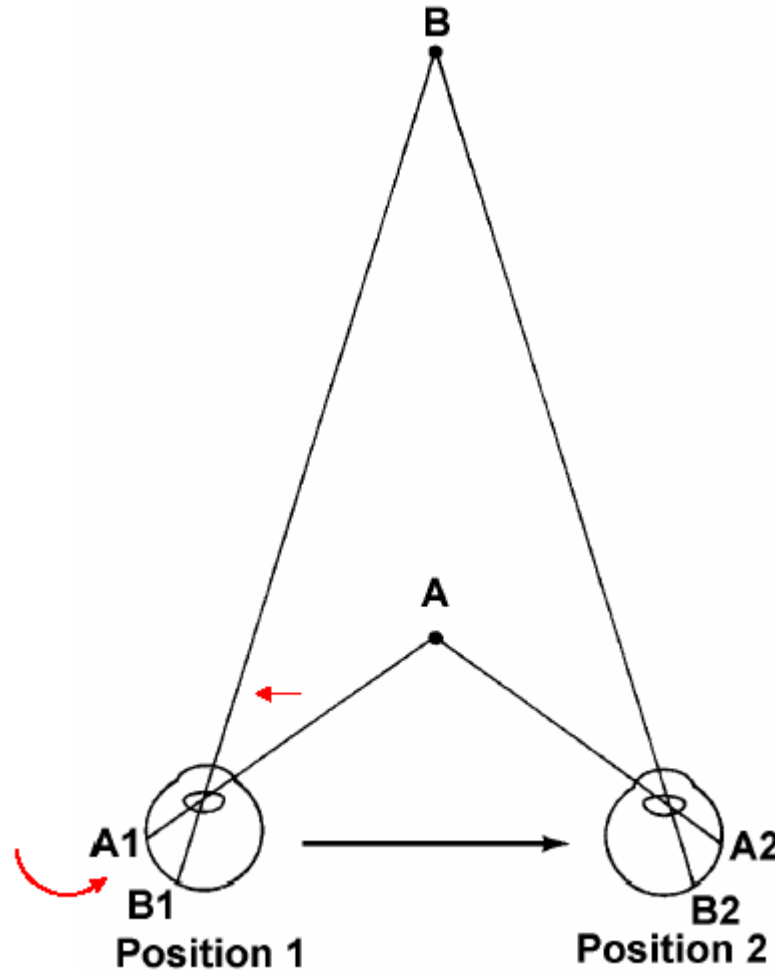
# Atmospheric Perspective

Picture: Lappe (2009)

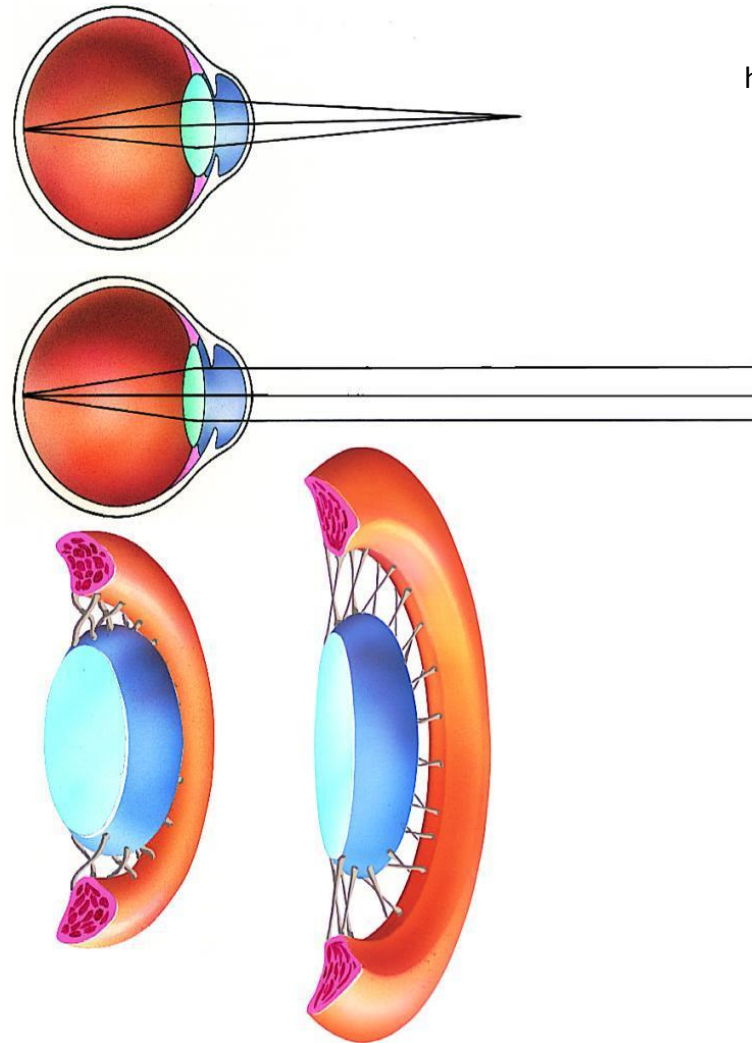


# Convergence

Drawing: Goldstein (WWW)



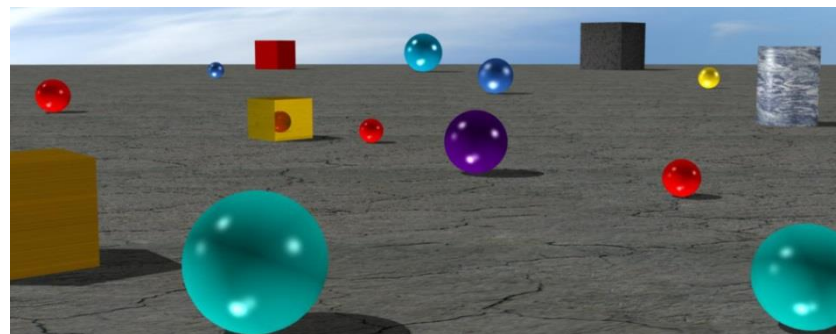
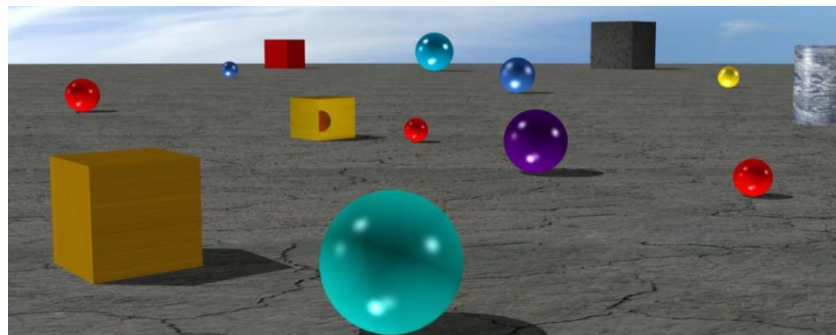
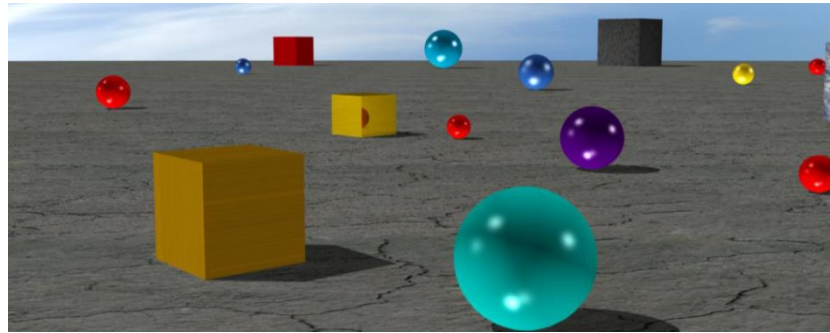
# Accomodation



