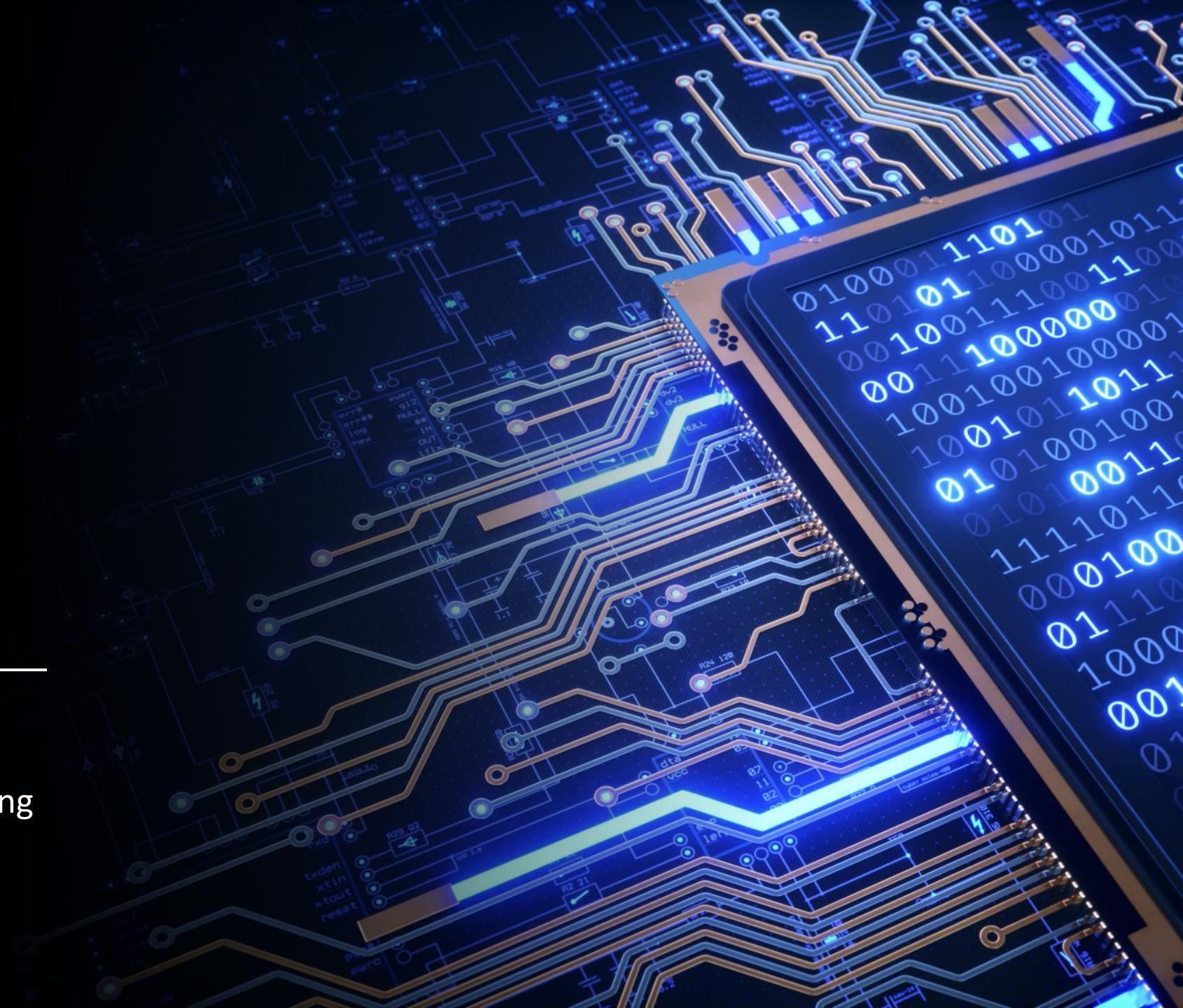




Microcomputer interface – Analog to Digital Conversion

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