

# Replacement Policies

CMPSCI 230 Computer Systems Principles

# Objectives

## ■ Cache Replacement Algorithms

- Least Frequently Used (LFU)
- Least Recently Used (LRU)

# Replacement Policies

## ■ Optimal Data Replacement Algorithm

### ■ Belady's Algorithm:

Replace the data that will **not be used** for the *longest period of time* in the future.

## ■ Problem:

- Need to **predict the future!**
- Not possible, but used as a “yard stick” to compare replacement algorithms to determine improvement.
- Use heuristics

# Caching Algorithms

- **Least Frequently Used (LFU)**
- **Least Recently Used (LRU)**

# Caching Algorithms (LFU)

## ■ Least Frequently Used (LFU)

- Count how often an entry is used by incrementing a counter associated with each entry in the cache.
- Remove the entry with the least frequently used counter first.

## ■ Request Pattern

- Discard entries that are not needed over the longest period.

Miss: 0

Hit: 0

# LFU Example

2	4	1	7
---	---	---	---

2	1	3	8
---	---	---	---

4	1	8	8
---	---	---	---

--	--	--	--

hit count:

0	0	0	0
---	---	---	---

Miss: 1

Hit: 0

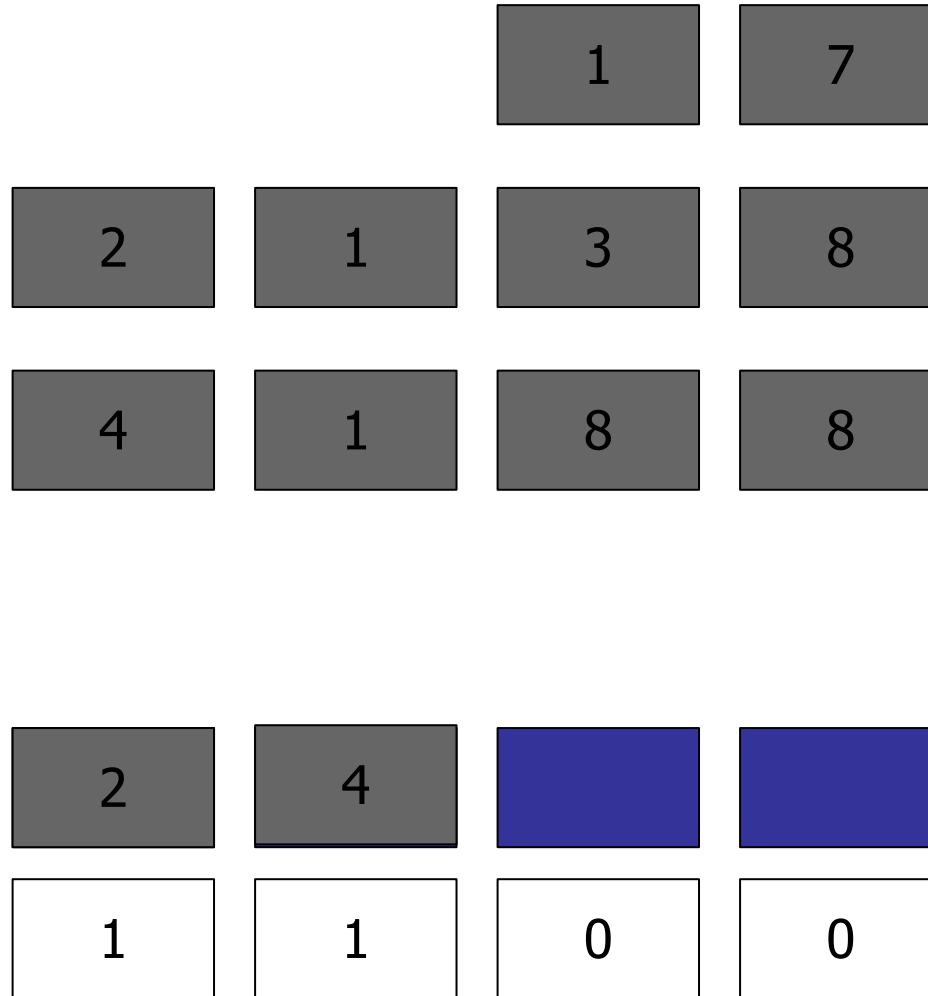
# LFU Example

	4	1	7
2	1	3	8
4	1	8	8
2			
hit count:	1	0	0

Miss: 2

Hit: 0

# LFU Example

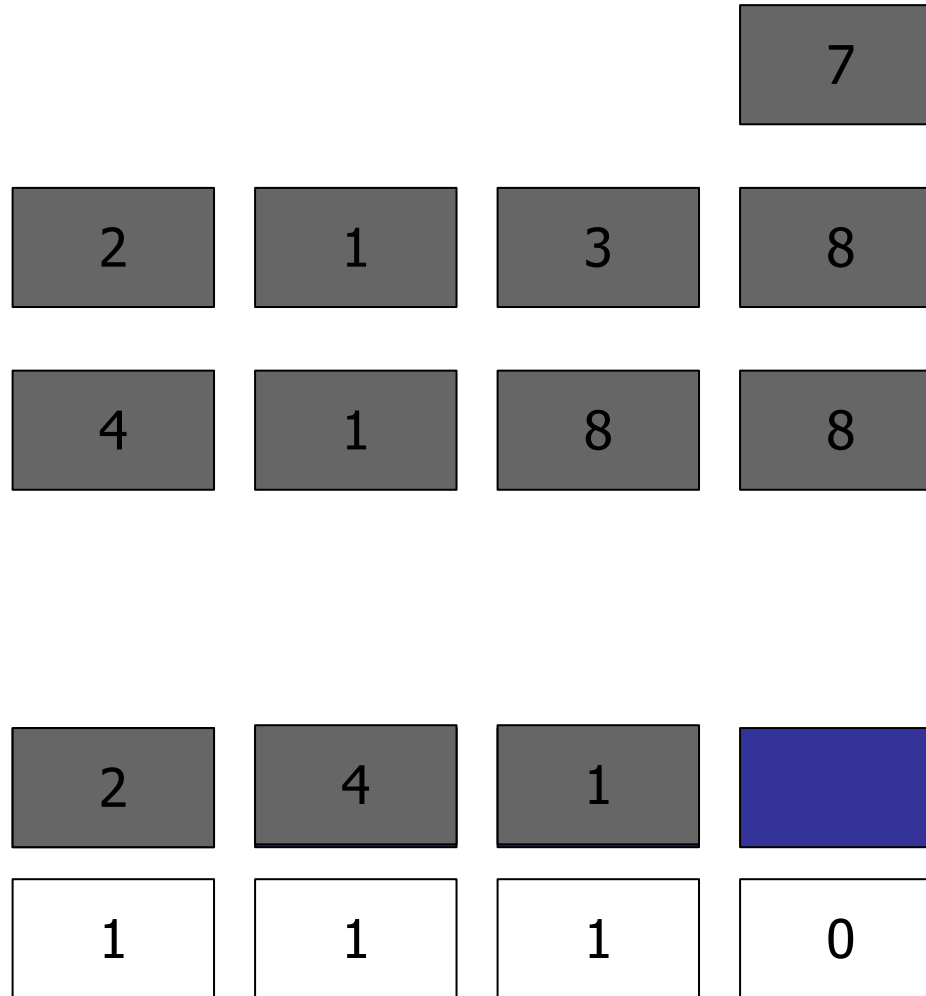




Miss: 3

Hit: 0

# LFU Example



Miss: 4

Hit: 0

# LFU Example

2	1	3	8
---	---	---	---

4	1	8	8
---	---	---	---

2	4	1	7
---	---	---	---

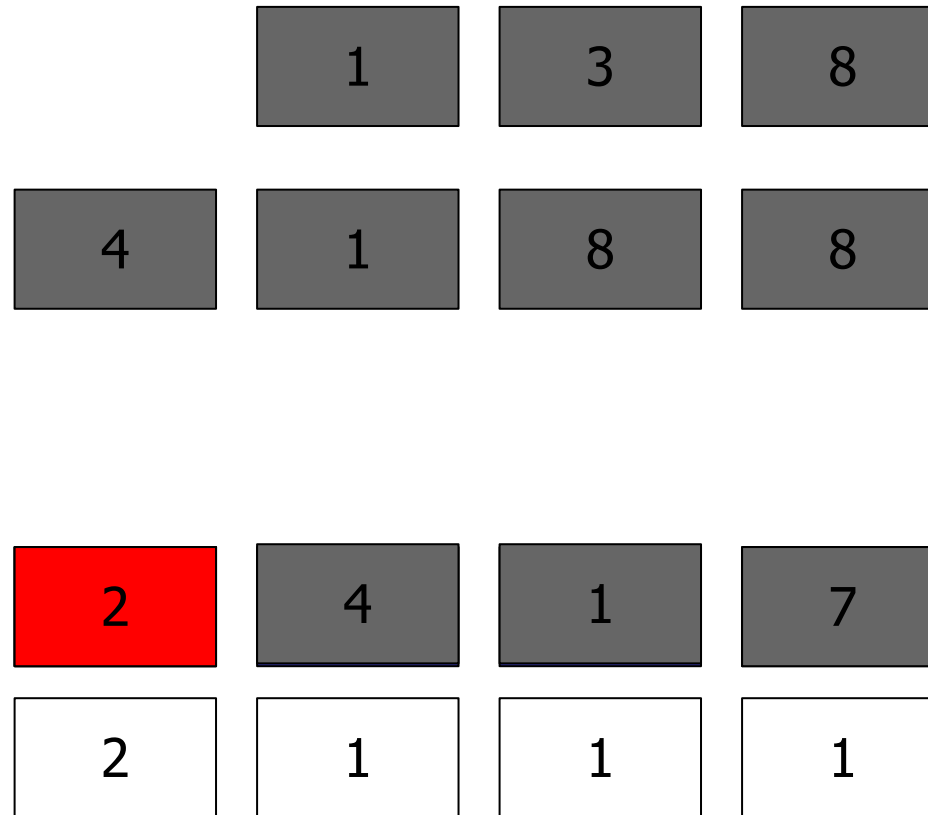
hit count:

