

## Codeforces Round #148 (Div. 1)

### A. Not Wool Sequences

time limit per test: 1 second

memory limit per test: 256 megabytes

input: standard input

output: standard output

A sequence of non-negative integers  $a_1, a_2, \dots, a_n$  of length  $n$  is called a *wool sequence* if and only if there exists two integers  $l$  and  $r$  ( $1 \leq l \leq r \leq n$ ) such that  $a_l \oplus a_{l+1} \oplus \dots \oplus a_r = 0$ . In other words each wool sequence contains a subsequence of consecutive elements with xor equal to 0.

The expression  $x \oplus y$  means applying the operation of a bitwise xor to numbers  $x$  and  $y$ . The given operation exists in all modern programming languages, for example, in languages C++ and Java it is marked as " $\wedge$ ", in Pascal — as " $\text{xor}$ ".

In this problem you are asked to compute the number of sequences made of  $n$  integers from 0 to  $2^m - 1$  that are not a wool sequence. You should print this number modulo 1000000009 ( $10^9 + 9$ ).

#### Input

The only line of input contains two space-separated integers  $n$  and  $m$  ( $1 \leq n, m \leq 10^5$ ).

#### Output

Print the required number of sequences modulo 1000000009 ( $10^9 + 9$ ) on the only line of output.

#### Sample test(s)

input
3 2
output
6

#### Note

Sequences of length 3 made of integers 0, 1, 2 and 3 that are not a wool sequence are (1, 3, 1), (1, 2, 1), (2, 1, 2), (2, 3, 2), (3, 1, 3) and (3, 2, 3).

## B. Boring Partition

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

This problem is the most boring one you've ever seen.

Given a sequence of integers  $a_1, a_2, \dots, a_n$  and a non-negative integer  $h$ , our goal is to partition the sequence into two subsequences (not necessarily consist of continuous elements). Each element of the original sequence should be contained in exactly one of the result subsequences. Note, that one of the result subsequences can be empty.

Let's define function  $f(a_i, a_j)$  on pairs of distinct elements (that is  $i \neq j$ ) in the original sequence. If  $a_i$  and  $a_j$  are in the same subsequence in the current partition then  $f(a_i, a_j) = a_i + a_j$  otherwise  $f(a_i, a_j) = a_i + a_j + h$ .

Consider all possible values of the function  $f$  for some partition. We'll call the *goodness* of this partition the difference between the maximum value of function  $f$  and the minimum value of function  $f$ .

Your task is to find a partition of the given sequence  $a$  that have the minimal possible goodness among all possible partitions.

### Input

The first line of input contains integers  $n$  and  $h$  ( $2 \leq n \leq 10^5$ ,  $0 \leq h \leq 10^8$ ). In the second line there is a list of  $n$  space-separated integers representing  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i \leq 10^8$ ).

### Output

The first line of output should contain the required minimum goodness.

The second line describes the optimal partition. You should print  $n$  whitespace-separated integers in the second line. The  $i$ -th integer is 1 if  $a_i$  is in the first subsequence otherwise it should be 2.

If there are several possible correct answers you are allowed to print any of them.

### Sample test(s)

input
3 2 1 2 3
output
1 1 2 2

  

input
5 10 0 1 0 2 1
output
3 2 2 2 2 2

### Note

In the first sample the values of  $f$  are as follows:  $f(1, 2) = 1 + 2 + 2 = 5$ ,  $f(1, 3) = 1 + 3 + 2 = 6$  and  $f(2, 3) = 2 + 3 = 5$ . So the difference between maximum and minimum values of  $f$  is 1.

In the second sample the value of  $h$  is large, so it's better for one of the sub-sequences to be empty.

## C. World Eater Brothers

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

You must have heard of the two brothers dreaming of ruling the world. With all their previous plans failed, this time they decided to cooperate with each other in order to rule the world.

As you know there are  $n$  countries in the world. These countries are connected by  $n - 1$  directed roads. If you don't consider direction of the roads there is a unique path between every pair of countries in the world, passing through each road at most once.

Each of the brothers wants to establish his reign in some country, then it's possible for him to control the countries that can be reached from his country using directed roads.

The brothers can rule the world if there exists at most two countries for brothers to choose (and establish their reign in these countries) so that any other country is under control of at least one of them. In order to make this possible they want to change the direction of minimum number of roads. Your task is to calculate this minimum number of roads.

### Input

The first line of input contains an integer  $n$  ( $1 \leq n \leq 3000$ ). Each of the next  $n - 1$  lines contains two space-separated integers  $a_i$  and  $b_i$  ( $1 \leq a_i, b_i \leq n; a_i \neq b_i$ ) saying there is a road from country  $a_i$  to country  $b_i$ .

Consider that countries are numbered from 1 to  $n$ . It's guaranteed that if you don't consider direction of the roads there is a unique path between every pair of countries in the world, passing through each road at most once.

### Output

In the only line of output print the minimum number of roads that their direction should be changed so that the brothers will be able to rule the world.