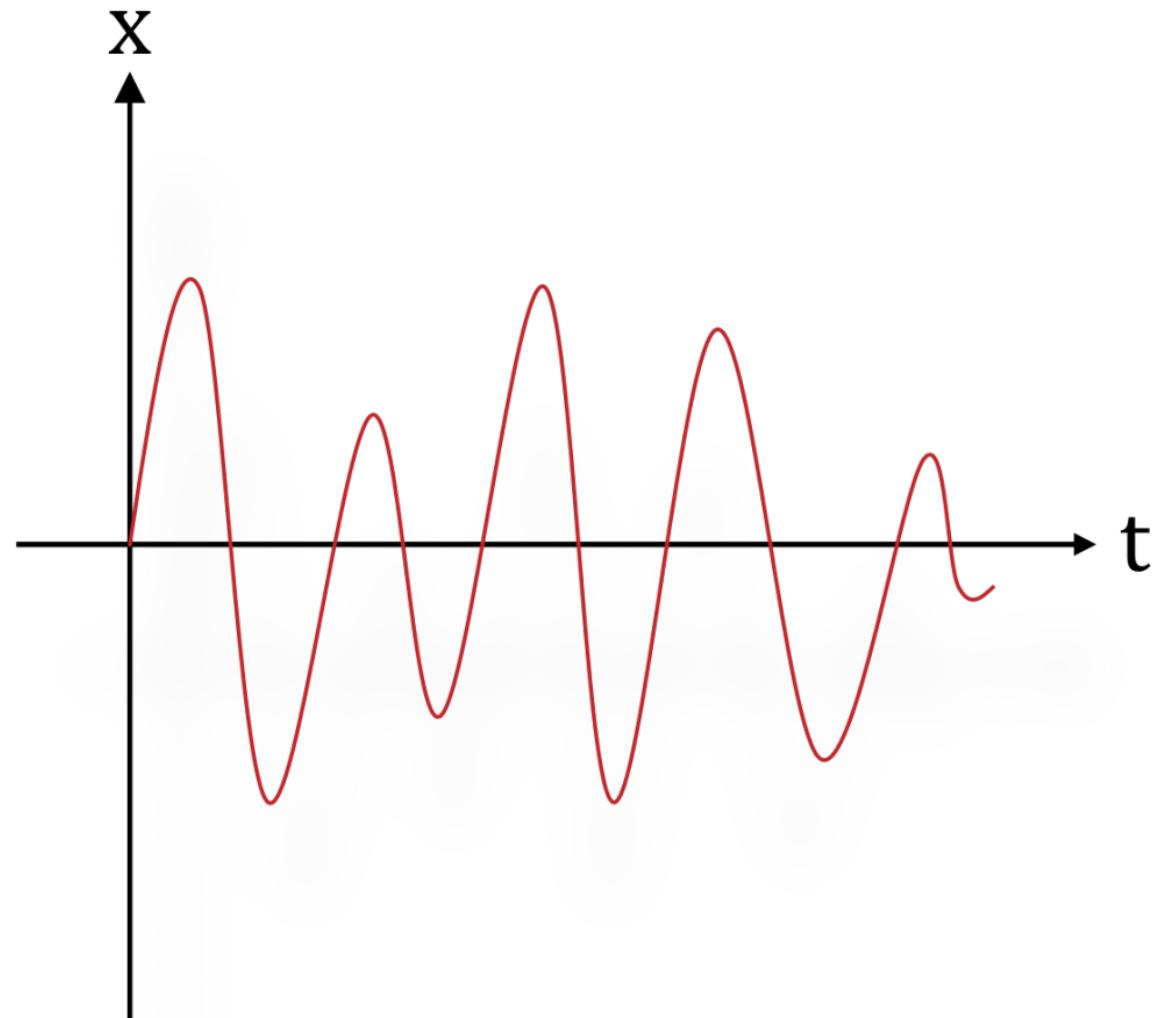
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Analog Signals [Revision]

