Common R

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R is an interpreted language (as opposed to a compiled language, such as C or PASCAL) which is converted to machine language (low-level) line by line.

In consideration of speed, we avoid For loops and instead use **vectorisation**, which applies the same operation to every entry in the vector.

We demonstrate vectorised code is faster and better-looking. First, the For loop:

```
#Sum of cos(x) using a for loop
fsum1 = function(x) {
  fsum = 0
  for (i in 1:length(x)) {
     fsum = fsum + cos(x[i])
  }
  return(fsum)
}
```

Now the same functionality vectorised:

```
#Sum of cos(x) using vectorisation
fsum2 = function(x) sum(cos(x))
```

Compare these in terms of system time:

0.00

```
x = 1:1e6 #runif(1e+06, min = -1, max = 1)
system.time(fsum1(x))

##     user     system elapsed
##     0.107     0.000     0.107
system.time(fsum2(x))

##     user     system elapsed
```

Matrix operations

0.03

##

Consider nested For loops - we see these perform very badly indeed.

0.03

Coin toss example:

Repeat this n times: Toss a fair coin 100 times and return the observed amount of heads.

First, with nested For loops:

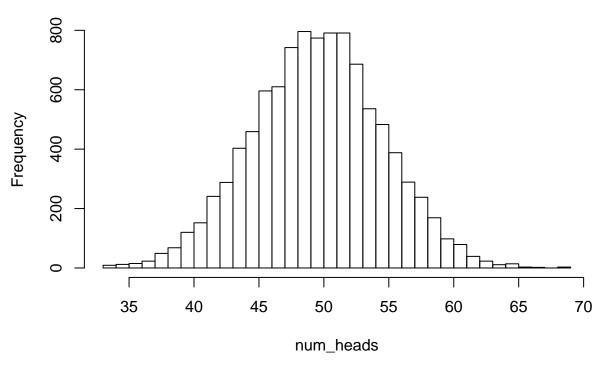
```
coin_toss1 <- function(n) {
  output <- rep(0, n) #initialise n vector
  for (i in 1:n) { #repeat n times
    num_heads <- 0
    for (j in 1:100) {</pre>
```

```
num_heads <- num_heads + sample(c(0,1), 1) #sum 100 coin tosses
}
output[i] <- num_heads #store number of heads
}
return(output)
}</pre>
```

Now vectorised:

```
coin_toss2 <- function(n) { #simulate and sum n coin tosses
  tosses <- matrix(sample(c(0,1), n*100, replace=TRUE), nrow=n, ncol=100) #form matrix with rows as exp
  return(rowSums(tosses)) #return row sums
}
num_heads <- coin_toss2(10000) #run with n = 10000
hist(num_heads, breaks=50) #plot histogram of experiment outcomes</pre>
```

Histogram of num_heads



And compare these methods in system time

```
n = 2000
system.time(coin_toss1(n))
##
      user
            system elapsed
##
     0.876
             0.017
                      0.893
system.time(coin_toss2(n))
##
      user
            system elapsed
     0.009
             0.000
                      0.009
```

This worsens with higher dimensions of iteration; more For loops leads to a greater divergence in system time. $(Scales\ quadratically?)$

apply() functions

We now look at an alternative method for iterating, the apply family. This includes apply(), lapply() for lists, sapply() for simplification (?), mapply() for multiple dimensions. These apply the same function on objects within an object.

apply() has the syntax apply(x, margin, fun, ...) where x is an array, margin is the vector of subscripts to apply to, and fun is the function to be applied.

