

We are given a partially defined matrix  $M_0$ :

$$M_0 = \begin{bmatrix} 0 & 1 & ? & 3 \\ ? & 2 & 3 & ? \\ 1 & ? & 1 & 1 \\ 2 & 1 & 5 & ? \end{bmatrix}$$

$$D_T(X) = U D_T(\Sigma) V^T$$

$$D_T(\Sigma) = \text{diag}(\max(\sigma_1 - \tau, 0), \dots, \max(\sigma_{\min(n_1, n_2)} - \tau, 0))$$

$$P_{\Omega}(A) = \begin{cases} a_{ij}, & (i,j) \in \Omega \\ 0, & (i,j) \notin \Omega \end{cases}$$

$\delta$  - STEP SIZE

$$X^{(k)} = D_T(Y^{(k-1)})$$

$$Y^{(k)} = Y^{(k-1)} + \delta_k P_{\Omega}(M - X^{(k)})$$

$$k=0:$$

$$X^{(0)} = 0$$

$$Y^{(0)} = 0$$

$$k=1:$$

$$X^{(1)} = D_T(0) = 0$$

$$Y^{(1)} = 0 + \delta_k \cdot P_{\Omega}(M - 0) = \delta_k \cdot P_{\Omega} \left( \begin{bmatrix} 0 & 1 & ? & 3 \\ ? & 2 & 3 & ? \\ 1 & ? & 1 & 1 \\ 2 & 1 & 5 & ? \end{bmatrix} \right) = \delta_k \begin{bmatrix} 0 & 1 & 0 & 3 \\ 0 & 2 & 3 & 0 \\ 1 & 0 & 1 & 1 \\ 2 & 1 & 5 & 0 \end{bmatrix}$$