<http://www.denstoredanske.dk>

# Motion Parallax

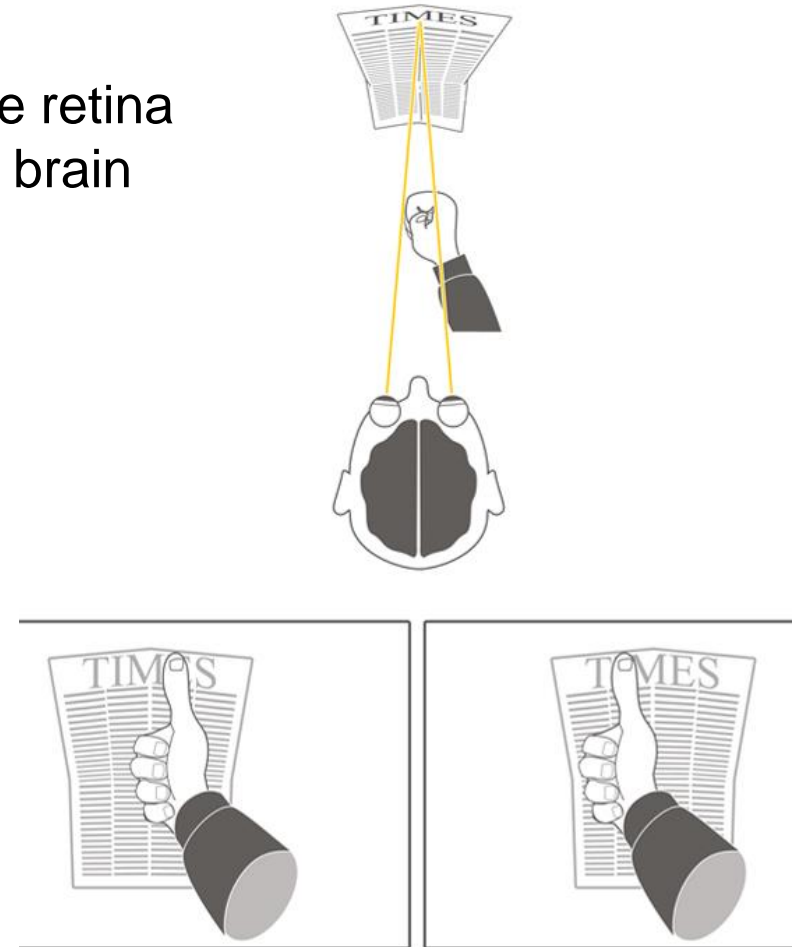
Tom Vaughan,  
[www.cyberlink.com](http://www.cyberlink.com)



# Stereoscopy

<http://www.more3d.com/3-D/Stereoskopie.html>

- Interocular distance (about 6 cm)
- Disparity of images projected onto the retina
- Processing in the visual cortex of the brain
- Works for distances up to 7 m

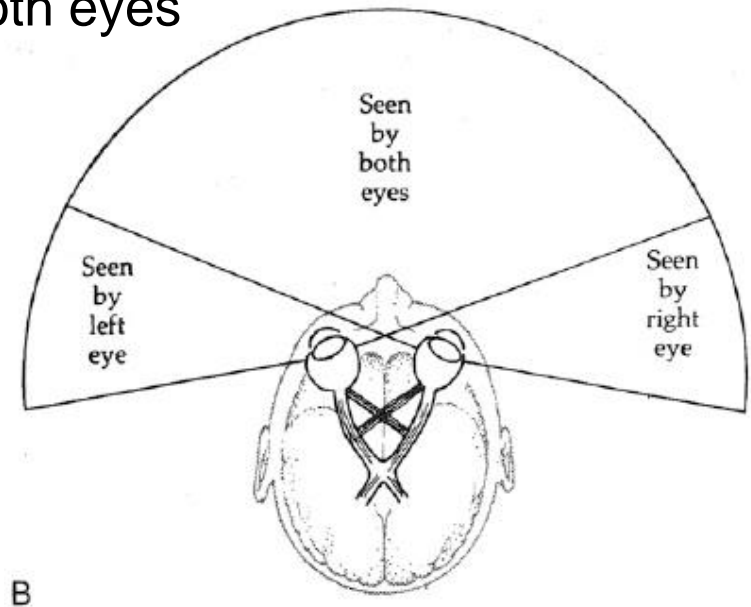




# Field of View

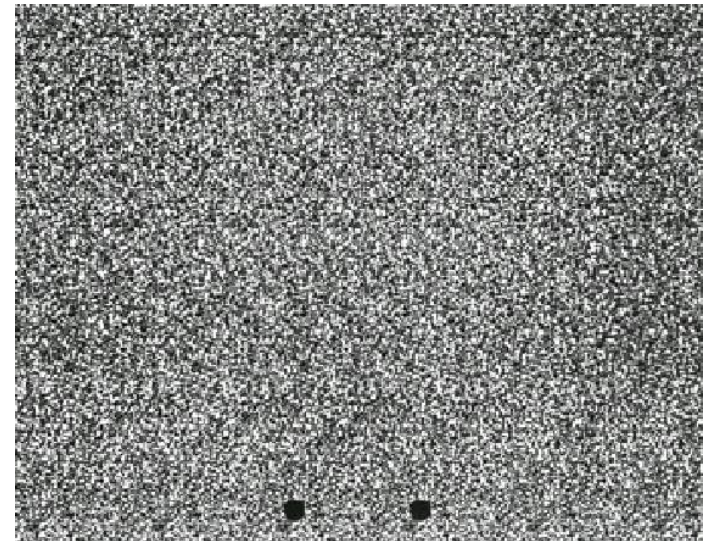
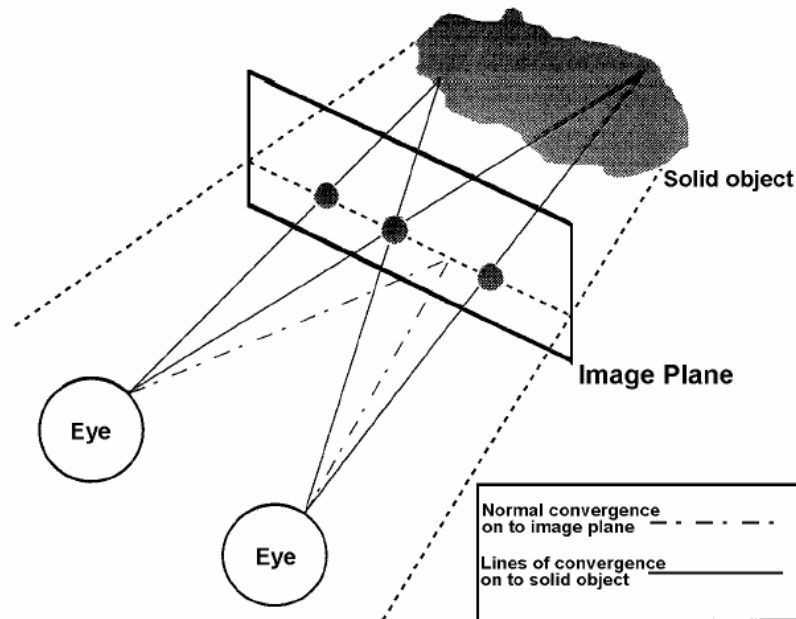
Riecke (2006)