1	1	1	1
---	---	---	---

# LFU Example

Miss: 4

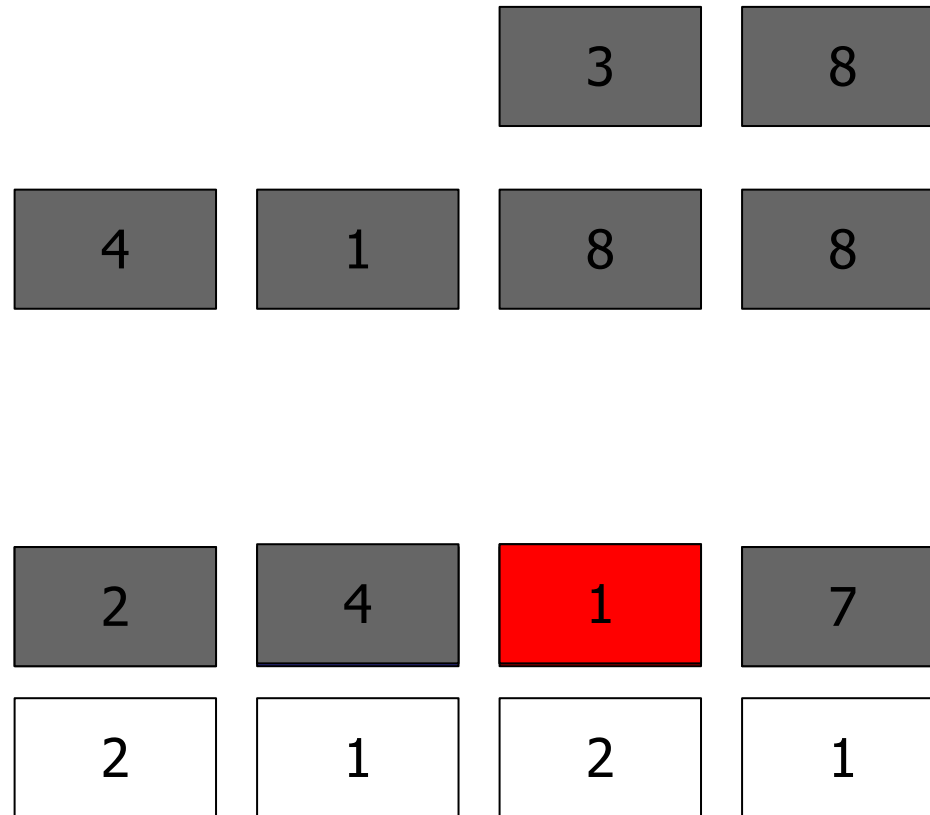
Hit: 1



# LFU Example

Miss: 4

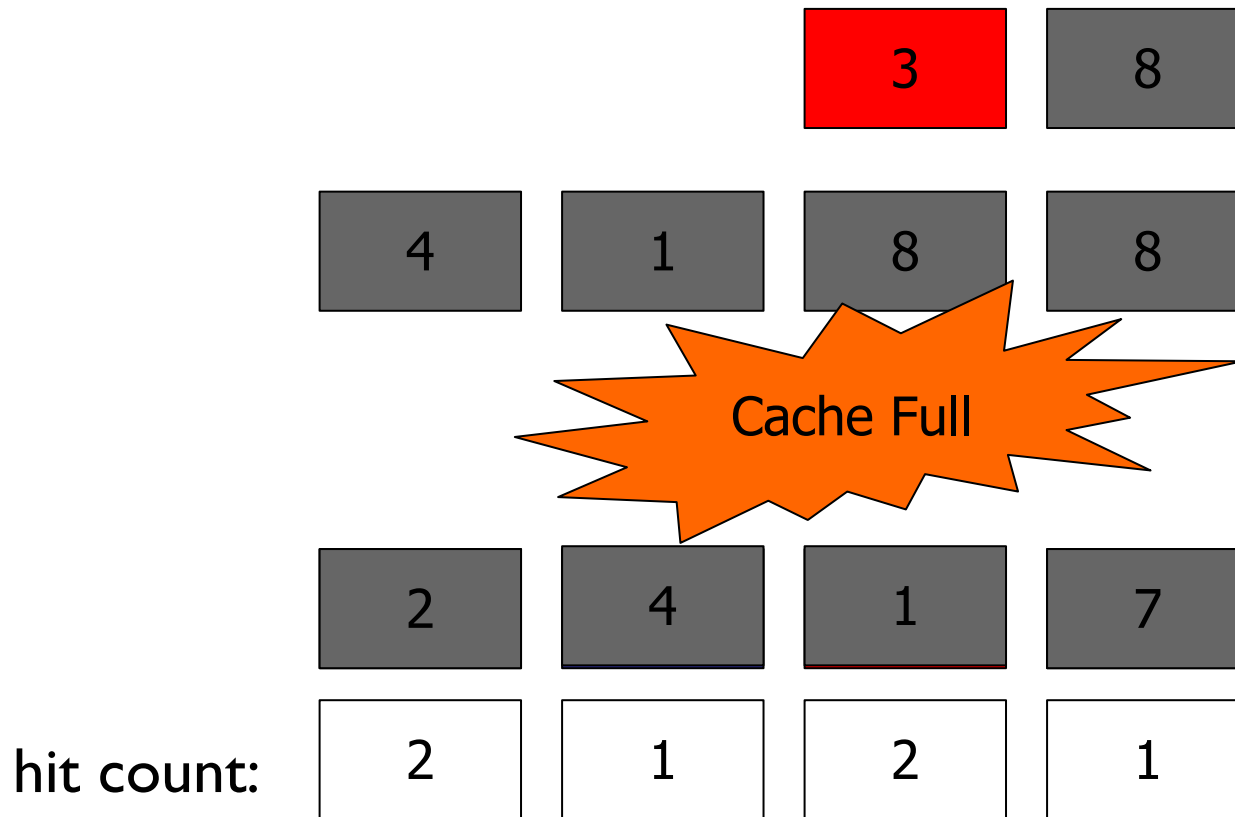
Hit: 2



Miss: 5

Hit: 2

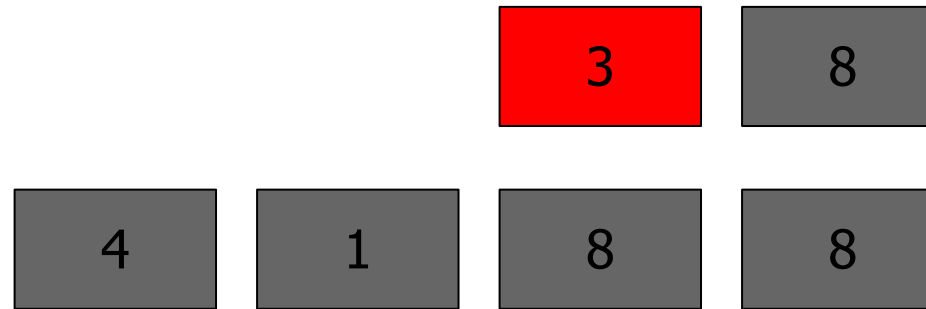
# LFU Example



Miss: 5

Hit: 2

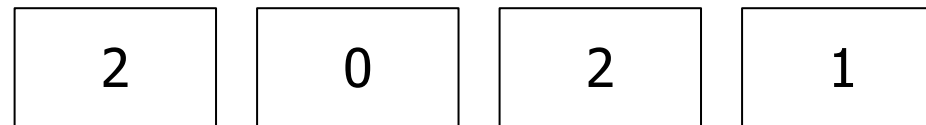
# LFU Example



**Evict Least Frequently**



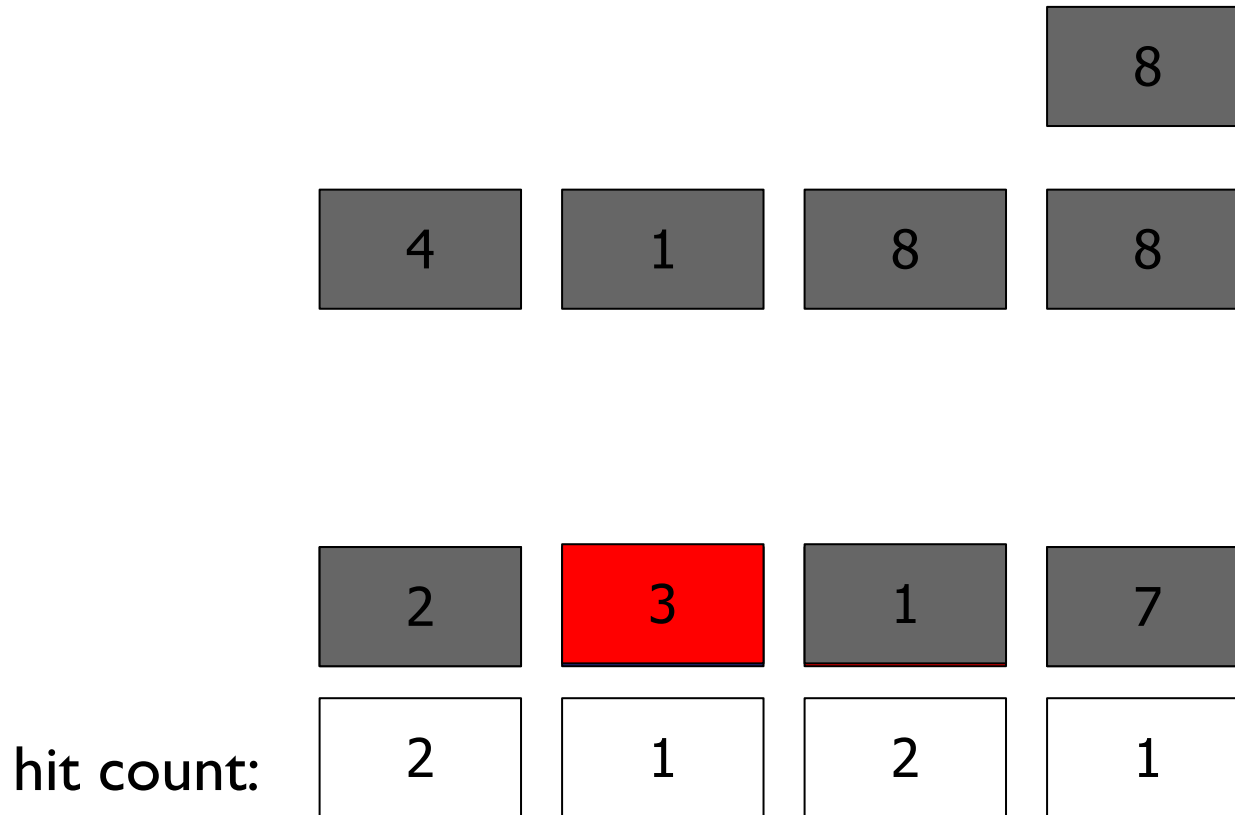
hit count:



Miss: 5

Hit: 2

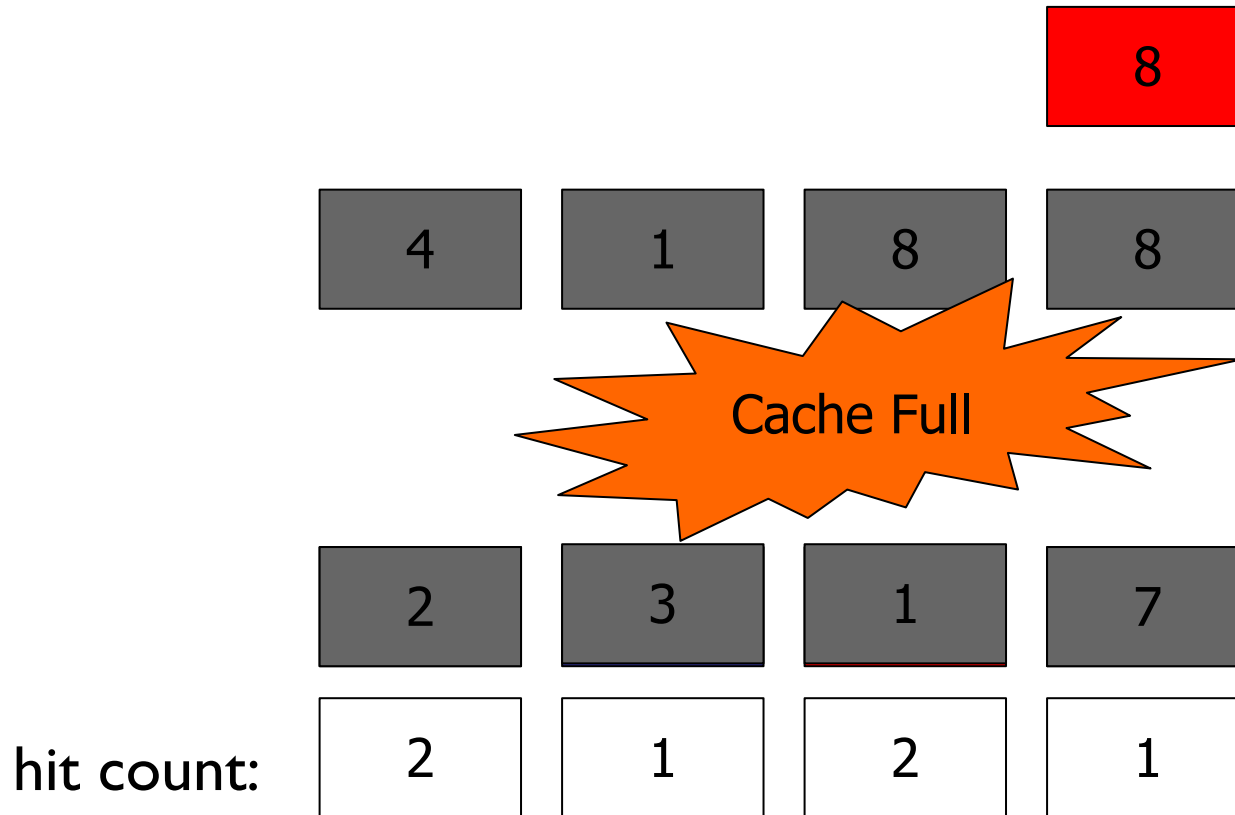
# LFU Example



Miss: 6

Hit: 2

# LFU Example

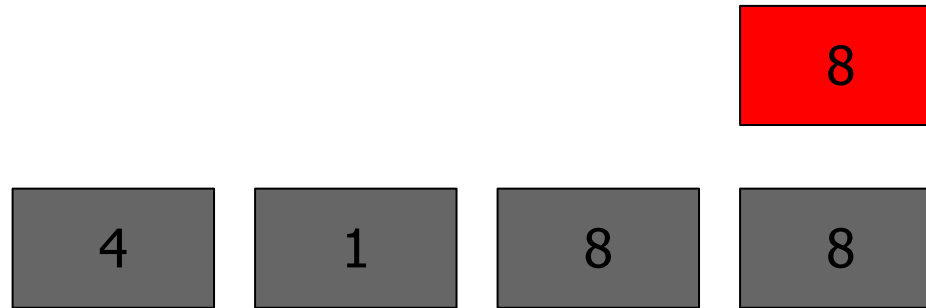




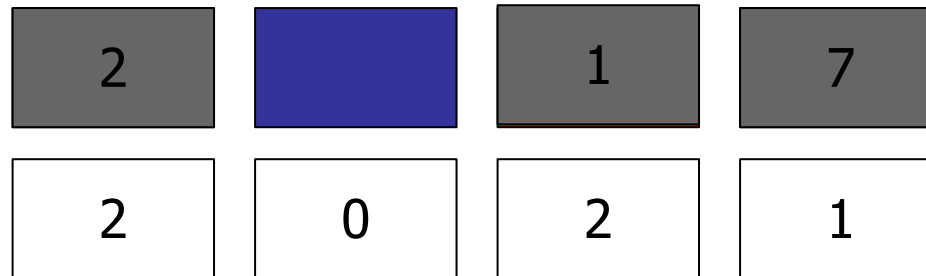
Miss: 6

Hit: 2

# LFU Example



**Evict Least Frequently Used**

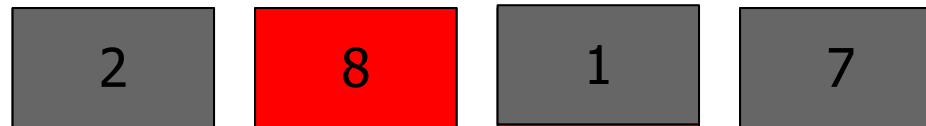


hit count:

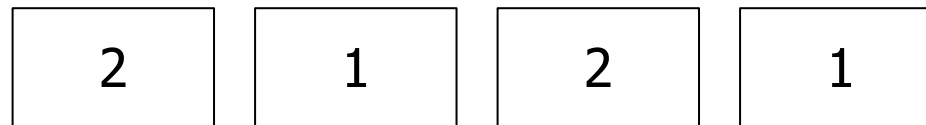
Miss: 6

Hit: 2

# LFU Example



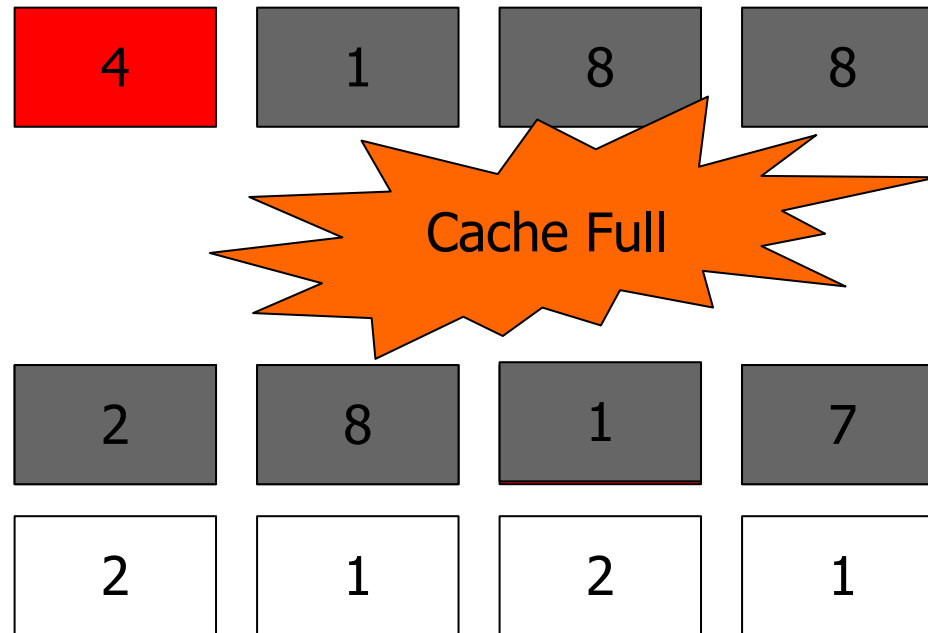
hit count:



Miss: 7

Hit: 2

# LFU Example



hit count:

