

## Codeforces Round #445 (Div. 1, based on Technocup 2018 Elimination Round 3)

### A. Petya and Catacombs

time limit per test: 1 second  
 memory limit per test: 256 megabytes  
 input: standard input  
 output: standard output

A very brave explorer Petya once decided to explore Paris catacombs. Since Petya is not really experienced, his exploration is just walking through the catacombs.

Catacombs consist of several rooms and bidirectional passages between some pairs of them. Some passages can connect a room to itself and since the passages are built on different depths they do not intersect each other. Every minute Petya arbitrary chooses a passage from the room he is currently in and then reaches the room on the other end of the passage in exactly one minute. When he enters a room at minute  $i$ , he makes a note in his logbook with number  $t_i$ :

- If Petya has visited this room before, he writes down the minute he was in this room last time;
- Otherwise, Petya writes down an arbitrary non-negative integer strictly less than current minute  $i$ .

Initially, Petya was in one of the rooms at minute 0, he didn't write down number  $t_0$ .

At some point during his wandering Petya got tired, threw out his logbook and went home. Vasya found his logbook and now he is curious: what is the minimum possible number of rooms in Paris catacombs according to Petya's logbook?

#### Input

The first line contains a single integer  $n$  ( $1 \leq n \leq 2 \cdot 10^5$ ) — then number of notes in Petya's logbook.

The second line contains  $n$  non-negative integers  $t_1, t_2, \dots, t_n$  ( $0 \leq t_i < i$ ) — notes in the logbook.

#### Output

In the only line print a single integer — the minimum possible number of rooms in Paris catacombs.

#### Examples

<b>input</b>
2 0 0
<b>output</b>
2
<b>input</b>
5 0 1 0 1 3
<b>output</b>
3

#### Note

In the first sample, sequence of rooms Petya visited could be, for example  $1 \rightarrow 1 \rightarrow 2$ ,  $1 \rightarrow 2 \rightarrow 1$  or  $1 \rightarrow 2 \rightarrow 3$ . The minimum possible number of rooms is 2.

In the second sample, the sequence could be  $1 \rightarrow 2 \rightarrow 3 \rightarrow 1 \rightarrow 2 \rightarrow 1$ .

## B. Restoration of string

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

A substring of some string is called the most frequent, if the number of its occurrences is not less than number of occurrences of any other substring.

You are given a set of strings. A string (not necessarily from this set) is called good if all elements of the set are the most frequent substrings of this string. Restore the non-empty good string with minimum length. If several such strings exist, restore lexicographically minimum string. If there are no good strings, print "NO" (without quotes).

A substring of a string is a contiguous subsequence of letters in the string. For example, "ab", "c", "abc" are substrings of string "abc", while "ac" is not a substring of that string.

The number of occurrences of a substring in a string is the number of starting positions in the string where the substring occurs. These occurrences could overlap.

String  $a$  is lexicographically smaller than string  $b$ , if  $a$  is a prefix of  $b$ , or  $a$  has a smaller letter at the first position where  $a$  and  $b$  differ.

### Input

The first line contains integer  $n$  ( $1 \leq n \leq 10^5$ ) — the number of strings in the set.

Each of the next  $n$  lines contains a non-empty string consisting of lowercase English letters. It is guaranteed that the strings are distinct.

The total length of the strings doesn't exceed  $10^5$ .

### Output

Print the non-empty good string with minimum length. If several good strings exist, print lexicographically minimum among them. Print "NO" (without quotes) if there are no good strings.

### Examples

input
4 mail ai lru cf
output
cfmailru

input
3 kek preceq cheburek
output
NO

### Note

One can show that in the first sample only two good strings with minimum length exist: "cfmailru" and "mailrucf". The first string is lexicographically minimum.

## C. Maximum Element

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

One day Petya was solving a very interesting problem. But although he used many optimization techniques, his solution still got Time limit exceeded verdict. Petya conducted a thorough analysis of his program and found out that his function for finding maximum element in an array of  $n$  positive integers was too slow. Desperate, Petya decided to use a somewhat unexpected optimization using parameter  $k$ , so now his function contains the following code:

```
int fast_max(int n, int a[]) {
    int ans = 0;
    int offset = 0;
    for (int i = 0; i < n; ++i)
        if (ans < a[i]) {
            ans = a[i];
            offset = 0;
        } else {
            offset = offset + 1;
            if (offset == k)
                return ans;
        }
    return ans;
}
```

That way the function iteratively checks array elements, storing the intermediate maximum, and if after  $k$  consecutive iterations that maximum has not changed, it is returned as the answer.

