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1 Basic

1.1 makefile

```
CPP = g++ -std=c++11 -02

name = $(basename $(file))
type = $(suffix $(file))
exe = $(name).out

$(exe): $(file)
ifeq ($(type),.cpp)
  $(CPP) -D AC -o $(exe) $(name).cpp
endif

clean:
  rm *.out
```

1.2 /.vimrc

```
"顯示行號
set nu
set tabstop=4 " tab 的字元數
set ai
set smartindent
set softtabstop=4
set shiftwidth=4
set cindent
se ai ar sm nu rnu is
se mouse=a bs=2 so=6 ts=4 ttm=100
nmap <F2> :! gedit %<.in %<*.in &<CR>
nmap <F4> :! date > %<.pt; cat -n % > %<.pt; lpr %<.pt
    <CR>
nmap <F8> :! clear ; python3 % <CR>
nmap <F9> :! clear ; make file=%; for i in %<*.in; do</pre>
   echo $i; ./%<.out < $i; echo -e "\n"; done <CR>
nmap <F10> :! clear ; make file=%; ./%<.out <CR>
nmap <C-I> :! read -p "CASE:" CASE; gedit %<_$CASE.in <</pre>
    CR>
```

1.3 default code

```
#include <bits/stdc++.h>
using namespace std;

int main(){
    #ifndef AC
        freopen("","r",stdin);
#endif
        ios_base::sync_with_stdio(false);
        cin.tie(0);
}
```

1.4 debug list

```
模板要記得 init
把邊界條件都加入測資
邊界條件 (過程溢位,題目數據範圍),會不會爆 long long
是否讀錯題目
環狀or凸包問題一定要每種都算n次
比較容易有問題的地方換人寫
注意公式有沒有推錯或抄錯
精度誤差 sqrt(大大的東西) + EPS
測試 %lld or %I64d
喇分 random_suffle 隨機演算法
```

2 Flow

2.1 Dinic

```
const int INF = 1<<29;</pre>
struct Dinic{ //O(VVE)
  static const int MAXV = 5003;
  struct Edge{
    int from, to, cap, flow;
  int n, m, s, t, d[MAXV], cur[MAXV];
 vector<Edge> edges;
  vector<int> G[MAXV];
  void init(int _n=MAXV){
    edges.clear();
    for (int i=0; i<_n; i++)G[i].clear();</pre>
  }
  void AddEdge(int from, int to, int cap){
    edges.push_back( {from,to,cap,0} );
    edges.push_back( {to,from,0,0} );
    m = edges.size();
    G[from].push_back(m-2);
    G[to].push_back(m-1);
  bool dinicBFS(){
    memset(d,-1,sizeof(d));
    queue<int> que;
    que.push(s); d[s]=0;
    while (!que.empty()){
      int u = que.front(); que.pop();
      for (int ei:G[u]){
        Edge &e = edges[ei];
        if (d[e.to]<0 && e.cap>e.flow){
          d[e.to]=d[u]+1;
          que.push(e.to);
        }
      }
    }
    return d[t]>=0;
  int dinicDFS(int u, int a){
    if (u==t || a==0)return a;
    int flow=0, f;
    for (int &i=cur[u]; i<(int)G[u].size(); i++){</pre>
      Edge &e = edges[ G[u][i] ];
      if (d[u]+1!=d[e.to])continue;
      f = dinicDFS(e.to, min(a, e.cap-e.flow) );
      if (f>0){
        e.flow += f;
        edges[ G[u][i]^1 ].flow -=f;
        flow += f;
        a -= f;
        if (a==0)break;
      }
    return flow;
  int maxflow(int s, int t){
    this->s = s, this->t = t;
    int flow=0, mf;
    while ( dinicBFS() ){
      memset(cur,0,sizeof(cur));
      while ( (mf=dinicDFS(s,INF)) )flow+=mf;
    return flow;
  }
}dinic;
// s=0, t=1;
int fnd(int id ,int out=0){
```

```
// out=0 入點 out=1 出點
static int spr=1;
//spr=2 時每個點分成入點,出點
return id*spr+out+2;
```

2.2 KM

```
struct KM{
// Maximum Bipartite Weighted Matching (Perfect Match)
  static const int MXN = 650;
  static const int INF = 2147483647; // long long
  int n,match[MXN],vx[MXN],vy[MXN];
  int edge[MXN][MXN],lx[MXN],ly[MXN],slack[MXN];
  // ^^^ long long
  void init(int _n){
    n = _n;
     for (int i=0; i<n; i++)</pre>
       for (int j=0; j<n; j++)</pre>
         edge[i][j] = 0;
  }
  void add_edge(int x, int y, int w){ // long long
     edge[x][y] = w;
  bool DFS(int x){
     vx[x] = 1;
     for (int y=0; y<n; y++){</pre>
       if (vy[y]) continue;
       if (lx[x]+ly[y] > edge[x][y]){
         slack[y] = min(slack[y], lx[x]+ly[y]-edge[x][y
             ]);
      } else {
         vy[y] = 1;
         if (match[y] == -1 \mid | DFS(match[y])){
           match[y] = x;
           return true;
         }
      }
    }
    return false;
  int solve(){
     fill(match, match+n,-1);
     fill(lx,lx+n,-INF);
     fill(ly,ly+n,0);
     for (int i=0; i<n; i++)</pre>
       for (int j=0; j<n; j++)</pre>
         lx[i] = max(lx[i], edge[i][j]);
     for (int i=0; i<n; i++){</pre>
       fill(slack,slack+n,INF);
       while (true){
         fill(vx,vx+n,0);
         fill(vy,vy+n,0);
         if ( DFS(i) ) break;
         int d = INF; // long long
         for (int j=0; j<n; j++)</pre>
           if (!vy[j]) d = min(d, slack[j]);
         for (int j=0; j<n; j++){
  if (vx[j]) lx[j] -= d;</pre>
           if (vy[j]) ly[j] += d;
           else slack[j] -= d;
         }
      }
    int res=0;
    for (int i=0; i<n; i++)</pre>
      res += edge[match[i]][i];
     return res;
  }
}graph;
```

```
const int MAX_N = 400 + 10;
const ll INF64 = 0x3f3f3f3f3f3f3f3f1L;
int nl , nr;
int pre[MAX_N];
ll slack[MAX_N];
ll W[MAX_N][MAX_N];
ll lx[MAX_N] , ly[MAX_N];
int mx[MAX_N] , my[MAX_N];
bool vx[MAX_N] , vy[MAX_N];
void augment(int u) {
    if(!u) return;
    augment(mx[pre[u]]);
    mx[pre[u]] = u;
    my[u] = pre[u];
inline void match(int x) {
    queue<int> que;
    que.push(x);
    while(1) {
        while(!que.empty()) {
            x = que.front();
            que.pop();
            vx[x] = 1;
            REP1(y , 1 , nr) {
                if(vy[y]) continue;
                ll t = lx[x] + ly[y] - W[x][y];
                if(t > 0) {
                    if(slack[y] >= t) slack[y] = t ,
                        pre[y] = x;
                    continue;
                }
                pre[y] = x;
                if(!my[y]) {
                    augment(y);
                    return;
                vy[y] = 1;
                que.push(my[y]);
        ll t = INF64;
        REP1(y , 1 , nr) if(!vy[y]) t = min(t , slack[y])
            ]);
        REP1(x , 1 , nl) if(vx[x]) lx[x] = t;
        REP1(y, 1, nr) {
            if(vy[y]) ly[y] += t;
            else slack[y] -= t;
        REP1(y , 1 , nr) {
            if(vy[y] || slack[y]) continue;
            if(!my[y]) {
                augment(y);
                return;
            vy[y] = 1;
            que.push(my[y]);
        }
    }
int main() {
    int m;
    RI(nl , nr , m);
    nr = max(nl , nr);
    while(m--) {
        int x , y;
        ll w;
        RI(x, y, w);
        W[x][y] = w;
        lx[x] = max(lx[x], w);
    REP1(i , 1 , nl) {
        REP1(x , 1 , nl) vx[x] = 0;
        REP1(y , 1 , nr) vy[y] = 0 , slack[y] = INF64;
        match(i);
    ll ans = 0LL:
    REP1(x , 1 , nl) ans += W[x][mx[x]];
```