- Oval shape
- At eye level:
  - Horizontal: About  $90^\circ$  to both sides
  - Vertical: About  $120^\circ$  (h  $50^\circ$  and i  $70^\circ$ )
- FOV center is being perceived by both eyes  
Stereoscopic field:  $100^\circ - 120^\circ$



# Auto-Stereograms

Drawing: Irtel (WWW)





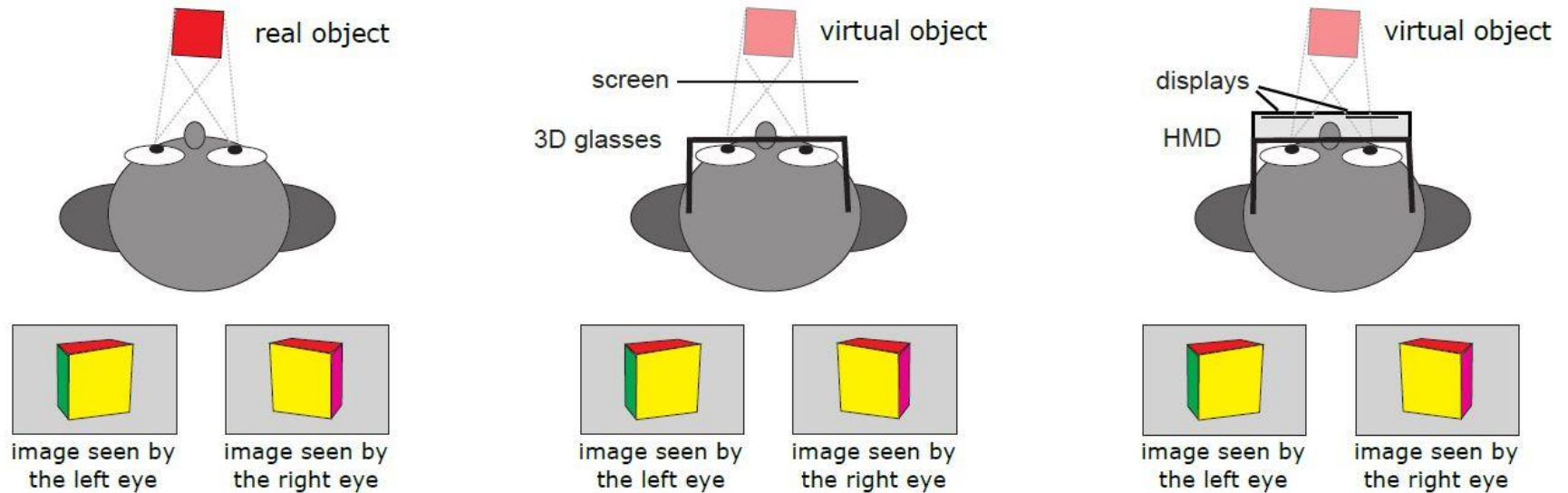
## Auto-Stereograms (cont;-)

