

Exercise 6 Solution

Question 1

(a)

$$k - 1 = 6, n - k = 3, n = 10, x^3 i(x) = q(x)g(x) + r(x), i(x) = x^6 + x^4 + x^2 + 1$$

$$\begin{array}{r} \underline{1101111} \\ 1101 \text{) } 1010101000 \end{array}$$

$$\underline{1101}$$

$$1111$$

$$\underline{1101}$$

$$1001$$

$$\underline{1101}$$

$$1000$$

$$\underline{1101}$$

$$1010$$

$$\underline{1101}$$

$$1110$$

$$\underline{1101}$$

$$11$$

$$\therefore 1010101000 = 1101111 \times 1101 + 011, \text{ codeword} = 1010101011$$

(5 marks)

(b)

$$\begin{array}{r} \underline{0011011} \\ 1101 \overline{)0010101011} \\ \underline{1101} \\ 1111 \\ \underline{1101} \\ 1001 \\ \underline{1101} \\ 1001 \\ \underline{1101} \\ 100 \end{array}$$

Since $r(x)$ is not zero, error is detected

(5 marks)