

1. Evaluate the following integrals.

(a)  $\int_0^2 x e^x dx$

(b)  $\int_0^2 x^2 e^x dx$

(c)  $\int \frac{2e^{\tan x}}{\cos^2 x} dx.$

2. Solve the following differential equations for  $y$ .

(a)  $\frac{dy}{dx} = 3 \cos 2x$

(b)  $\frac{dy}{dx} = 3x^2 e^{-y}$  with the initial condition of  $y(0) = 1$

(c)  $\frac{dy}{dx} = \frac{y^2}{x^2} + \frac{y}{x} + 1$  (Hint: You may let  $z = \frac{y}{x}$ )

3.

(a) Reduce each of the following expressions to a single sinusoidal function:

(i)  $(\sin x - \cos x)^2 - 1$

(ii)  $\sin x \cos x \cos 2x \cos 4x$

(b) Reduce the following expression to a single sinusoidal function and state the amplitude, frequency and phase of the single sinusoidal function:

$$2 \sin (3t + \pi/6) + 4 \cos 3t$$