

Robust Energy-Aware Routing with Uncertain Traffic Demands

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Abstract—Energy conservation has become a major challenge to the Internet. In existing approaches, a part of line cards are switched into sleep mode for energy conservation, and the routing is configured carefully to balance energy saving and traffic engineering goals, such as the maximum link utilization ratio (MLUR). Typically, traffic demands are used as inputs, and routing is computed accordingly. However, accurate traffic matrices are difficult to obtain and are changing frequently. This makes the approaches difficult to implement. Further, the routing may shift frequently, and is not robust to sudden traffic changes.

In this paper, we propose a different approach that finds one energy-aware routing robust to a set of traffic matrices, particularly to arbitrary traffic demands. Such a routing without energy consideration is known as the demand-oblivious routing, and is well studied. However, the problem becomes much more challenging when energy conservation is involved. To overcome the challenges, we first define a new metric, namely oblivious performance ratio (OPR) with energy constraint, which reflects the MLUR distance from a routing to the optimal routing when certain energy conservation requirement is satisfied. We model the problem of minimizing the performance ratio, and analyze the lower and the upper bounds. Then, we propose Robust Energy-Aware Routing (REAR) to solve the problem in two phases. REAR select sleeping links based on extended robust link utilization (ERLU) or algebraic connectivity, and compute the routing based on a classical demand-oblivious routing algorithm. We evaluate our algorithms on real and synthetic topologies. The simulation results show that REAR can save 19% of line card power while the performance ratio is less than 34%.

I. INTRODUCTION

Energy conservation has become a global concern nowadays. The Internet is one of the major energy consumers, and its rapid growth makes the green Internet a hot research topic. In the Internet backbone, energy is mainly drawn by routers and switches. Such devices consume almost full power even if the traffic load is small. Thus, an effective method to save energy in the Internet is to aggregate traffic into part of the routers when the traffic load is small, and switch the under-utilized components (routers or line cards) into off/sleep mode. Such a method is known as the energy efficient routing.

An important issue for energy efficient routing is to avoid network congestion after the traffic is aggregated. Many approaches have been proposed in existing works. Most approaches compute the routing based on real-time traffic matrices or link loads, to achieve a good load balancing and avoid congestion. However, such approaches come at a cost of obtaining real-time traffic data. Furthermore, the routing may shift frequently with the traffic changes, and a sudden traffic

change may still induce congestions. To this end, we need to study the robustness of energy efficient routing.

Specifically, we study the energy efficient routing when traffic matrices cannot be obtained or predicted precisely, i.e., with uncertain traffic demands. To achieve robustness, we need to find a routing, which can perform near optimally under a range of traffic matrices. The key technique that makes this possible is the advanced *demand-oblivious routing*. A seminal work [2] find that, the distance between the maximum link utilization ratio (MLUR) of a demand-oblivious routing and the MLUR of the optimal routing is bounded. Thus, no matter how the traffic demand changes, the demand-oblivious routing can guarantee certain performance. We note that this conclusion is in a network without off/sleep components, and we need to consider the situation when energy conservation is required.

However, existing demand-oblivious routing algorithms cannot be directly applied to energy efficient routing. There are several challenges. First, we need to define a metric that can effectively measure the distance between a robust energy efficient routing and the optimal routing, because the existing metric for demand-oblivious routing fails in the situation when some components are switched into off/sleep mode. Second, we need to analyze whether the metric can be bounded, just like for demand-oblivious routing. If there exists no bound, then it is not feasible to find a robust energy efficient routing. Third, we need practical algorithms to compute the robust energy efficient routing. Specifically, we need to determine: 1) which routers or line cards should be switched into off/sleep mode, to achieve energy efficiency; and 2) in which path to forward the traffic for robustness, while the path does not traverse the off/sleep components.

In this paper, we overcome the aforementioned challenges. First, we define a new metric, namely the oblivious performance ratio with energy constraint (OPRE). The OPRE reflects the MLUR distance from a routing to the optimal one when certain energy conservation requirement is satisfied. We model the problem of minimizing the OPRE. Second, we prove that there exists a robust energy efficient routing with the minimum OPRE, which has an upper bound given a network. Then, we propose Robust Energy-Aware Routing (REAR) scheme, which uses heuristic algorithms to solve the problem. We develop algorithm XXX, which chooses off/sleep line cards in a way that the OPRE can be minimized potentially. We

then develop algorithm XXX to compute the routing in the remaining topology, by extending existing optimal demand-oblivious routing algorithm. We evaluate our algorithms by simulations on real topologies and synthetic traffic demands with random fluctuations. The results show that REAR can achieve an OPRE of 1.34 while 19% of line card power is saved.