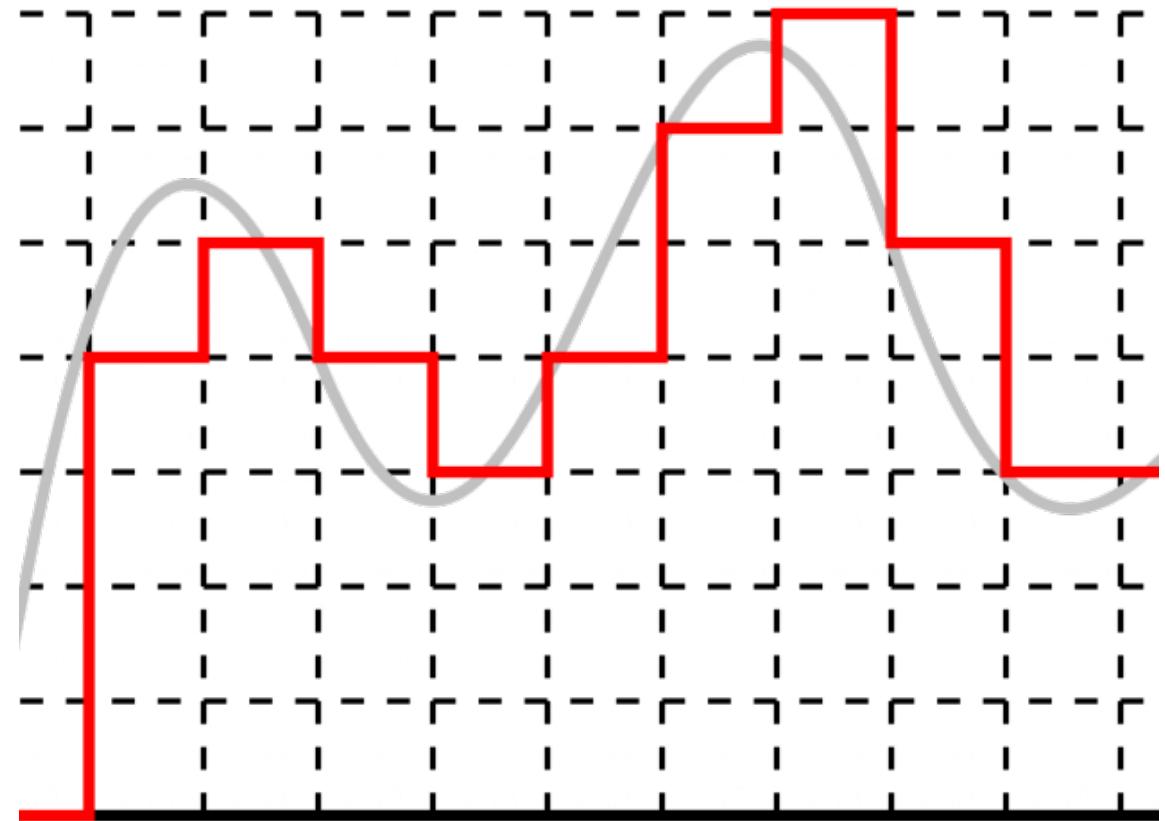
- Voltage of a pin with reference to signal ground (GND)
- What is an analog value?
 - Vary within a range, not in discrete values; Theoretically infinite number of possible values within that range.
- Typically, sensors delivers analog signal. However, some will give discrete levels, such as 0V and 3.3V, or a numerical value.



Digital Signals

[Revision]

- Digital signals carry the data although it is a bit different. These signals are discrete or not continuous.
- A digital signal carries the data in the form of binary because it signifies in the bits. [Later, we will discuss in analog to digital conversion.]





Something need to know first

- Relationship between binary, decimal, hexadecimal numbers?
- What are analog and digital signals?
- What is analog-to-digital converter?

Number Representation

	2	3	6
Multiplier	10^2	10^1	10^0

- Daily life, we use decimal
 - Each digit is a number from 0 to 9
 - Eg. a number 236_d is interpreted in the following way:

Binary Representation

- Similarly, we can have a binary representation
 - Each binary digit (called **bit**) is either 0 or 1
 - Eg. 110101_b

1	1	0	1	0	1
$2^5 = 32$	$2^4 = 16$	$2^3 = 8$	$2^2 = 4$	$2^1 = 2$	$2^0 = 1$

$$\text{So, } 110101_b = (32+16+4+1)_d = 53_d$$

↑
Indicate it is binary

↑
Indicate it is decimal

Hexadecimal Representation

- Also for hexadecimal representation
 - Each digit is from 0-15 (we use A-F to represent 10-15)

