

Lecture 5 03/30/19

MULTIPLE Regression → estimate the data

$$\hat{y} = \beta x$$

$$\beta = (x'x)^{-1}x'y$$

ANOVA

$$N = 32$$

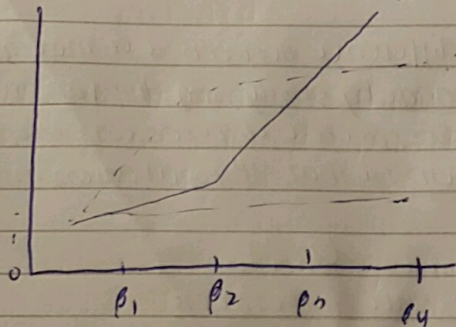
$$n = 8$$

$$y_i = \mu + \alpha_i \beta_j \quad \alpha_i = \mu_i - \mu$$

• write the observations as a huge vector

H_0 : μ_1 and μ_2 are the same

H_1 : at least the mean is different



$$\bar{\alpha} = \alpha \times \# \text{ of comparisons}$$

$$F = \frac{MSB}{MSE}$$

- Divide systematic & unsystematic variance

$$SST = \sum_{i=1}^n \sum_{j=1}^4 (x_{ij} - \bar{x}_{..})^2 \rightarrow \text{overall variance! systematic.}$$

$$SSB = n \sum_{j=1}^4 (\bar{x}_{.j} - \bar{x}_{..})^2$$

need to do it for 4 different means

$$SSE = \sum_{i=1}^n \sum_{j=1}^4 (x_{ij} - \bar{x}_{.j})^2$$

source	df	ss	ms	F	p
β					
error					
total					

Bonferroni

⊗ Tukey

• Reject H_0 if $p_i \leq \frac{\alpha}{M} = 0.008$

$$SE = \sqrt{\frac{MSE}{n}}$$

critical t (confidence intervals) = observed t critical t x SE

- main effects

$$y_{ijk} = \mu + \alpha_i + \beta_j + \alpha\beta_{ij} + \epsilon_{ijk}$$

↑
main effect ↘
 age (main effect)

$$\sum_{k=1}^K \alpha_k = 0$$

- systematic components of variance

$$SST = \sum_i \sum_j \sum_k (x_{ijk} - \bar{x})^2$$

$$SSA = 10 \sum_{i=1}^2 (\bar{x}_{i.} - \bar{x})^2$$

$$SSB = 10 \sum_{j=1}^2 (\bar{x}_{.j} - \bar{x})^2$$

$$SSE = \sum_i \sum_j \sum_k (x_{ijk} - \bar{x}_{ij.})^2$$

$$SST = SSA + SSB + SSE + SSAB$$

$$SSAB = \sum_{j,k} (x_{ijk} - \bar{x}_{i.} - \bar{x}_{.j} + \bar{x})^2$$

source / SS / df / MS / F / P

→ then do ANOVA table after this

- losing df