Consider this matrix example.

```
x <- matrix("n", nrow=5, ncol=4) #5*4 matrix, entries "n"
apply(x, 1, cat) #apply cat (concatenate) function on rows
## n n n nn n n n n n n n n n n n n n
## NULL
apply(x, c(1,2), cat) #apply cat (concatenate) function on rows and columns
## nnnnnnnnnnnnnnnnnn
## NULL
lapply() has the syntax lapply(x, fun, ...) and outputs a list.
lapply(rep(1,5), exp) #output list of exp(1), ..., exp(5)
## [[1]]
## [1] 2.718282
##
## [[2]]
## [1] 2.718282
##
## [[3]]
## [1] 2.718282
## [[4]]
## [1] 2.718282
##
## [[5]]
## [1] 2.718282
x <- list(a=1:10, b=exp(-3:3), c=c(TRUE,FALSE,FALSE,TRUE)) #construct x list
lapply(x, mean) #apply mean function to lists within x
## $a
## [1] 5.5
##
## $b
## [1] 4.535125
##
## $c
## [1] 0.5
lapply(x, quantile, probs=(1:50)/50) #apply quantile function to lists
## $a
     2%
##
            4%
                        8%
                             10%
                                   12%
                                         14%
                                               16%
                                                     18%
                                                            20%
                                                                  22%
                                                                        24%
  1.18 1.36 1.54 1.72 1.90 2.08 2.26 2.44 2.62 2.80 2.98
                                                                       3.16
```

```
##
     26%
           28%
                  30%
                        32%
                              34%
                                    36%
                                           38%
                                                 40%
                                                       42%
                                                              44%
                                                                    46%
                                                                          48%
##
    3.34
          3.52
                3.70
                      3.88
                             4.06
                                   4.24
                                          4.42
                                                4.60
                                                      4.78
                                                            4.96
                                                                   5.14
                                                                         5.32
##
     50%
           52%
                 54%
                        56%
                              58%
                                    60%
                                           62%
                                                 64%
                                                       66%
                                                             68%
                                                                    70%
                                                                          72%
    5.50
          5.68
                5.86
                       6.04
                             6.22
                                   6.40
                                          6.58
                                                6.76
                                                      6.94
                                                            7.12
                                                                   7.30
                                                                         7.48
##
##
     74%
           76%
                 78%
                        80%
                              82%
                                    84%
                                           86%
                                                 88%
                                                       90%
                                                             92%
                                                                    94%
                                                                          96%
    7.66
          7.84
                8.02
                      8.20
                             8.38
                                   8.56
                                         8.74
                                                8.92
                                                      9.10
                                                            9.28
                                                                   9.46
                                                                         9.64
##
     98%
          100%
##
    9.82 10.00
##
##
##
   $b
##
            2%
                         4%
                                     6%
                                                  8%
                                                              10%
                                                                          12%
                0.07031864
                             0.08058443
                                         0.09085021
                                                      0.10111600
##
    0.06005285
                                                                   0.11138178
##
           14%
                        16%
                                    18%
                                                 20%
                                                              22%
                                                                          24%
    0.12164757
                0.13191335
                             0.15393882
                                          0.18184411
                                                                   0.23765471
##
                                                      0.20974941
##
           26%
                        28%
                                    30%
                                                 32%
                                                              34%
                                                                          36%
##
    0.26556001
                0.29346531
                             0.32137061
                                         0.34927591
                                                      0.39316426
                                                                   0.46901873
##
           38%
                        40%
                                                 44%
                                                                          48%
                                    42%
                                                              46%
##
    0.54487320
                0.62072766
                             0.69658213
                                         0.77243660
                                                      0.84829107
                                                                   0.92414553
##
                                    54%
                                                             58%
                                                                          60%
           50%
                        52%
                                                 56%
##
    1.0000000
                1.20619382
                             1.41238764
                                          1.61858146
                                                      1.82477528
                                                                   2.03096910
##
           62%
                        64%
                                    66%
                                                 68%
                                                              70%
                                                                          72%
##
    2.23716292
                2.44335674
                             2.64955056
                                          3.09194377
                                                      3.65243668
                                                                   4.21292960
                        76%
##
           74%
                                                 80%
                                                             82%
                                                                          84%
                                    78%
    4.77342251
                5.33391542
                             5.89440833
                                         6.45490124
                                                      7.01539416
                                                                  7.89691533
##
                                    90%
                                                 92%
                                                             94%
##
           86%
                        88%
                                                                          96%
##
    9.42049303 10.94407073 12.46764843 13.99122613 15.51480383 17.03838153
##
           98%
                       100%
   18.56195922 20.08553692
##
##
## $c
##
          4%
                    8%
                        10%
                              12%
                                  14%
                                        16%
                                             18%
                                                   20%
                                                        22%
                                                             24%
                                                                   26%
                                                                        28%
   0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00\ 0.00
         34%
              36%
                   38%
                         40%
                              42%
                                   44%
                                        46%
                                              48%
                                                   50%
                                                        52%
                                                             54%
                                                                   56%
                                                                        58%
                                                                             60%
   0.00\ 0.02\ 0.08\ 0.14\ 0.20\ 0.26\ 0.32\ 0.38\ 0.44\ 0.50\ 0.56\ 0.62\ 0.68\ 0.74\ 0.80
         64%
              66%
                   68%
                        70%
                              72%
                                   74%
                                        76%
                                             78%
                                                   80%
                                                        82%
                                                             84%
                                                                  86%
92%
        94%
              96%
                   98% 100%
## 1.00 1.00 1.00 1.00 1.00
```

