

Quiz 4

Full mark

Question 1 EXE3 Q14

(5 marks)

For matrix A

$$\begin{aligned}\text{Determinant} &= 0(0 - 0) - 0(0 - 0) + 1(1 - 0) \\ &= 1\end{aligned}$$

For matrix B

$$\begin{aligned}\text{Determinant} &= 0(0 - 1) - 1(0 - 1) + 1(1 - 0) \\ &= -1(-1) + 1(1) \\ &= 1+1 \\ &= 2\end{aligned}$$

For matrix C

$$\begin{aligned}\text{Determinant} &= 1(1-1) - 1(1-1) + 1(1-1) \\ &= 0\end{aligned}$$

Question 2 EXE3 Q27

(5 marks)

If A isn't a square matrix, then  $|A|$  doesn't exist because its size is not  $n \times n$ , cannot find the determinant of A.

Question 3 EXE3 Q34

(5 marks)

U and V are orthogonal

Therefore  $U^T = U^{-1}$  and  $V^T = V^{-1}$

$$\begin{aligned}UV(UV)^T &= UV(V)^T(U)^T \\ &= UIU^T \\ &= UU^T \\ &= I\end{aligned}$$

$$W = \frac{1}{\sqrt{2}} \begin{bmatrix} U & U \\ V & -V \end{bmatrix}$$

$$WW^T = I$$

$$W^T = W^{-1}$$

Therefore it is orthogonal.