The rest of the paper is organized as follows. Section II shows the related work. Section III presents metric OPRE and formally models the problem. We presents the bounds on OPRE in Section IV, and propose our algorithms in Section V. Section VI shows our simulation setup and results, and Section VII concludes our work.

II. RELATED WORK

related work

III. PROBLEM STATEMENT

A. Background of Demand-Oblivious Routing

As mentioned above, demand-oblivious routing aims at finding one routing that performs near optimally under a range of traffic demands. In traffic engineering, a typical metric to evaluate routing performance is the maximum link utilization ratio (MLUR). Clearly, the MLUR is corresponded with a specified traffic matrix (TM). Demand-oblivious routing defines oblivious performance ratio (OPR) to evaluate the routing performance without the knowledge of TM. We briefly present the background.

Given a TM, the distance between a routing to the optimal one is defined as the ratio between their MLURs. Formally, a network is modeled as undirected graph $G(V, E)$, where V is the set of vertices (nodes), and E is the set of edges (links). Let cap_{ij} denote the capacity of the link $(i, j) \in E$. Let d_{ab} denote the traffic demand from origin node a and destination node b , and m denote the TM that contains d_{ab} for all $a, b \in V$. Let $f_{ab}(i, j)$ be the fraction of d_{ab} that is routed on link (i, j) ($0 \leq f_{ab}(i, j) \leq 1$). Routing r is specified by $f_{ab}(i, j)$ for all $a, b \in V$ and $(i, j) \in E$, and we will formally define routing consistency later in Section III.C. Let $U_{r,m,G}$ be the MLUR of routing r under TM m . We have

$$U_{r,m,G} = \max_{(i,j) \in E} \frac{\sum_{a,b} d_{ab} f_{ab}(i, j)}{cap_{ij}}. \quad (1)$$

Let $P(\{r\}, \{m\}, G)$ be the *performance ratio* of routing r under TM m , which reflects how far from the routing to the optimal one, and is defined as

$$P(\{r\}, \{m\}, G) = \frac{U_{r,m,G}}{\min_{r'} U_{r',m,G}}. \quad (2)$$

The *oblivious performance ratio* (OPR) for routing r is defined by extending TM m to a set of TMs M , where M can be the set of any TMs. We have

$$P(\{r\}, M, G) = \max_{m \in M} P(\{r\}, \{m\}, G). \quad (3)$$

The target of demand-oblivious routing is to find routing r that minimizes OPR $P(\{r\}, M, G)$. Such a “robust” routing is

independent of a specific TM, but can perform near optimally. A seminal work [2] uses linear programming to find the routing that minimizes the OPR, and finds that the optimal solution exists, which means that the OPR is bounded.

B. Oblivious Performance Ratio with Energy Constraint

With energy constraint, a network may have to switch part of line cards into off/sleep mode to save the total energy consumption. This changes the network topology and makes metric OPR fail to evaluate the robustness of a routing. We use an example to show this. Assume that G is a cycle with n unit capacity links. Then, the minimal OPR of G is $2 - 2/n$ [2]. Now we pruning one link from G to save energy, and the topology changes to G^* . Because there is only one routing feasible in G^* , OPR $P(\{r\}, M, G^*)$ equals 1. Since 1 is less than $2 - 2/n$ for $n > 2$, it means that the routing after pruning one link is more robust than before. However, it is false because there are less links and the network is more likely to be congested.

The intrinsic reason for such a “fake robust” is that the topology is not changing when performance ratio is computed in Eq. (2). To address this issue, we extend the definition of OPR. Formally, let G^* be a sub-graph of G that satisfies the energy constraint (We will formally give the model in Section III.C). The extended performance ratio is defined as

$$P(\{r\}, \{m\}, G, G^*) = \frac{U_{r,m,G^*}}{\min_{r'} U_{r',m,G}}. \quad (4)$$

Let $P^*(\{r\}, M, G)$ be the *oblivious performance ratio with energy constraint* (OPRE) for routing r . We define $P^*(\{r\}, M, G)$ by extending m to M , and finding G^* that satisfies the energy constraint and has the minimum performance ratio. We have

$$P^*(\{r\}, M, G) = \min_{G^*} \max_{m \in M} P(\{r\}, \{m\}, G, G^*) \quad (5)$$

Note that when there is no energy constraint, G is the sub-graph that has the minimum performance ratio, and Eq. (5) naturally reduces to Eq. (3).

