$$= \int \frac{1}{8 \tan^2 \theta} \left(2 \sec \theta \tan \theta d\theta\right) = \int \frac{\sec \theta}{4 \tan^2 \theta} d\theta$$

$$= \frac{1}{4} \int \frac{\cos \theta}{\sin^2 \theta} d\theta = \int \frac{1}{\cos^2 \theta} d\theta = \int \frac{\cos^2 \theta}{\sin^2 \theta} d\theta = \int \frac{\cos^2 \theta}{\sin^2 \theta} d\theta$$

$$=\frac{1}{4}\frac{d(\sin\theta)}{\sin^2\theta} = \frac{1}{4}\left[\sin^2\theta\right] d(\sin\theta) = \frac{1}{4}\sin^2\theta + C = \frac{1}{4}\frac{1}{\sqrt{x^2-4}} + C = \frac{1}{4}\frac{1}{\sqrt{x^2-4}} + C$$

$$\frac{1}{x^{2}} \ln x \, dx = \int \ln x \left(\frac{1}{x^{2}} dx \right) = \frac{1}{x} \ln x - \int \left(\frac{1}{x} \right) \, d(\ln x)$$

$$= -\frac{1}{x} \ln x + \int \frac{1}{x^{2}} dx$$

$$= -\frac{1}{x} \ln x + \int \frac{1}{x^{2}} dx$$

(c)
$$J = \int \frac{9x^2}{(x^2 + 2x + 10)} dx$$

= $\int \frac{2}{x^2 + 2x + 10} dx$

= $2 \ln|x^2| + \int \frac{7x + 10}{x^2 + 2x + 10} dx$

Partial fractions $\frac{9x^{2}}{(x-2)(x^{2}+2x+10)} = \frac{A}{x-2} + \frac{B\times tC}{x^{2}+2x+10}$ $\Rightarrow 9x^{2} = A(x^{2}+2x+10) + (Bx+c)(x-2)$ $x=2: 36 = 18A \Rightarrow A=2$ compare the conficient $1x^{2}: 9=A+B \Rightarrow B=9-2=7$ compare the constant term: $\delta = 10A \neq 2C \Rightarrow C=10$ $\frac{d}{dx}(x^{2}+2x+10) = 2x+2$ express 7x+10 = a(2x+2)+b = 2ax+(2a+b) $\Rightarrow 52a=7 \Rightarrow a=\frac{7}{2}$ $12a+b=10 \Rightarrow b=10-7=3$

$$\int_{X^{2}+2X+10}^{2} dx = \frac{7}{2} \int_{X^{2}+2X+10}^{2X+2} dx + 3 \int_{X^{2}+2X+10}^{1} dx$$

$$= \int_{(X+1)^{2}+9}^{1} dx = \frac{1}{9} \int_{(X+1)^{2}+1}^{1} dx = \frac{1}{9} \int_{($$

$$R = \begin{cases} 2y = x + 4 \Rightarrow y = \frac{1}{2}x + \frac{1}{2} \\ y = x \\ x = 0 \end{cases}$$

$$x = \frac{1}{2}x + 2$$

$$x = 0$$

$$V_y = V_{outer} - V_{miner}$$

$$= \int_0^4 \pi \chi_{outer}^2 dy - \int_2^4 \pi \chi_{miner}^2 dy = \frac{3^2}{3^3} \pi$$

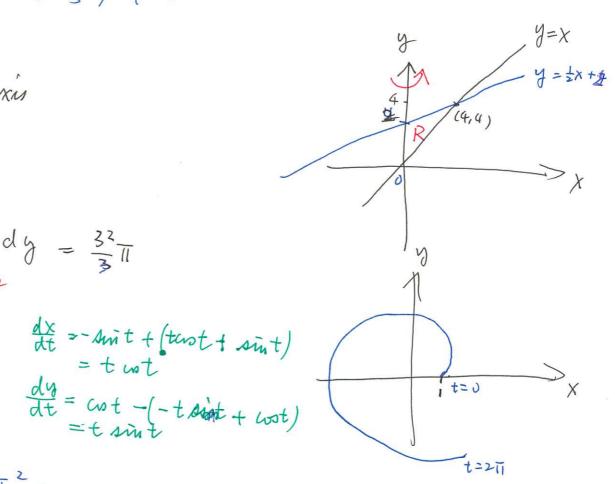
$$= \int_0^4 \pi \chi_{outer}^2 dy - \int_2^4 \pi \chi_{miner}^2 dy = \frac{3^2}{3^3} \pi$$

(b)
$$\int x = \cot t + t \sin t$$
 $0 \le t \le 2\pi$

$$\int y = \sin t - t \cot t$$

$$\int \frac{ds}{dt} = \int \frac{dx}{dt} + \left(\frac{dy}{dt}\right)^2 = |t|$$

$$\lambda = \int_{0}^{2\pi} \frac{ds}{dt} dt = \int_{0}^{2\pi} |t| dt = \frac{t^{2}}{2} \Big|_{0}^{2\pi} = 2\pi^{2} \|$$



Volume of parallelepiped $V = |\vec{a} \cdot \vec{b} \times \vec{c}| = |-17| = 17$ g

R Volume of Tetrahedron $\frac{1}{6}|\vec{a} \cdot \vec{b} \times \vec{c}| = \frac{17}{6}$

Q Find the plane equation containing A, B, C let $Q = \chi \vec{l} + y \vec{j} + 3\vec{k}$ on the plane. $\overrightarrow{AQ} = \overrightarrow{OZ} - \overrightarrow{OA} = \chi \vec{l} + (y-1)\vec{j} + (3+2)\vec{k}$ $0 = \overrightarrow{AD} \cdot \vec{N} = \forall \times +5(y-1) + 6(3+2) \Rightarrow \times +5y-5 + 63 + 12 = 0$ N=ABXAC

>> x+5y+63 = 5-12=-7 ← plane equation.