Decimal: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

Hexadecimal: 0 1 2 3 4 5 6 7 8 9 A B C D E F

- E.g. 13F_h

1	3	F
16^2	16^1	16^0

$$\text{So, } 13F_h = (1 \times 256 + 3 \times 16 + 15 \times 1)_d = 319_d$$



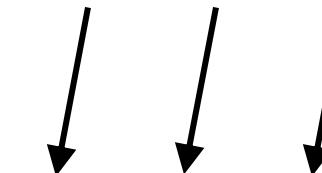
Indicate it is hexadecimal

Decimal to Binary Conversion

- Decimal to Binary

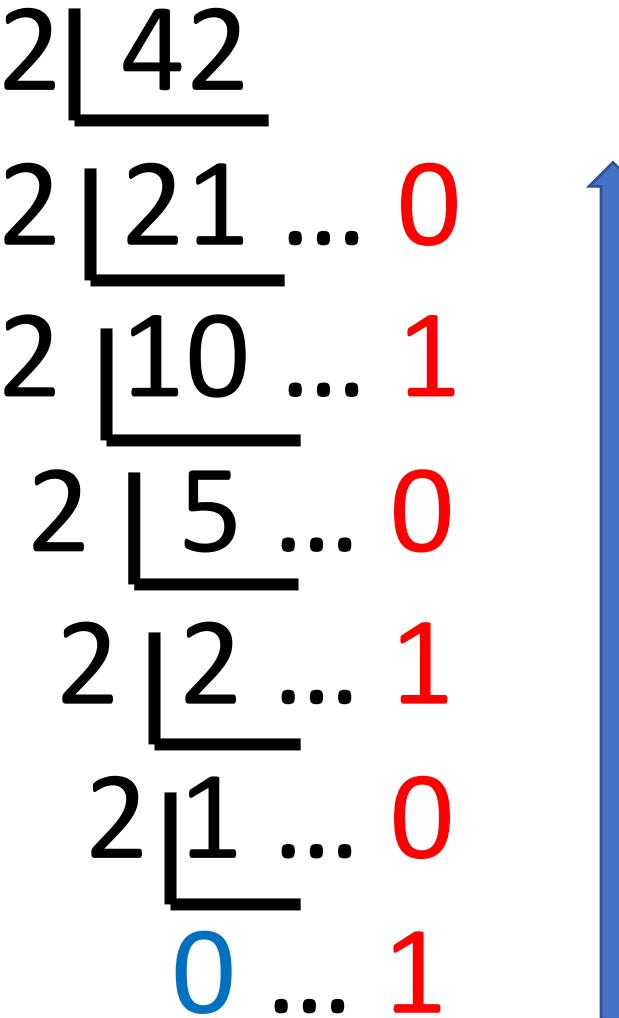
- $42_d = 101010_b$

- 1 0 1 0 1 0



$$2^5 + 2^3 + 2^1 = 32 + 8 + 2 = 42$$

Long division



Decimal to Hexadecimal Conversion

- Decimal to Hexadecimal: $495_d = \text{1EF}_h$

$$\begin{array}{r} 16 \mid 495 \\ \hline 16 \mid 30 \dots 15(F) \\ \hline 16 \mid 1 \dots 14(E) \\ \hline 0 \dots 1 \end{array}$$

$$1 \times 16^2 + 14 \times 16 + 15 = 495_d$$

1EF_h

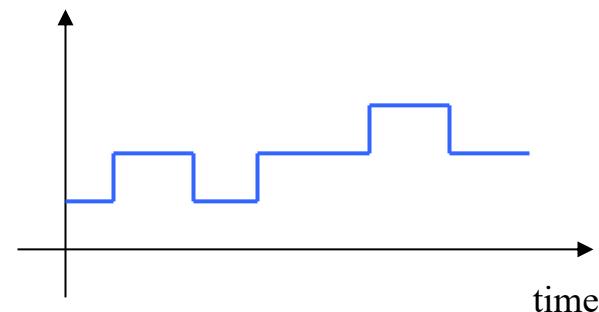
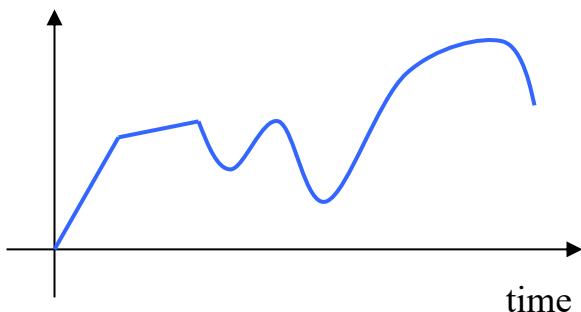
Binary to Hexadecimal Conversion

- From Binary to hexadecimal
 - 4 binary bits to 1 hexadecimal digital
 - Eg. **0110** 1010 -> **6 A**
 - From hexadecimal to binary
 - 1 hexadecimal digital to 4 bit
 - Eg. **6** => **0110**, **A** => 1010
- So **6 A** -> **0110 1010**

4 bits	1 hex
0000	0
0001	1
0010	2
0011	3
0100	4
0101	5
0110	6
0111	7
1000	8
1001	9
1010	A
1011	B
1100	C
1101	D
1110	E
1111	F