C. Problem Formulation

We formulate our problem as following:

$$\text{Minimize } \max_{m \in M} \frac{U_{r,m,G^*}}{\min_{r'} U_{r',m,G}} \quad (6)$$

$$G^* = (V, E^*), E^* \subset E \quad (7)$$

$$\begin{aligned} & \forall (\epsilon, \gamma) \in \{(E, r'), (E^*, r)\} \\ & \sum_{(i,j) \in \epsilon} f_{ab}(i, j) O_{(i,j)}^i - \sum_{(i,j) \in \epsilon} f_{ab}(i, j) I_{(i,j)}^i = \\ & \begin{cases} 1, i = b \\ -1, i = a \\ 0, i \neq a, b \end{cases}, \quad a, b, i \in V, a \neq b, f_{ab}(i, j) \in \gamma \end{aligned} \quad (8)$$

$$\sum_{l \in E^*} p(l) / \sum_{l \in E} p(l) < 1 - \theta \quad (9)$$

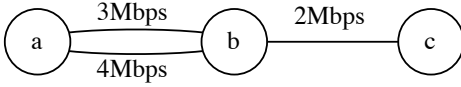


Fig. 1. Model Example, TM I : (a, b, 2M), (a, c, 1M); TM II : (a, b, 1M), (a, c, 1M).

Eq. (6) is our target, which minimize the value of OPRE defined in III.B. Eq. (7) say G^* be a sub-graph of G , which means remove/sleep some links from G , and keep vertices the same. Eq. (8) ensures the graph is connected and define the routing. In details, $O_{(i,j)}^i$ equal to 1 if i is the tail node of link (i, j) , and $I_{(i,j)}^i$ equal to 1 if i is the head node of link (i, j) , this equation states the flow conservation constraints. In the other hand, $f_{ab}(i, j)$ is specified by routing γ , if the graph is not connected it will be unavailable for some origin and destination pair. And from Eq. (8) we know that routing r is corresponded with G^* , and r' with G . We calculate the power constraints in Eq. (9), it ensure that we can save more than θ energy consumption. The function p which maps link to power consumption is proposed in [1].

D. Model Example

We will take an example to explain how to choose the link to close in our algorithm. Three hostes include : a, b, c, three links are with repectively capacity of 3M, 4M and 2M. For simpleness, we suppose there are two TM : (a, b, 2M), (a, c, 1M) and (a, b, 1M), (a, c, 1M). For each traffic matrix, the optimal route is obvious, we will trace 2M from a to b across the lower link and trace the 1M from a to c across the upper one for the first traffic matrix, whose maximum link utilization is 0.5. we will trace all the traffic across the lower link for the second traffic matrix, whose maximum link utilization is 0.5 as well.

Now for some reason, we will choose one link to shut down for power saving without lose connection of the network. There are two choice, remove either the upper link or the lower link. Let us take a little calculation: when remove the upper one, we should change all the traffic across the lower link, as a result, in the first TM the maximum link utilization is 0.75 and the second is 0.5; when close the lower link, we should trace all the traffic across the upper link, in the first TM the link utilization is 1 and the other is 0.667. So according to our theory, the $P^*(M, G)$ should be 1.5 and the optimal successor network topology will be the one which 3M link is closed.

IV. ALGORITHM

In our paper, Robust Energy-Aware Routing (REAR) algorithm works in two phases. Firstly, REAR select links should be put to sleep from the origin topology based on extended

robust link utilization or algebraic connectivity, then compute the robust routing by demand-oblivious routing algorithm. There are two metrics for selecting removed links, our two-phase algorithm is flexible because we can replace the metric with whatever metric.

A. Algebraic Connectivity

Network topology is represented by $G = (V, E)$ as mentioned in Model section, where V is the set of vertices and E is the set of links. We say $A(G)$ is the Adjacency Matrix of graph G , that include information for which vertices of the graph are adjacent to which other vertices. $A(G)$ is a $N \times N$ matrix, where $N = |V|$ and non-diagonal entry a_{ij} equal to the number of edges from vertex i to vertex j , in this paper, a_{ij} always be 1 if $(i, j) \in E$ otherwise 0. And we stipulate the diagonal element a_{ii} be 0.

We say $D(G)$ is the Degree Matrix of graph G , which is a diagonal matrix and diagonal entry d_{ii} denote the degree of node i . It is obvious that there is $d_{ii} = \sum_j a_{ij}$.

Then we define Laplacian Matrix $L(G)$ of graph G as the difference between Degree Matrix and Adjacency Matrix :

$$L(G) = D(G) - A(G) \quad (10)$$

where $D(G)$ is the Degree Matrix and $A(G)$ is the Adjacency Matrix.

In the mathematical field of graph theory, the number of eigenvalues equal to 0 is the number of connected components of G , so the smallest eigenvalue always be 0 in arbitrary graph . And we call the second smallest one as algebraic connectivity, which is greater than 0 if and only if graph G is connected. Further more, it measures the connectivity and stability of graph, the greater of the value, the more connective of graph; and it is a metric of average distance between any two vertices of graph G . We call the algebraic connectivity as $\lambda_2(G)$.