2.4 min cost max flow

```
// from: https://github.com/bobogei81123/bcw_codebook/
     blob/master/codes/Graph/Flow/CostFlow.cpp
typedef pair<long long, long long> pll;
struct CostFlow {
  static const int MXN = 205;
  static const long long INF = 102938475610293847LL;
  struct Edge {
    int v, r;
    long long f, c;
  };
  int n, s, t, prv[MXN], prvL[MXN], inq[MXN];
  long long dis[MXN], fl, cost;
  vector<Edge> E[MXN];
  void init(int _n, int _s, int _t) {
   n = _n; s = _s; t = _t;
    for (int i=0; i<n; i++) E[i].clear();</pre>
    fl = cost = 0;
  }
  void add_edge(int u, int v, long long f, long long c)
     E[u].PB(\{v, SZ(E[v]), f, c\});
    E[v].PB({u, SZ(E[u])-1, 0, -c});
  pll flow() {
    while (true) {
       for (int i=0; i<n; i++) {</pre>
         dis[i] = INF;
         inq[i] = 0;
       dis[s] = 0;
       queue<int> que;
       que.push(s);
       while (!que.empty()) {
         int u = que.front(); que.pop();
         inq[u] = 0;
         for (int i=0; i<SZ(E[u]); i++) {</pre>
           int v = E[u][i].v;
           long long w = E[u][i].c;
           if (E[u][i].f > 0 && dis[v] > dis[u] + w) {
             prv[v] = u; prvL[v] = i;
             dis[v] = dis[u] + w;
             if (!inq[v]) {
               inq[v] = 1;
               que.push(v);
             }
           }
        }
       if (dis[t] == INF) break;
       long long tf = INF;
       for (int v=t, u, l; v!=s; v=u) {
         u=prv[v]; l=prvL[v];
         tf = min(tf, E[u][l].f);
       for (int v=t, u, l; v!=s; v=u) {
        u=prv[v]; l=prvL[v];
         E[u][l].f -= tf;
         E[v][E[u][l].r].f += tf;
       cost += tf * dis[t];
       fl += tf;
    return {fl, cost};
|}flow;
```

3 Geometry

3.1 2D Point Template

```
typedef double T;
struct Point {
 T x, y;
 Point (T _x=0, T _y=0):x(_x),y(_y){}
  bool operator < (const Point &b)const{</pre>
    return atan2(y,x) < atan2(b.y,b.x);</pre>
  bool operator == (const Point &b)const{
    return atan2(y,x) == atan2(b.y,b.x);
  Point operator + (const Point &b)const{
    return Point(x+b.x,y+b.y);
  Point operator - (const Point &b)const{
    return Point(x-b.x,y-b.y);
  T operator * (const Point &b)const{
    return x*b.x + y*b.y;
  T operator % (const Point &b)const{
    return x*b.y - y*b.x;
  Point operator * (const T &d)const{
    return Point(d*x,d*y);
 T abs2() { return x*x+y*y; }
 T abs() { return sqrt( abs2() ); }
};
typedef Point pdd;
inline double abs2(pdd a){
  return a.abs2();
```

3.2 Intersection of two circle

3.3 Convex Hull

```
#include <bits/stdc++.h>
using namespace std;

typedef long long LL;
const int MAXN = 100005;
const LL INF = (1LL) << 62;

struct Point{
    LL x, y;
    Point (LL x=0, LL y=0):x(x),y(y){}
    bool operator < (const Point &B)const {
        if (x!=B.x)return x<B.x;
        return y<B.y;
    }</pre>
```

```
Point operator - (Point B) {
        return Point(x-B.x,y-B.y);
};
LL cross(Point A, Point B){
   return A.x*B.y-A.y*B.x;
LL Abs(LL x){
   return x>0?x:-x;
LL AreaU[MAXN], AreaD[MAXN];
void find CH(int N, Point P[], LL Area[]){
    static vector<Point> U, D;
    static vector<int> Ui, Di;
    U.clear(), Ui.clear();
    D.clear(), Di.clear();
    int uz=0, dz=0;
    for (int i=0; i<N; i++){</pre>
        while (uz>=2 && cross(P[i]-U[uz-2],U[uz-1]-U[uz
            -2])<=0)U.pop_back(), Ui.pop_back(), uz--;
        if (uz<=1)AreaU[i]=0;</pre>
        else AreaU[i] = AreaU[ Ui[uz-1] ] + Abs(cross(P
            [i]-U[0],U[uz-1]-U[0]));
        U.push_back(P[i]),Ui.push_back(i),uz++;
        while (dz>=2 && cross(P[i]-D[dz-2],D[dz-1]-D[dz
             -2])>=0)D.pop_back(), Di.pop_back(), dz--;
        if (dz<=1)AreaD[i]=0;</pre>
        else AreaD[i] = AreaD[ Di[dz-1] ] + Abs(cross(P
            [i]-D[0],D[dz-1]-D[0]));
        D.push_back(P[i]),Di.push_back(i),dz++;
        Area[i] = AreaU[i] + AreaD[i];
        //printf("Area[%d]=%lld\n",i ,Area[i]);
    //puts("");
}
int N;
Point P[MAXN];
LL AreaL[MAXN], AreaR[MAXN];
int main(){
    input();
    find_CH(N,P,AreaL);
    for (int i=0; i<N; i++)P[i].x*=-1;</pre>
    reverse(P,P+N);
    find_CH(N,P,AreaR);
    reverse(AreaR, AreaR+N);
    reverse(P,P+N);
    LL Ans = min(AreaL[N-1], AreaR[0]);
    for (int i=0; i<N-1; i++){</pre>
        if (P[i].x!=P[i+1].x){
            Ans = min (Ans,AreaL[i]+AreaR[i+1]);
  if (P[0].x==P[N-1].x)Ans=0;
    printf("%lld\n",(Ans+1)/2LL);
```