Analog Signal and Digital Value

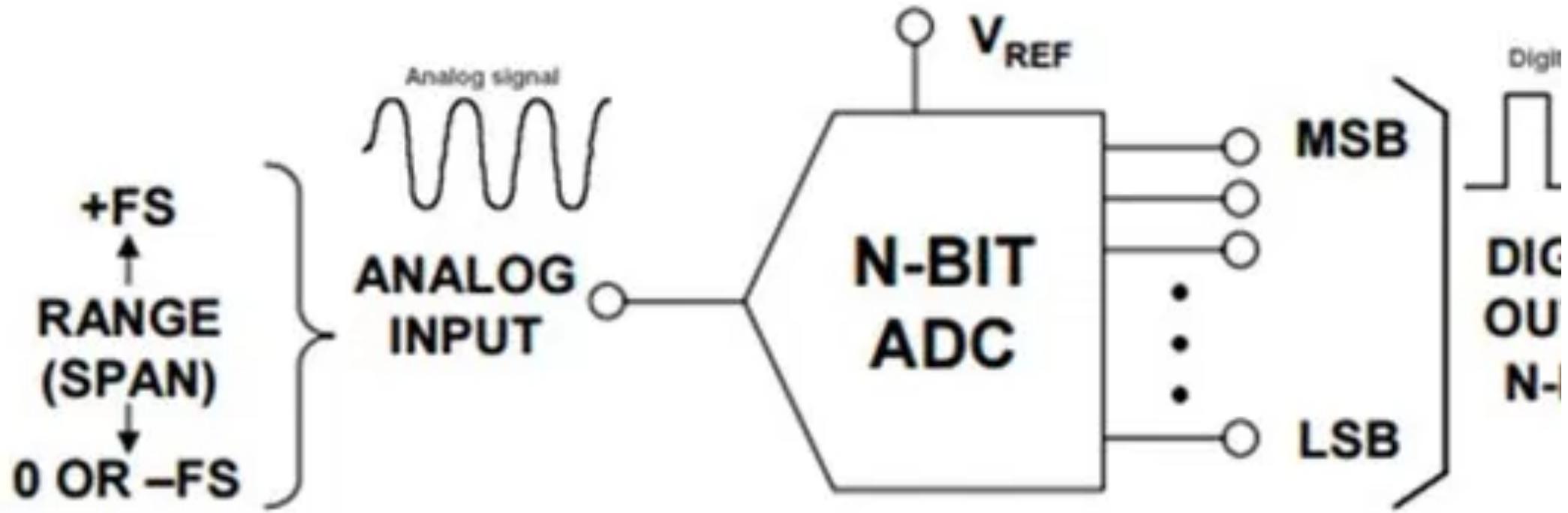
- analog signal: the signal can have a continuous range of amplitudes.
 - Example: temperature of a room
- Digital signal: the signal is **quantized** and has finite set of amplitudes.





ADC in Micro:bit

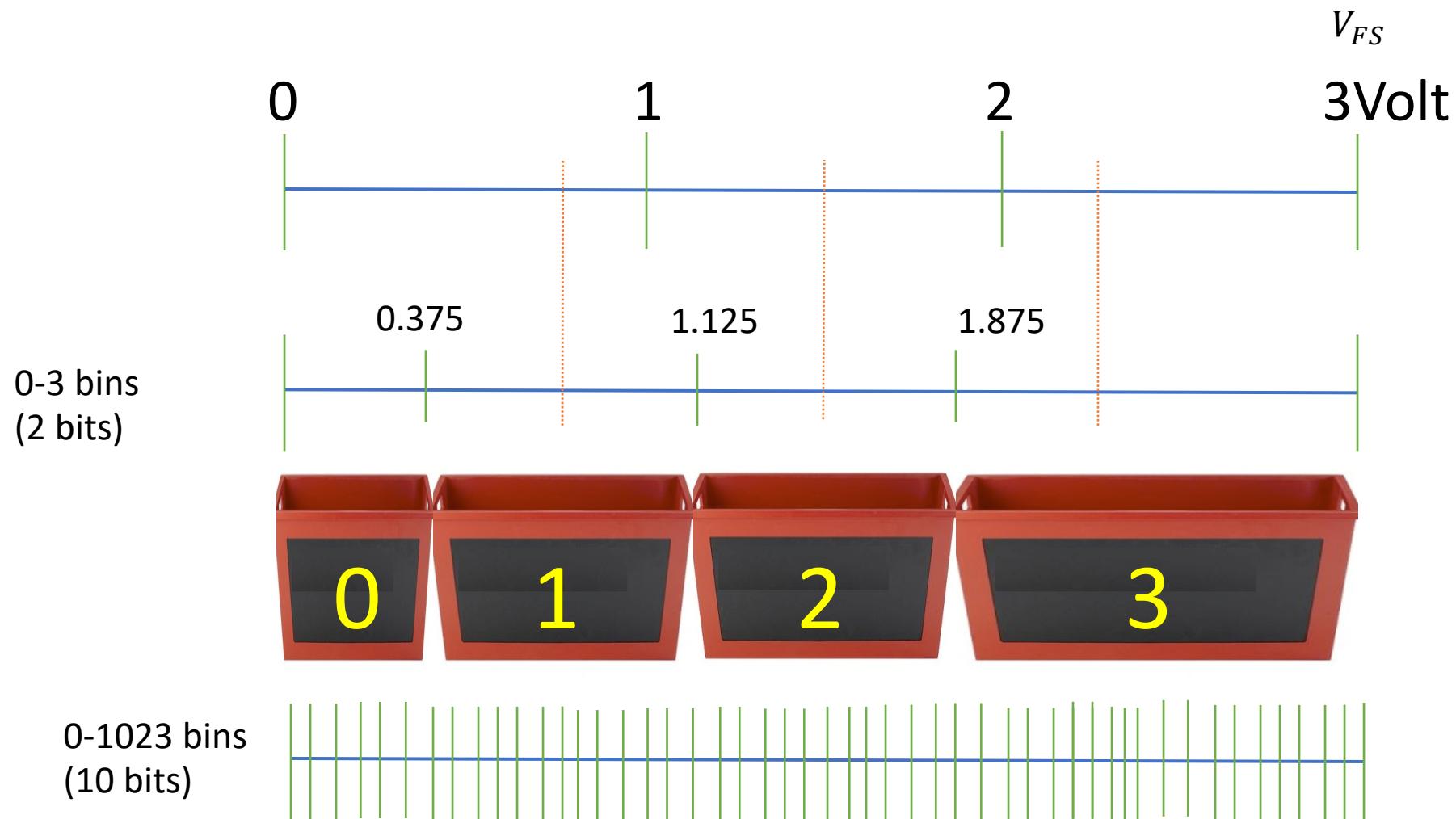
- A device called analog-to-Digital Converter (ADC) is inside the processor of Micro:bit
- ADC converts an analog signal (in voltage) to digital output
- The output is in binary, called as code word
- Resolution measured by number of bits in code word
 - Resolution of micro:bit = 10 bits (N=10 bits)



