

## Codeforces Round #296 (Div. 1)

### A. Glass Carving

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

Leonid wants to become a glass carver (the person who creates beautiful artworks by cutting the glass). He already has a rectangular  $w$  mm  $\times$   $h$  mm sheet of glass, a diamond glass cutter and lots of enthusiasm. What he lacks is understanding of what to carve and how.

In order not to waste time, he decided to practice the technique of carving. To do this, he makes vertical and horizontal cuts through the entire sheet. This process results in making smaller rectangular fragments of glass. Leonid does not move the newly made glass fragments. In particular, a cut divides each fragment of glass that it goes through into smaller fragments.

After each cut Leonid tries to determine what area the largest of the currently available glass fragments has. Since there appear more and more fragments, this question takes him more and more time and distracts him from the fascinating process.

Leonid offers to divide the labor — he will cut glass, and you will calculate the area of the maximum fragment after each cut. Do you agree?

#### Input

The first line contains three integers  $w, h, n$  ( $2 \leq w, h \leq 200\,000$ ,  $1 \leq n \leq 200\,000$ ).

Next  $n$  lines contain the descriptions of the cuts. Each description has the form  $H\ y$  or  $V\ x$ . In the first case Leonid makes the horizontal cut at the distance  $y$  millimeters ( $1 \leq y \leq h - 1$ ) from the lower edge of the original sheet of glass. In the second case Leonid makes a vertical cut at distance  $x$  ( $1 \leq x \leq w - 1$ ) millimeters from the left edge of the original sheet of glass. It is guaranteed that Leonid won't make two identical cuts.

#### Output

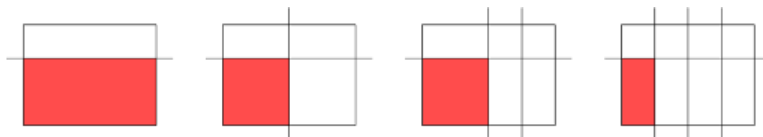
After each cut print on a single line the area of the maximum available glass fragment in  $\text{mm}^2$ .

#### Sample test(s)

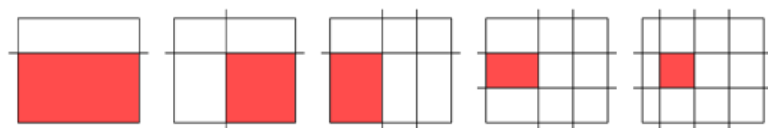
input
4 3 4 H 2 V 2 V 3 V 1
output
8 4 4 2
input
7 6 5 H 4 V 3 V 5 H 2 V 1
output
28 16 12 6 4

#### Note

Picture for the first sample test:



Picture for the second sample test:



## B. Clique Problem

time limit per test: 2 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

The clique problem is one of the most well-known NP-complete problems. Under some simplification it can be formulated as follows. Consider an undirected graph  $G$ . It is required to find a subset of vertices  $C$  of the maximum size such that any two of them are connected by an edge in graph  $G$ . Sounds simple, doesn't it? Nobody yet knows an algorithm that finds a solution to this problem in polynomial time of the size of the graph. However, as with many other NP-complete problems, the clique problem is easier if you consider a specific type of a graph.

Consider  $n$  distinct points on a line. Let the  $i$ -th point have the coordinate  $x_i$  and weight  $w_i$ . Let's form graph  $G$ , whose vertices are these points and edges connect exactly the pairs of points  $(i, j)$ , such that the distance between them is not less than the sum of their weights, or more formally:  
 $|x_i - x_j| \geq w_i + w_j$ .

Find the size of the maximum clique in such graph.

### Input

The first line contains the integer  $n$  ( $1 \leq n \leq 200\,000$ ) — the number of points.

Each of the next  $n$  lines contains two numbers  $x_i, w_i$  ( $0 \leq x_i \leq 10^9, 1 \leq w_i \leq 10^9$ ) — the coordinate and the weight of a point. All  $x_i$  are different.

### Output

Print a single number — the number of vertexes in the maximum clique of the given graph.

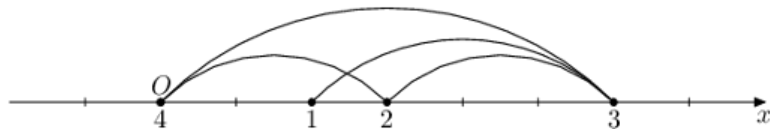
### Sample test(s)

input
4 2 3 3 1 6 1 0 2
output
3

### Note

If you happen to know how to solve this problem without using the specific properties of the graph formulated in the problem statement, then you are able to get a prize of one million dollars!