sapply() does the same as lapply() but attempts to coerce the returned list into a simpler form; for instance, if a list of singleton lists would be returned by lappy() then sapply() will convert this to a single list of numbers.

sapply(x, quantile, probs=(1:50)/50) #return quantiles in single list

```
##
            а
                         b
## 2%
         1.18
               0.06005285 0.00
## 4%
         1.36
               0.07031864 0.00
## 6%
         1.54
               0.08058443 0.00
## 8%
         1.72
               0.09085021 0.00
## 10%
         1.90
               0.10111600 0.00
##
  12%
         2.08
               0.11138178 0.00
##
   14%
         2.26
               0.12164757 0.00
## 16%
         2.44
               0.13191335 0.00
## 18%
         2.62
               0.15393882 0.00
```

```
## 20%
         2.80
               0.18184411 0.00
## 22%
         2.98
               0.20974941 0.00
               0.23765471 0.00
  24%
         3.16
               0.26556001 0.00
##
  26%
         3.34
##
   28%
         3.52
               0.29346531 0.00
  30%
               0.32137061 0.00
##
         3.70
## 32%
               0.34927591 0.00
         3.88
               0.39316426 0.02
## 34%
         4.06
## 36%
         4.24
               0.46901873 0.08
## 38%
         4.42
               0.54487320 0.14
## 40%
         4.60
               0.62072766 0.20
## 42%
         4.78
               0.69658213 0.26
##
  44%
         4.96
               0.77243660 0.32
## 46%
               0.84829107 0.38
         5.14
## 48%
         5.32
               0.92414553 0.44
## 50%
         5.50
               1.00000000 0.50
## 52%
               1.20619382 0.56
         5.68
## 54%
         5.86
               1.41238764 0.62
               1.61858146 0.68
## 56%
         6.04
## 58%
         6.22
               1.82477528 0.74
##
  60%
         6.40
               2.03096910 0.80
## 62%
         6.58
               2.23716292 0.86
## 64%
               2.44335674 0.92
         6.76
## 66%
               2.64955056 0.98
         6.94
## 68%
         7.12
               3.09194377 1.00
  70%
         7.30
               3.65243668 1.00
  72%
         7.48
               4.21292960 1.00
##
##
  74%
         7.66
               4.77342251 1.00
## 76%
         7.84
               5.33391542 1.00
## 78%
         8.02
               5.89440833 1.00
## 80%
         8.20
               6.45490124 1.00
## 82%
         8.38
               7.01539416 1.00
## 84%
         8.56
               7.89691533 1.00
               9.42049303 1.00
## 86%
         8.74
##
   88%
         8.92 10.94407073 1.00
## 90%
         9.10 12.46764843 1.00
## 92%
         9.28 13.99122613 1.00
## 94%
         9.46 15.51480383 1.00
## 96%
         9.64 17.03838153 1.00
         9.82 18.56195922 1.00
## 98%
## 100% 10.00 20.08553692 1.00
mapply() extends sapply() to multiple dimensions. Has the syntax mapply(fun, ...) and the ... denotes
arguments to the function.
mapply(function(x, y) seq_len(x) + y, c(a=1, b=2, c=3), c(A=10, B=0, C=-10)) #return list according to
## $a
## [1] 11
##
## $b
##
   [1] 1 2
##
## $c
## [1] -9 -8 -7
```