Miss: 7

Hit: 2

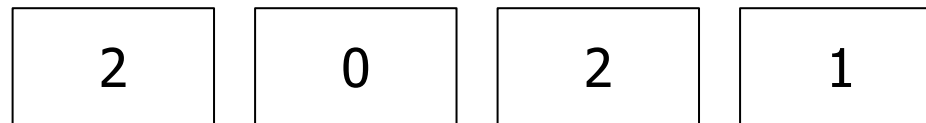
# LFU Example



**Evict Least Frequently Used**



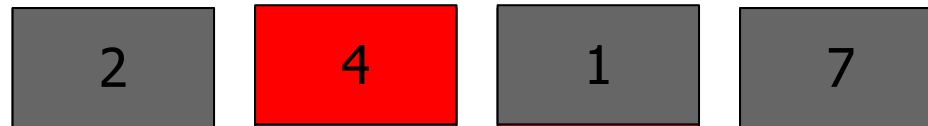
hit count:



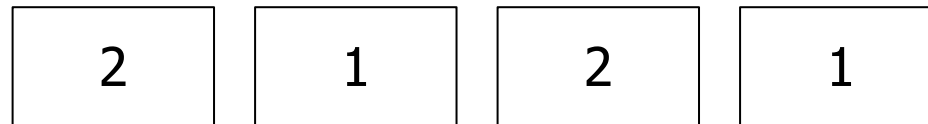
Miss: 7

Hit: 2

# LFU Example



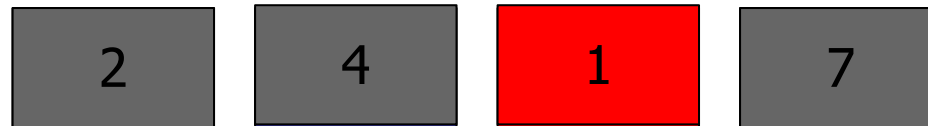
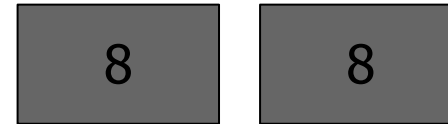
hit count:



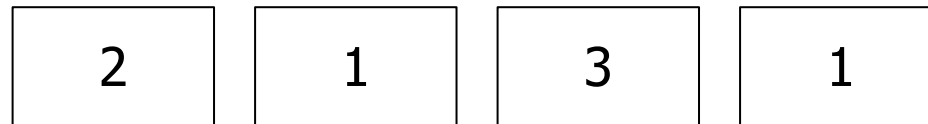
# LFU Example

Miss: 7

Hit: 3



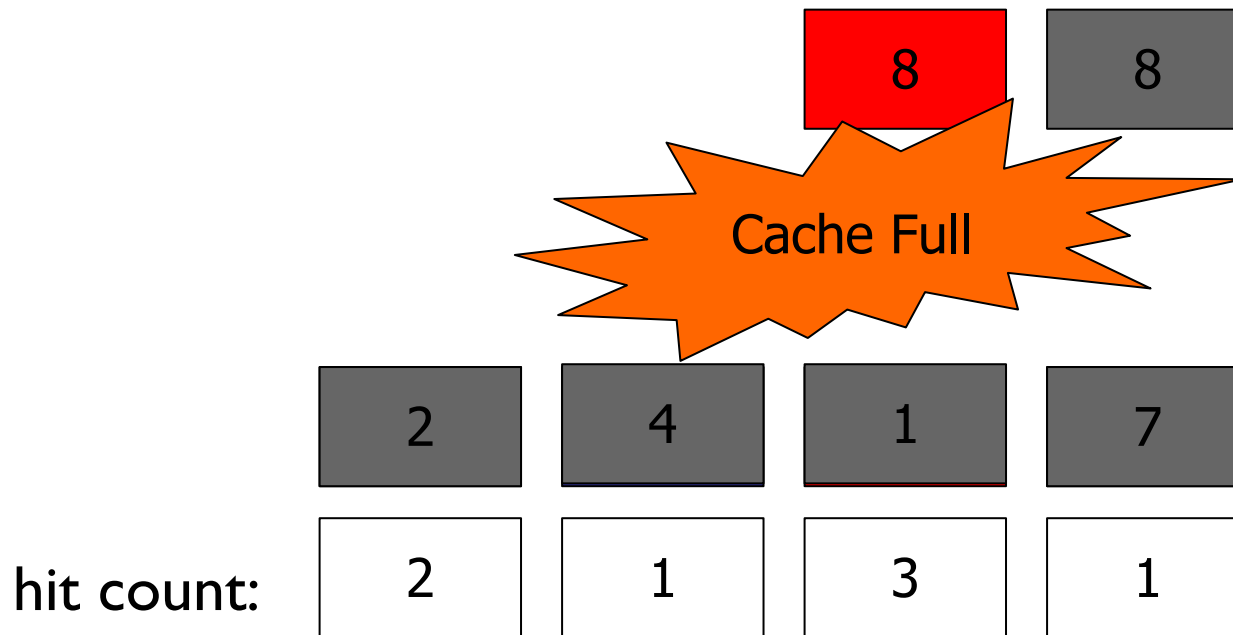
hit count:



Miss: 7

Hit: 3

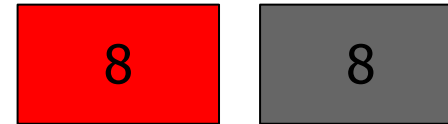
# LFU Example



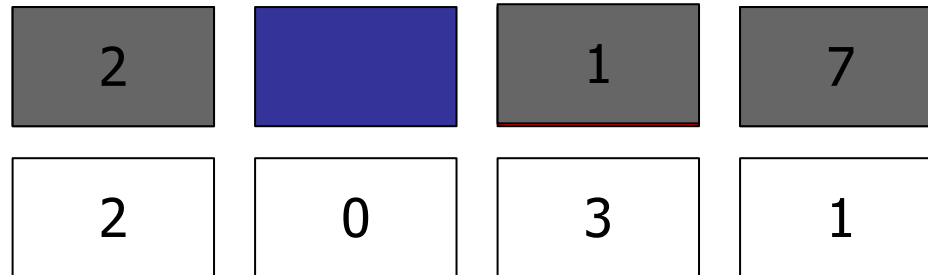
Miss: 7

Hit: 3

# LFU Example



**Evict Least Frequently Used**



hit count:



# LFU Example

Miss: 8

Hit: 3

8

2

8

1

7

hit count:

2

1

3

1

# LFU Example

Miss: 8

Hit: 4

	2	8	1	7
hit count:	2	2	3	1

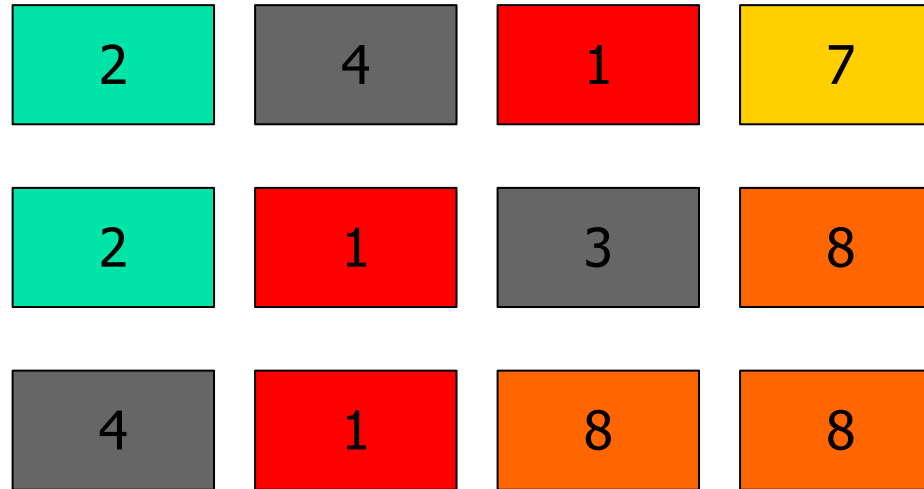
# LFU Example

Miss: 8

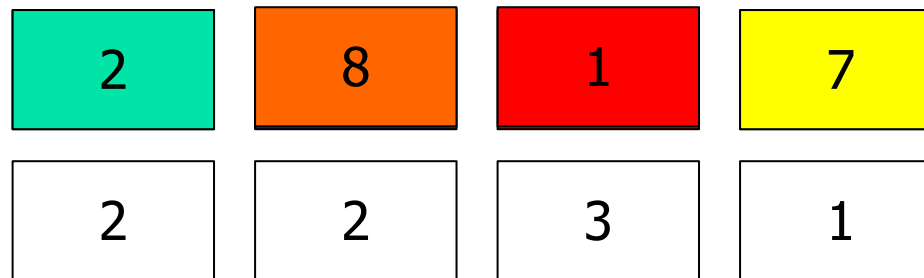
Hit: 4

MR = 67%

HR = 33%



## Final State of the Cache



hit count:

# Caching Algorithms: LRU

## ■ Least Recently Used (LRU)

- New items are placed in the top of the cache. When cache exceeds size limit, discard items from the bottom.
- **Remove the least recently used item first**