The picture for the sample test.



## C. Data Center Drama

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

The project of a data center of a Big Software Company consists of  $n$  computers connected by  $m$  cables. Simply speaking, each computer can be considered as a box with multiple cables going out of the box. Very Important Information is transmitted along each cable in one of the two directions. As the data center plan is not yet approved, it wasn't determined yet in which direction information will go along each cable. The cables are put so that each computer is connected with each one, perhaps through some other computers.

The person in charge of the cleaning the data center will be Claudia Ivanova, the janitor. She loves to tie cables into bundles using cable ties. For some reasons, she groups the cables sticking out of a computer into groups of two, and if it isn't possible, then she gets furious and attacks the computer with the water from the bucket.

It should also be noted that due to the specific physical characteristics of the Very Important Information, it is strictly forbidden to connect in one bundle two cables where information flows in different directions.

The management of the data center wants to determine how to send information along each cable so that Claudia Ivanova is able to group all the cables coming out of each computer into groups of two, observing the condition above. Since it may not be possible with the existing connections plan, you are allowed to add the minimum possible number of cables to the scheme, and then you need to determine the direction of the information flow for each cable (yes, sometimes data centers are designed based on the janitors' convenience...)

### Input

The first line contains two numbers,  $n$  and  $m$  ( $1 \leq n \leq 100\,000$ ,  $1 \leq m \leq 200\,000$ ) — the number of computers and the number of the already present cables, respectively.

Each of the next lines contains two numbers  $a_i, b_i$  ( $1 \leq a_i, b_i \leq n$ ) — the indices of the computers connected by the  $i$ -th cable. The data centers often have a very complex structure, so a pair of computers may have more than one pair of cables between them and some cables may connect a computer with itself.

### Output

In the first line print a single number  $p$  ( $p \geq m$ ) — the minimum number of cables in the final scheme.

In each of the next  $p$  lines print a pair of numbers  $c_i, d_i$  ( $1 \leq c_i, d_i \leq n$ ), describing another cable. Such entry means that information will go along a certain cable in direction from  $c_i$  to  $d_i$ .

Among the cables you printed there should be all the cables presented in the original plan in some of two possible directions. It is guaranteed that there is a solution where  $p$  doesn't exceed  $500\,000$ .

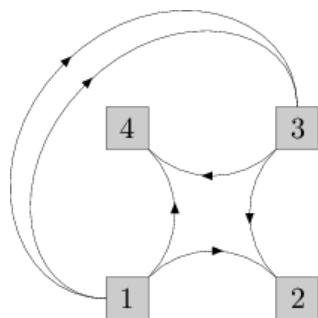
If there are several possible solutions with minimum possible value of  $p$ , print any of them.

### Sample test(s)

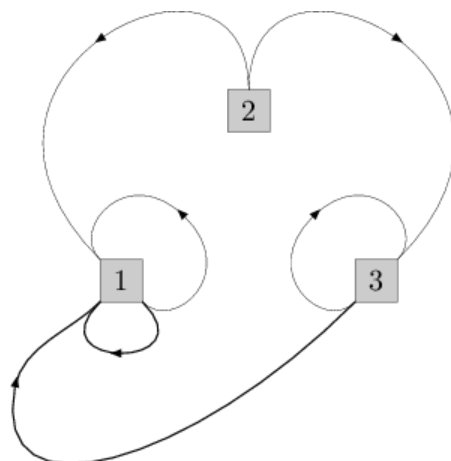
input
4 6 1 2 2 3 3 4 4 1 1 3 1 3
output
6 1 2 3 4 1 4 3 2 1 3 1 3
input
3 4 1 2 2 3 1 1 3 3
output
6 2 1 2 3 1 1 3 3 3 1 1 1

### Note

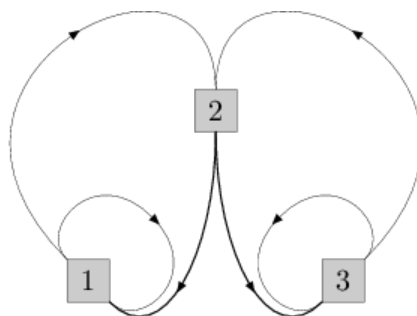
Picture for the first sample test. The tied pairs of cables are shown going out from the same point.



Picture for the second test from the statement. The added cables are drawn in bold.