- Input: 0 to V_{FS} (full scale voltage)
- Output: 10 bits
 - Smallest: 00000 00000 \Rightarrow 0
 - Largest: 11111 11111 \Rightarrow 1023

More Details

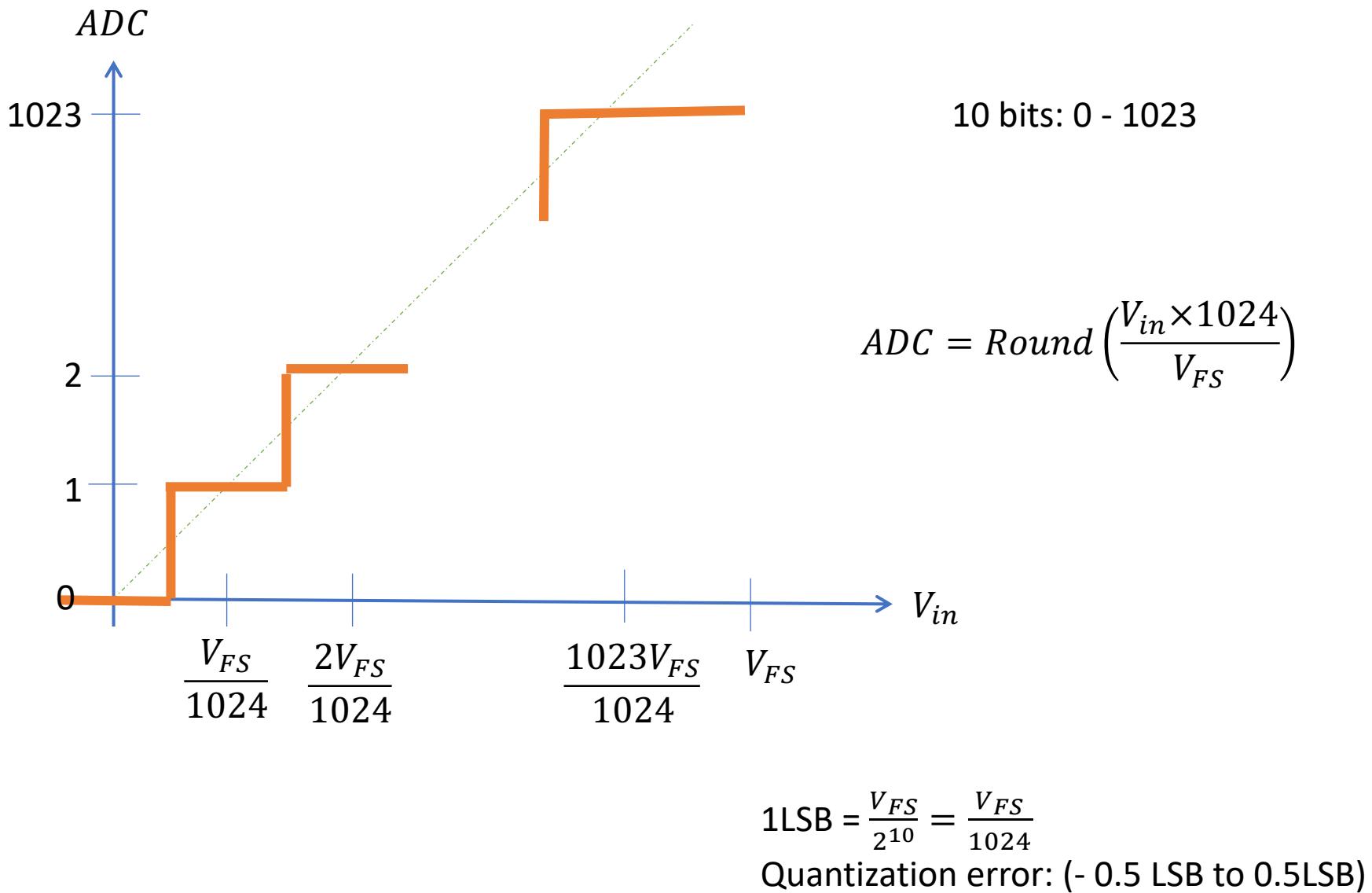
Illustration



$$1 \text{ Least significant bit (LSB)} = \frac{V_{FS}}{2^N}$$

Quantization error: (- 0.5 LSB to 0.5 LSB)

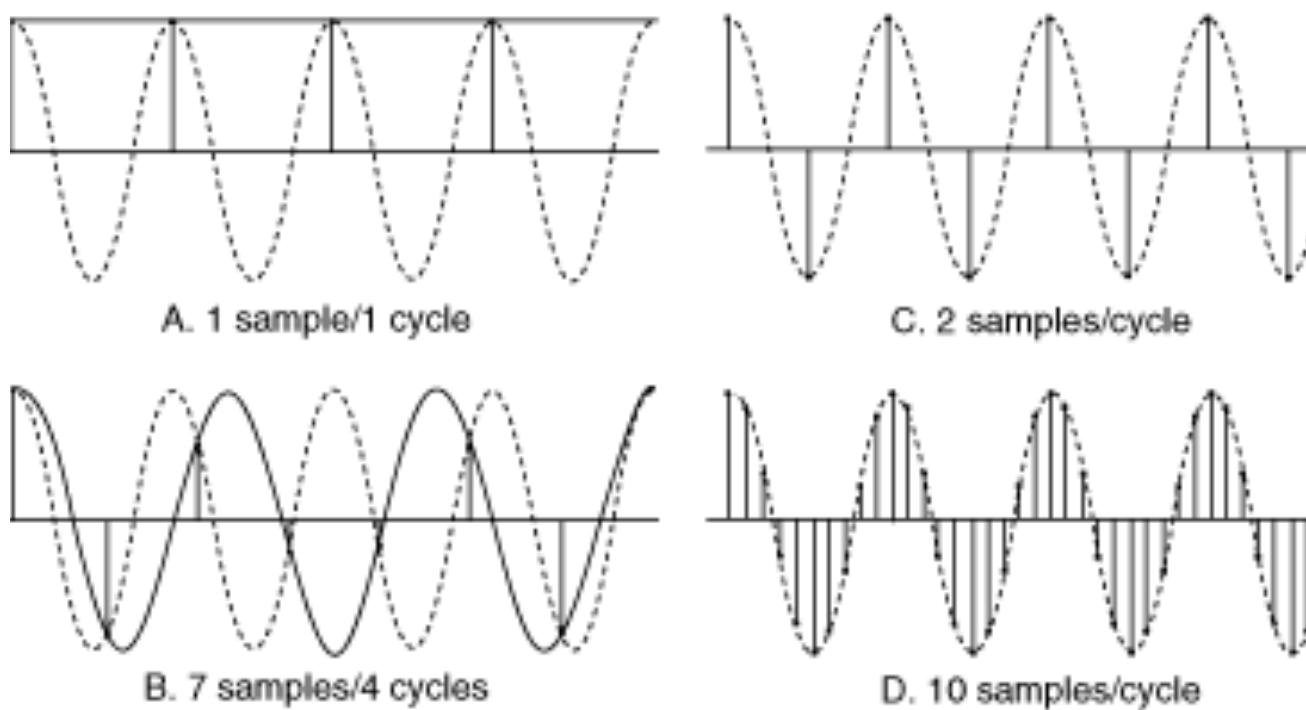
ADC



Conversion Time

- After sampling the signal, the conversion time is the time required for ADC to complete a single conversion.
- Conversion time for micro:bit takes (typically) $68\mu\text{s}$ to convert a single sample in 10 bit

Shannon Sampling Theory



According to the sampling theorem (Shannon, 1949), to reconstruct a one-dimensional signal from a set of samples, the sampling rate must be equal to or greater than twice the highest frequency in the signal.

Analog Read

- Perform ADC on the voltage at the pin (eg. P0) and obtain the digital value
- Range of digital value: 0 – 1023 (10 bit ADC)
- Relationship between the digital value and the input:

$$ADC = Round\left(\frac{V_{in} \times 1024}{V_{dd}}\right) \quad V_{FS} = V_{dd}$$

where ADC is the digital value, V_{in} is the analog input.