#### Sample test(s)

input
4 2 1 3 1 4 1
output
1

  

input
5 2 1 2 3 4 3 4 5
output
0

## D. Tape Programming

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

There is a programming language in which every program is a non-empty sequence of "<" and ">" signs and digits. Let's explain how the interpreter of this programming language works. A program is interpreted using movement of instruction pointer (IP) which consists of two parts.

- Current character pointer (CP);
- Direction pointer (DP) which can point left or right;

Initially CP points to the leftmost character of the sequence and DP points to the right.

We repeat the following steps until the first moment that CP points to somewhere outside the sequence.

- If CP is pointing to a digit the interpreter prints that digit then CP moves one step according to the direction of DP. After that the value of the printed digit in the sequence decreases by one. If the printed digit was 0 then it cannot be decreased therefore it's erased from the sequence and the length of the sequence decreases by one.
- If CP is pointing to "<" or ">" then the direction of DP changes to "left" or "right" correspondingly. Then CP moves one step according to DP. If the new character that CP is pointing to is "<" or ">" then the previous character will be erased from the sequence.

If at any moment the CP goes outside of the sequence the execution is terminated.

It's obvious the every program in this language terminates after some steps.

We have a sequence  $s_1, s_2, \dots, s_n$  of "<", ">" and digits. You should answer  $q$  queries. Each query gives you  $l$  and  $r$  and asks how many of each digit will be printed if we run the sequence  $s_l, s_{l+1}, \dots, s_r$  as an independent program in this language.

### Input

The first line of input contains two integers  $n$  and  $q$  ( $1 \leq n, q \leq 10^5$ ) — represents the length of the sequence  $s$  and the number of queries.

The second line contains  $s$ , a sequence of "<", ">" and digits (0 . . 9) written from left to right. Note, that the characters of  $s$  are not separated with spaces.

The next  $q$  lines each contains two integers  $l_i$  and  $r_i$  ( $1 \leq l_i \leq r_i \leq n$ ) — the  $i$ -th query.

### Output

For each query print 10 space separated integers:  $x_0, x_1, \dots, x_9$  where  $x_i$  equals the number of times the interpreter prints  $i$  while running the corresponding program. Print answers to the queries in the order they are given in input.

### Sample test(s)

input
7 4 1>3>22< 1 3 4 7 7 7 1 7
output
0 1 0 1 0 0 0 0 0 0 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 2 3 2 1 0 0 0 0 0 0

## E. Meeting Her

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

Urpal lives in a big city. He has planned to meet his lover tonight.

The city has  $n$  junctions numbered from 1 to  $n$ . The junctions are connected by  $m$  directed streets, all the roads have equal length. Urpal lives in junction  $a$  and the date is planned in a restaurant in junction  $b$ . He wants to use public transportation to get to junction  $b$ . There are  $k$  bus transportation companies. At the beginning of every second, a bus from the  $i$ -th company chooses a random shortest path between junction  $s_i$  and junction  $t_i$  and passes through it. There might be no path from  $s_i$  to  $t_i$ . In that case no bus will leave from  $s_i$  to  $t_i$ . If a bus passes through a junction where Urpal stands, he can get on the bus. He can also get off the bus at any junction along the path.

Now Urpal wants to know if it's possible to go to the date using public transportation in a finite amount of time (the time of travel is the sum of length of the traveled roads) and what is the minimum number of buses he should take in the worst case.

**At any moment Urpal knows only his own position and the place where the date will be. When he gets on the bus he knows only the index of the company of this bus. Of course Urpal knows the city map and the the pairs  $(s_i, t_i)$  for each company.**

Note that Urpal doesn't know buses velocity.

### Input

The first line of the input contains four integers  $n, m, a, b$  ( $2 \leq n \leq 100$ ;  $0 \leq m \leq n \cdot (n - 1)$ ;  $1 \leq a, b \leq n$ ;  $a \neq b$ ).

The next  $m$  lines contain two integers each  $u_i$  and  $v_i$  ( $1 \leq u_i, v_i \leq n$ ;  $u_i \neq v_i$ ) describing a directed road from junction  $u_i$  to junction  $v_i$ . All roads in the input will be distinct.

The next line contains an integer  $k$  ( $0 \leq k \leq 100$ ). There will be  $k$  lines after this, each containing two integers  $s_i$  and  $t_i$  ( $1 \leq s_i, t_i \leq n$ ;  $s_i \neq t_i$ ) saying there is a bus route starting at  $s_i$  and ending at  $t_i$ . Please note that there might be no path from  $s_i$  to  $t_i$ , this case is described in the problem statement.

### Output

In the only line of output print the minimum number of buses Urpal should get on on his way in the worst case. If it's not possible to reach the destination in the worst case print -1.

### Sample test(s)

input
7 8 1 7 1 2 1 3 2 4 3 4 4 6 4 5 6 7 5 7 3 2 7 1 4 5 7
output
2

  

input
4 4 1 2 1 2 1 3 2 4 3 4 1 1 4
output
-1