Topology always have different algebraic connectivity values, it is clear that when one link is added or removed from the graph, the algebraic connectivity value changes accordingly. And we say the changed value is the impact of this link on the graph. Supposed we sleep link l from graph G , new graph is described as G^* , we defined the impact of link l as :

$$\Delta_l = \lambda_2(G) - \lambda_2(G^*) \quad (11)$$

where $\lambda_2(G)$ and $\lambda_2(G^*)$ is algebraic connectivity of G and G^* respectively.

Clearly, Δ_l is always greater than 0, because graph will always lose connectivity when link is removed. Further more, some link will play a more important role in the connectivity of graph, such as the backbone link of network topology. And we say a link l affect more if Δ_l is greater.

B. Extended Robust Link Utilization

The demand-oblivious routing is not always the best one for specific TM , but good enough for a range of TM . we mentioned the definition of link utilization above when demand and routing are determined, as demand become oblivious, the

definition is also not suitable. So we define a notation named extended robust link utilization (ERLU) replace the normal link utilization like :

$$u_{ij}^e = \frac{\sum_{a,b} f_{ab}(i,j)}{cap_{ij}} \quad (12)$$

Proposing this definition for two consideration: firstly, the more flows across the link, the greater the u_{ij}^e is; secondly, the more fraction of one flow across the link, the greater the u_{ij}^e is. The link with greater ERLU is also more important than others in a sense. Although there is no demand here, we mean there is more probability that this link have greater link utilization when specific demand come. Similarly, we define the impact of link l as :

$$\Delta_l = u_l^e \quad (13)$$

And there is the same conclusion that a link l affect more if Δ_l is greater.

C. Algorithm Phase One

REAR sleep as many links as possible without losing much connectivity or transportation of graph for different metrics. Originly, we should calculate impact of all the links and sleep the lowest one from the graph, then repeat calculate and remove process until arrive some specific threshold. Obviously, it is NP-Hard, following is a heuristic algorithm.

For the origin graph, we calculate the impact of every link as Δ_{l_i} , and then sort these values from small to big, output ordered list denoted as Γ :

$$\Gamma = \{..., l_i, ..., l_j, ...\} \quad (14)$$

where $\Delta_{l_i} < \Delta_{l_j}$.

Pay attention we only compute the link impact once at the begining of algorithmt, and the ordered list Γ show the order of 'importance' among links in the graph.

Now we begin selecting which links should be sleep. We denote the set of the sleeping links as S , and the output of this phase is final graph $G^* = (V, E - S)$. We set $S = \emptyset$, and repeat our selecting process, each iteration we select one link, remove it from Γ and put it into S . In iteration i , algorithm scan links as the order in Γ , we try to remove this link from the graph to check if the graph is still connected and the energy conservation have not arrive the threshold. If so, we select this one then go next iteration. Otherwise choose the next link from Γ for trying to remove. Algorithm stop until all the links in Γ is tried but no one is satisfied with both connectivity and power threshold.

So before going ahead our algorithm, there is another thing we should done, how to measure the power of graph. We simple take an power model from [1] showed in Table II, and defined the difference of power consumption between two graphs as:

$$diff_p = \frac{\rho(G_{S,l}^o)}{\rho(G^o)} * 100 \quad (15)$$

where $\rho(G_{S,l}^o)$ is the power consumption of the final graph, when the links set S and link l are both removed from the

origin graph G^o , and the $\rho(G^o)$ is the power consumption of the origin graph.

If we set $diff_p$ valued 90%, it means that whenever we try to remove the link l from the origin graph in iteration, the power consumption should never lower than the 90% of origin one. In another words, the output of this phase protect as much connectivity and transportation as possible. Following is our implementation:

Algorithm REAR : Phase One

Input: $G(V, E)$, *threshold*;
Output: S in which links should be switched off;
 $G(V, E - S)$ which is the final network topology;

