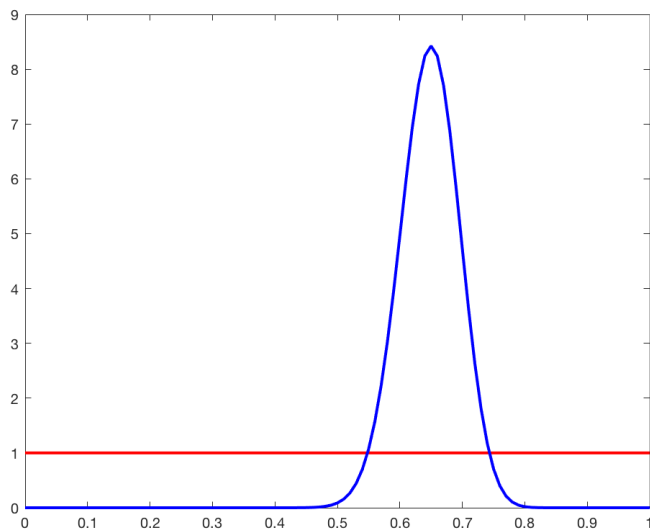


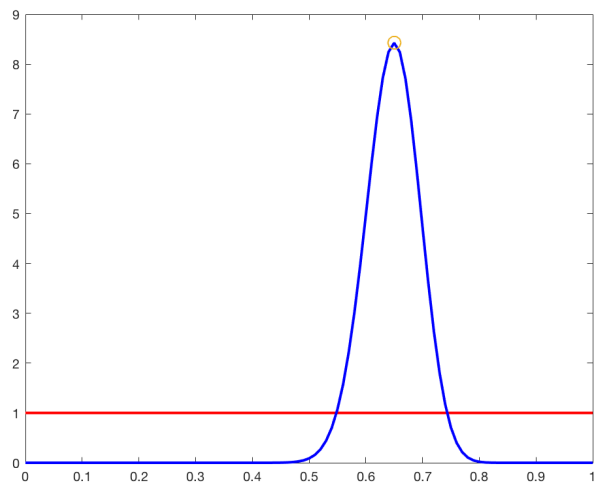
Problem Assignment 3

Problem 1:

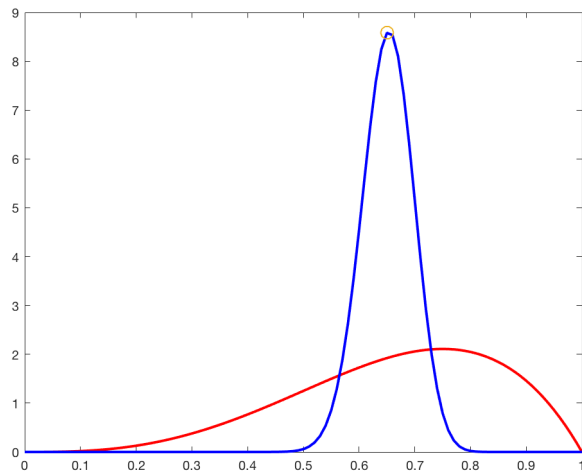
1. An ML estimate of θ is .65
2. Blue line = posterior, red line = prior



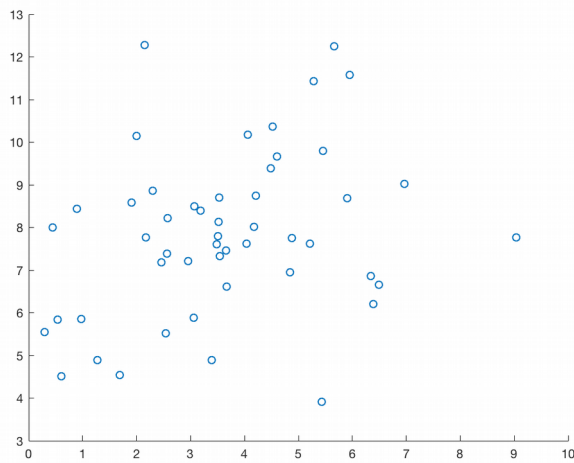
$$\begin{aligned} 3. \theta_{\text{map}} &= (a_1 + N_1 - 1) / (a_1 + a_2 + N_1 + N_2 - 2) \\ &= (1 + 65 - 1) / (1 + 1 + 65 + 35 - 2) \\ &= 65 / 100 \\ &= .65 \end{aligned}$$



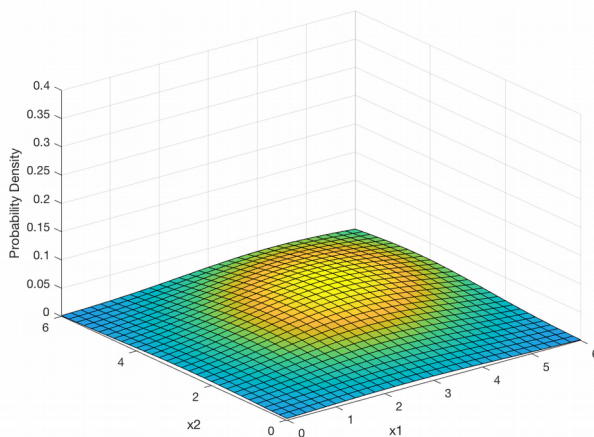
$$\begin{aligned} 4. \theta_{\text{map}} &= (a_1 + N_1 - 1) / (a_1 + a_2 + N_1 + N_2 - 2) \\ &= (4 + 65 - 1) / (4 + 2 + 65 + 35 - 2) \\ &= 68 / 104 \\ &= .653846 \end{aligned}$$