How do these compare to For loops in terms of speed? We use x^x elementwise on (1, ..., 1e6) with sapply and For loops.

```
ftest1 <- function(x) x^x</pre>
x \leftarrow 1:1e6 \#runif(1e+06, min = -1, max = 1)
ftest1_apply <- function(x) sapply(x, ftest1) # with sapply</pre>
ftest1_loop <- function(x) { #as for loop</pre>
  y <- rep(NA, length(x))
  for (i in 1:length(x)) y[i] <- ftest1(x[i])</pre>
}
system.time(ftest1_apply(x)) #sapply time
##
      user system elapsed
##
     1.776
             0.020
                      1.796
system.time(ftest1_loop(x)) #loop time
##
      user
            system elapsed
##
     0.499
             0.004
                      0.503
system.time(ftest1(x)) #vectorised time
##
            system elapsed
      user
##
     0.063
             0.000
                      0.064
```

So the apply function takes about 3 times as long as the for loop function, which itself takes around 8 times as long as the vector function.

Map, reduce, filter

Map is a wrapper for mapply which doesn't simplify the result (often returning a list of lists). The function given as input is applied to each entry of the input object, and a list is returned. This can be used with lambda notation, a one line function.

```
x < -1:5
y <- Map({function(a) a*a}, x) #square entries of x, using Map
у
## [[1]]
## [1] 1
## [[2]]
## [1] 4
##
## [[3]]
## [1] 9
##
## [[4]]
## [1] 16
##
## [[5]]
## [1] 25
```

Reduce acts similarly to Map, applying a function succesively to pairs in the vector/list and returning a single number.

```
Reduce(function(a,b)a*b, x) #multiply all entries in x

## [1] 120

Filter processes a vector to keep only those entries which meet a specific condition, giving a possibly shorter vector as a result.

Filter(function(x) x>2, x) #return entries of x greater than 2

## [1] 3 4 5
```

[1] 2 3 4 5

Parallelisation

Why use parallel programming? Typically, R will use one core of the CPU. Larger jobs can be parallelised to make use of more than one core or more than one processor, allowing faster processing. Problems may also be *memory-bound*, requiring more RAM than is available; I/O bound, taking too long to read and write to the permanent memory; or network bound, taking too long to transfer over a connection.

Speed gains are not linear - n-fold increases in processes do not cause n-fold gains in time.

Using mclapply()

Often, computations will depend on previous results, preventing vectorisation.

Filter(function(x)x-1, x) #remove entries equal to 1

```
library(parallel)
num_cores <- detectCores() #how many cores does this machine have?
num_cores</pre>
```

[1] 8

We demonstrate parallelisation on the Wright-Fisher model. X_k is a Markov Process such that

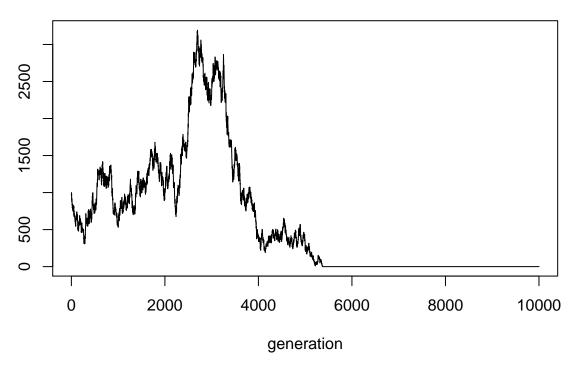
$$X_k \sim Binomial(N, \frac{X_{k-1}}{N})$$

Clearly, this is step-dependent, so can't be vectorised.