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1: for each link  $l$  in  $E$ 
2:    $G^* \leftarrow G(V, E - \{l\})$ ;
3:    $\Gamma[l] \leftarrow \Delta_l \leftarrow \lambda_2(G) - \lambda_2(G^*)$ ;
4: Resort  $\Gamma$  in increasing order based on  $\Delta_l$ ;
5:  $S \leftarrow \emptyset$ , goon  $\leftarrow$  true;
6: while goon
7:   goon  $\leftarrow$  false;
8:   for each link  $l$  in  $\Gamma - S$ 
9:     if  $G_{S,l}$  is connected and  $\rho(G_{S,l})/\rho(G) > threshold$ 
10:       $S \leftarrow S \cup \{l\}$ ;
11:      goon  $\leftarrow$  true;
12:     break;
13: return  $S, G(V, E - S)$ ;
```

D. Algorihtm Phase Two

Once we get the output network topology from the first phase based on either metric, it is time to compute the robust routing. On one hand, computation process may cost too much time if we directly calculate the robust routing in the final graph; on the other hand, the robust routing based on the final graph may not be the best one. There is a heuristic algorithm based on the demand-oblivious routing on the origin graph, which should be obtained at first. then adjust routing in details according to the links we switched off.

The demand-oblivious routing can be computed by a single LP with $O(mn^2)$ variables and $O(nm^2)$ constraints[1] :

$$\begin{aligned}
& \min r \\
& f_{ij}(e) \text{ is a routing} \\
& \forall \text{ links } l: \sum_m cap(m)t(l, m) \leq r \\
& \forall \text{ links } l, \forall \text{ pairs } i \rightarrow j: \\
& \quad f_{ij}(l)/cap(l) \leq p_l(i, j) \\
& \forall \text{ links } l, \forall \text{ nodes } i, \forall \text{ edges } e = j \rightarrow k: \\
& \quad \pi(l, link - of(e)) + p_l(i, j) - p_l(i, k) \geq 0 \\
& \forall \text{ links } l, m: \pi(l, m) \geq 0 \\
& \forall \text{ links } l, \forall \text{ nodes } i: p_l(i, i) = 0 \\
& \forall \text{ links } l, \forall \text{ nodes } i, j: p_l(i, j) \geq 0
\end{aligned}$$

where the $cap(l)$ is the capacity of link l ; and $\pi(l, m)$ is the weights for every pair of links l, m ; and the variables $p_l(i, j)$ for each link l and OD pair i, j is the length of the shortest path from i to j according to the link weights $\pi(l, m)$.

The routing we get indicate how to arrive at destination node from source node for every OD pair in the origin topology. What is different is that, the flow can be splited in the routing, i.e. there may be two paths ($path_1, path_2$) both from source node s to destination node d , and the optimal obilious routing trace 70% traffic on $path_1$ and left on $path_2$. Although splitting flow is hard handled, we take a transformation for

the case like that: when an flow is coming, there is 70% probability we trace it on $path_1$, otherwise $path_2$. This is easily implemented in real world.

Because all the routing is based on the origin topology, when some links are switched off, we must adjust the routing as well. Supposed there are some paths between two vertices s and d , maybe one link in some paths be removed, and these paths become not reachable any more, we should adjust the traffic in these paths to other paths. Of course, we can not put the whole traffic on another path, this will make some links of the path congested, so we should split the traffic to some paths ‘averagely’, in the sense of extended robust link utilization. Similarly to link utilization, we define the extended robust link utilization as the maximum extended robust link utilization of links.

Take pair (s, d) for example, routing includes paths from s to d , such as p_1, p_2, \dots, p_n . While only p_1 trace the removed link, and of course it will be unreachable. We split the traffic of p_1 , and put them on other paths to make the extend robust link utilization of paths almost closely.

