Exam 17/18 B

Q|(a) 
$$\int \frac{e^{3x} - 3}{e^{x+1}} e^{x-2} dx = \int \left[ \frac{e^{3y}}{e^{x+1}} - 3 \frac{e^{-x-2}}{e^{x+1}} \right] dx$$

$$= \int \left[ \frac{3x - (x+1)}{e^{x+1}} - 3 \frac{e^{-x-2} - (x+1)}{e^{x+1}} \right] dx$$

$$= \int e^{2x-1} - 3 e^{-2x-3} dx$$

$$= \frac{e^{2x-1}}{2} - 3 \frac{e^{-2x-3}}{2} + C$$

$$y = x^{4} + 2 \not\equiv 3 \frac{dy}{dx} = 4x^{3} \implies dx = \frac{dy}{4x^{2}}$$

$$= \frac{1}{4} \int \sec^{2}(x^{4} + 2) dx = \frac{1}{4} \int \sec^{2}y dy = \frac{1}{4} \tan y + C$$

$$= \frac{1}{4} \int \tan (x^{4} + 2) + C$$

(c)  $\int_{0}^{2} |x - 1| dx = \int_{0}^{1} |x - 1| dx + \int_{1}^{2} |x - 1| dx$ 

$$= \left[ \frac{x - 1}{2} + x \right]_{0}^{1} + \left[ \frac{x^{2}}{2} - 1 \right]_{1}^{2}$$

$$= \frac{1}{4} \int \frac{1}{4} \tan (x^{4} + 2) dx = \frac{1}{4} \int \frac{1}{4} \tan (x^{4} + 2) dx$$

$$= \left[ \frac{x - 1}{2} + x \right]_{0}^{1} + \left[ \frac{x^{2}}{2} - 1 \right]_{1}^{2}$$

$$\int \frac{x}{\sqrt{9-x^2}} dx$$

$$= \int \frac{9 \sin^2 \theta}{\sqrt{9-x^2}} 3\cos \theta d\theta$$

$$= \int \frac{9 \sin^2 \theta}{\sqrt{9-x^$$

 $x^{2}+1$   $\frac{1}{x^{2}}+x$ 

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$$J_1 = \int \frac{x^2 + x}{x^2 + 1} dx$$

improper rational function, need hong dissur

$$= \int \left[\frac{1}{2} + \frac{\left(x - \frac{1}{2}\right)}{x^2 + 1}\right] dx$$

$$= \int_{2}^{1} dx + \int_{x^{2}+1}^{x} dx - \int_{2}^{1} \int_{x^{2}+1}^{1} dx$$

$$= \int_{2}^{1} dx - \int_{2}^{1} \int_{x^{2}+1}^{1} dx$$

$$= \int_{2}^{1} dx - \int_{2}^{1} \int_{x^{2}+1}^{1} dx$$

$$= \int_{2}^{1} dx - \int_{2}^{1} \int_{x^{2}+1}^{1} dx$$

 $=\frac{1}{2}x + \frac{1}{2}\ln|x^2+1| - \frac{1}{2}\tan^2 x + C$ 

$$\int_{0}^{\infty} \int_{0}^{\infty} (x+1) tan^{-1} x dx = \left(\frac{x^{2}}{2} + x\right) tan^{-1} x - \frac{1}{2}x - \frac{1}{2} \ln|x^{2} + 1| + \frac{1}{2} tan^{-1} x + C$$

$$\frac{264}{15} \int \frac{10 \times (x+3)(x^2+4x+13)}{(x+3)(x^2+4x+13)} dx$$

$$\frac{10\times}{(X+3)(\chi^2+4\chi+13)} = \frac{A}{\chi+3} + \frac{B\chi+C}{\chi^2+4\chi+13}$$

$$\Rightarrow$$
 10 x = A(x2+4x+13) + (Bx+c) (A+4x+13) (x)

$$X=-3: -30 = A(9-12+13) = 10A \Rightarrow A=-3$$

Compare the coefficient 
$$x^2$$
:  $0 = A + B = B = -A = 3$   
compare the constant term:  $0 = 13A + 3C \Rightarrow BC = \frac{13}{3}A = 13$ 

$$I = \int \frac{-3}{x+3} dx + \int \frac{3x+13}{x^2+14x+13} dx$$

$$-3 \ln |x+3|$$

$$y = x^{2} + 4x + 13 \Rightarrow \frac{dy}{dx} = 2x + 4$$
  
express  $3x + 13 = a(2x + 4) + b$   
 $= 2ax + (4a + b)$   
 $\Rightarrow 32a = 3 \Rightarrow a = \frac{2}{3}$ 

$$I_{1} = \int \frac{3 \times + 13}{x^{2} + 4x + 13} dx = \frac{3}{2} \int \frac{2x + 4}{x^{2} + 4x + 13} dx + 7 \int \frac{1}{x^{2} + 4x + 13} dx$$

$$\begin{vmatrix} 4a+b=13 \\ \end{vmatrix} \Rightarrow b=13-4a=13-6=7$$

$$\int \frac{d(x^2+4x+13)}{X^2+4x+13} = \ln |x^2+4x+13|$$

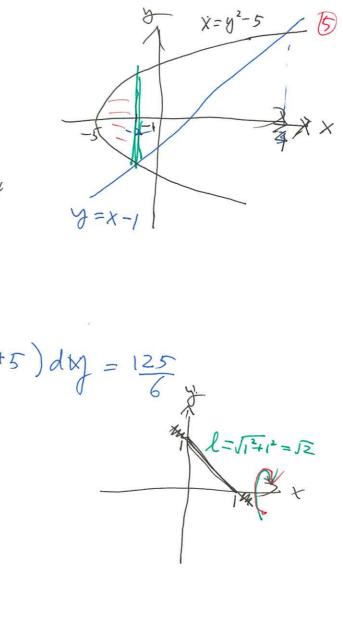
$$\int \frac{1}{(x+2)^{2}+9} dx = \frac{1}{9} \int \frac{1}{(x+2)^{2}+1} dx$$