First, we simulate the model without parallelisation.

```
simulate_wright_fisher <- function(N, n_gen, init_freq) {
    # population size, number of generation to simulate, and initial frequency of mutant
    counts <- numeric(n_gen)
    counts[1] <- round(N * init_freq)
    for (k in 2:n_gen) {
        counts[k] <- rbinom(1, size=N, prob=counts[k-1]/N)
    }
    return(counts)
}
counts <- simulate_wright_fisher(5000, 10000, 0.2)
plot(counts, type='l', main='Frequency of mutant', xlab='generation', ylab='')</pre>
```

Frequency of mutant



We inspect how long this takes.

```
system.time(simulate_wright_fisher(5000, 10000, 0.2)) #how long did this take?
##
      user
           system elapsed
     0.024
            0.008
                     0.032
We can, however, parallelise multiple iterations of the same function.
library(MASS)
wrapper <- function(init_freq) simulate_wright_fisher(5000, 10, init_freq) #specify model call as funct
init_freqs <- rep(0.2, 3)</pre>
res <- mclapply(init_freqs, wrapper, mc.cores=4) #apply model call to initial frequency vector, using 4
res
## [[1]]
   [1] 1000 978 932
                        950
                             939 1005 1046 1027 1038 1053
##
## [[2]]
  [1] 1000 1000 1001 973
                             980
                                  960
                                       966
                                             967
                                                  957
                                                       984
##
## [[3]]
  [1] 1000 979 937 906 926 956 927 935 965 953
wrapper2 <- function(init_freq) tail(simulate_wright_fisher(5000, 1000, init_freq), 1) #return last ent
init_freqs2 <- rep(0.2, 500)</pre>
system.time(lapply(init_freqs2, wrapper2)) #how long?
##
      user system elapsed
     1.031
             0.000
                     1.031
##
system.time(mclapply(init_freqs2, wrapper2, mc.cores=2)) #how long with two cores?
```

```
## user system elapsed
## 0.546 0.064 0.586

system.time(mclapply(init_freqs2, wrapper2, mc.cores=4)) #how long with four?

## user system elapsed
## 0.573 0.023 0.383
```

We see the time taken decreases, but at a decreasing rate with respect to the number of cores used.

foreach() and doparallel()

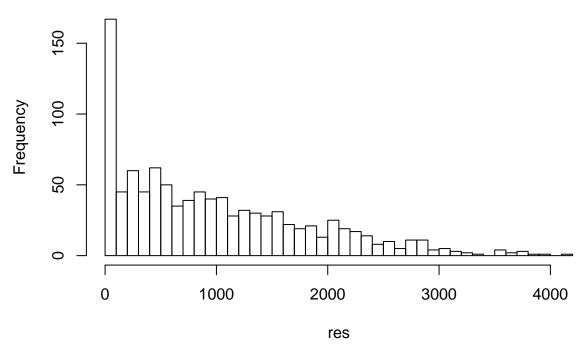
foreach() parallelises the For loop and returns a list. %do% evaluates sequentially, and %dopar% evaluates in parallel. This is preferable to mclapply() in terms of flexibility.

```
library(foreach)
foreach (i=1:3) %do% {
  i*i
}
## [[1]]
## [1] 1
## [[2]]
## [1] 4
##
## [[3]]
## [1] 9
res <- foreach (i=1:2, .combine=rbind) %do% { #run model twice sequentially, combining by row
  simulate_wright_fisher(5000, 10, 0.2)
}
res
            [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10]
## result.1 1000 1039 1063 1044 1023 1044 1039 1019 985
## result.2 1000 1027 1012 999 988 989 1010 1009 1043 1031
```