And this is our implementation:

Algorithm REAR : Phase Two

Input: $G(V, E)$ which is the origin topology;
 S which is the switch-off links set generated by Phase One;
 R which is the Robust Routing on origin topology;
Output: *Routing* Robust Energy-Aware Routing on new topology
1: $G^* \leftarrow G(V, E - S)$;
2: **for** each link l in S
3: **for** each $s, d, paths$ in R
4: $traffic \leftarrow 0$;
5: **for** each $path$ in $paths$
6: **if** link in $path$
7: $traffic \leftarrow traffic + path.traffic$;
8: $paths.remove(path)$;
9: $yen_paths \leftarrow yens_algorithm(G^*, s, d)$;
10: **while** $traffic \neq 0$
11: $sort_paths_by_extend_robust_link_utilization(yen_paths)$
12: $yen_paths[0].traffic = traffic / N$
13: $traffic = traffic - traffic / N$
14: $paths.add(yen_paths[0])$
15: $paths.merge()$;
16: **return** R ;

V. SAMPLES AND PROOF

For showing obilious performance ratio with energy constraint really make a difference in the switching off link process, we will explain it in two simple topologies, cliques and cycles. On the other hand, we also say that there will be an upper bound for obilious performance ratio with energy constraint, and get the bound according to the topology. For simpleness, we refer the energy constraint to the quantity of removed links.

A. Circles

Cycles topology connect all the nodes by a cycle, any node in which has two links joined. Figure 1 show the six nodes cycles topology, let nodes named from A to F and links named from a to f in the figure. Now suppose a traffic in the topology then calculate the optimal routing for it, let D_a and C_a be the demand and capacity of the link, without loss of generality,

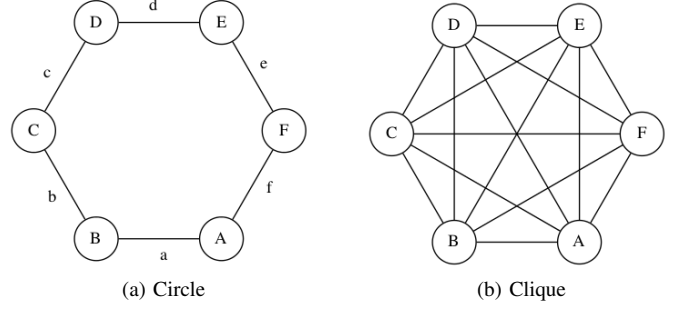


Fig. 2. Circle and Clique topology of 6 nodes

we say the link d is the bottleneck, i.e. with the maximum link utilization. There are two solutions for us, switching off the link d , or the other link, such as link f .

For case one, when we switch off the link d , the origin traffic pass the link will be redirected. The worst situation is that all the traffic on the link d will be put to the other path : $D \leftarrow C \leftarrow B \leftarrow A \leftarrow F \leftarrow E$. After traffic redirection, the bottleneck link may become the link e , according to our definition of extended robust link utilization:

$$\frac{\frac{D_e + D_d}{C_e}}{\frac{D_d}{C_d}} = (1 + \frac{D_e}{D_d}) \frac{C_d}{C_e} \quad (16)$$

Because the link utilization of link d is the maximum one, we have :

$$\frac{D_d}{C_d} > \frac{D_e}{C_e} \quad (17)$$

$$\frac{D_e * C_d}{C_e * D_d} < 1 \quad (18)$$

so we have the extended robust link utilization in case one :

$$(1 + \frac{D_e}{D_d}) \frac{C_d}{C_e} < \frac{C_d}{C_e} + 1 \quad (19)$$

For case two, similar to case one, all the traffic will be redirected on the other path between F and A . There are two sub cases after traffic redirection, the link D is still the bottleneck or the link E become the new bottleneck. In sub case one:

$$\frac{\frac{D_d + D_f}{C_d}}{\frac{D_d}{C_d}} = 1 + \frac{D_f}{D_d} \quad (20)$$

Because the link utilization of link d is the maximum one in origin topology, we have as:

$$\frac{D_d}{C_d} > \frac{D_f}{C_f} \quad (21)$$

$$\frac{D_f}{D_d} < \frac{C_d}{C_f} \quad (22)$$

So we get the extended robust link utilization in this case :

$$(1 + \frac{D_f}{D_d}) < \frac{C_d}{C_f} + 1 \quad (23)$$

In sub case two, we get the new extended robust link utilization in link E :

$$\frac{\frac{D_e+D_d}{C_e}}{\frac{D_d}{C_d}} = \frac{D_e * C_d}{D_d * C_e} * \frac{C_d * D_f}{C_e * D_e} \quad (24)$$