= Q 5(a) Simplify the complex number into Cartesian form (a+bi)

$$\frac{1+2i'}{3-4i} - \frac{3-2i}{5i} = \frac{1+2i}{3-4i} \frac{3+4i}{3+4i} - \frac{3-2i'-i}{5i} = \frac{-1+2i'}{5} = \frac{-1+2i'}{5} = \frac{1+5i'}{5} = \frac{1+5i'}{5} = \frac{1+2i'}{5}$$

(b) Solve i =3=13-i in Euler form with principal argument

Key Step; Express Z3 mito a complex number

$$\Rightarrow 2^3 = \frac{\sqrt{3} - i}{i} = \frac{-1 - \sqrt{3}i}{1} = -(-\sqrt{3}i)$$

$$|-|-|_{3i}| = \overline{(4)^2 + (-13)^2} = \overline{1+3} = 2$$

$$ang(-1-\bar{R}i) = -(\bar{\Pi} - \theta) = -(\bar{\Pi} - \tan|-\bar{\Pi}|) = -(\bar{\Pi} - \tan|\bar{\Pi}|)$$

$$\pm^{3} = 2e^{i(-2\sqrt{3})} = 2e^{i(-2\sqrt{3} + 2k\pi)}$$

$$= \frac{1}{2} = \frac{3}{3} e^{i(\frac{3\pi}{3} + 2k\pi)/3}, k=0,1,2.$$

$$= \frac{1}{3} e^{-i2\pi/9}$$

$$Z_{2} = 2^{1/3} e^{i(-2\pi + 4\pi)/3} = 2^{1/3} e^{i(9\pi - 2\pi)} = 2^{1/3} e^{i(9\pi - 2\pi)} = 2^{1/3} e^{-i\frac{9\pi}{9}}$$

$$A_{5}(G) \left(\begin{array}{c} 1 \\ 3 \end{array} \right)^{-1} = \frac{1}{|A|} adj A = \frac{1}{4 - 6} \left(\begin{array}{c} 4 \\ -2 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right) = \left(\begin{array}{c} -2 \\ \frac{3}{2} \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -3 \end{array} \right)^{T} = \frac{1}{2} \left(\begin{array}{c} 4 \\ -$$

Gaus elimination

$$\frac{1}{1} \frac{1}{1} = \begin{pmatrix} 2 & -1 & 0 & -5 & 1 \\ 1 & -1 & 2 & 0 & 2 \\ -3 & 1 & 2 & 10 & 0 \end{pmatrix} \xrightarrow{R_1 \leftrightarrow R_1} \begin{pmatrix} 1 & -1 & 2 & 0 & 2 \\ 2 & -1 & 0 & -5 & 1 \\ -3 & 1 & 2 & 10 & 0 \end{pmatrix}$$

$$\frac{R_2 - 2R_1}{R_3 + 3R_1} \begin{pmatrix}
1 & -1 & 2 & 0 & 2 \\
0 & 1 & -4 & -5 & 3 \\
0 & -2 & 8 & 10 & 6
\end{pmatrix}
\xrightarrow{R_3 + 2R_2} \begin{pmatrix}
0 & -1 & 2 & 0 & 2 \\
0 & 0 & -4 & -5 & -3 \\
0 & 0 & 0 & 0 & 0
\end{pmatrix}$$

R3: 0=0 consistent

C3 and C4 have no privots > 3 = 5, W= t are free variables

$$R_1: X-y+2f = 2 \implies X = 2+y-2f = 2+(-3+45+5+)-25$$

$$=-1+25+5+$$

vector solution
$$\begin{pmatrix} x \\ y \\ z \\ w \end{pmatrix} = \begin{pmatrix} -1 & t^2 & t^2 & t^2 \\ -3 & t^4 & t^4 & t^4 \\ s & t \end{pmatrix} = \begin{pmatrix} -1 \\ 3 \\ 0 \\ 0 \end{pmatrix} + s \begin{pmatrix} 2 \\ 4 \\ 1 \\ 0 \end{pmatrix} + t \begin{pmatrix} 5 \\ 5 \\ 0 \\ 1 \end{pmatrix}$$

. bill) Corresponding homogeneous system

 $\begin{cases} 2x - y & -5w = 0 \\ x - y + 2y & = 0 \\ -3x + y + 2y + 10w = 0 \end{cases}$ Two linearly independent solutions $\begin{cases} \frac{3}{4} \\ \frac{1}{6} \end{cases} = \begin{cases} \frac{5}{5} \\ \frac{1}{6} \end{cases}$