nmf-comparison

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1 Fundamentals of Machine Learning - Exercise 9

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```
In [1]: import math
    import matplotlib.pyplot as plt
    import numpy as np
    import pandas as pd
    from sklearn.datasets import load_digits
    from sklearn import decomposition
```

1.1 1 Setup

```
In [2]: digits = load_digits()
    X = digits["data"] / 255
    Y = digits["target"]
```

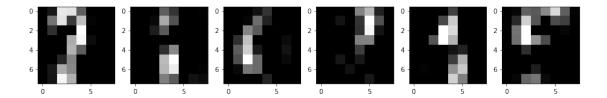
1.2 2 Non-negative matrix factorization vs. SVD comparison

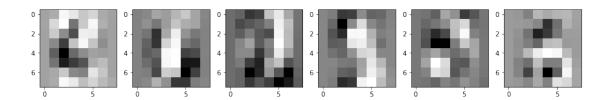
```
In [3]: nmf = decomposition.NMF(n_components=10)
    W1 = nmf.fit_transform(X)
    H1 = nmf.components_

means = np.mean(X, axis=0)
    X_centered = X - means

U, S, V = np.linalg.svd(X_centered, full_matrices=True)
    V = V + means

fig, axes = plt.subplots(2, 6, figsize=(15, 10))
    axes = axes.ravel()
    fig.suptitle('Top: components of NMF, Bottom: components of SVD')
    for i in range(6):
        axes[i].imshow(H1[i,:].reshape(8, 8), cmap=plt.cm.Greys_r)
    for i in range(6, 12):
        axes[i].imshow(V[i-6, :].reshape(8, 8), cmap=plt.cm.Greys_r)
    plt.show()
```





For the NMF components most of the values are 0 which makes senes, since for all numbers the biggest part of the image is just black background. One can also see prototypical parts of the numbers out of whom the different numbers can be formed. For the SVD the values of the components vary way more and rather form prototypical numbers and not prototypical parts of numbers.