3.4 外心 Circumcentre

```
#include "2Dpoint.cpp"

pdd circumcentre(pdd &p0, pdd &p1, pdd &p2){
   pdd a = p1-p0;
   pdd b = p2-p0;
   double c1 = a.abs2()*0.5;
   double c2 = b.abs2()*0.5;
   double d = a % b;
   double x = p0.x + ( c1*b.y - c2*a.y ) / d;
   double y = p0.y + ( c2*a.x - c1*b.x ) / d;
   return pdd(x,y);
```

|}

3.5 Smallest Covering Circle

```
#include "circumcentre.cpp"
pair<pdd,double> SmallestCircle(int n, pdd _p[]){
  static const int MAXN = 1000006;
  static pdd p[MAXN];
  memcpy(p,_p,sizeof(pdd)*n);
  random_shuffle(p,p+n);
  double r2=0;
  pdd cen;
  for (int i=0; i<n; i++){</pre>
    if ( (cen-p[i]).abs2() <=r2)continue;</pre>
    cen = p[i], r2=0;
    for (int j=0; j<i; j++){</pre>
      if ( (cen-p[j]).abs2()<=r2 )continue;</pre>
      cen = (p[i]+p[j])*0.5;
      r2 = (cen-p[i]).abs2();
      for (int k=0; k<j; k++){</pre>
        if ( (cen-p[k]).abs2()<=r2 )continue;</pre>
        cen = circumcentre(p[i],p[j],p[k]);
        r2 = (cen-p[k]).abs2();
    }
  }
  return {cen,r2};
// auto res = SmallestCircle(,);
```

4 Mathmatics

4.1 LinearPrime

```
const int MAXP = 100; //max prime
vector<int> P; // primes
void build_prime(){
    static bitset<MAXP> ok;
    int np=0;
    for (int i=2; i<MAXP; i++){
        if (ok[i]==0)P.push_back(i), np++;
        for (int j=0; j<np && i*P[j]<MAXP; j++){
            ok[ i*P[j] ] = 1;
            if ( i%P[j]==0 )break;
        }
    }
}</pre>
```

4.2 BigInt

```
struct Bigint{
 static const int LEN = 60;
 static const int BIGMOD = 10000;
 int s;
 int vl, v[LEN];
 // vector<int> v;
 Bigint() : s(1) { vl = 0; }
 Bigint(long long a) {
   s = 1; vl = 0;
    if (a < 0) { s = -1; a = -a; }
   while (a) {
     push_back(a % BIGMOD);
     a /= BIGMOD;
   }
 Bigint(string str) {
   s = 1; vl = 0;
    int stPos = 0, num = 0;
```

```
if (!str.empty() && str[0] == '-') {
    stPos = 1;
    s = -1;
  for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
    num += (str[i] - '0') * q;
    if ((q *= 10) >= BIGMOD) {
      push_back(num);
      num = 0; q = 1;
  if (num) push_back(num);
int len() const { return vl; /* return SZ(v); */ }
bool empty() const { return len() == 0; }
void push_back(int x) { v[vl++] = x; /* v.PB(x); */ }
void pop_back() { vl--; /* v.pop_back(); */ }
int back() const { return v[vl-1]; /* return v.back()
    ; */
void n() { while (!empty() && !back()) pop_back(); }
void resize(int nl) {
 vl = nl; fill(v, v+vl, 0);
        v.resize(nl); // fill(ALL(v), 0);
 //
}
void print() const {
 if (empty()) { putchar('0'); return; }
  if (s == -1) putchar('-');
  printf("%d", back());
  for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
friend std::ostream& operator << (std::ostream& out,</pre>
    const Bigint &a) {
  if (a.empty()) { out << "0"; return out; }</pre>
  if (a.s == -1) out << "-";
  out << a.back();</pre>
  for (int i=a.len()-2; i>=0; i--) {
    char str[10];
    snprintf(str, 5, "%.4d", a.v[i]);
    out << str;
 return out;
int cp3(const Bigint &b)const {
  if (s != b.s) return s > b.s ? 1 : -1;
  if (s == -1) return -(-*this).cp3(-b);
  if (len() != b.len()) return len()>b.len()?1:-1;
  for (int i=len()-1; i>=0; i--)
    if (v[i]!=b.v[i]) return v[i]>b.v[i]?1:-1;
  return 0;
bool operator < (const Bigint &b)const{ return cp3(b)</pre>
    ==-1; }
bool operator <= (const Bigint &b)const{ return cp3(b</pre>
    ) <= 0; }
bool operator >= (const Bigint &b)const{ return cp3(b
bool operator == (const Bigint &b)const{ return cp3(b
    )==0; }
bool operator != (const Bigint &b)const{ return cp3(b
    )!=0; }
bool operator > (const Bigint &b)const{ return cp3(b)
    ==1; }
Bigint operator - () const {
 Bigint r = (*this);
 r.s = -r.s;
 return r;
Bigint operator + (const Bigint &b) const {
  if (s == -1) return -(-(*this)+(-b));
  if (b.s == -1) return (*this)-(-b);
  Bigint r;
  int nl = max(len(), b.len());
  r.resize(nl + 1);
  for (int i=0; i<nl; i++) {</pre>
    if (i < len()) r.v[i] += v[i];</pre>
    if (i < b.len()) r.v[i] += b.v[i];</pre>
    if(r.v[i] >= BIGMOD) {
```

```
r.v[i+1] += r.v[i] / BIGMOD;
         r.v[i] %= BIGMOD;
    }
    r.n();
    return r;
  Bigint operator - (const Bigint &b) const {
    if (s == -1) return -(-(*this)-(-b));
    if (b.s == -1) return (*this)+(-b);
    if ((*this) < b) return -(b-(*this));</pre>
    Bigint r;
     r.resize(len());
    for (int i=0; i<len(); i++) {</pre>
      r.v[i] += v[i];
      if (i < b.len()) r.v[i] -= b.v[i];</pre>
      if (r.v[i] < 0) {
        r.v[i] += BIGMOD;
        r.v[i+1]--;
    }
    r.n();
    return r;
  Bigint operator * (const Bigint &b) {
    Bigint r:
    r.resize(len() + b.len() + 1);
    r.s = s * b.s;
    for (int i=0; i<len(); i++) {</pre>
       for (int j=0; j<b.len(); j++) {</pre>
        r.v[i+j] += v[i] * b.v[j];
         if(r.v[i+j] >= BIGMOD) {
           r.v[i+j+1] += r.v[i+j] / BIGMOD;
           r.v[i+j] %= BIGMOD;
        }
      }
    }
    r.n();
    return r;
  Bigint operator / (const Bigint &b) {
    Bigint r;
    r.resize(max(1, len()-b.len()+1));
    int oriS = s;
    Bigint b2 = b; // b2 = abs(b)
    s = b2.s = r.s = 1;
    for (int i=r.len()-1; i>=0; i--) {
      int d=0, u=BIGMOD-1;
      while(d<u) {</pre>
        int m = (d+u+1)>>1;
         r.v[i] = m;
        if((r*b2) > (*this)) u = m-1;
         else d = m;
      r.v[i] = d;
    s = oriS;
    r.s = s * b.s;
    r.n();
    return r;
  Bigint operator % (const Bigint &b) {
    return (*this)-(*this)/b*b;
|};
```