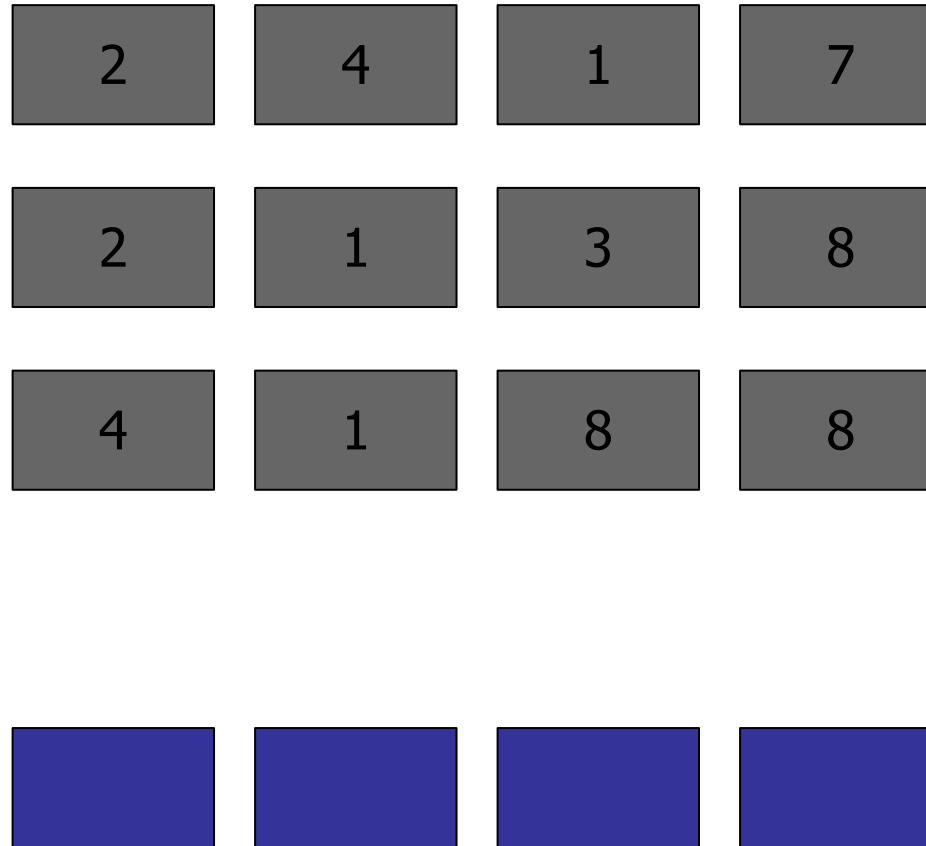
## ■ Request Pattern

- Discard entries that are least recently used
- ***Fast!***

Miss: 0

Hit: 0

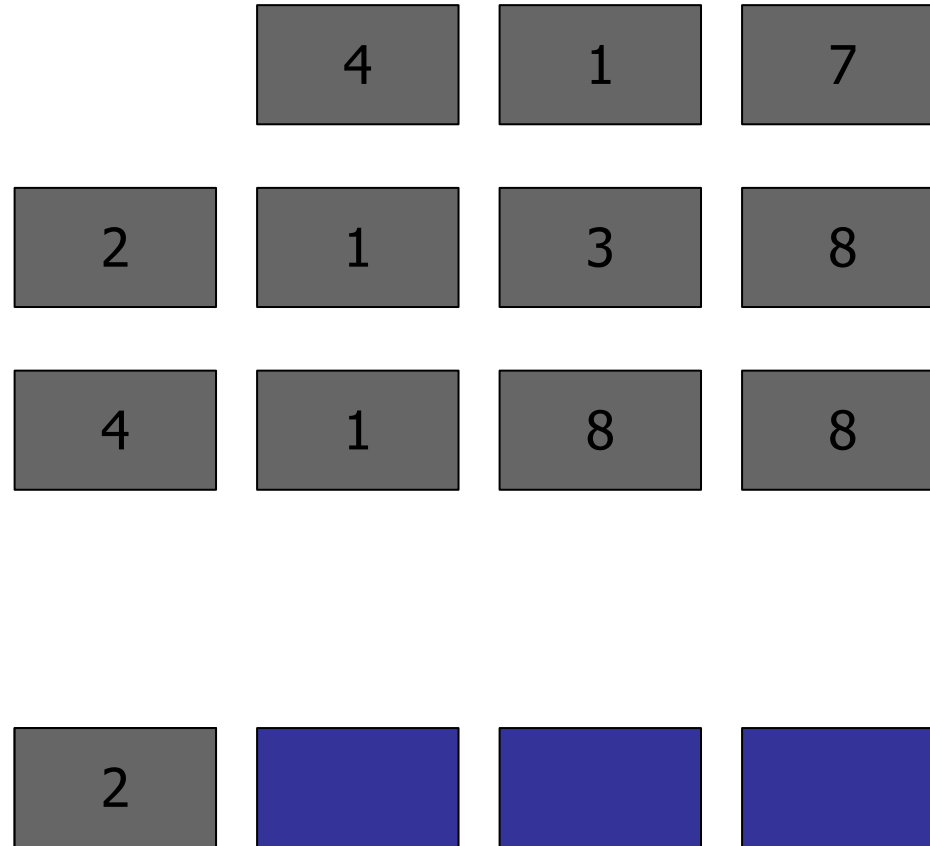
# LRU Example



# LRU Example

Miss: 1

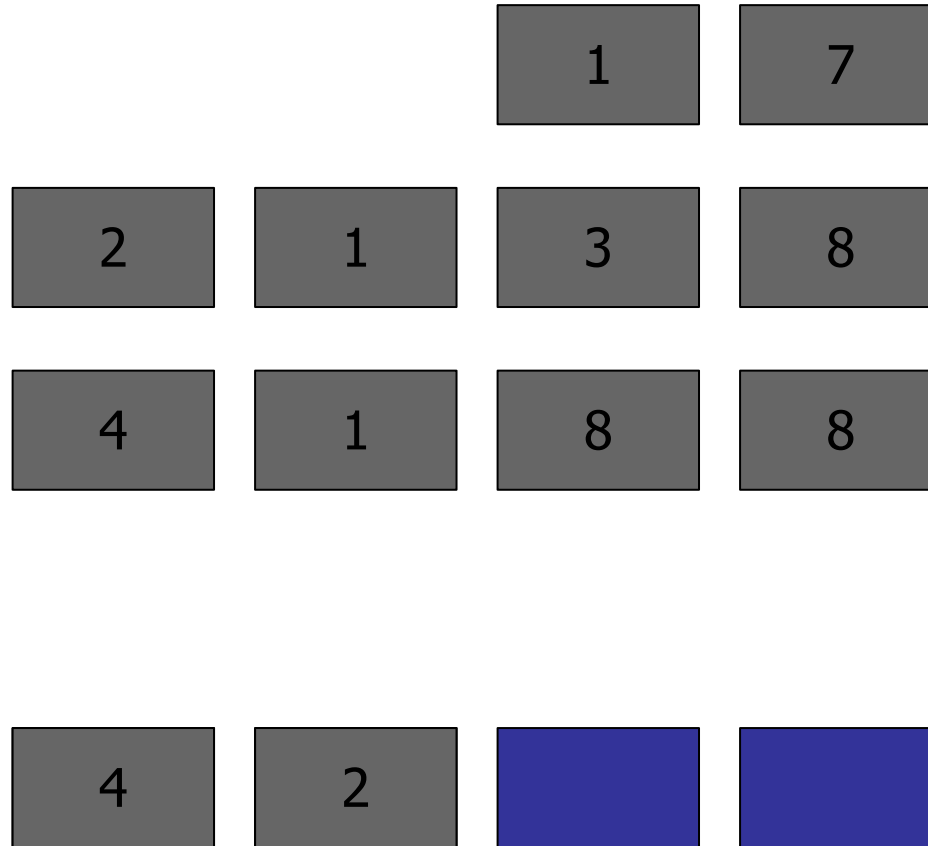
Hit: 0



# LRU Example

Miss: 2

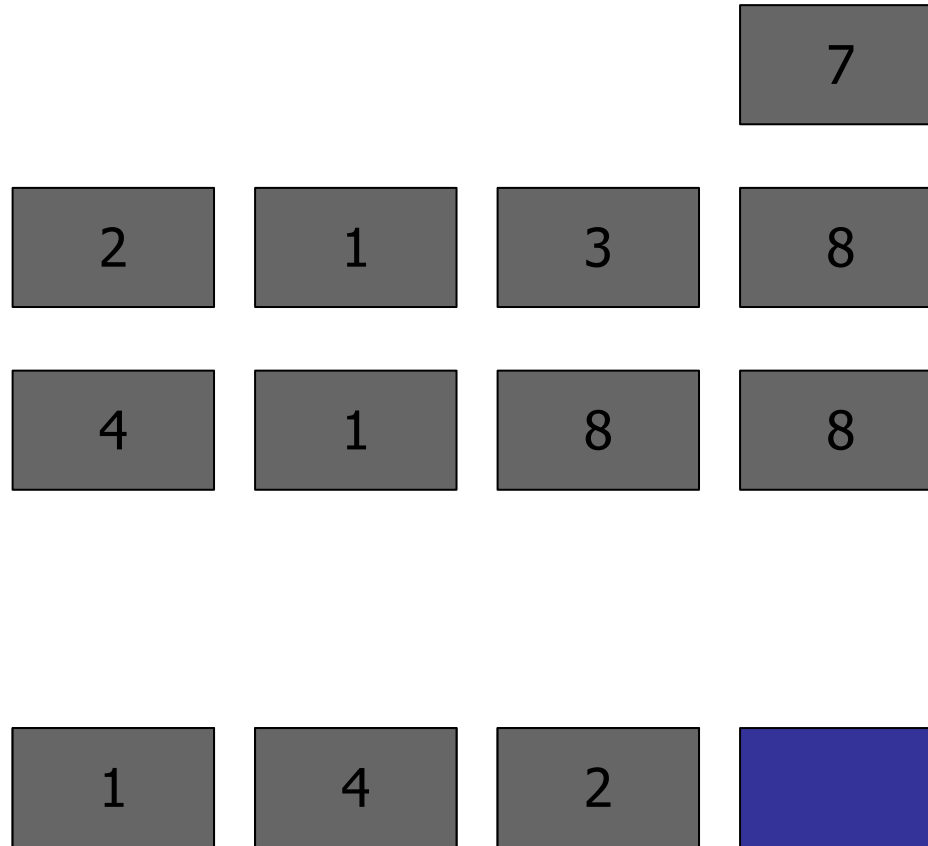
Hit: 0



# LRU Example

Miss: 3

Hit: 0

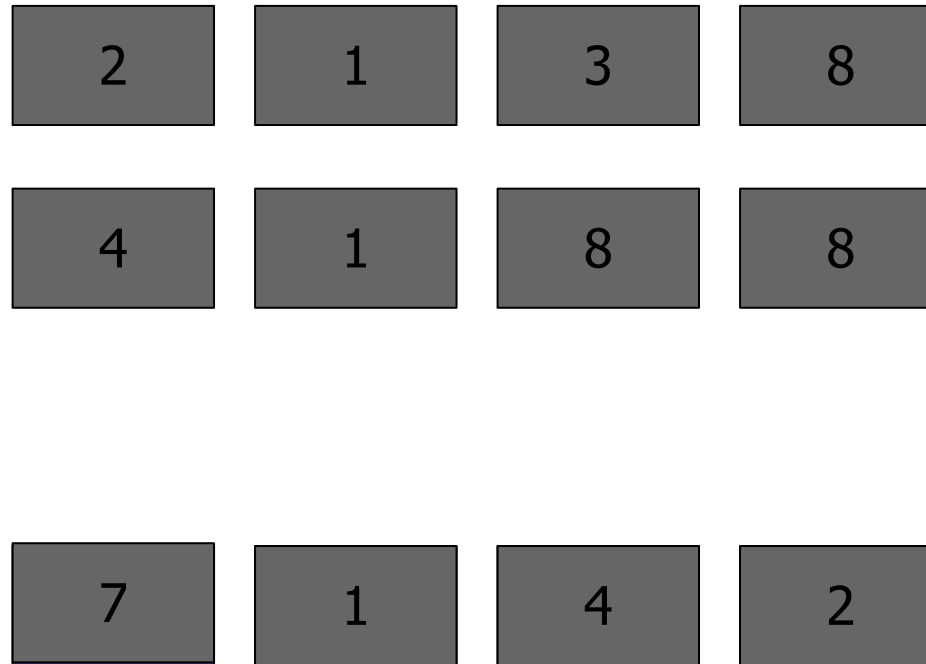