Similarly as mentioned above, we get equations :

$$\frac{D_d}{C_d} > \frac{D_e}{C_e} \Rightarrow \frac{D_e * C_d}{C_e * D_d} < 1 \quad (25)$$

$$\frac{D_d}{C_d} > \frac{D_f}{C_f} \Rightarrow \frac{D_f * C_d}{D_d} < C_f \quad (26)$$

So we get the extended robust link utilization:

$$\frac{D_e * C_d}{D_d * C_e} + \frac{C_d * D_f}{C_e * D_d} < 1 + \frac{C_f}{C_e} \quad (27)$$

As a result, the upper bound of extended robust link utilization must be :

$$Max\{1 + \frac{C_d}{C_e}, 1 + \frac{C_d}{C_f}, 1 + \frac{C_f}{C_e}\} \quad (28)$$

Particularly, if all the links have the same capacity, the upper bound equal to 2 when switch off one link. Otherwise, the upper bound only dependent to the greatest ratio of link capacity.

B. Cliques

In clique topology, all the nodes connect to each other, it means that situation become more difficult because the traffic can be adjusted to multi paths rather than one path in circle. And we will see that splitting traffic on multi paths is always better than put all the traffic to one, so if we get the upper bound of the worst case, it must be the upper bound of other case. Similarly to circle topology, we say the link a is the bottleneck, and we will switch off it or other link like b .

In case one, after we switch off link a , the new bottleneck link must be the affected link, the link contains the origin traffic on link a . Otherwise if the link b is the bottleneck, but we adjust the traffic on other links, it means that we can do the same thing in the origin topology, and the bottleneck become link b rather than a . It is conflict with our assumption. So we have the extended robust link utilization as :

$$\frac{\frac{D_b+D_a}{C_b}}{\frac{D_a}{C_a}} = (1 + \frac{D_b}{D_a}) \frac{C_a}{C_b} \quad (29)$$

Because the link a is the bottleneck link with the maximum link utilization, like what we do above, we can get

$$(1 + \frac{D_b}{D_a}) \frac{C_a}{C_b} < 1 + \frac{C_a}{C_b} \quad (30)$$

In case two, the bottleneck may still be link a or the new link c . If it is link a , and no new traffic across it, the extended robust

TABLE I
TOPOLOGIES

Topology	Nodes	Links	Links can be Removed
Abilene	12	15	4
Geant	23	37	15
Cernet2	20	22	3

link utilization equal to 1 obiliously. Or we adjust the new traffic D_b on it, we can get the extended robust link utilization:

$$\frac{\frac{D_a+D_b}{C_a}}{\frac{D_a}{C_a}} = 1 + \frac{D_b}{D_a} < 1 + \frac{C_b}{C_a} \quad (31)$$

If the bottleneck become new link c , similar to our proof of circle topology, we can get extended robust link utilization:

$$\frac{\frac{D_c+D_b}{C_c}}{\frac{D_a}{C_a}} = \frac{D_c * C_a}{D_a * C_c} + \frac{D_b * C_a}{D_a * C_c} < 1 + \frac{C_b}{C_c} \quad (32)$$

So we obtain the same conclusion as circle topology, the extended robust link utilization must be :

$$Max\{1 + \frac{C_a}{C_b}, 1 + \frac{C_b}{C_a}, 1 + \frac{C_b}{C_c}\} \quad (33)$$

C. Other Topology

We can also see that, when we switch off different link, it really matters the performance which dependent on not only the demand or traffic, but also the capacity of links. Particularly, the upper bound is just related with the capacity of links. And from our proof process, there is no special limitation for specific topology, so we can get the similar conclusion on other topology.

VI. EXPERIMENTS AND RESULTS

