

## Codeforces Round #286 (Div. 1)

### A. Mr. Kitayuta, the Treasure Hunter

time limit per test: 1 second

memory limit per test: 256 megabytes

input: standard input

output: standard output

The Shuseki Islands are an archipelago of 30001 small islands in the Yutampo Sea. The islands are evenly spaced along a line, numbered from 0 to 30000 from the west to the east. These islands are known to contain many treasures. There are  $n$  gems in the Shuseki Islands in total, and the  $i$ -th gem is located on island  $p_i$ .

Mr. Kitayuta has just arrived at island 0. With his great jumping ability, he will repeatedly perform jumps between islands to the east according to the following process:

- First, he will jump from island 0 to island  $d$ .
- After that, he will continue jumping according to the following rule. Let  $l$  be the length of the previous jump, that is, if his previous jump was from island  $prev$  to island  $cur$ , let  $l = cur - prev$ . He will perform a jump of length  $l - 1$ ,  $l$  or  $l + 1$  to the east. That is, he will jump to island  $(cur + l - 1)$ ,  $(cur + l)$  or  $(cur + l + 1)$  (if they exist). The length of a jump must be positive, that is, he cannot perform a jump of length 0 when  $l = 1$ . If there is no valid destination, he will stop jumping.

Mr. Kitayuta will collect the gems on the islands visited during the process. Find the maximum number of gems that he can collect.

#### Input

The first line of the input contains two space-separated integers  $n$  and  $d$  ( $1 \leq n, d \leq 30000$ ), denoting the number of the gems in the Shuseki Islands and the length of the Mr. Kitayuta's first jump, respectively.

The next  $n$  lines describe the location of the gems. The  $i$ -th of them ( $1 \leq i \leq n$ ) contains a integer  $p_i$  ( $d \leq p_1 \leq p_2 \leq \dots \leq p_n \leq 30000$ ), denoting the number of the island that contains the  $i$ -th gem.

#### Output

Print the maximum number of gems that Mr. Kitayuta can collect.

#### Sample test(s)

input
4 10 10 21 27 27
output
3

input
8 8 9 19 28 36 45 55 66 78
output
6

input
13 7 8 8 9 16 17 17 18 21 23 24 24

26
30
output
4

**Note**

In the first sample, the optimal route is  $0 \rightarrow 10 \text{ (+1 gem)} \rightarrow 19 \rightarrow 27 \text{ (+2 gems)} \rightarrow \dots$

In the second sample, the optimal route is  $0 \rightarrow 8 \rightarrow 15 \rightarrow 21 \rightarrow 28 \text{ (+1 gem)} \rightarrow 36 \text{ (+1 gem)} \rightarrow 45 \text{ (+1 gem)} \rightarrow 55 \text{ (+1 gem)} \rightarrow 66 \text{ (+1 gem)} \rightarrow 78 \text{ (+1 gem)} \rightarrow \dots$

In the third sample, the optimal route is  $0 \rightarrow 7 \rightarrow 13 \rightarrow 18 \text{ (+1 gem)} \rightarrow 24 \text{ (+2 gems)} \rightarrow 30 \text{ (+1 gem)} \rightarrow \dots$

## B. Mr. Kitayuta's Technology

time limit per test: 1 second  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Shuseki Kingdom is the world's leading nation for innovation and technology. There are  $n$  cities in the kingdom, numbered from 1 to  $n$ .

Thanks to Mr. Kitayuta's research, it has finally become possible to construct teleportation pipes between two cities. A teleportation pipe will connect two cities unidirectionally, that is, a teleportation pipe from city  $x$  to city  $y$  cannot be used to travel from city  $y$  to city  $x$ . The transportation within each city is extremely developed, therefore if a pipe from city  $x$  to city  $y$  and a pipe from city  $y$  to city  $z$  are both constructed, people will be able to travel from city  $x$  to city  $z$  instantly.

Mr. Kitayuta is also involved in national politics. He considers that the transportation between the  $m$  pairs of city  $(a_i, b_i)$  ( $1 \leq i \leq m$ ) is important. He is planning to construct teleportation pipes so that for each important pair  $(a_i, b_i)$ , it will be possible to travel from city  $a_i$  to city  $b_i$  by using one or more teleportation pipes (but not necessarily from city  $b_i$  to city  $a_i$ ). Find the minimum number of teleportation pipes that need to be constructed. So far, no teleportation pipe has been constructed, and there is no other effective transportation between cities.