Picture: WWW

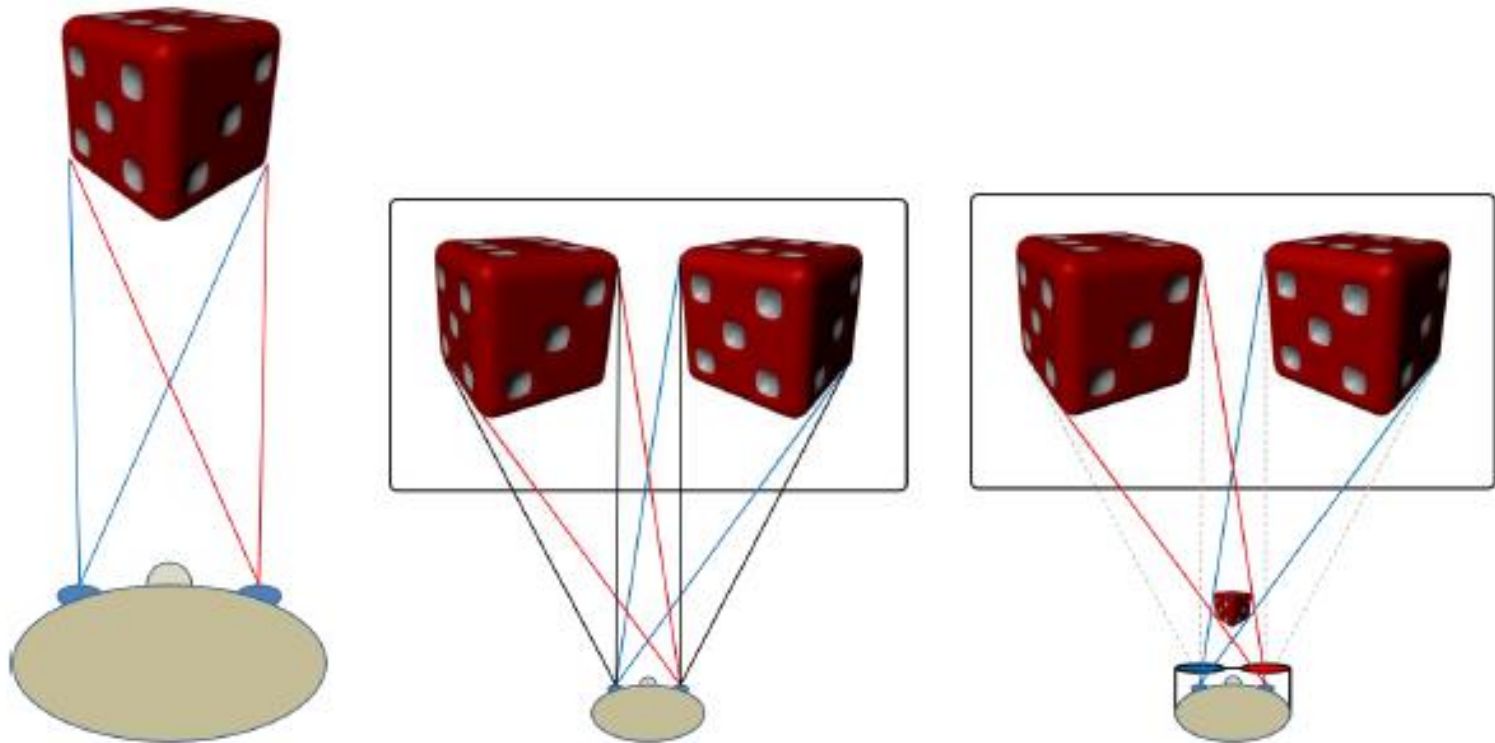


**Look for several seconds at the pic  
and you may recognize a giraffe!**

# Stereo in Head-Mounted & Room-Mounted Displays

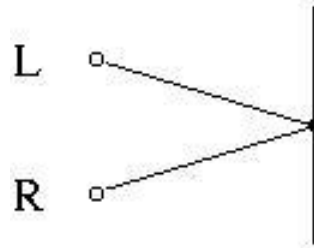


# Stereo Parallax on Room-Mounted Displays

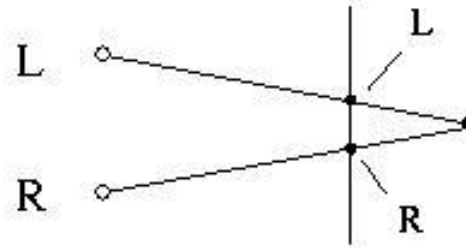


Tom Vaughan,  
[www.cyberlink.com](http://www.cyberlink.com)

