

# VP160 RC1

---

Github: <https://github.com/joydddd/VP160-2020-SU-NOTES>

you may need chrome + MathJax Plugin for Github to view properly

Github version will be the most up to date one.

## Concepts

Physical Quantities: ALWAYS number + unit

Scale / Vector ?

Numbers

- Scientific notation:  $6.02 \times 10^{23}$
- significant figures
- uncertainty
  - e.g.  $1.259 \pm 0.001 \mu A$

Units

- unit prefixes: nm ( $10^{-9}$ , nano),  $\mu m$  ( $10^{-6}$ , micro), um ( $10^{-3}$ , mili), km ( $10^3$ , kilo) ...
- unit conversions

Vectors

- addition/ constant multiplication/ subtraction --> vector
- dot product: vector . vector --> scale
  - $\vec{u} \cdot \vec{v} = \left( \begin{pmatrix} u_x & u_y & u_z \end{pmatrix}, \begin{pmatrix} v_x & v_y & v_z \end{pmatrix} \right) = u_x v_x + u_y v_y + u_z v_z$
  - e.g.  $P = \vec{F} \cdot \vec{v} = |\vec{F}| |\vec{v}| \cos \theta$
- cross product: vector x vector --> vector

$$\vec{u} \times \vec{v} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ u_x & u_y & u_z \\ v_x & v_y & v_z \end{vmatrix} = \begin{pmatrix} u_y v_z - u_z v_y \\ u_z v_x - u_x v_z \\ u_x v_y - u_y v_x \end{pmatrix}$$

o e.g.  $\vec{F} = I \vec{L} \times \vec{B}$

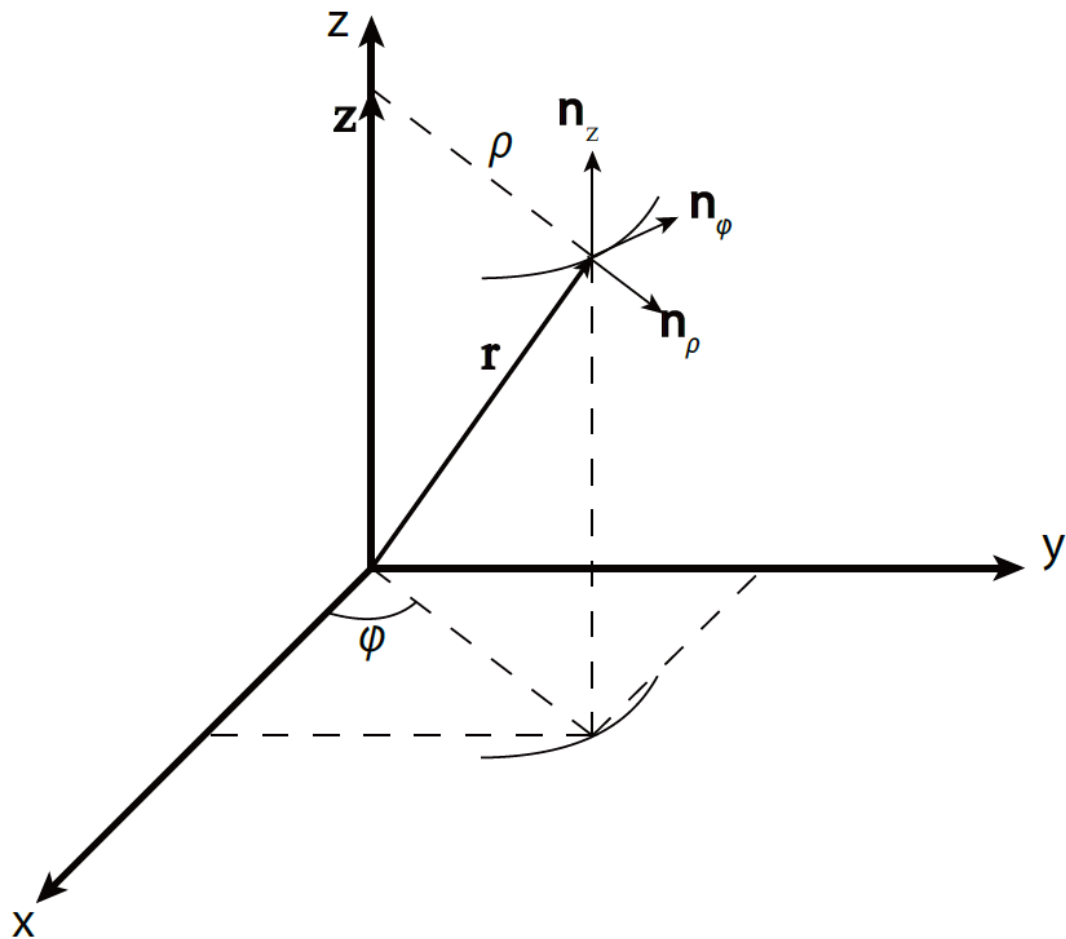
o length: the cross section area of two vector  $|\vec{F}| = I |\vec{L}| |\vec{B}| \sin \theta$