4.3 Random

```
inline int ran(){
  static int x = 20167122;
  return x = (x * 0xdefaced + 1) & INT_MAX;
}
```

4.4 Theorem

4.5 Miller Rabin

```
typedef long long LL;
inline LL bin_mul(LL a, LL n,const LL& MOD){
  LL re=0;
  while (n>0){
    if (n&1) re += a;
    a += a; if (a>=MOD) a-=MOD;
    n>>=1;
  }
  return re%MOD;
}
inline LL bin_pow(LL a, LL n,const LL& MOD){
  LL re=1;
  while (n>0){
    if (n&1) re = bin_mul(re,a,MOD);
    a = bin_mul(a,a,MOD);
    n>>=1:
  return re;
}
bool is_prime(LL n){
  //static LL sprp[3] = { 2LL, 7LL, 61LL};
  static LL sprp[7] = { 2LL, 325LL, 9375LL,
    28178LL, 450775LL, 9780504LL,
    1795265022LL };
  if (n==1 || (n&1)==0 ) return n==2;
  int u=n-1, t=0;
  while ( (u&1)==0 ) u>>=1, t++;
  for (int i=0; i<3; i++){</pre>
    LL x = bin_pow(sprp[i]%n, u, n);
    if (x==0 || x==1 || x==n-1)continue;
    for (int j=1; j<t; j++){</pre>
      x=x*x%n;
      if (x==1 || x==n-1)break;
    if (x==n-1)continue;
    return 0;
  return 1;
}
```

4.6 ax+by=gcd(a,b)

```
typedef pair<int, int> pii;
pii extgcd(int a, int b){
  if(b == 0) return make_pair(1, 0);
  else{
   int p = a / b;
   pii q = extgcd(b, a % b);
   return make_pair(q.second, q.first - q.second * p);
}
```

|}

4.7 FFT

```
const double pi = atan(1.0)*4;
struct Complex {
    double x,y;
    Complex(double _x=0,double _y=0)
        :x(_x),y(_y) {}
    Complex operator + (Complex &tt) { return Complex(x
        +tt.x,y+tt.y); }
    Complex operator - (Complex &tt) { return Complex(x
        -tt.x,y-tt.y); }
    Complex operator * (Complex &tt) { return Complex(x
        *tt.x-y*tt.y,x*tt.y+y*tt.x); }
void fft(Complex *a, int n, int rev) {
    // n是大于等于相乘的两个数组长度的2的幂次
    // 从 0 开 始 表 示 长 度 , 对 a 进 行 操 作
    // rev==1进行DFT,==-1进行IDFT
    for (int i = 1,j = 0; i < n; ++ i) {
        for (int k = n>>1; k > (j^=k); k >>= 1);
        if (i<j) std::swap(a[i],a[j]);</pre>
    for (int m = 2; m <= n; m <<= 1) {</pre>
        Complex wm(cos(2*pi*rev/m),sin(2*pi*rev/m));
        for (int i = 0; i < n; i += m) {</pre>
            Complex w(1.0,0.0);
            for (int j = i; j < i+m/2; ++ j) {</pre>
                Complex t = w*a[j+m/2];
                a[j+m/2] = a[j] - t;
                a[j] = a[j] + t;
                w = w * wm;
            }
        }
    if (rev==-1) {
        for (int i = 0; i < n; ++ i) a[i].x /= n,a[i].y</pre>
             /= n;
    }
}
```

4.8 FWHT

```
// FWHT template
const int MAXN = 1<<20;
void FWHT(int a[], int l=0, int r=MAXN-1){
   if (l==r)return;

   int mid = (l+r)>>1+1, n = r-l+1;
   FWHT(a,l,mid-1);
   FWHT(a,mid,r);

for (int i=0; i<(n>>1); i++){
   int al=a[l+i], a2=a[mid+i];
   a[l+i] = a1+a2;
   a[mid+i] = a1-a2;
}
```

4.9 Hash

```
typedef long long LL;
LL X=7122;
LL P1=712271227;
LL P2=179433857;
LL P3=179434999;
struct HASH{
```

```
LL a, b, c;
    HASH(LL a=0, LL b=0, LL c=0):a(a),b(b),c(c){ }
    HASH operator + (HASH B){
        return HASH((a+B.a)%P1,(b+B.b)%P2,(c+B.c)%P3);
    }
    HASH operator + (LL B){
        return (*this)+HASH(B,B,B);
}
HASH operator * (LL B){
        return HASH(a*B%P1,a*B%P2,a*B%P3);
}
bool operator < (const HASH &B)const{
        if (a!=B.a)return a<B.a;
        if (b!=B.b)return b<B.b;
        return c<B.c;
}
void up(){ (*this) = (*this)*X; }
};
int main(){</pre>
```