Problem 2:



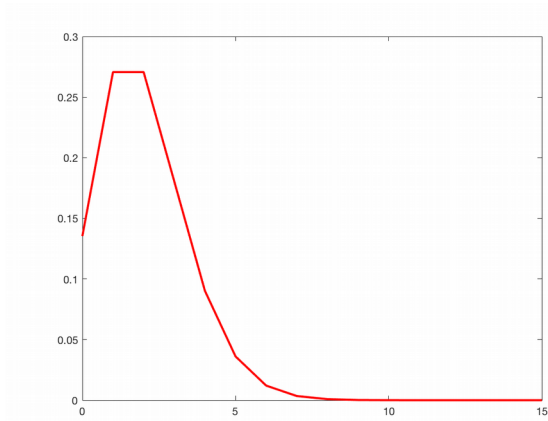
- 1.
2. ML estimate for the mean: 3.6377, 7.8506



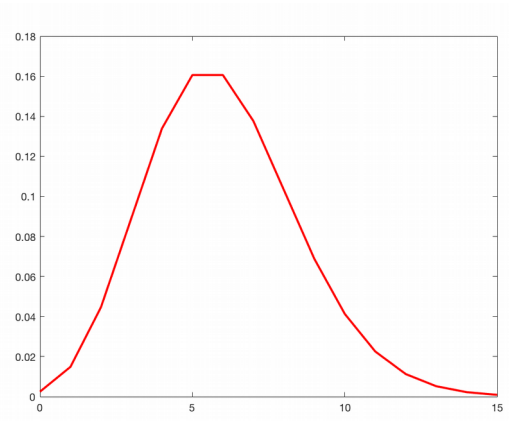
- 3.
4. I believe that the multivariate model is better because it will be easier for us to see dependencies between variables.

Problem 3:

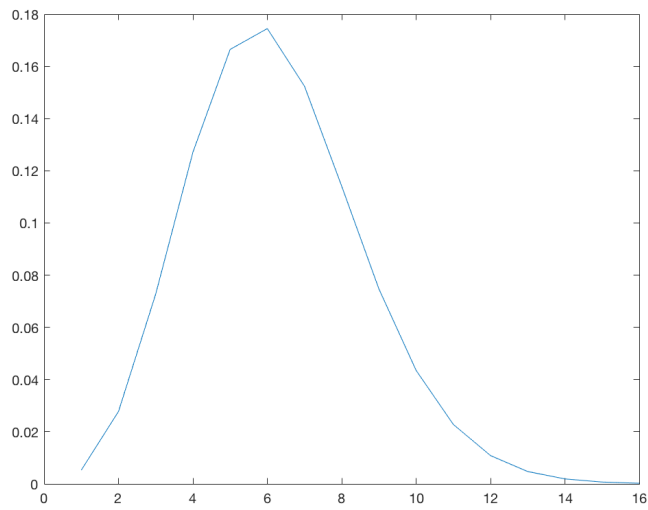
1. $\lambda = 2$



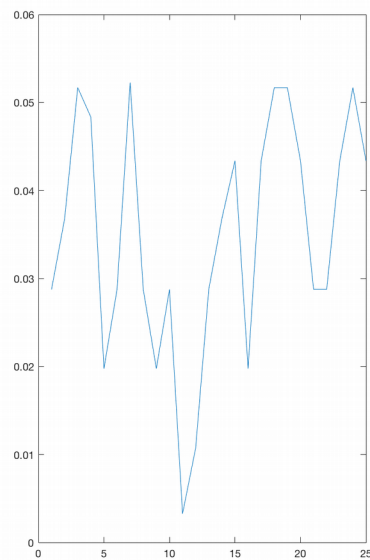
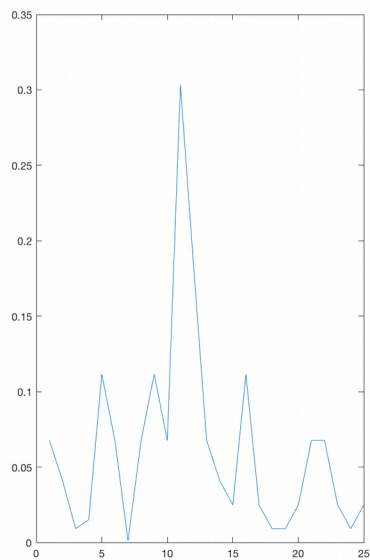
$\lambda = 6$



2. $ML = 5.2400$



3. left side is $a = 1, b = 2$, right side is $a = 3, b = 5$



```

4. Gamma( $\lambda$ |a + sum(data) , b/(nb + 1 ))
a = 1, b = 2
Gamma(  $\lambda$ | 1 + 131, 2/(25*2 + 1))
Gamma(  $\lambda$ |132, .03921)
a = 3, b = 5
Gamma(  $\lambda$ | 3 + 131, 5/(25*5 + 1))
Gamma(  $\lambda$ |132, .0397)
Left is a = 1, b = 2. Right is a = 3, b = 5

```