o direction: right handed rule

## Coordinate Systems

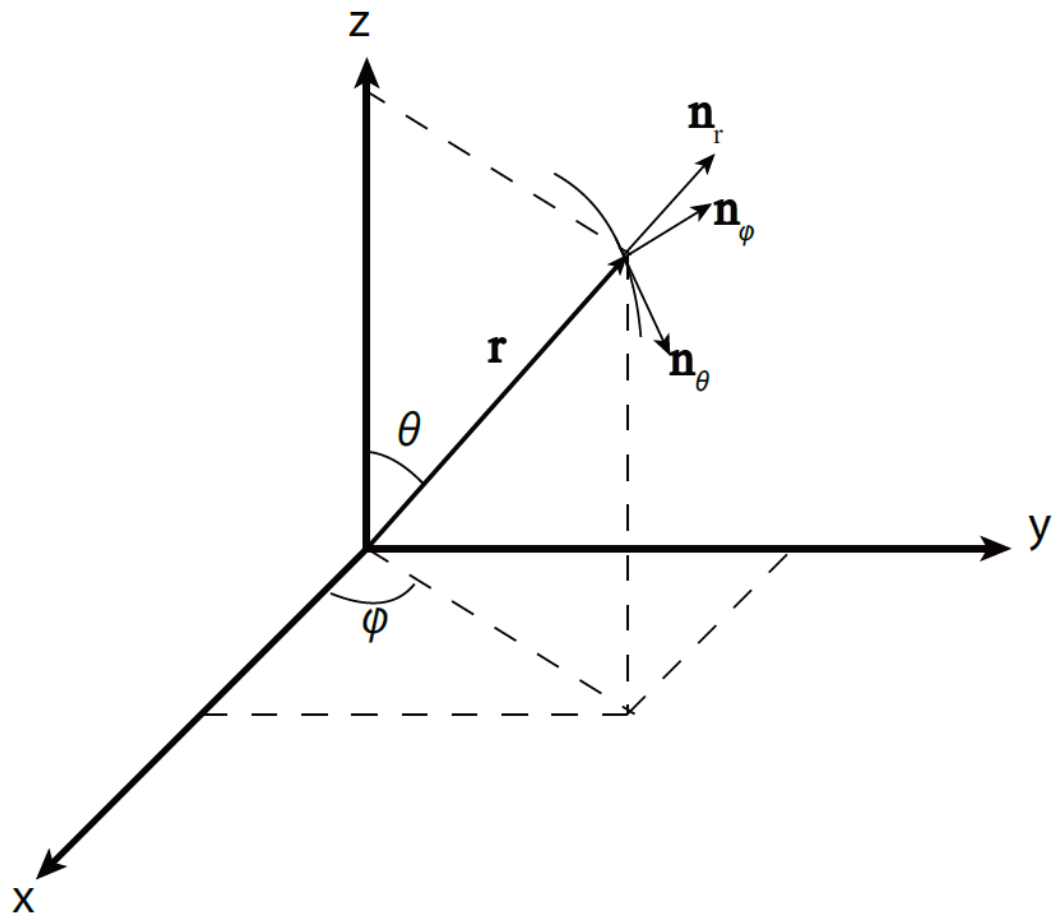
- Cartesian
  - $|\vec{w}| = \sqrt{w_x^2 + w_y^2 + w_z^2}$
  - $\{\hat{n}_x, \hat{n}_y, \hat{n}_z\} / \{\hat{i}, \hat{j}, \hat{k}\}$ 
    - mutually perpendicular  $\hat{n}_x \cdot \hat{n}_y = 0$
    - unit length  $|\hat{n}_x| = 1$
    - Right-hand Rule  $\hat{n}_x \times \hat{n}_y = \hat{n}_z$
  - $\vec{r} = x\hat{n}_x + y\hat{n}_y + z\hat{n}_z$ 
    - differentiate:  $\frac{d\vec{u}}{dt} = \frac{d}{dt}(u_x(t)\hat{n}_x + u_y(t)\hat{n}_y + u_z(t)\hat{n}_z) = \dot{u}_x(t)\hat{n}_x + u_x(t)\dot{\hat{n}}_x + \dot{u}_y(t)\hat{n}_y + u_y(t)\dot{\hat{n}}_y + \dot{u}_z(t)\hat{n}_z + u_z(t)\dot{\hat{n}}_z$
    - integrate
    - dot product  $\vec{u} \cdot \vec{w} = u_x w_x + u_y w_y + u_z w_z$
    - cross product  $\vec{u} \times \vec{w} = (u_y w_z - u_z w_y)\hat{n}_x + (u_z w_x - u_x w_z)\hat{n}_y + (u_x w_y - u_y w_x)\hat{n}_z$