Now Petya is interested in fault rate of his function. He asked you to find the number of permutations of integers from 1 to  $n$  such that the return value of his function on those permutations is not equal to  $n$ . Since this number could be very big, output the answer modulo  $10^9 + 7$ .

### Input

The only line contains two integers  $n$  and  $k$  ( $1 \leq n, k \leq 10^6$ ), separated by a space — the length of the permutations and the parameter  $k$ .

### Output

Output the answer to the problem modulo  $10^9 + 7$ .

### Examples

<b>input</b>
5 2
<b>output</b>
22

<b>input</b>
5 3
<b>output</b>
6

<b>input</b>
6 3
<b>output</b>
84

### Note

Permutations from second example:

[4, 1, 2, 3, 5], [4, 1, 3, 2, 5], [4, 2, 1, 3, 5], [4, 2, 3, 1, 5], [4, 3, 1, 2, 5], [4, 3, 2, 1, 5].

## D. Symmetric Projections

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

You are given a set of  $n$  points on the plane. A line containing the origin is called good, if projection of the given set to this line forms a symmetric multiset of points. Find the total number of good lines.

Multiset is a set where equal elements are allowed.

Multiset is called symmetric, if there is a point  $P$  on the plane such that the multiset is [centrally symmetric](#) in respect of point  $P$ .

### Input

The first line contains a single integer  $n$  ( $1 \leq n \leq 2000$ ) — the number of points in the set.

Each of the next  $n$  lines contains two integers  $x_i$  and  $y_i$  ( $-10^6 \leq x_i, y_i \leq 10^6$ ) — the coordinates of the points. It is guaranteed that no two points coincide.

### Output

If there are infinitely many good lines, print  $-1$ .

Otherwise, print single integer — the number of good lines.

### Examples

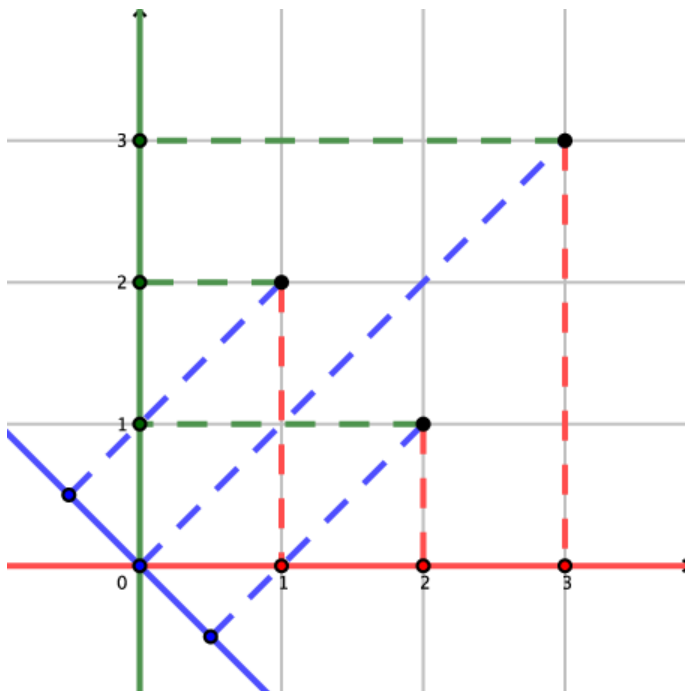
input
3 1 2 2 1 3 3
output
3

input
2 4 3 1 2
output
-1

### Note

Picture to the first sample test:



In the second sample, any line containing the origin is good.

## E. Mod Mod Mod

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

You are given a sequence of integers  $a_1, a_2, \dots, a_n$ . Let  $f(x, n) = x \bmod a_n$ , and  $f(x, i) = (x \bmod a_i) + f(x \bmod a_i, i + 1)$  for  $1 \leq i < n$ . Here, **mod** denotes the modulus operation. Find the maximum value of  $f(x, 1)$  over all nonnegative integers  $x$ .

### Input

The first line contains a single integer  $n$  ( $1 \leq n \leq 200000$ ) — the length of the sequence.

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 10^{13}$ ) — the elements of the sequence.

### Output

Output a single integer — the maximum value of  $f(x, 1)$  over all nonnegative integers  $x$ .

### Examples

<b>input</b>
2 10 5
<b>output</b>
13
<b>input</b>
5 5 4 3 2 1
<b>output</b>
6
<b>input</b>
4 5 10 5 10
<b>output</b>
16

### Note

In the first example you can choose, for example,  $x = 19$ .

In the second example you can choose, for example,  $x = 3$  or  $x = 2$ .