### Input

The first line contains two space-separated integers  $n$  and  $m$  ( $2 \leq n \leq 10^5$ ,  $1 \leq m \leq 10^5$ ), denoting the number of the cities in Shuseki Kingdom and the number of the important pairs, respectively.

The following  $m$  lines describe the important pairs. The  $i$ -th of them ( $1 \leq i \leq m$ ) contains two space-separated integers  $a_i$  and  $b_i$  ( $1 \leq a_i, b_i \leq n$ ,  $a_i \neq b_i$ ), denoting that it must be possible to travel from city  $a_i$  to city  $b_i$  by using one or more teleportation pipes (but not necessarily from city  $b_i$  to city  $a_i$ ). It is guaranteed that all pairs  $(a_i, b_i)$  are distinct.

### Output

Print the minimum required number of teleportation pipes to fulfill Mr. Kitayuta's purpose.

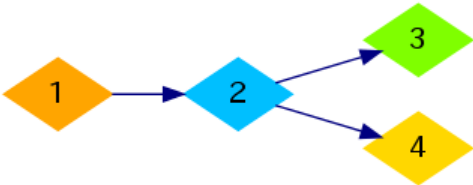
#### Sample test(s)

input
4 5 1 2 1 3 1 4 2 3 2 4
output
3

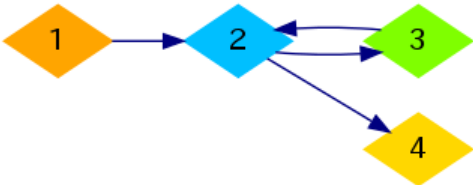
input
4 6 1 2 1 4 2 3 2 4 3 2 3 4
output
4

### Note

For the first sample, one of the optimal ways to construct pipes is shown in the image below:



For the second sample, one of the optimal ways is shown below:



# C. Mr. Kitayuta vs. Bamboos

time limit per test: 2 seconds  
memory limit per test: 256 megabytes  
input: standard input  
output: standard output

Mr. Kitayuta's garden is planted with  $n$  bamboos. (Bamboos are tall, fast-growing tropical plants with hollow stems.) At the moment, the height of the  $i$ -th bamboo is  $h_i$  meters, and it grows  $a_i$  meters at the end of each day.

Actually, Mr. Kitayuta hates these bamboos. He once attempted to cut them down, but failed because their stems are too hard. Mr. Kitayuta have not given up, however. He has crafted Magical Hammer with his intelligence to drive them into the ground.

He can use Magical Hammer at most  $k$  times during each day, due to his limited Magic Power. Each time he beat a bamboo with Magical Hammer, its height decreases by  $p$  meters. If the height would become negative by this change, it will become 0 meters instead (it does not disappear). In other words, if a bamboo whose height is  $h$  meters is beaten with Magical Hammer, its new height will be  $\max(0, h - p)$  meters. It is possible to beat the same bamboo more than once in a day.

Mr. Kitayuta will fight the bamboos for  $m$  days, starting today. His purpose is to minimize the height of the tallest bamboo after  $m$  days (that is,  $m$  iterations of "Mr. Kitayuta beats the bamboos and then they grow"). Find the lowest possible height of the tallest bamboo after  $m$  days.

### Input

The first line of the input contains four space-separated integers  $n, m, k$  and  $p$  ( $1 \leq n \leq 10^5, 1 \leq m \leq 5000, 1 \leq k \leq 10, 1 \leq p \leq 10^9$ ). They represent the number of the bamboos in Mr. Kitayuta's garden, the duration of Mr. Kitayuta's fight in days, the maximum number of times that Mr. Kitayuta beat the bamboos during each day, and the power of Magic Hammer, respectively.

The following  $n$  lines describe the properties of the bamboos. The  $i$ -th of them ( $1 \leq i \leq n$ ) contains two space-separated integers  $h_i$  and  $a_i$  ( $0 \leq h_i \leq 10^9, 1 \leq a_i \leq 10^9$ ), denoting the initial height and the growth rate of the  $i$ -th bamboo, respectively.

### Output

Print the lowest possible height of the tallest bamboo after  $m$  days.