4.10 GaussElimination

```
// by bcw_codebook
const int MAXN = 300;
const double EPS = 1e-8;
int n;
double A[MAXN][MAXN];
void Gauss() {
  for(int i = 0; i < n; i++) {</pre>
    bool ok = 0;
    for(int j = i; j < n; j++) {</pre>
      if(fabs(A[j][i]) > EPS) {
        swap(A[j], A[i]);
         ok = 1;
         break;
    if(!ok) continue;
    double fs = A[i][i];
    for(int j = i+1; j < n; j++) {</pre>
      double r = A[j][i] / fs;
       for(int k = i; k < n; k++) {</pre>
         A[j][k] -= A[i][k] * r;
  }
}
```

4.11 Inverse

```
int inverse[100000];
void invTable(int b, int p) {
   inverse[1] = 1;
   for( int i = 2; i <= b; i++ ) {
      inverse[i] = (long long)inverse[p%i] * (p-p/i) % p;
   }
}
int inv(int b, int p) {
   return b == 1 ? 1 : ((long long)inv(p % b, p) * (p-p/b) % p);
}</pre>
```

4.12 IterSet

```
// get all subset in set S
for (int i = S; i ; i = (i-1) & S ) {
}
```

4.13 SG

```
Sprague-Grundy
1. 雙人、回合制
2. 資訊完全公開
3. 無隨機因素
4. 可在有限步內結束
5. 沒有和局
6. 雙方可採取的行動相同
SG(S) 的值為 0:後手(P)必勝
不為 0: 先手(N) 必勝
int mex(set S) {
 // find the min number >= 0 that not in the S
  // e.g. S = {0, 1, 3, 4} mex(S) = 2
state = []
int SG(A) {
  if (A not in state) {
   S = sub_states(A)
   if( len(S) > 1 ) state[A] = reduce(operator.xor, [
       SG(B) for B in S])
   else state[A] = mex(set(SG(B) for B in next_states(
       A)))
 }
  return state[A]
```

5 Graph

5.1 2-SAT

```
const int MAXN = 2020;
struct TwoSAT{
    static const int MAXv = 2*MAXN;
    vector<int> GO[MAXv],BK[MAXv],stk;
    bool vis[MAXv];
    int SC[MAXv];
    void imply(int u,int v){ // u imply v
        GO[u].push_back(v);
        BK[v].push_back(u);
    int dfs(int u,vector<int>*G,int sc){
        vis[u]=1, SC[u]=sc;
        for (int v:G[u])if (!vis[v])
            dfs(v,G,sc);
        if (G==G0)stk.push_back(u);
    int scc(int n=MAXv){
        memset(vis,0,sizeof(vis));
        for (int i=0; i<n; i++)if (!vis[i])</pre>
            dfs(i,G0,-1);
        memset(vis,0,sizeof(vis));
        int sc=0:
        while (!stk.empty()){
            if (!vis[stk.back()])
                dfs(stk.back(),BK,sc++);
            stk.pop_back();
        }
```

```
}
}SAT;

int main(){
    SAT.scc(2*n);
    bool ok=1;
    for (int i=0; i<n; i++){
        if (SAT.SC[2*i]==SAT.SC[2*i+1])ok=0;
    }
    if (ok){
        for (int i=0; i<n; i++){
            if (SAT.SC[2*i]>SAT.SC[2*i+1]){
                 cout << i << endl;
            }
        }
     }
    else puts("NO");
}</pre>
```

5.2 LCA

5.3 Strongly Connected Component(SCC)

```
#define MXN 100005
#define PB push_back
#define FZ(s) memset(s,0,sizeof(s))
struct Scc{
int n, nScc, vst[MXN], bln[MXN];
vector<int> E[MXN], rE[MXN], vec;
void init(int _n){
  n = _n;
for (int i=0; i<MXN; i++){</pre>
    E[i].clear();
    rE[i].clear();
  }
}
void add_edge(int u, int v){
  E[u].PB(v);
  rE[v].PB(u);
void DFS(int u){
  vst[u]=1;
  for (auto v : E[u])
    if (!vst[v]) DFS(v);
  vec.PB(u);
void rDFS(int u){
  vst[u] = 1;
  bln[u] = nScc;
  for (auto v : rE[u])
    if (!vst[v]) rDFS(v);
void solve(){
  nScc = 0;
  vec.clear();
  FZ(vst);
  for (int i=0; i<n; i++)</pre>
    if (!vst[i]) DFS(i);
  reverse(vec.begin(),vec.end());
  FZ(vst);
  for (auto v : vec){
     if (!vst[v]){
      rDFS(v);
      nScc++:
  }
}
};
```

5.4 Euler Circuit

//CF 723E

```
#include <bits/stdc++.h>
using namespace std;
const int MAXN = 300;
struct EDGE{
    int u ,v ;
    int type;
int n, m, deg[MAXN];
vector <EDGE> edges;
vector<int> G[MAXN];
bool vis[MAXN*MAXN];
bool alive[MAXN][MAXN];
bool visN[MAXN];
vector<int> ans;
void add_edge(int u, int v, int type=0){
  edges.push_back( EDGE{u,v,type} );
    edges.push_back( EDGE{v,u,type} );
    G[u].push_back( edges.size()-2 );
    G[v].push_back( edges.size()-1 );
    deg[u]++, deg[v]++;
    alive[u][v]=alive[v][u]|=type^1;
}
void input(){
    memset(visN,0,sizeof(visN));
    memset(vis,0,sizeof(vis));
    memset(alive,0,sizeof(alive));
    memset(deg,0,sizeof(deg));
    edges.clear();
    ans.clear();
    for (int i=0; i<MAXN; i++)G[i].clear();</pre>
    scanf("%d%d",&n ,&m);
    for (int i=0, u, v; i<m; i++){
    scanf("%d%d", &u, &v);</pre>
         add_edge(u,v);
    }
}
void add_Graph(){
    vector<int> tmp;
    for (int i=1; i<=n; i++)if (deg[i]%2==1){</pre>
         tmp.push_back(i);
    printf("%d\n",n-tmp.size());
    for (int i=0; i<tmp.size(); i+=2){</pre>
         add_edge(tmp[i],tmp[i+1],1);
}
void dfs(int u){
    for (int i=0; i<G[u].size(); i++)if (!vis[ G[u][i</pre>
         ]>>1 ]){
         EDGE &e = edges[ G[u][i] ];
         int v = e.v;
         vis[ G[u][i]>>1 ]=1;
         dfs(v);
    ans.push_back(u);
}
int main(){
    int T; scanf("%d",&T);
    while (T--){
         input();
         add_Graph();
         for (int i=1; i<=n; i++)if (!visN[i]){</pre>
             dfs(i);
             for (int j=0 ;j<ans.size()-1; j++){</pre>
                  int u = ans[j], v=ans[j+1];
                  if (alive[u][v]){
                      alive[u][v]=alive[v][u]=0;
```