Miss: 4

Hit: 0

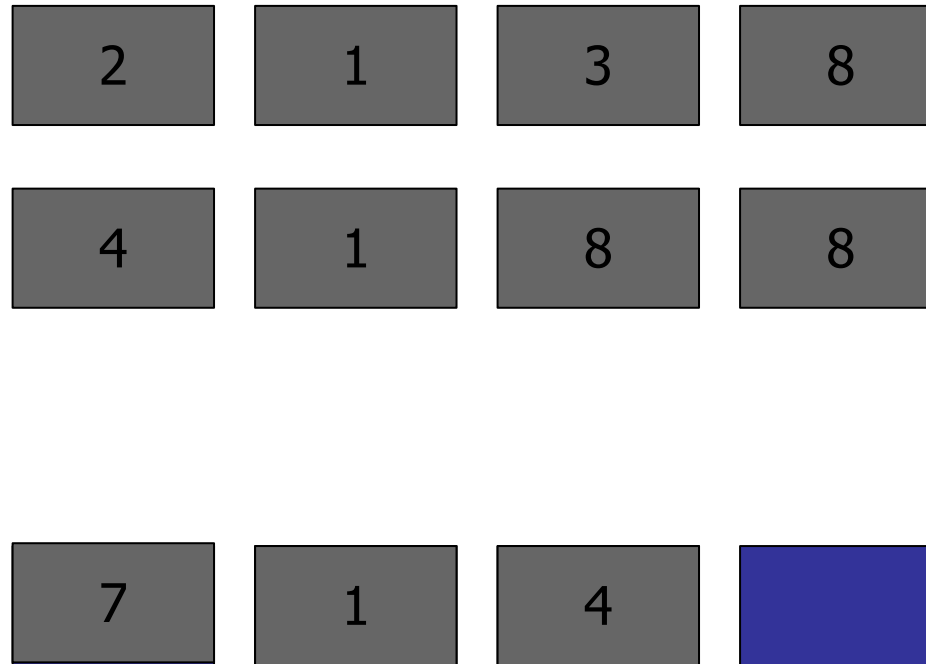
# LRU Example



Miss: 4

Hit: 1

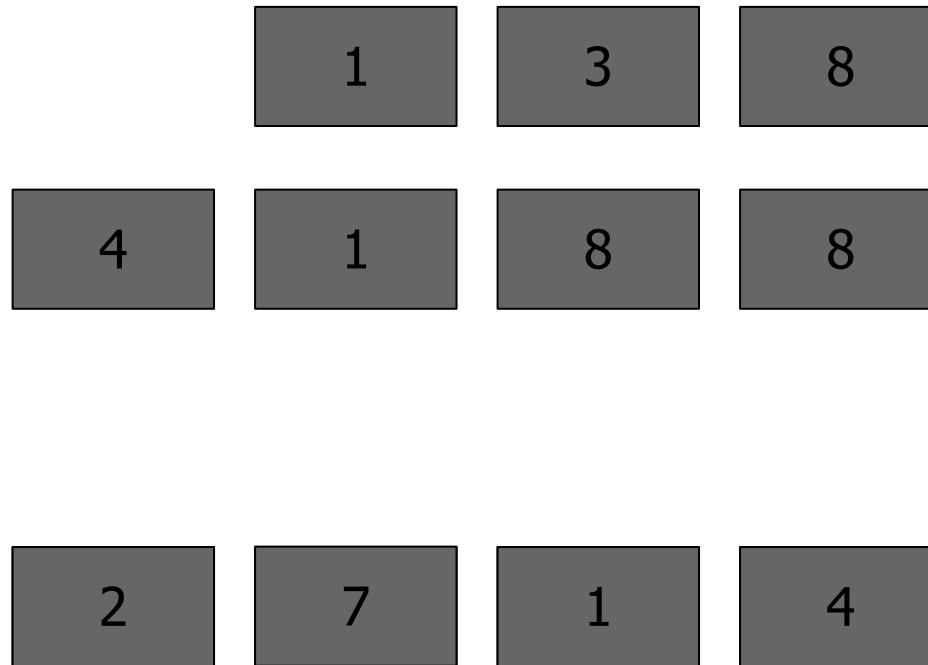
# LRU Example



# LRU Example

Miss: 5

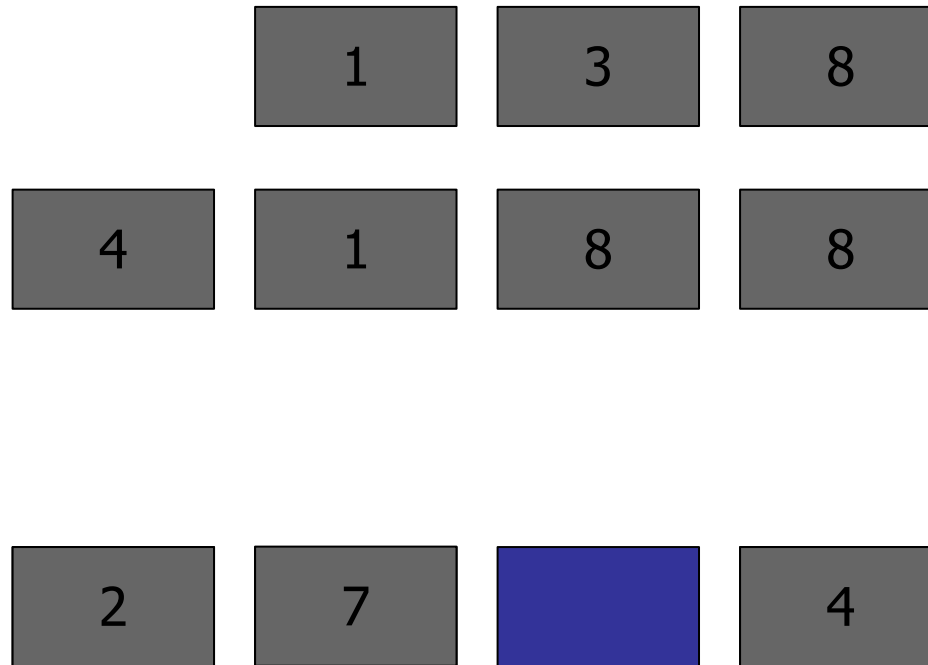
Hit: 1



# LRU Example

Miss: 5

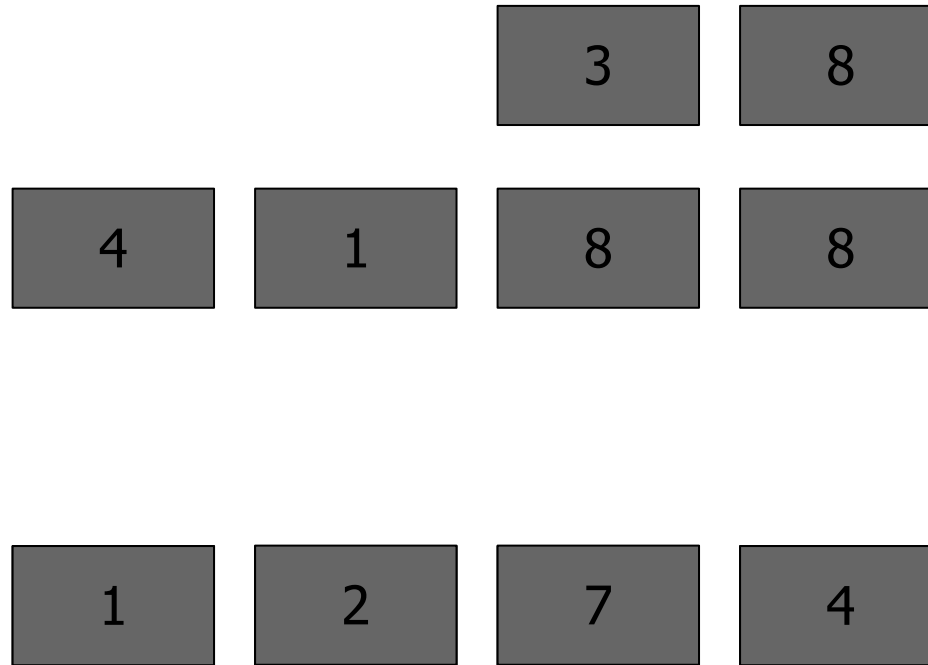
Hit: 2



# LRU Example

Miss: 5

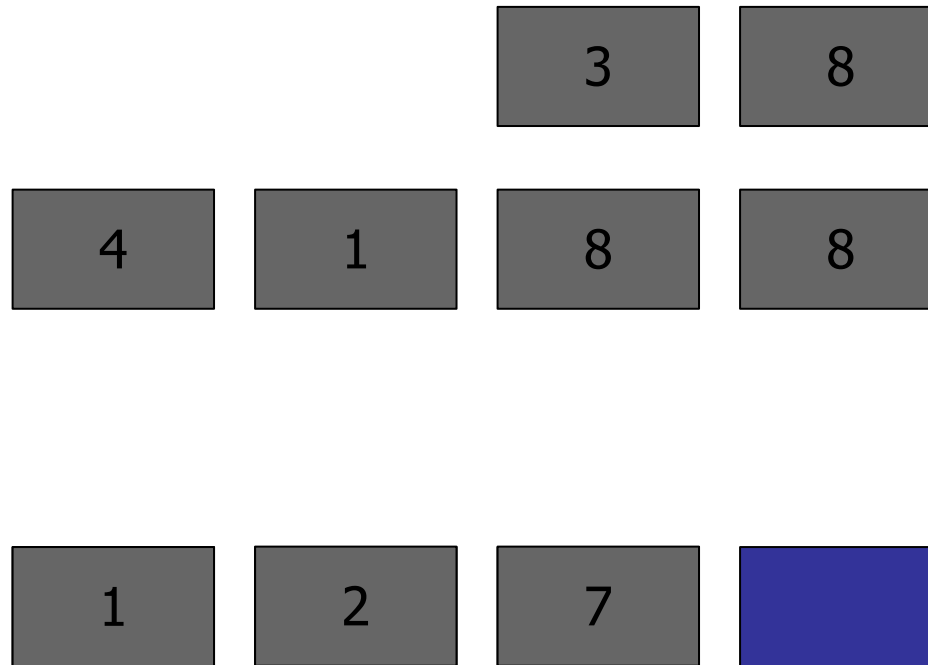
Hit: 2



# LRU Example

Miss: 6