#### Sample test(s)

input
3 1 2 5 10 10 10 10 15 2
output
17
input
2 10 10 1000000000 0 10 0 10
output
10
input
5 3 3 10 9 5 9 2 4 7 9 10 3 8
output
14

## D. Mr. Kitayuta's Colorful Graph

time limit per test: 4 seconds

memory limit per test: 256 megabytes

input: standard input

output: standard output

Mr. Kitayuta has just bought an undirected graph with  $n$  vertices and  $m$  edges. The vertices of the graph are numbered from 1 to  $n$ . Each edge, namely edge  $i$ , has a color  $c_i$ , connecting vertex  $a_i$  and  $b_i$ .

Mr. Kitayuta wants you to process the following  $q$  queries.

In the  $i$ -th query, he gives you two integers -  $u_i$  and  $v_i$ .

Find the number of the colors that satisfy the following condition: the edges of that color connect vertex  $u_i$  and vertex  $v_i$  directly or indirectly.

### Input

The first line of the input contains space-separated two integers -  $n$  and  $m$  ( $2 \leq n \leq 10^5$ ,  $1 \leq m \leq 10^5$ ), denoting the number of the vertices and the number of the edges, respectively.

The next  $m$  lines contain space-separated three integers -  $a_i$ ,  $b_i$  ( $1 \leq a_i < b_i \leq n$ ) and  $c_i$  ( $1 \leq c_i \leq m$ ). Note that there can be multiple edges between two vertices. However, there are no multiple edges of the same color between two vertices, that is, if  $i \neq j$ ,  $(a_i, b_i, c_i) \neq (a_j, b_j, c_j)$ .

The next line contains a integer-  $q$  ( $1 \leq q \leq 10^5$ ), denoting the number of the queries.

Then follows  $q$  lines, containing space-separated two integers -  $u_i$  and  $v_i$  ( $1 \leq u_i, v_i \leq n$ ). It is guaranteed that  $u_i \neq v_i$ .

### Output

For each query, print the answer in a separate line.

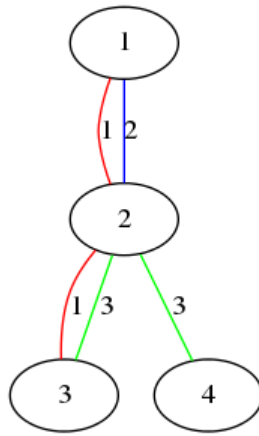
### Sample test(s)

input
4 5 1 2 1 1 2 2 2 3 1 2 3 3 2 4 3 3 1 2 3 4 1 4
output
2 1 0

input
5 7 1 5 1 2 5 1 3 5 1 4 5 1 1 2 2 2 3 2 3 4 2 5 1 5 5 1 2 5 1 5 1 4
output
1 1 1 1 2

### Note

Let's consider the first sample.



The figure above shows the first sample.

- Vertex 1 and vertex 2 are connected by color 1 and 2.
- Vertex 3 and vertex 4 are connected by color 3.
- Vertex 1 and vertex 4 are not connected by any single color.

## E. Mr. Kitayuta's Gift

time limit per test: 6 seconds  
memory limit per test: 768 megabytes  
input: standard input  
output: standard output

Mr. Kitayuta has kindly given you a string  $s$  consisting of lowercase English letters. You are asked to insert exactly  $n$  lowercase English letters into  $s$  to make it a palindrome. (A *palindrome* is a string that reads the same forward and backward. For example, "noon", "testset" and "a" are all palindromes, while "test" and "kitayuta" are not.) You can choose any  $n$  lowercase English letters, and insert each of them to any position of  $s$ , possibly to the beginning or the end of  $s$ . You have to insert exactly  $n$  letters even if it is possible to turn  $s$  into a palindrome by inserting less than  $n$  letters.

Find the number of the palindromes that can be obtained in this way, modulo 10007.

### Input

The first line contains a string  $s$  ( $1 \leq |s| \leq 200$ ). Each character in  $s$  is a lowercase English letter.

The second line contains an integer  $n$  ( $1 \leq n \leq 10^9$ ).

### Output

Print the number of the palindromes that can be obtained, modulo 10007.

### Sample test(s)

input
revive 1
output
1

input
add 2
output
28

### Note

For the first sample, you can obtain the palindrome "reviver" by inserting 'r' to the end of "revive".

For the second sample, the following 28 palindromes can be obtained: "adada", "adbda", ..., "adzda", "dadad" and "ddadd".