$$= \frac{1}{9} \int \frac{1}{(x+2)^{2}+1} dx$$

= 3 lm (x2+4x+13) + = tan-1(x+2)+c

$$I = -3 \ln |x+3| + \frac{3}{2} \ln |x^2 + 4x + |3| + \frac{7}{3} \tan^{-1} (\frac{x+2}{3}) + \frac{1}{2} \ln |x+3| + \frac{1}{3} \tan^{-1} (\frac{x+2}{3}) + \frac{1}{3} \tan^{-1} (\frac{x+2$$

$$\begin{array}{lll} & \mathbb{R}^{2} \cdot \mathbb{R}^{2} - \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} - \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} - \mathbb{R}^{2} \cdot \mathbb{R}^{2} + \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2} \\ & \mathbb{R}^{2} \cdot \mathbb{R}^{2$$



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Q 499/ P(1,2,3), Q(-3,1,-2), 2 [PR] = 3/QR) => 1PR = 3/QR == 3/QR
                                     R between P, Q => 2 PR = 3 RQ
      method(I) 2 PR = 3 RQ DR = xī +yj +3k
                                                (x-1) 1 + (3-2) f + (3-3) k
                                          2[(x-1)]' + (y-2)J' + (3-3)E] = 3[(-3-x)]' + (1-y)J' + (-2-3)E)
                        \Rightarrow 0 \ 2(x-1) = 3(-3-x) \Rightarrow 2x-2 = -9 - 3x = 5x = -7 \Rightarrow x = -\frac{7}{5}
                              (3) 2(4分)=3(1-4)=) 2分-4=3-34 ラケリーキョケーキョンケーキョ
                            (3) 2(3-3) = 3(-2-3) \Rightarrow -6=33 \Rightarrow 53=0 \Rightarrow 5=0
                                     ·· R=(-=, =, )
       · R=(-妻, 圭,0) (
          (b) A = (-1, -2, -3) B = (3, -1, 2), C = (1, 3, 0)
                    \overrightarrow{AB} = \overrightarrow{OB} - \overrightarrow{OA} = 4\overrightarrow{C} + \overrightarrow{J} + 5\overrightarrow{K}
\overrightarrow{AC} = \overrightarrow{OC} - \overrightarrow{OA} = 4\overrightarrow{C} + 5\overrightarrow{J} + 3\overrightarrow{K}
\overrightarrow{N} = \overrightarrow{AB} \times \overrightarrow{AC} = -22\overrightarrow{C} - 2\overrightarrow{J} + 18\overrightarrow{K}
           P(x,y,3) \Rightarrow \overline{OP} = x_1 + y_1 + z_2 \qquad \overline{AP} = \overline{OP} - \overline{OA} = (x+1)_1 + (y+1)_1 + (y+
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$$\frac{0.540}{1-i} \left(\frac{1+i'}{1-i}\right)^{2018} = \frac{1+i'}{1-i} \cdot \frac{1+i'}{1+i} = \frac{1+2i+(-1)}{1^2+1^2} = \frac{2018}{1^2+1^2} = (-1)^{1009} = \frac{1}{1^2+1^2} = \frac{1}{1^2+1^2$$

 $z_2 = (2^{\frac{1}{6}} e^{i(2\frac{1}{3} + 4\pi)/3} = 12^{\frac{1}{6}} e^{i(4\frac{11}{3})} = 12^{\frac{1}{6}} e^{i(4\frac{11}{3} - 2\pi)} = 12^{\frac{1}{6}} e^{i(-4\frac{11}{3})}$ 

$$\begin{vmatrix} \hat{Q} & 6 & 9 \\ 0 & | A | = \begin{vmatrix} 3 & 1 & 1 & -2 \\ -2 & 2 & 2 & 2 \\ 0 & -1 & -1 \end{vmatrix} = \begin{vmatrix} 3 & 1 & 1 & -2 \\ 0 & -1 & -1 & 1 \end{vmatrix}^{2} = -6$$

$$|A^{T} A^{-2}| = |A^{T}| |A^{-1}|^{2} = \frac{1}{|A|} = -6 = -\frac{1}{4}$$

$$|A| (|A|)^{2}$$

$$\begin{array}{c} R_2 \longrightarrow R_3 \\ \hline 0 & + 1 \\ \hline 0 & + 1 \\ \end{array} \begin{array}{c} R_3 + 4R_2 \\ \hline 0 & -1 \\ \hline 0 & -3 \\ \end{array} \begin{array}{c} row e chelon form \\ \hline \end{array}$$

$$\frac{-R_{2}}{-\frac{1}{3}R_{3}} \begin{pmatrix} D & -1 & -1 & 0 & -\frac{1}{2} & 0 \\ 0 & 0 & 1 & 0 & 0 & -1 \\ 0 & 0 & 1 & 0 & 0 & -\frac{1}{3} & \frac{1}{4} & \frac{1}{3} \\ 0 & 0 & 1 & -\frac{1}{2} & -\frac{1}{4} & \frac{1}{3} \\ 0 & 0 & 1 & -\frac{1}{2} & -\frac{1}{2} & -\frac{1}{2} \\ 0 & 0 & 1 & -\frac{1}{2} & -\frac{1}{2} & -\frac{1}{2} \\ 0 & 0 & 1 & -\frac{1}{$$