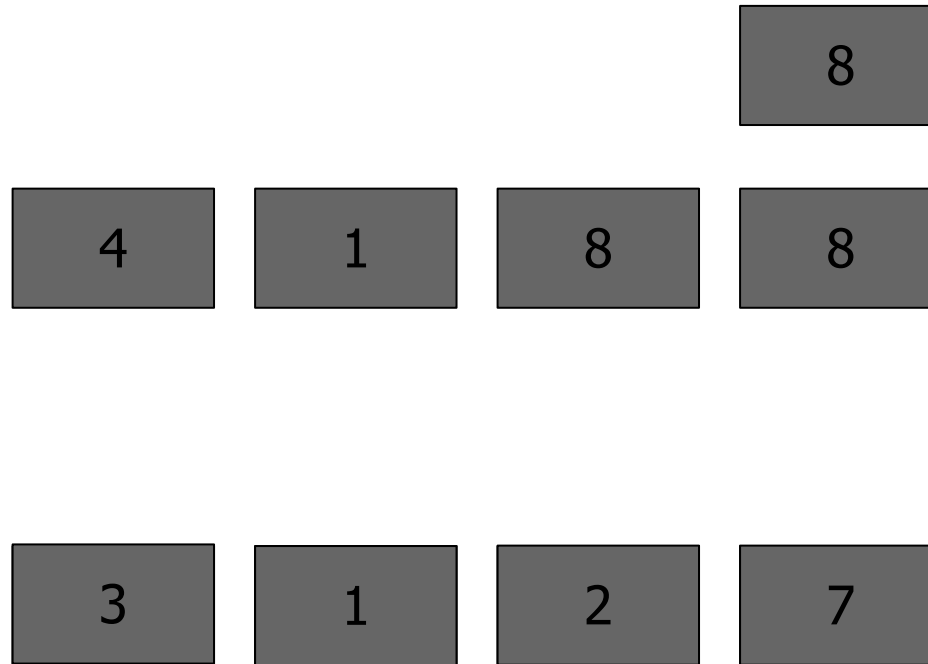
Hit: 2



# LRU Example

Miss: 6

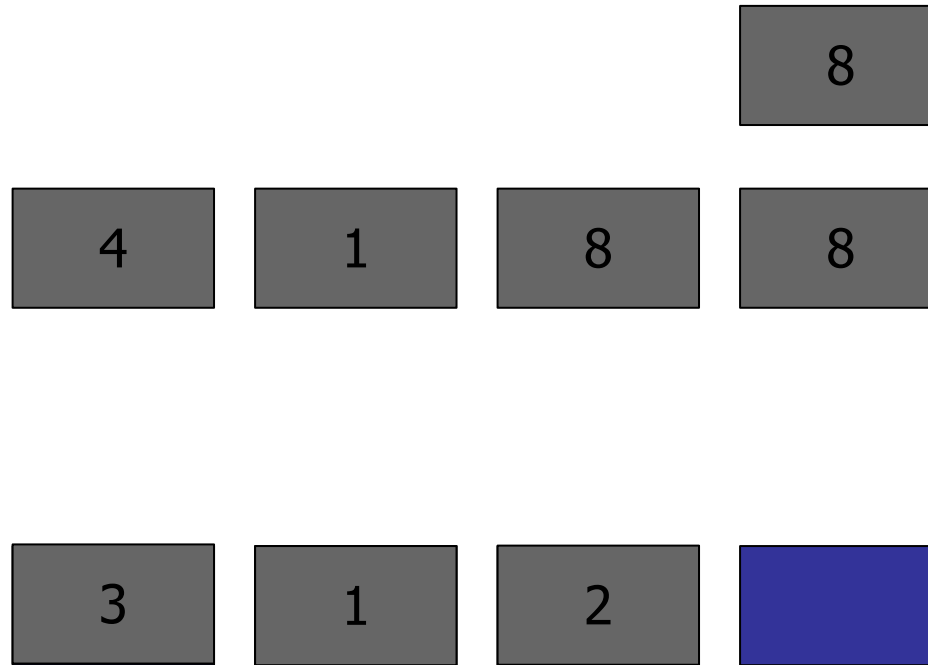
Hit: 2



# LRU Example

Miss: 7

Hit: 2

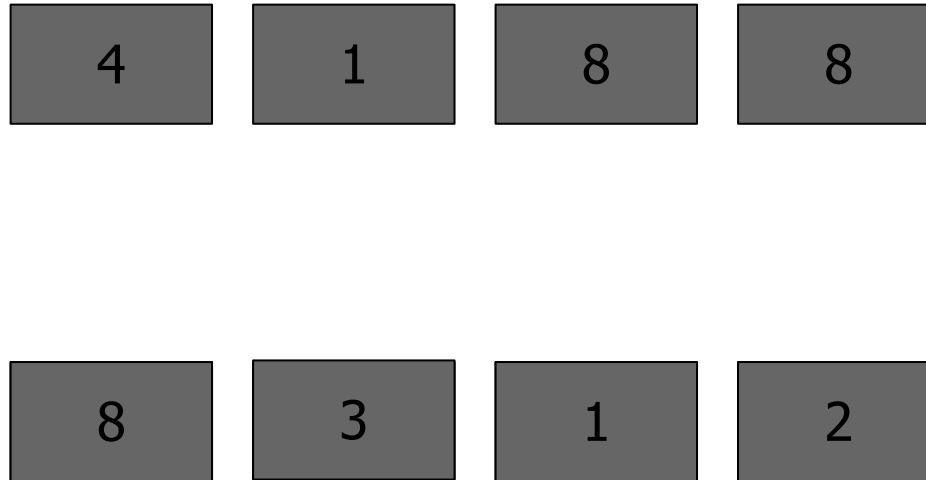




# LRU Example

Miss: 7

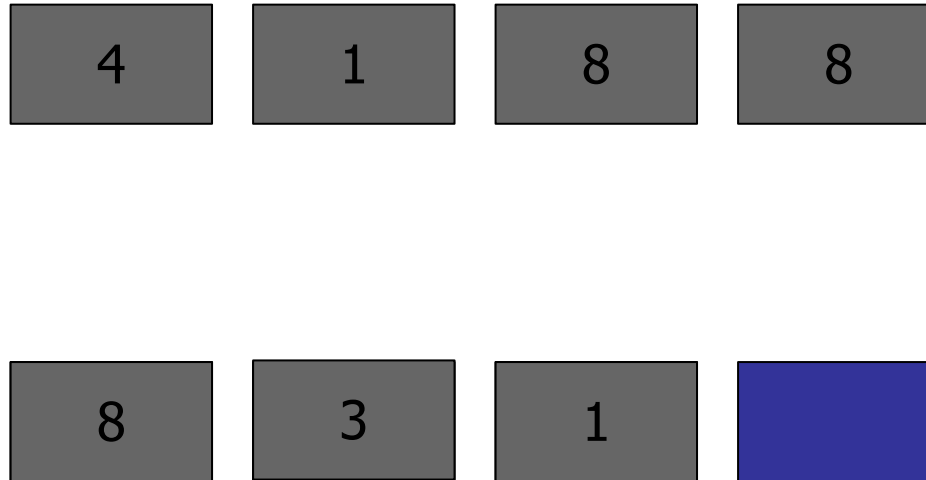
Hit: 2



# LRU Example

Miss: 8

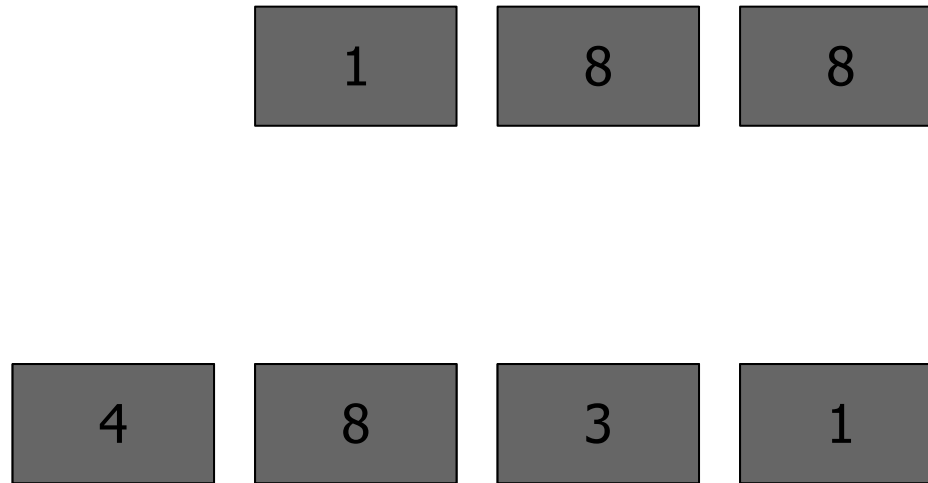
Hit: 2



# LRU Example

Miss: 8

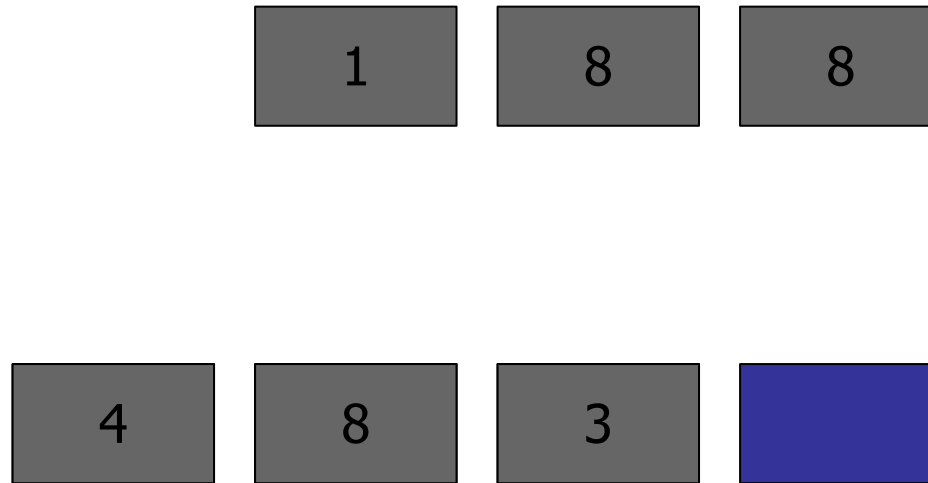
Hit: 2