- Eg. $V_{dd} = 3V$, $V_{in}=1V$, we have 341_d (or 0101010101_b)

Note: A GPIO pin must not be exposed to higher voltage than VDD + 0.3 V.

Example

- Analog Input to Microbit

The screenshot shows the Microsoft micro:bit Python code editor interface. The top navigation bar includes the micro:bit logo, Home, Share, Blocks, Python (selected), Help, Settings, and Microsoft. The main area displays a digital representation of a micro:bit board with its pins labeled (0, 224, 1, 2, 3V, GND). Below the board is an Explorer sidebar. The Python code block contains the following script:

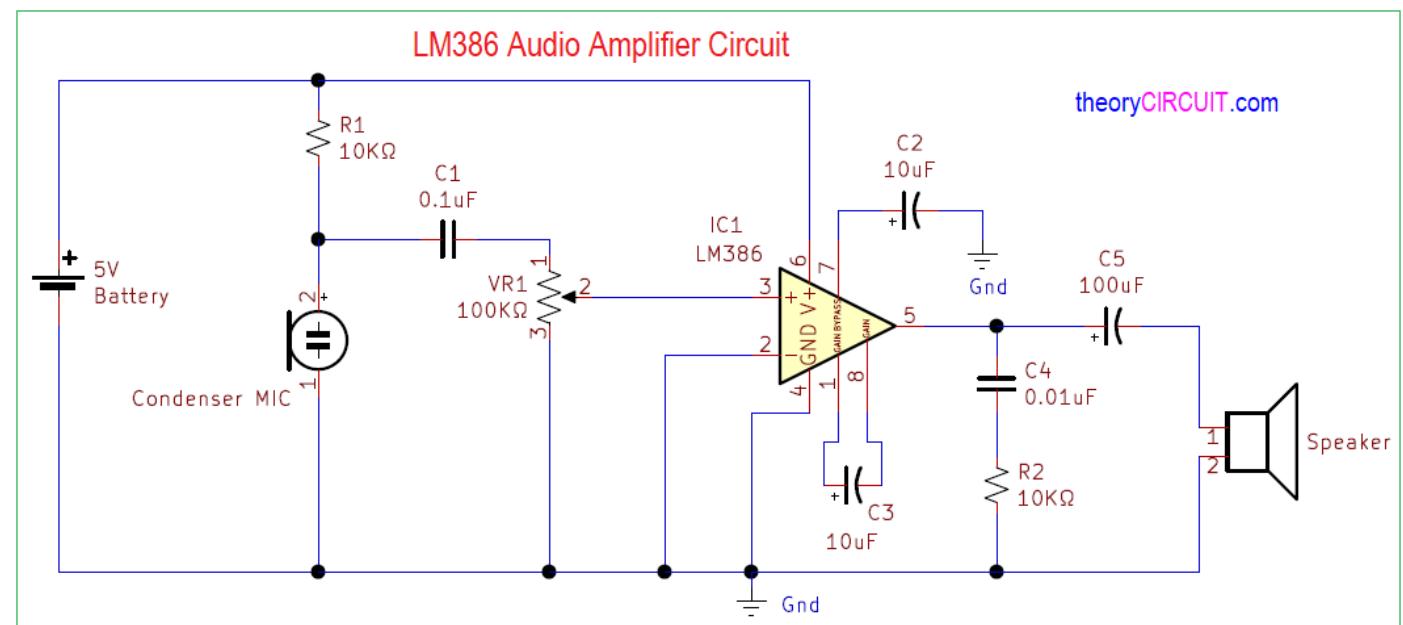
```
1 P0_data = 0
2
3 def on_forever():
4     global P0_data
5     P0_data = pins.analog_read_pin(AnalogPin.P0)
6     if P0_data > 682:
7         basic.show_number(3)
8     elif P0_data > 342:
9         basic.show_number(2)
10    else:
11        basic.show_number(1)
12 basic.forever(on_forever)
```

Analog audio amplifier

- The input is an analog signal derived from the condenser microphone
- The output of the audio amplifier – LM 386 is also an analog signal. Preferably, its waveshape is the same as the input analog signal.

Question:

If the input and output waveshape are the same, why is it necessary to use an amplifier?



Digital audio amplifier

- The input can be an analog signal derived from the condenser microphone, or a digital source
- The amplifier consists of a switching stage which generates pulsedwidth modulation (PWM) signal. Due to the presence of low-pass filter, the signal applied to the speaker is the same as the source.

Question:

What is PWM? How is it related to the amplitude or frequency of the signal?