5.5 Hungarian

```
vector<int> G[MAXN];
int n;
int match[MAXN]; // Matching Result
int visit[MAXN];
bool dfs(int u) {
    for ( auto v:G[u] ) {
        if (!visit[v]) {
            visit[v] = true;
            if (match[v] == -1 \mid | dfs(match[v])) {
                match[v] = u;
                match[u] = v;
                return true;
            }
        }
   return false;
}
int hungarian() {
    int res = 0;
    memset(match, -1, sizeof(match));
    for (int i = 0; i < n; i++) {</pre>
        if (match[i] == -1) {
            memset(visit, 0, sizeof(visit));
            if (dfs(i)) res += 1;
    }
    return res;
```

5.6 Maximum Clique

```
const int MAXN = 105;
int best;
int m ,n;
int num[MAXN];
// int x[MAXN];
int path[MAXN];
int g[MAXN][MAXN];
bool dfs( int *adj, int total, int cnt ){
    int i, j, k;
    int t[MAXN];
    if( total == 0 ){
        if( best < cnt ){</pre>
             // for( i = 0; i < cnt; i++) path[i] = x[i
            best = cnt; return true;
        }
        return false;
    for( i = 0; i < total; i++){</pre>
        if( cnt+(total-i) <= best ) return false;</pre>
        if( cnt+num[adj[i]] <= best ) return false;</pre>
        // x[cnt] = adj[i];
        for( k = 0, j = i+1; j < total; j++ )</pre>
             if( g[ adj[i] ][ adj[j] ] )
                 t[ k++ ] = adj[j];
                 if( dfs( t, k, cnt+1 ) ) return true;
    } return false;
```

5.7 Tarjan

```
int n;
vector<int> G[MAXN];
stack<int> stk;
int dfn[MAXN], low[MAXN];
bool ins[MAXN];
int scc[MAXN], scn, count;
void tarjan(int u){
  dfn[u] = low[u] = ++count;
  stk.push(u);
  ins[u] = true;
  for(auto v:G[u]){
    if(!dfn[v]){
      tarjan(v);
      low[u] = min(low[u], low[v]);
    }else if(ins[v]){
      low[u] = min(low[u], dfn[v]);
  }
  if(dfn[u] == low[u]){
    int v;
    do {
      v = stk.top();
      stk.pop();
      scc[v] = scn;
      ins[v] = false;
    } while(v != u);
    scn++;
  }
}
void GetSCC(){
  count = scn = 0;
  for(int i = 0 ; i < n ; i++ ){</pre>
    if(!dfn[i]) tarjan(i);
}
```

5.8 一般圖匹配

```
| #define MAXN 505
| vector<int>g[MAXN];//用vector存圖
| int pa[MAXN],match[MAXN],st[MAXN],S[MAXN],vis[MAXN];
| int t,n;
| inline int lca(int u,int v){//找花的花托
| for(++t;;swap(u,v)){
| if(u==0)continue;
| if(vis[u]==t)return u;
| vis[u]=t;//這種方法可以不用清空vis陣列
| u=st[pa[match[u]]];
| }
| }
| #define qpush(u) q.push(u),S[u]=0
| inline void flower(int u,int v,int l,queue<int> &q){
```

```
while(st[u]!=l){
    pa[u]=v; //所有未匹配邊的pa都是雙向的
    if(S[v=match[u]]==1)qpush(v);//所有奇點變偶點
    st[u]=st[v]=l,u=pa[v];
  }
inline bool bfs(int u){
  for(int i=1;i<=n;++i)st[i]=i;//st[i]表示第i個點的集合
  memset(S+1,-1,sizeof(int)*n);//-1:沒走過 0:偶點 1:奇
  queue<int>q;qpush(u);
  while(q.size()){
    u=q.front(),q.pop();
    for(size_t i=0;i<g[u].size();++i){</pre>
      int v=g[u][i];
      if(S[v]==-1){
        pa[v]=u,S[v]=1;
        if(!match[v]){//有增廣路直接擴充
          for(int lst;u;v=lst,u=pa[v])
            lst=match[u],match[u]=v,match[v]=u;
          return 1;
        }
        qpush(match[v]);
      }else if(!S[v]&&st[v]!=st[u]){
        int l=lca(st[v],st[u]);//遇到花,做花的處理
        flower(v,u,l,q),flower(u,v,l,q);
    }
  }
  return 0;
inline int blossom(){
  memset(pa+1,0,sizeof(int)*n);
  memset(match+1,0,sizeof(int)*n);
  int ans=0;
  for(int i=1;i<=n;++i)</pre>
    if(!match[i]&&bfs(i))++ans;
  return ans;
}
int main(){
  int T, m; cin >> T;
  while ( cin >> n >> m ){
    for (int i=1; i<=n; i++) g[i].clear();</pre>
    for (int i=1, u, v; i<=m; i++){</pre>
      cin >> u >> v;
      g[u].push_back(v);
      g[v].push_back(u);
    cout << blossom() << endl;</pre>
  }
}
```

5.9 LCA

```
|//lv紀錄深度
|//father[多少冪次][誰]
|//已經建好每個人的父親是誰 (father[0][i]已經建好)
|//已經建好深度 (lv[i]已經建好)
|void makePP() {
| for(int i = 1; i < 20; i++) {
| for(int j = 2; j <= n; j++) {
| father[i][j]=father[i-1][ father[i-1][j] ];
| }
| }
| int find(int a, int b) {
| if(lv[a] < lv[b]) swap(a,b);
| int need = lv[a] - lv[b];
| for(int i = 0; need!=0; i++) {
| if(need&1) a=father[i][a];
| need >>= 1;
| }
```

```
for(int i = 19 ;i >= 0 ;i--){
   if(father[i][a] != father[i][b]){
     a=father[i][a];
     b=father[i][b];
   }
}
return a!=b?father[0][a] : a;
}
```