Alternative answer for the second sample test:



## D. Fuzzy Search

time limit per test: 3 seconds

memory limit per test: 256 megabytes

input: standard input

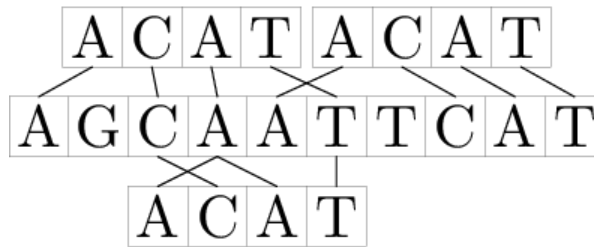
output: standard output

Leonid works for a small and promising start-up that works on decoding the human genome. His duties include solving complex problems of finding certain patterns in long strings consisting of letters 'A', 'T', 'G' and 'C'.

Let's consider the following scenario. There is a fragment of a human DNA chain, recorded as a string  $S$ . To analyze the fragment, you need to find all occurrences of string  $T$  in a string  $S$ . However, the matter is complicated by the fact that the original chain fragment could contain minor mutations, which, however, complicate the task of finding a fragment. Leonid proposed the following approach to solve this problem.

Let's write down integer  $k \geq 0$  — the error threshold. We will say that string  $T$  occurs in string  $S$  on position  $i$  ( $1 \leq i \leq |S| - |T| + 1$ ), if after putting string  $T$  along with this position, each character of string  $T$  corresponds to the same character of the same value in string  $S$  at the distance of at most  $k$ . More formally, for any  $j$  ( $1 \leq j \leq |T|$ ) there must exist such  $p$  ( $1 \leq p \leq |S|$ ), that  $|(i + j - 1) - p| \leq k$  and  $S[p] = T[j]$ .

For example, corresponding to the given definition, string "ACAT" occurs in string "AGCAATTCAT" in positions 2, 3 and 6.



Note that at  $k = 0$  the given definition transforms to a simple definition of the occurrence of a string in a string.

Help Leonid by calculating in how many positions the given string  $T$  occurs in the given string  $S$  with the given error threshold.

### Input

The first line contains three integers  $|S|$ ,  $|T|$ ,  $k$  ( $1 \leq |T| \leq |S| \leq 200\,000$ ,  $0 \leq k \leq 200\,000$ ) — the lengths of strings  $S$  and  $T$  and the error threshold.

The second line contains string  $S$ .

The third line contains string  $T$ .

Both strings consist only of uppercase letters 'A', 'T', 'G' and 'C'.

### Output

Print a single number — the number of occurrences of  $T$  in  $S$  with the error threshold  $k$  by the given definition.

### Sample test(s)

input
10 4 1 AGCAATTCAT ACAT
output
3

### Note

If you happen to know about the structure of the human genome a little more than the author of the problem, and you are not impressed with Leonid's original approach, do not take everything described above seriously.

## E. Triangles 3000

time limit per test: 5 seconds

memory limit per test: 512 megabytes

input: standard input

output: standard output

You are given a set  $L = \{l_1, l_2, \dots, l_n\}$  of  $n$  pairwise non-parallel lines on the Euclidean plane. The  $i$ -th line is given by an equation in the form of  $a_i x + b_i y = c_i$ .  $L$  doesn't contain three lines coming through the same point.

A subset of three distinct lines is chosen equiprobably. Determine the expected value of the area of the triangle formed by the three lines.

### Input

The first line of the input contains integer  $n$  ( $3 \leq n \leq 3000$ ).

Each of the next lines contains three integers  $a_i, b_i, c_i$  ( $-100 \leq a_i, b_i \leq 100, a_i^2 + b_i^2 > 0, -10\,000 \leq c_i \leq 10\,000$ ) — the coefficients defining the  $i$ -th line.

It is guaranteed that no two lines are parallel. Besides, any two lines intersect at angle at least  $10^{-4}$  radians.

If we assume that  $I$  is a set of points of pairwise intersection of the lines (i. e.  $I = \{l_i \cap l_j \mid i < j\}$ ), then for any point  $a \in I$  it is true that the coordinates of  $a$  do not exceed  $10^6$  by their absolute values. Also, for any two distinct points  $a, b \in I$  the distance between  $a$  and  $b$  is no less than  $10^{-5}$ .

### Output

Print a single real number equal to the sought expected value. Your answer will be checked with the absolute or relative error  $10^{-4}$ .

### Sample test(s)

input
4 1 0 0 0 1 0 1 1 2 -1 1 -1
output
1.25

### Note

A sample from the statement is shown below. There are four triangles on the plane, their areas are 0.25, 0.5, 2, 2.25.

