

## Test 2

Q1 EXE 2 Question 7

(8 marks)

(a)  $d_{BA} + d_{BC} + d_{BF} = d_{BH}$

For left hand side,

$$d_{BH} + d_{BC} + d_{BF}$$

$$= u + v + h$$

Because it is a parallelogram

$$AD = BC = v$$

$$BD = u+v$$

For the right hand side,

$$d_{BH}$$

$$= BD + DH$$

Because ABCDEFGH is a right prism

$$BF = DH = h$$

$$BD + DH$$

$$= u + v + h$$

$$= \text{Left hand side}$$

(b)(i)  $d_{BA} = B - A$

$$= (5, 3, 4) - (4, 0, 3)$$

$$= (1, 3, 1)$$

$$d_{BC} = B - C$$

$$= (5, 3, 4) - (1, 4, 5)$$

$$= (4, -1, -1)$$

$$d_{BF} = B - F$$

$$= (5, 3, 4) - (4, 2, 8)$$

$$= (1, 1, -4)$$

$$d_{BA} + d_{BC} + d_{BF} = (1, 3, 1) + (4, -1, -1) + (1, 1, -4)$$

$$= (6, 3, -4)$$

$$d_{BH} = (6, 3, -4)$$

$$(5, 3, 4) - H = (6, 3, -4)$$

$$H = (5, 3, 4) - (6, 3, -4)$$

$$H = (-1, 0, 8)$$

(b)(ii)  $BH = 7.81$   
 $OH = 8.06$

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Q2 EXE 2 Question 23

(6 marks)

(a)  $1T\mathbf{w}$  means multiplying all the value of  $\mathbf{n}$ -vector by one and add up all together to see the total words in the document.

(b)  $w_{282}=0$  means that the word count of the  $i^{\text{th}}$  keyboard is zero, that means in the document there are no that word present.

(c)  $\mathbf{w}/(\mathbf{U}^T\mathbf{w})$

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Q3 EXE 2 Question 25

(4 marks)

$$b_1 = \beta_3 a_1 + \beta_4 a_2$$

$$b_2 = \beta_1 a_1 + \beta_2 a_2$$

$$c = a_1 b_1 + a_2 b_2$$

$$= a_1(\beta_1 a_1 + \beta_2 a_2) + a_2(\beta_3 a_1 + \beta_4 a_2)$$

$$= (a_1 \beta_1 + a_2 \beta_3) a_1 + (a_1 \beta_2 + a_2 \beta_4) a_2$$

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This shows that  $c$  is a linear combination of  $a_1$  and  $a_2$ .