6 Data Structure

6.1 Disjoint Set

6.2 Sparse Table

```
const int MAXN = 200005;
const int lgN = 20;
struct SP{ //sparse table
  int Sp[MAXN][lgN];
  function<int(int,int)> opt;
  void build(int n, int *a){ // 0 base
     for (int i=0 ;i<n; i++) Sp[i][0]=a[i];</pre>
     for (int h=1; h<lgN; h++){</pre>
       int len = 1<<(h-1), i=0;</pre>
       for (; i+len<n; i++)</pre>
         Sp[i][h] = opt( Sp[i][h-1] , Sp[i+len][h-1] );
       for (; i<n; i++)</pre>
         Sp[i][h] = Sp[i][h-1];
    }
  int query(int l, int r){
    int h = __lg(r-l+1);
     int len = 1<<h;</pre>
     return opt( Sp[l][h] , Sp[r-len+1][h] );
  }
|};
```

6.3 Treap

```
#include<bits/stdc++.h>
using namespace std;
template<class T,unsigned seed>class treap{
  public:
    struct node{
    T data;
    int size;
    node *l,*r;
    node(T d){
    size=1;
```

```
data=d;
    l=r=NULL;
  inline void up(){
    size=1;
    if(l)size+=l->size;
    if(r)size+=r->size;
  inline void down(){
  }
}*root;
inline int size(node *p){return p?p->size:0;}
inline bool ran(node *a, node *b){
  static unsigned x=seed;
  x=0xdefaced*x+1;
  unsigned all=size(a)+size(b);
  return (x%all+all)%all<size(a);</pre>
void clear(node *&p){
  if(p)clear(p->l),clear(p->r),delete p,p=NULL;
~treap(){clear(root);}
void split(node *o,node *&a,node *&b,int k){
  if(!k)a=NULL,b=o;
  else if(size(o)==k)a=o,b=NULL;
  else{
    o->down();
    if(k<=size(o->l)){
      b=o:
      split(o->l,a,b->l,k);
      b->up();
    }else{
      a=o;
      split(o->r,a->r,b,k-size(o->l)-1);
      a->up();
    }
 }
void merge(node *&o,node *a,node *b){
  if(!a||!b)o=a?a:b;
  else{
    if(ran(a,b)){
      a->down();
      o=a:
      merge(o->r,a->r,b);
    }else{
      b->down();
      o=b;
      merge(o->l,a,b->l);
    o->up();
  }
}
void build(node *&p,int l,int r,T *s){
  if(l>r)return;
  int mid=(l+r)>>1;
  p=new node(s[mid]);
  build(p->l,l,mid-1,s);
  build(p->r,mid+1,r,s);
  p->up();
inline int rank(T data){
 node *p=root;
  int cnt=0;
  while(p){
    if(data<=p->data)p=p->l;
    else cnt+=size(p->l)+1,p=p->r;
  return cnt;
inline void insert(node *&p,T data,int k){
  node *a,*b,*now;
  split(p,a,b,k);
  now=new node(data);
  merge(a,a,now);
  merge(p,a,b);
```

```
};
treap<int ,20141223>bst;
int n,m,a,b;
int main(){
    //當成二分查找樹用
    while(~scanf("%d",&a))bst.insert(bst.root,a,bst.rank(a));
    while(~scanf("%d",&a))printf("%d\n",bst.rank(a));
    bst.clear(bst.root);
    return 0;
}
```

7 String

7.1 KMP

```
template<typename T>
void build_KMP(int n, T *s, int *f){ // 1 base
  f[0]=-1, f[1]=0;
  for (int i=2; i<=n; i++){</pre>
    int w = f[i-1];
    while (w>=0 && s[w+1]!=s[i])w = f[w];
    f[i]=w+1;
  }
}
template<typename T>
int KMP(int n, T *a, int m, T *b){
  build_KMP(n,b,f);
  int ans=0;
  for (int i=1, w=0; i<=n; i++){</pre>
    while ( w>=0 && b[w+1]!=a[i] )w = f[w];
    if (w==m) {
      ans++:
      w=f[w];
    }
  }
  return ans;
```

7.2 AC

```
// by bcw_codebook
struct ACautomata{
  struct Node{
    int cnt,dp;
    Node *go[26], *fail;
    Node (){
      cnt = 0;
      dp = -1;
      memset(go,0,sizeof(go));
      fail = 0;
    }
  Node *root, pool[1048576];
  int nMem;
 Node* new_Node(){
    pool[nMem] = Node();
    return &pool[nMem++];
  void init(){
   nMem = 0;
    root = new_Node();
  void add(const string &str){
    insert(root,str,0);
  void insert(Node *cur, const string &str, int pos){
```

```
if (pos >= (int)str.size()){
       cur->cnt++;
       return:
     int c = str[pos]-'a';
     if (cur->go[c] == 0){
      cur->go[c] = new_Node();
     insert(cur->go[c],str,pos+1);
  void make_fail(){
     queue<Node*> que;
     que.push(root);
    while (!que.empty()){
       Node* fr=que.front();
       que.pop();
       for (int i=0; i<26; i++){</pre>
         if (fr->go[i]){
           Node *ptr = fr->fail;
           while (ptr && !ptr->go[i]) ptr = ptr->fail;
           if (!ptr) fr->go[i]->fail = root;
           else fr->go[i]->fail = ptr->go[i];
           que.push(fr->go[i]);
    }
  }
|};
```

7.3 Z-value

```
| z[0] = 0;

for ( int bst = 0, i = 1; i < len; i++ ) {

   if ( z[bst] + bst <= i ) z[i] = 0;

   else z[i] = min(z[i - bst], z[bst] + bst - i);

   while ( str[i + z[i]] == str[z[i]] ) z[i]++;

   if ( i + z[i] > bst + z[bst] ) bst = i;

}
```

7.4 Suffix Array

```
const int MAX = 1020304;
int ct[MAX], he[MAX], rk[MAX];
int sa[MAX], tsa[MAX], tp[MAX][2];
void suffix_array(char *ip){
  int len = strlen(ip);
  int alp = 256;
  memset(ct, 0, sizeof(ct));
  for(int i=0;i<len;i++) ct[ip[i]+1]++;</pre>
  for(int i=1;i<alp;i++) ct[i]+=ct[i-1];</pre>
  for(int i=0;i<len;i++) rk[i]=ct[ip[i]];</pre>
  for(int i=1;i<len;i*=2){</pre>
    for(int j=0;j<len;j++){</pre>
      if(j+i>=len) tp[j][1]=0;
      else tp[j][1]=rk[j+i]+1;
      tp[j][0]=rk[j];
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][1]+1]++;</pre>
    for(int j=1;j<len+2;j++) ct[j]+=ct[j-1];</pre>
    for(int j=0;j<len;j++) tsa[ct[tp[j][1]]++]=j;</pre>
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][0]+1]++;</pre>
    for(int j=1;j<len+1;j++) ct[j]+=ct[j-1];</pre>
    for(int j=0;j<len;j++)</pre>
      sa[ct[tp[tsa[j]][0]]++]=tsa[j];
    rk[sa[0]]=0;
    for(int j=1;j<len;j++){</pre>
      if( tp[sa[j]][0] == tp[sa[j-1]][0] &&
        tp[sa[j]][1] == tp[sa[j-1]][1])
         rk[sa[j]] = rk[sa[j-1]];
      else
        rk[sa[j]] = j;
```

```
}
for(int i=0,h=0;i<len;i++){
   if(rk[i]==0) h=0;
   else{
      int j=sa[rk[i]-1];
      h=max(0,h-1);
      for(;ip[i+h]==ip[j+h];h++);
   }
   he[rk[i]]=h;
}</pre>
```