The .final argument determines what should be returned by foreach(). To select the terminal number of mutants in the population, we use the following:

```
n_gen <- 1000
res <- foreach (i=1:1000, .combine=rbind, .final=function(x) x[,n_gen]) %do% { #select final entry
    simulate_wright_fisher(5000, n_gen, 0.2)
}
hist(res, breaks=50)</pre>
```

Histogram of res



Let's introduce parallel computation.

t2-t1

```
library(doParallel)
## Loading required package: iterators
registerDoParallel(4) # register 4 cores
n runs <- 500 #500 runs
system.time(foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %do% { #how long does th
  simulate_wright_fisher(5000, n_gen, 0.2)
})
##
      user
            system elapsed
             0.004
     1.264
system.time(foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %dopar% {#how long does
  simulate_wright_fisher(5000, n_gen, 0.2)
})
##
            system elapsed
##
     2.289
             0.184
                     0.542
t1 <- Sys.time()</pre>
res1 <- foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %do% {
  simulate_wright_fisher(5000, n_gen, 0.2)
}
t2 <- Sys.time()
res2 <- foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %dopar% {
  simulate_wright_fisher(5000, n_gen, 0.2)
}
t3 <- Sys.time()
```

Time difference of 1.287343 secs

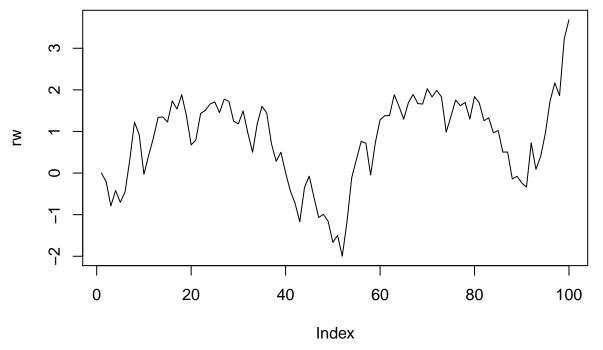
Consider now the damped random walk

$$X_t = \alpha X_{t-1} + Z_t;$$

where

$$Z_t \sim \mathcal{N}(0,1)$$
, $|\alpha| < 1$, and $X_t = 0$

```
simulate_rw <- function(X0, alpha, n){ #create random walk
   X <- rep(X0, n)
   for (i in 2:n) {
      X[i] <- X[i-1] + alpha*rnorm(1, 0,1)
   }
   X
}
rw <- simulate_rw(0,0.5,100)
plot(rw, type = "l")</pre>
```

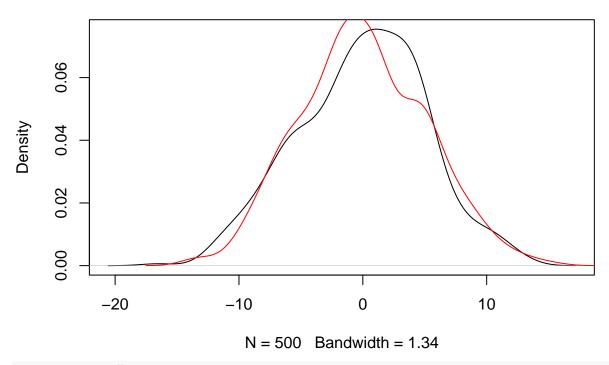


Let's compare parallelisation methods for this.

```
n_gen <- 100
n_runs <- 500
t1 <- Sys.time()
res1 <- foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %do% { #run random walk 500
    simulate_rw(0,0.5,n_gen)
}
plot(density(res1))

t2 <- Sys.time()
res2 <- foreach (i=1:n_runs, .combine=rbind, .final=function(x) x[,n_gen]) %dopar% { #run 500 times in
    simulate_rw(0,0.5,n_gen)
}
lines(density(res2), col="red") #plot parallel density in red</pre>
```

density.default(x = res1)



t3 <- Sys.time()
t2-t1</pre>

Time difference of 0.2769976 secs

Note here that the empirical means of both stay around zero, suggesting the series is stationary.

clean up the cluster
stopImplicitCluster()