# LRU Example

Miss: 8

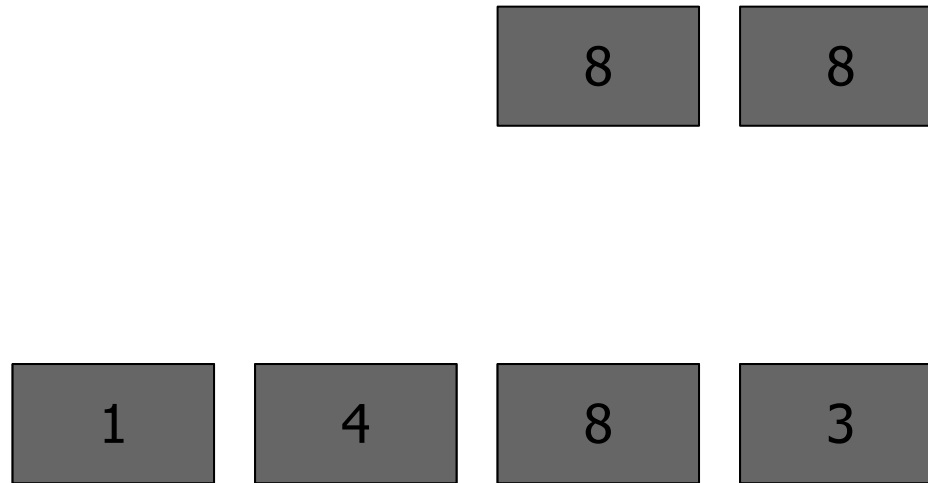
Hit: 3



# LRU Example

Miss: 8

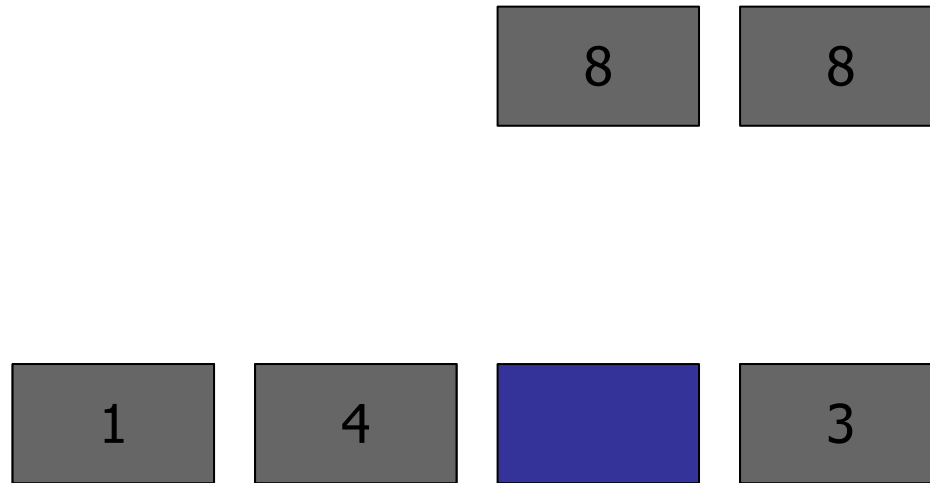
Hit: 3



# LRU Example

Miss: 8

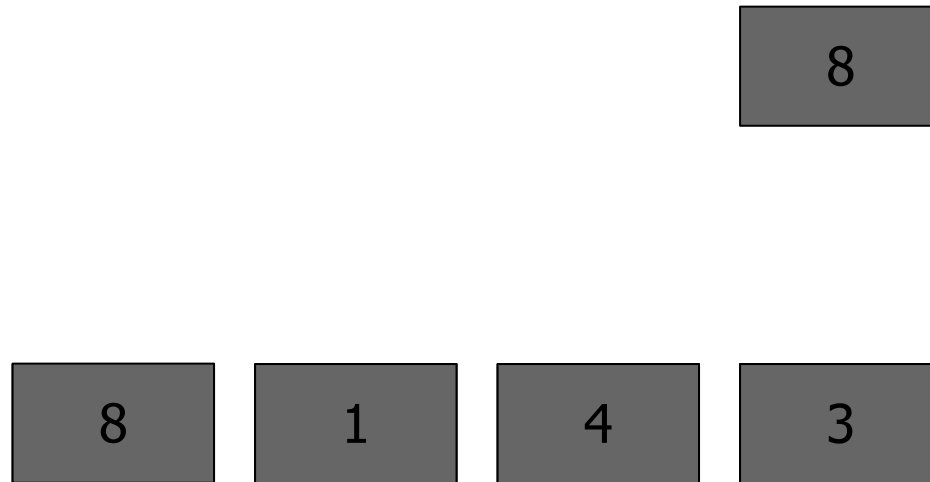
Hit: 4



# LRU Example

Miss: 8

Hit: 4



# LRU Example

Miss: 7

Hit: 5

MR = 62%

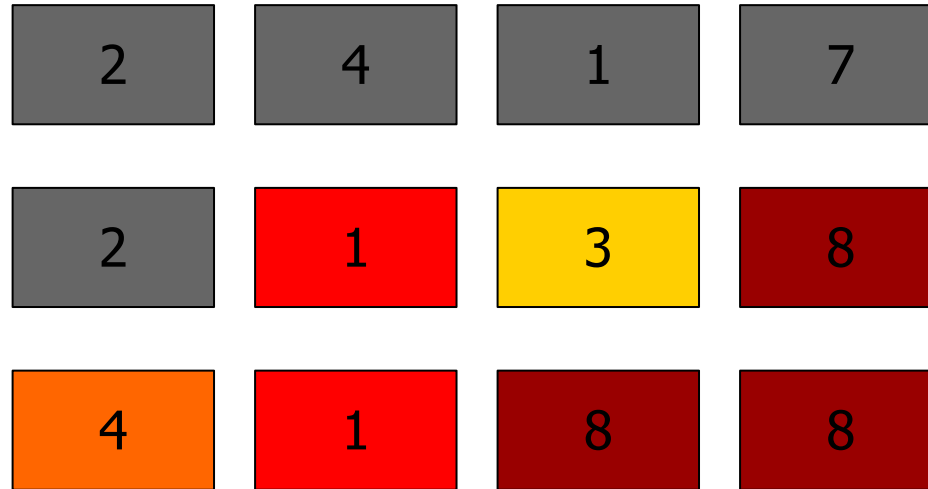
HR = 38%

## Final State of the Cache





# LRU Example



## Final State of the Cache