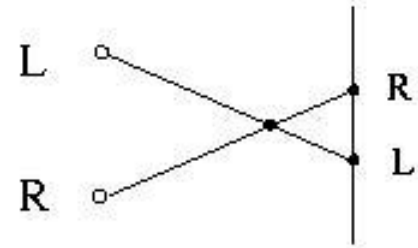
# Stereograms



zero parallax

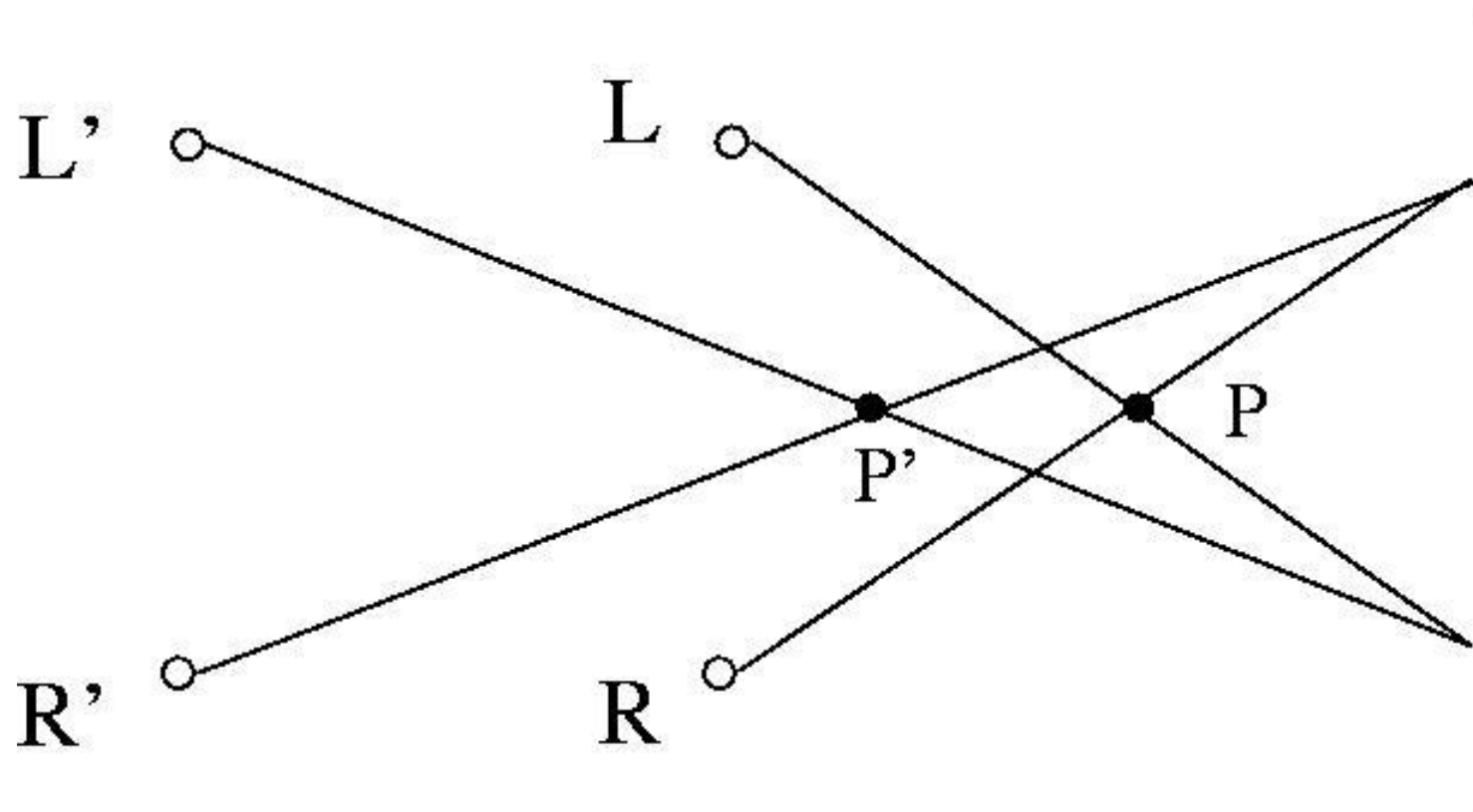


non-crossed  
(positive) parallax

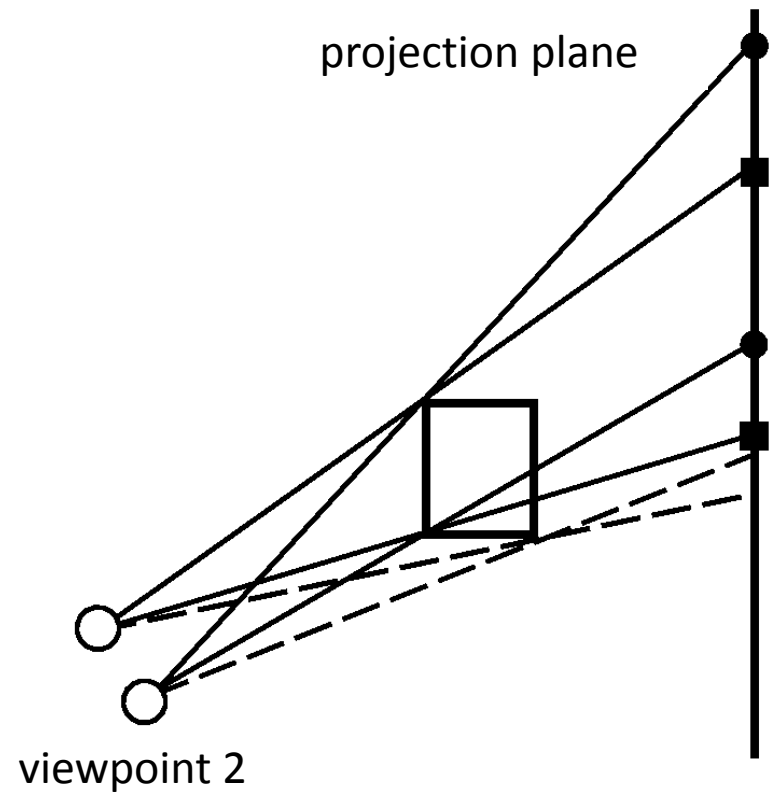
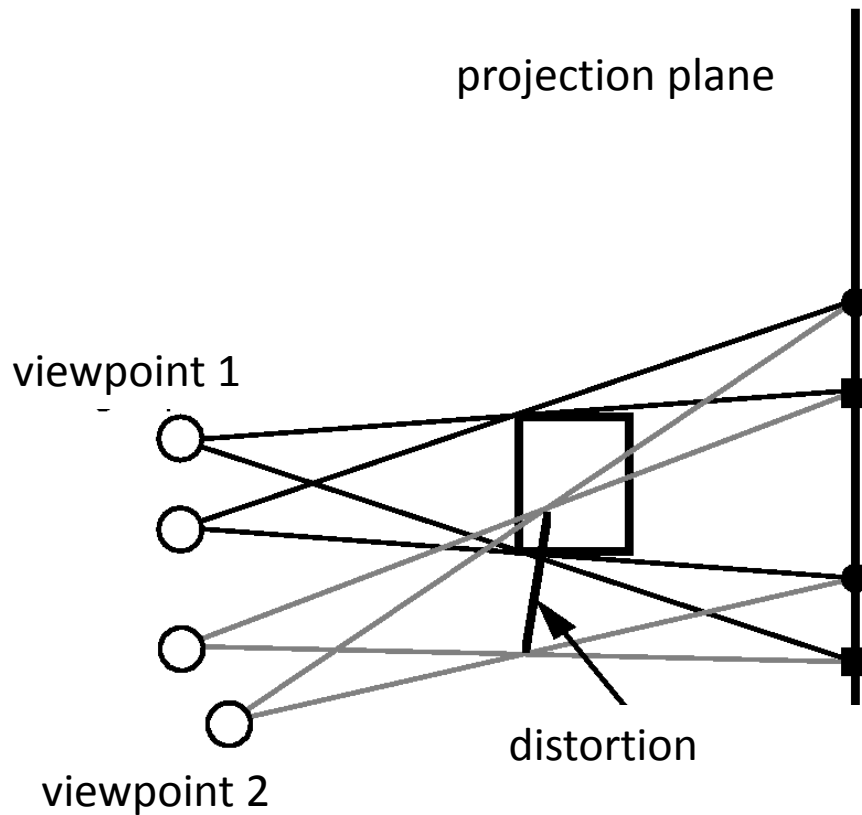


crossed  
(negative) parallax

# Distortions in Static Stereograms



# Adaptation of projection to the viewpoint

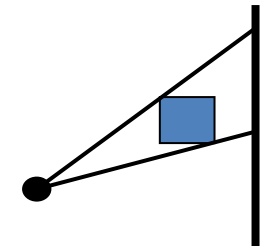
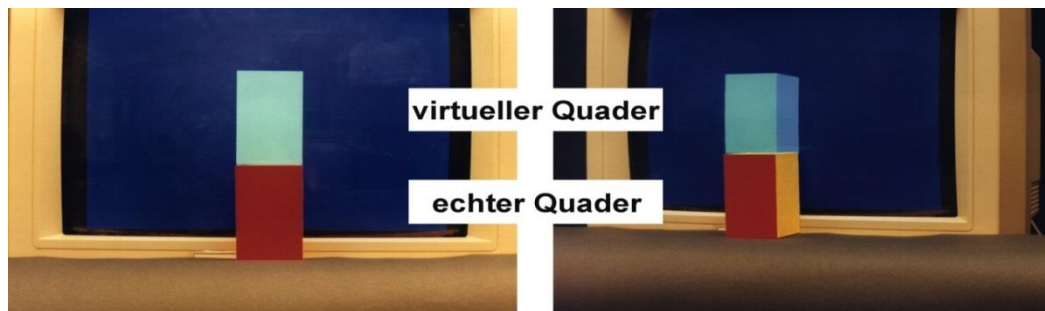
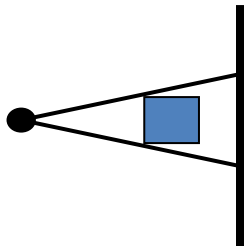
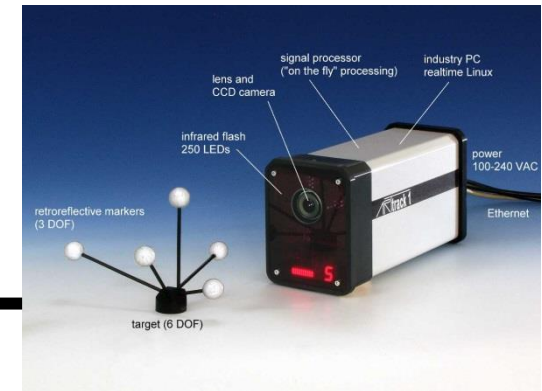