- Cylindrical



- $\{\hat{n}_\rho, \hat{n}_\phi, \hat{n}_z\}$ 
  - $\rho = \sqrt{x^2 + y^2}$
  - $\phi = \arctan \frac{y}{x}$
  - $z = z$
  - $x = \rho \cos \phi$
  - $y = \rho \sin \phi$
- $\vec{r} = \rho \hat{n}_\rho + z \hat{n}_z$ 
  - NOT directly differentiable!!! Will discuss later

- Spherical



- longitude and latitude system
- $\{\hat{n}_r, \hat{n}_\varphi, \hat{n}_\theta\}$ 
  - $\rho = \sqrt{x^2 + y^2 + z^2}$
  - $\varphi = \arctan \frac{y}{x} (0, \pi)$
  - $\theta = \arctan \frac{\sqrt{x^2 + y^2}}{z} (0, \pi/2)$
  - $x = r \sin \theta \cos \varphi$
  - $y = r \sin \theta \sin \varphi$
  - $z = r \cos \theta$
- $\vec{r} = r \hat{n}_r$ 
  - NOT directly differentiable!!! Will discuss later
- 2D polar coordinates
  - Cylindrical coordinates with  $z = 0$
  - Spherical coordinates with  $\theta = 0$

## 1D kinematics

### Average vs. Instantaneous

#### Velocity

- average velocity:
  - $v_{av,x} = \frac{x(t+\Delta t) - x(t)}{\Delta t}$
- velocity
  - When the time interval  $\Delta t \rightarrow 0$
  - $\frac{dx(t)}{dt} = \dot{x}(t) \stackrel{\text{def}}{=} v_x(t)$
  - velocity is location change rate w.r.t time

#### Acceleration

- average acceleration
  - $a_{av,x} = \frac{v_x(t+\Delta t) - v_x(t)}{\Delta t}$
- acceleration
  - When time interval  $\Delta t \rightarrow 0$
  - $a_x(t) = \frac{dv_x(t)}{dt} = \dot{v}_x(t) = \frac{d^2x(t)}{dt^2} = \ddot{x}(t)$
  - acceleration is velocity change rate w.r.t and twice differentiation of position w.r.t time.

see lecture notes for pics

Relativity of Velocity/acceleration