7.5 Suffix Automaton

```
// par : fail link
// val : a topological order ( useful for DP )
// go[x] : automata edge ( x is integer in [0,26) )
struct SAM{
  struct State{
    int par, go[26], val;
    State () : par(0), val(0){ FZ(go); }
    State (int _val) : par(0), val(_val){ FZ(go); }
  vector<State> vec;
  int root, tail;
  void init(int arr[], int len){
    vec.resize(2);
    vec[0] = vec[1] = State(0);
    root = tail = 1;
    for (int i=0; i<len; i++)</pre>
      extend(arr[i]);
  void extend(int w){
    int p = tail, np = vec.size();
    vec.PB(State(vec[p].val+1));
    for ( ; p && vec[p].go[w]==0; p=vec[p].par)
      vec[p].go[w] = np;
    if (p == 0){
      vec[np].par = root;
    } else {
      if (vec[vec[p].go[w]].val == vec[p].val+1){
        vec[np].par = vec[p].go[w];
      } else {
        int q = vec[p].go[w], r = vec.size();
        vec.PB(vec[q]);
        vec[r].val = vec[p].val+1;
        vec[q].par = vec[np].par = r;
        for ( ; p && vec[p].go[w] == q; p=vec[p].par)
          vec[p].go[w] = r;
    tail = np;
  }
|};
```

8 Dark Code

8.1 輸入優化

```
bool input(T& a) {
    a=(T)0;
    register char p;
    while ((p = getc()) < '-')
        if (p==0 || p==EOF) return false;
    if (p == '-')
        while ((p = getc()) >= '0') a = a*10 - (p^'0');
    else {
        a = p ^ '0';
        while ((p = getc()) >= '0') a = a*10 + (p^'0');
    }
    return true;
}

template <class T, class... U>
bool input(T& a, U&... b) {
    if (!input(a)) return false;
    return input(b...);
}
```

9 Search

10 Others

10.1 數位統計

```
int dfs(int pos, int state1, int state2 ...., bool
    limit, bool zero) {
    if (pos == -1) return 是否符合條件;
    int &ret = dp[pos][state1][state2][....];
    if ( ret != -1 && !limit ) return ret;
    int ans = 0;
    int upper = limit ? digit[pos] : 9;
    for ( int i = 0 ; i <= upper ; i++ ) {</pre>
        ans += dfs(pos - 1, new_state1, new_state2,
            limit & ( i == upper), ( i == 0) && zero);
   if ( !limit ) ret = ans;
   return ans;
int solve(int n) {
   int it = 0;
   for ( ; n ; n /= 10 ) digit[it++] = n % 10;
   return dfs(it - 1, 0, 0, 1, 1);
```

10.2 Stable Marriage

```
// normal stable marriage problem
// input:
//3
//Albert Laura Nancy Marcy
//Brad Marcy Nancy Laura
//Chuck Laura Marcy Nancy
//Laura Chuck Albert Brad
//Marcy Albert Chuck Brad
//Nancy Brad Albert Chuck
#include<bits/stdc++.h>
using namespace std:
const int MAXN = 505;
int n:
int favor[MAXN][MAXN]; // favor[boy_id][rank] = girl_id
int order[MAXN][MAXN]; // order[girl_id][boy_id] = rank
int current[MAXN]; // current[boy_id] = rank; boy_id
    will pursue current[boy_id] girl.
int girl_current[MAXN]; // girl[girl_id] = boy_id;
```

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```
void initialize() {
  for ( int i = 0 ; i < n ; i++ ) {</pre>
   current[i] = 0;
    girl_current[i] = n;
    order[i][n] = n;
}
map<string, int> male, female;
string bname[MAXN], gname[MAXN];
int fit = 0;
void stable_marriage() {
  queue<int> que;
  for ( int i = 0 ; i < n ; i++ ) que.push(i);</pre>
  while ( !que.empty() ) {
    int boy_id = que.front();
    que.pop();
    int girl_id = favor[boy_id][current[boy_id]];
    current[boy_id] ++;
    if ( order[girl_id][boy_id] < order[girl_id][</pre>
         girl_current[girl_id]] ) {
      if ( girl_current[girl_id] < n ) que.push(</pre>
           girl_current[girl_id]); // if not the first
      girl_current[girl_id] = boy_id;
    } else {
      que.push(boy_id);
    }
  }
int main() {
 cin >> n;
  for ( int i = 0 ; i < n; i++ ) {</pre>
    string p, t;
    cin >> p;
    male[p] = i;
    bname[i] = p;
    for ( int j = 0 ; j < n ; j++ ) {</pre>
      cin >> t;
      if ( !female.count(t) ) {
        gname[fit] = t;
        female[t] = fit++;
      favor[i][j] = female[t];
    }
  }
  for ( int i = 0 ; i < n ; i++ ) {</pre>
    string p, t;
    cin >> p;
    for ( int j = 0 ; j < n ; j++ ) {</pre>
      cin >> t;
      order[female[p]][male[t]] = j;
  }
  initialize();
  stable_marriage();
  for ( int i = 0 ; i < n ; i++ ) {
  cout << bname[i] << " " << gname[favor[i][current[i]]</pre>
        ] - 1]] << endl;
  }
```

```
// algorithm
random_shuffle(a,a+n);
next_permutation(a,a+n); // need sort
nth_element (a, a+k, a+n); // kth
*min_element(a,a+n);
*unique(a,a+n); // need sort
stable_sort(a,a+n); // merge sort
// bitset (s[0] is right most)
operator[] //
count() // count number of 1
set() // all to 1
set(k) // s[k] to 1
set(k,0) // s[k] to 0
flip() // all flip
flip(k) // s[k] flip
to_ulong()
to_string()
```

11 Persistence