# Motion Parallax & Viewer Centered Projection

## stereo parallax



## motion parallax



# The Effect of Motion Parallax

Courtesy of Bill Sherman



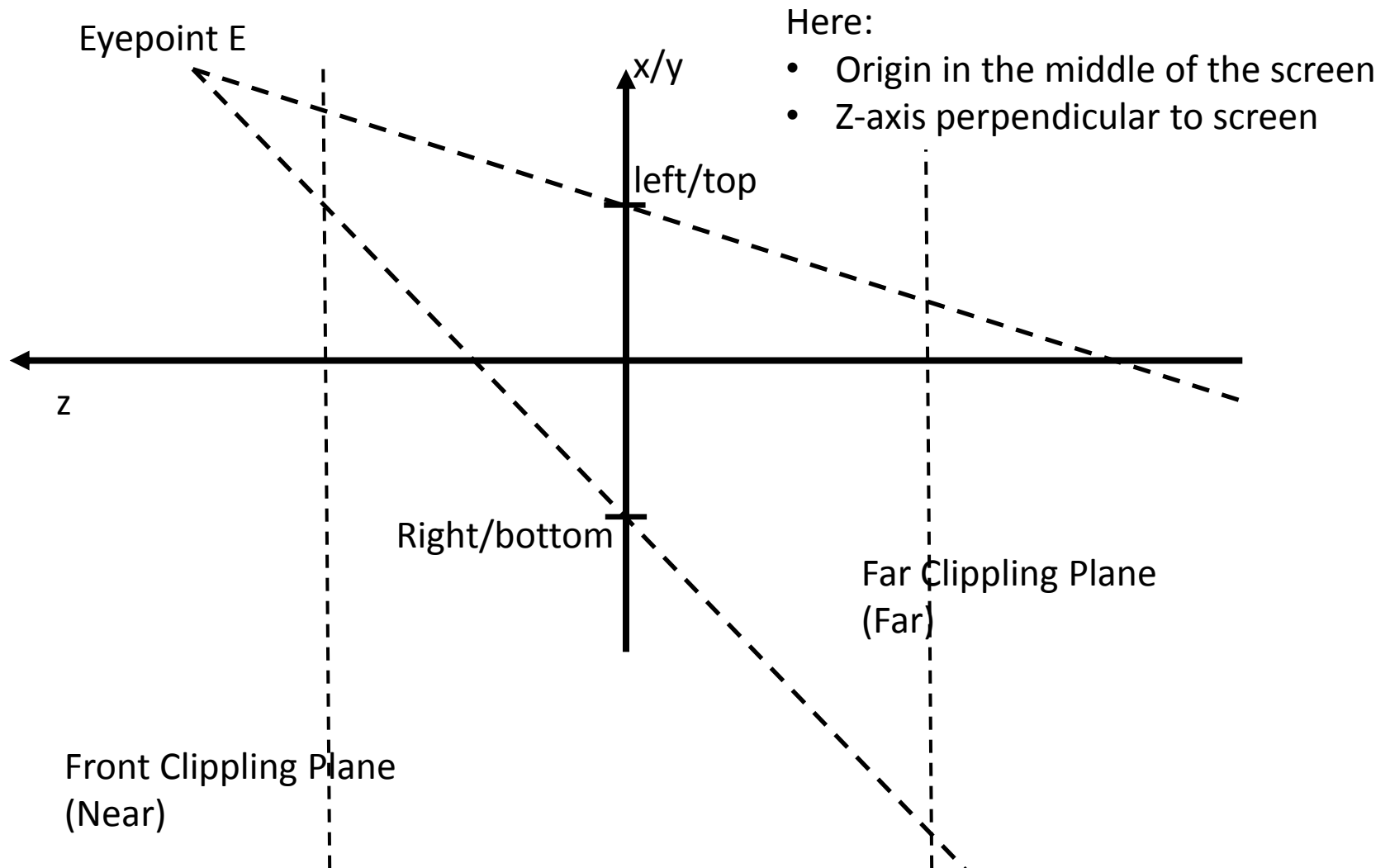


# Video: Viewer Centered Projection

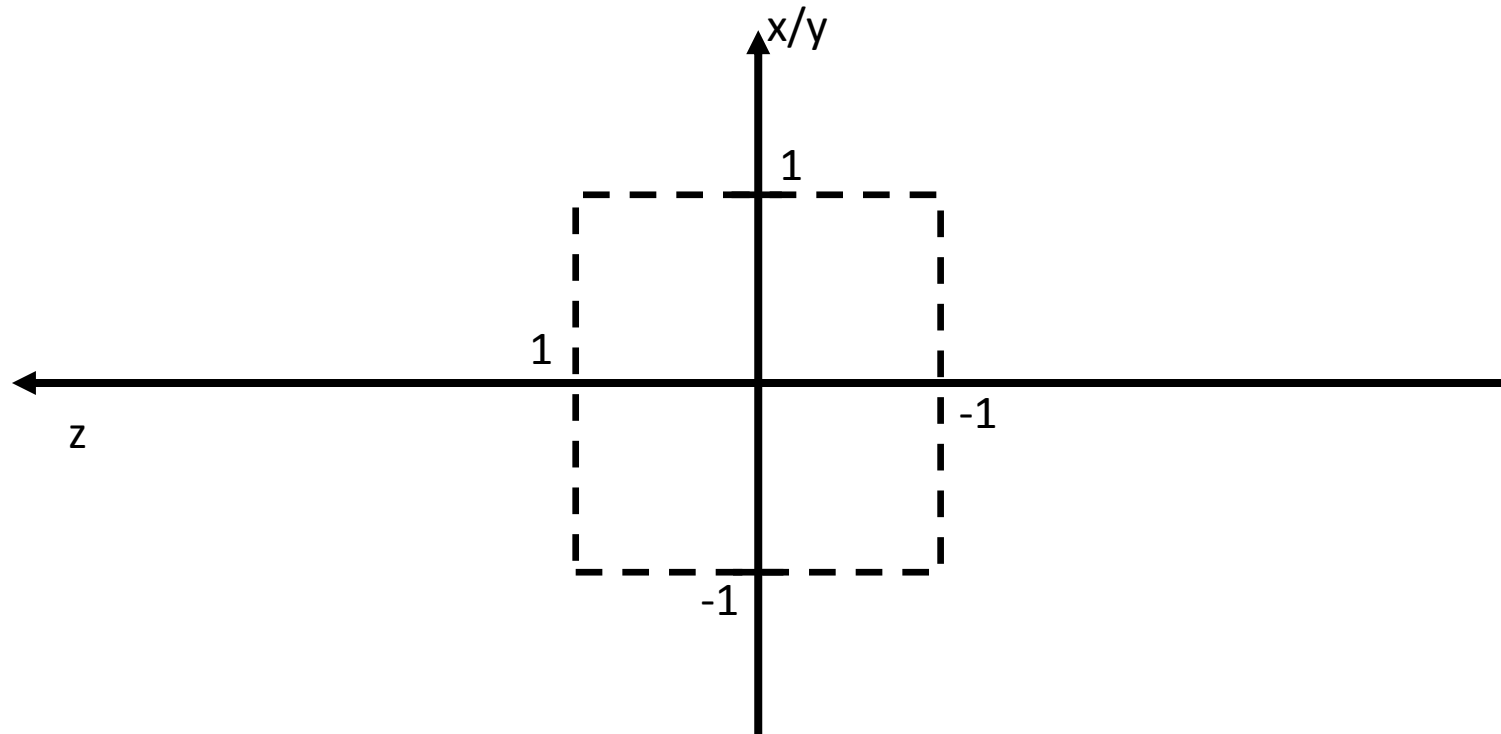
Video: Courtesy of VRVis, Vienna



# Diagonal Projection



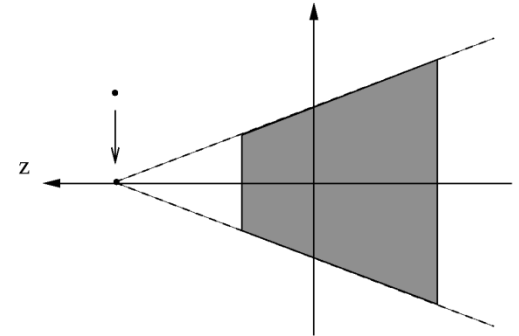
# Goal: Canonical View Volume



# Derivation of the Projection Matrix (I)

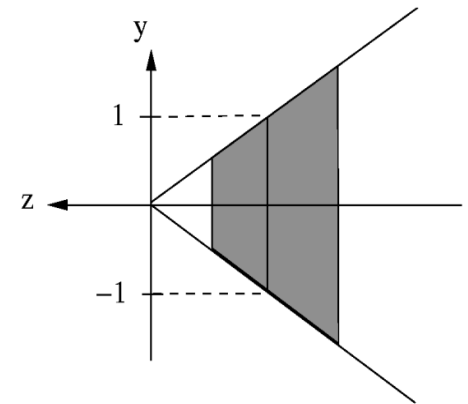
Step 1: Shearing of view volume

$$P_1 = SH_{xy}\left(\frac{-E_x}{E_z}, \frac{-E_y}{E_z}\right) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ \frac{-E_x}{E_z} & \frac{-E_y}{E_z} & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$



