

Answers

Tutorial 1

Q1

- (i) It is not complete in mathematics to include real numbers only. Some mathematical problems cannot be solved by using real numbers only. Complex numbers are needed to solve them.

(ii)

| | Modulus | Argument | Complex conjugates |
|-------------------------------|------------|----------|-------------------------------|
| $-j$ | 1 | $-\pi/2$ | j |
| -3 | 3 | π | -3 |
| $1 + j$ | $\sqrt{2}$ | $\pi/4$ | $1 - j$ |
| $\cos \theta + j \sin \theta$ | 1 | θ | $\cos \theta - j \sin \theta$ |

Q2

$$(a) \frac{9}{41} + \frac{40}{41}j$$

$$(b) \frac{2}{13} - \frac{3}{13}j$$

$$(c) \frac{4}{13}$$

$$(d) \frac{x}{x^2+y^2} + \frac{y}{x^2+y^2}j$$

Q3

(i)

$$z_1 = \frac{\sqrt{2}}{2} - j\frac{\sqrt{2}}{2}$$

$$z_1^2 = -j$$

(ii)

$$z_2 = \sqrt{3} \angle \arctg(-\sqrt{2})$$

$$z_2^2 = 3 \angle \arctg(2\sqrt{2})$$

(iii)

$$\frac{z_1}{z_2} = \left(\frac{1}{3} + \frac{\sqrt{2}}{6}\right) + j\left(\frac{1}{3} - \frac{\sqrt{2}}{6}\right)$$

Tutorial 2

Q1

(a)

$$\frac{dy}{dx} = 6x$$

At $x = 3$, $\frac{dy}{dx} = 18$

(b)

(i)

$$\frac{dy}{dx} = 2x \sec^2(x^2 + 1)$$

(ii)

$$\frac{dy}{dx} = 8x \sec^2(2x^2 - 1) \tan(2x^2 - 1)$$

(iii)

$$\frac{dy}{dx} = \frac{e^x - \sin x}{e^x + \cos x}$$

Q2

(a)

$$\frac{dy}{dt} = -e^{-t} + e^t$$

At $t = 5$,

$$\frac{dy}{dt} = -e^{-5} + e^5$$

(b)

At $t = 0$, $y' = 0$. $\therefore (0,0)$

Q3

(a)

$$\frac{dy}{dx} = -\sin x \cos(\cos x)$$

(b)

$$\frac{dg}{dx} = e^x [\sin(\cos x) - \sin x \cos(\cos x)]$$

Tutorial 3

Q1

(a) $e^2 + 1$

(b) 12.78

(c) $2e^{\tan x} + 2c$

Q2

(a) $\frac{3}{2}\sin 2x + C$. This is the required general solution.

(b) $y = \ln(x^3 + e)$

(c) $y = x \tan(\ln|Dx|)$

Q3

(a)

(i) $-\sin 2x$

(ii) $\frac{1}{8}\sin 8x$

(b) The amplitude is $2\sqrt{7}$, the frequency is $\frac{3}{2\pi}$ Hz, and the phase is 1.2373.