Step 2: Translation of E to the origin

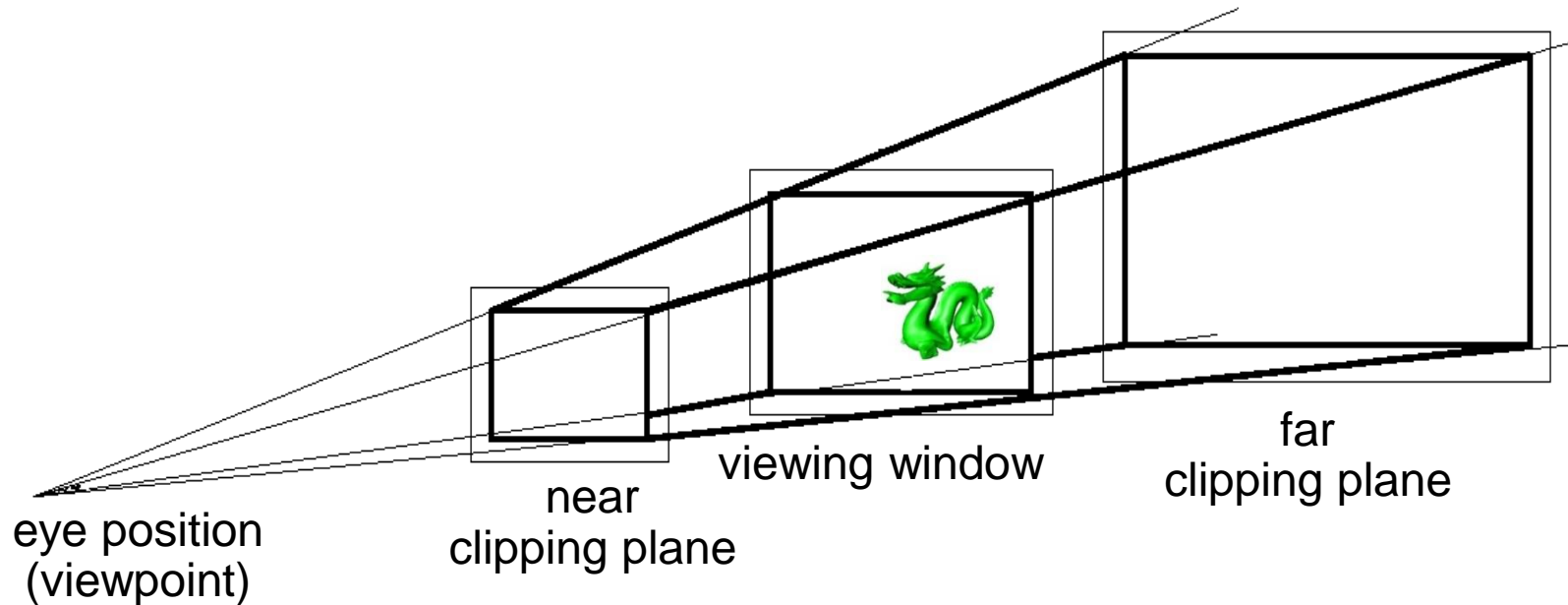
$$P_2 = T(0, 0, -E_z) = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -E_z & 1 \end{pmatrix}$$



Step 3: Scaling of the window to the unit rectangular

$$P_3 = S\left(\frac{2}{\text{right} - \text{left}}, \frac{2}{\text{top} - \text{bottom}}, 1, 1\right) = \begin{pmatrix} \frac{2}{\text{right} - \text{left}} & 0 & 0 & 0 \\ 0 & \frac{2}{\text{top} - \text{bottom}} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

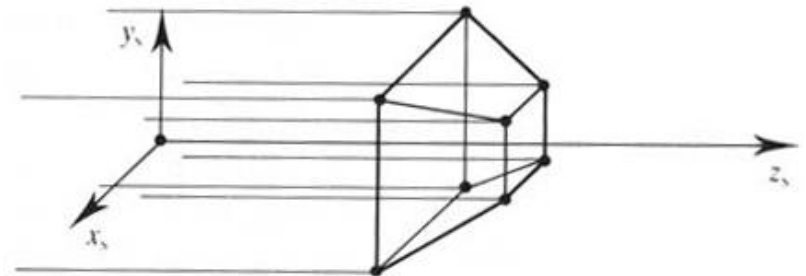
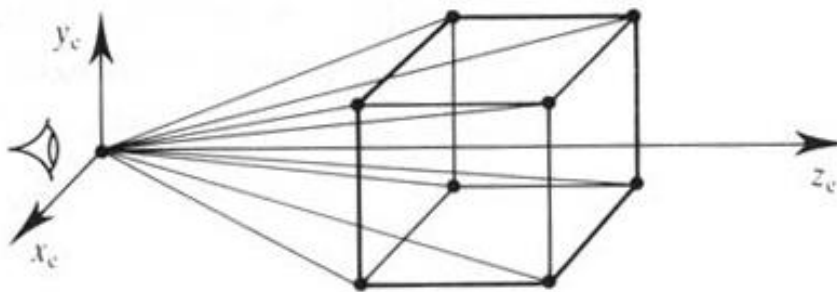
# View Volume



# Z-Buffering

## Z-Buffer

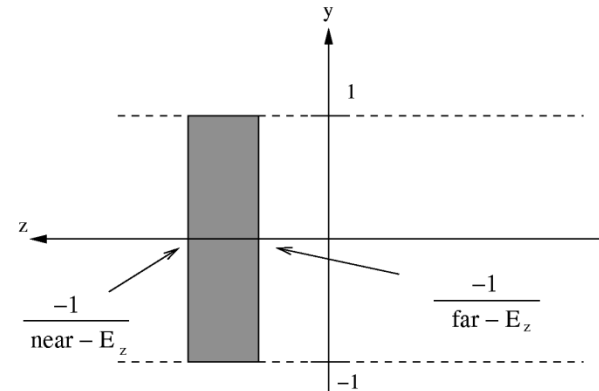
- Special memory on graphics hardware, 1 entry for every pixel
- Updated with the highest z value of 3-D object points that cover its pixel
- Accuracy depends on
  - Length of memory words („depth“) (usually 24 bits/pixel)
  - Z-value of front and back clipping plane
- Compare points lying on the same projector (OpenGL: parallel projection!)



# Derivation of the Projection Matrix (II)

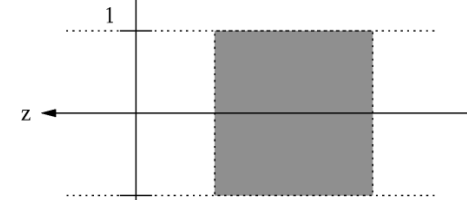
Step 4: Scaling as a function in z

$$P_4 = SZ \begin{pmatrix} E_z & 0 & 0 & 0 \\ 0 & E_z & 0 & 0 \\ 0 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$



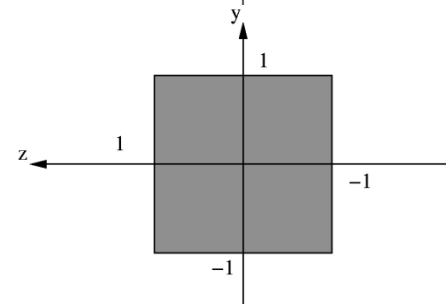
Step 5: Scaling of the view volume in z

$$P_5 = S(1, 1, \frac{2(far - E_z)(near - E_z)}{far - near}, 1)$$



Step 6: Translation in the direction of z

$$P_6 = T(0, 0, \frac{-2E_z - far - near}{far - near})$$



$$P = \prod_{i=1}^6 P_i$$

# The Projection Matrix

Parameters:

- Position of the view window: left, right, top, bottom
- Near and far clipping plane: near, far
- Eye position E

$$\mathbf{P} = \begin{pmatrix} \frac{2e_z}{r-l} & 0 & 0 & 0 \\ 0 & \frac{2e_z}{o-u} & 0 & 0 \\ \frac{-2(e_x - \frac{r+l}{2})}{r-l} & \frac{-2(e_y - \frac{o+u}{2})}{o-u} & \frac{2e_z - f - n}{f-n} & -1 \\ -\frac{r+l}{r-l}e_z & -\frac{o+u}{o-u}e_z & \frac{-e_z(2e_z - f - n) + 2(f - e_z)(n - e_y)}{f-n} & e_z \end{pmatrix}$$

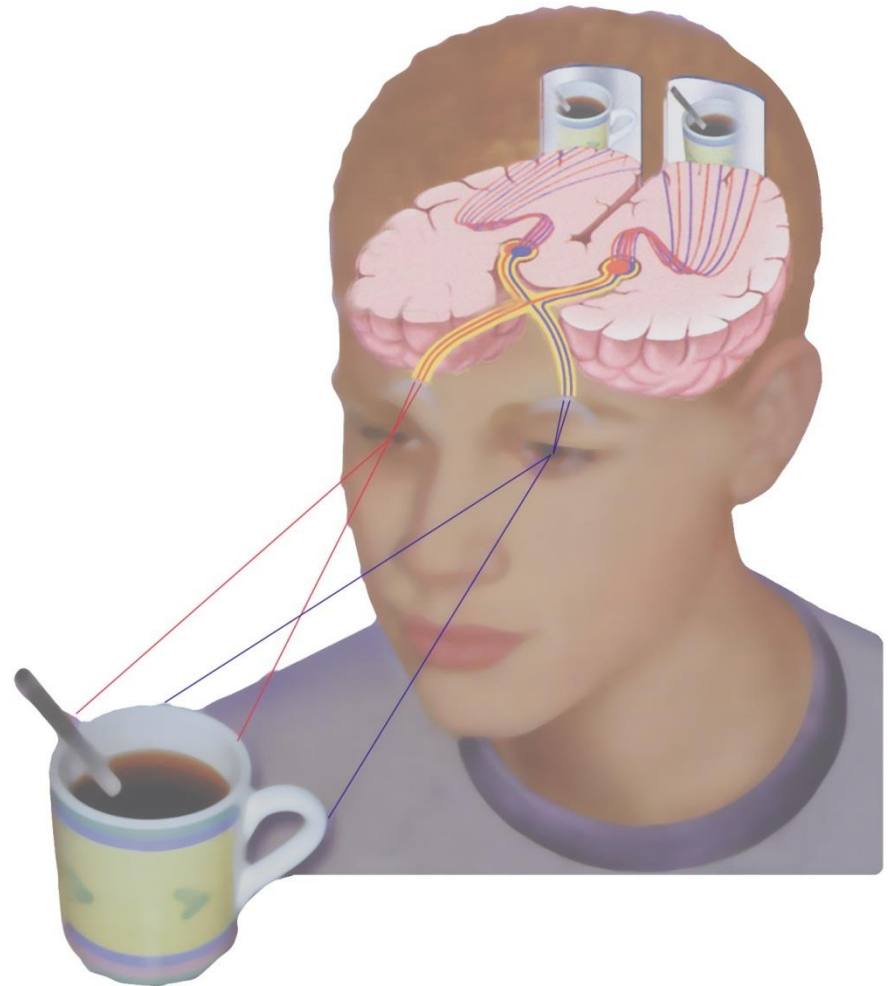


# Exact correspondence of visual perception in the real world and in the virtual world

## Virtual Reality:

- **Physiological clues**

- Stereopsis
- Ocular motor factors
  - Accomodation
  - Convergence
- Motion parallax



# Perception of Distances in VR

**Distances are typically under-estimated in virtual environments:**

- **Influence candidates:**
  - Rendering Quality
    - Illumination model
    - Positions of light sources
    - Resolution / aliasing
  - Framerate
  - Display hardware characteristics / quality
    - Brightness Uniformity
    - Accomodation / Convergence
- Distance estimation „nearly“ independent from rendering /display technology
- Many contradictory studies
- No explanation for under-estimation