We simulated our algorithm on real world topology, including Abilene, Geant and Cernet2, whose number of nodes and links are listed in Table I. Then we generate random traffic matrix with Gravity Model [3], which assume that the traffic demand between nodes is proportional to their combined capacity of connecting links. To extrapolate a complete TM, we take an attribute margin w to scale the traffic range from $1/w$ to w base on the basic traffic demand. Particularly, when the w limit extremity, we say the traffic matrix is really arbitrary, and our algorithm is irrelevant with traffic.

A. OPRE versus Power Saving

In Figure 3, we see that the value of OPRE is at least 1 for all topologies even no links removed, particularly in Geant the value is 1.24, it means the robust routing always not be the optimal for all TMs. It is reasonable because our robust routing is used for a range of traffic rather than a specific TM.

When we switch off links, the topology lose connectivity and some routing paths will be failed, traffic on those paths will be adjusted to others, which result in the value of OPRE increased. We take margin from 1.5 to 3.5 and observe this phenomena from Figure. Pay attention that we scale the y-axis as logarithm for comparing TMP and ERLU in one figure.

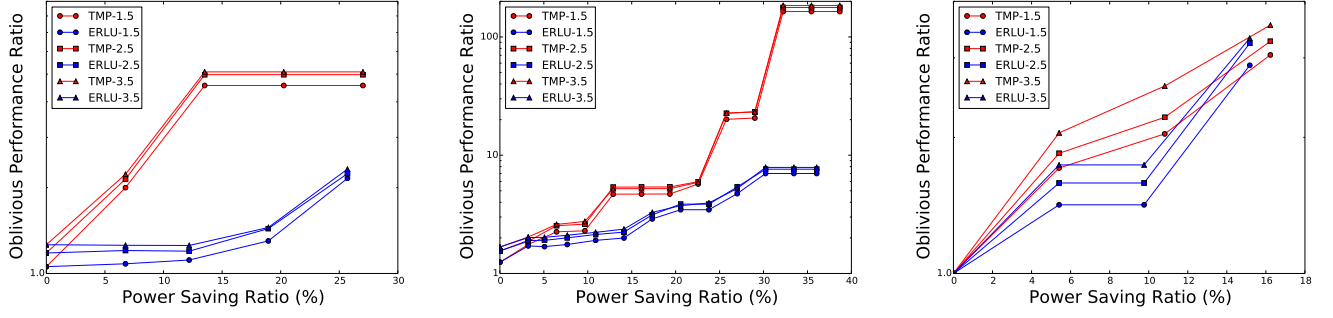


Fig. 3. OPRE versus Power Saving: (1). Abilene, (b). Geant, (c). Cernet2

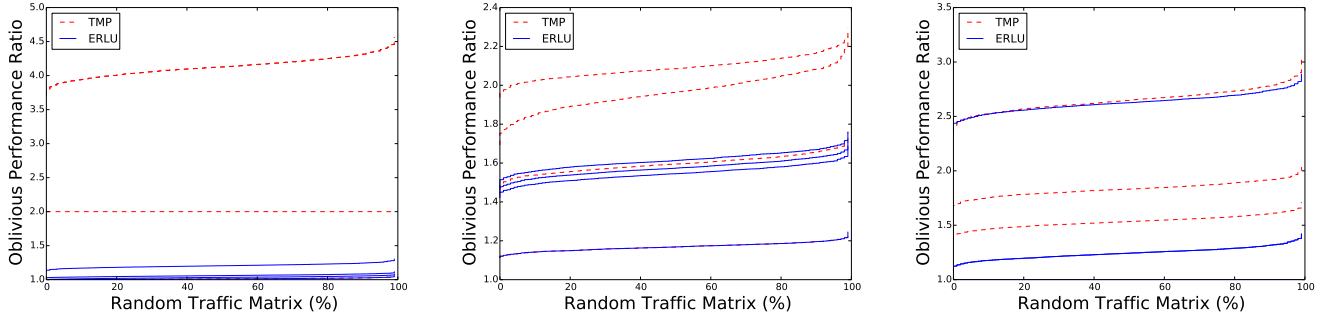


Fig. 4. OPRE versus TMs: (a). Abilene, (b). Geant, (c). Cernet2

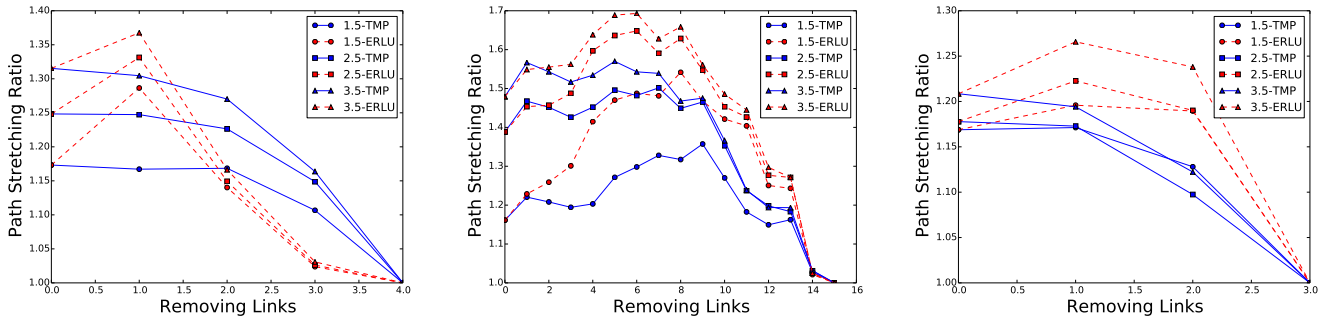


Fig. 5. Path Stretching: (a). Abilene, (b). Geant, (c). Cernet2

Intuitively, we can see ERLU is always better than TMP whatever margin or power saving target is, because ERLU consider much more than TMP, such as capacity and robust traffic flows. Another information from Figure 4 is that, we should carefully set the value of power saving for avoiding removing too much links, which result in the OPRE increases rapidly, induce network congestions easily and make the robust routing be less ‘robust’.

we concern more about how is the OPRE varifying when achived specific power saving target. Obviously, the more links we removed, the more power we saved, but how to quantify the power of one link is difficult. Green TE proposed a simple power model [1], which can be represented in Table II. In which, the total energy of topology is dominant by line cards of routers or switches, when saying switch off the links we mean put down the according line cards.

TABLE II
GREEN TE POWER MODEL

Line-Card	Speed(Mbps)	Power(Watts)
1-Port OC3	155.52	60
8-Port OC3	1244.16	100
1-Port OC48	2488.32	140
1-Port OC192	9953.28	174

We compute the power saving ratio as the total power of the removed links over the total power of all the links. In Figure 3 (a), it shows we can save 19% energy only with an OPRE of 1.30 in Abilene topology, and in Geant and Cernet2, the OPRE is little higher. Curves present some scalariform, it means that in some range of power saving, the OPRE rise slowly, and in the end of range, the energy conservation is efficient.

B. OPRE versus Margin

We take the margin w as one of the input for computing robust routing, and margin identify a range of TMs the routing is robust for. Once the w limit extremely, our robust routing is said without knowledge of traffic matrix. Figure 3 shows the OPRE increases little as w increases, particularly in Geant, the difference almost can not be observed. It is obvious because when the w is greater, the traffic matrix is random in more wider range, and our OPRE may achieve worse case with more probability.

C. OPRE versus TMs

To simulate the worst case, we generate 1000 traffic matrices for every topology with margin attribute w . Figure 4 shows the OPRE distribution in the process of experiment. For avoiding mess result from too many lines, we just show the first three lines and the base line, which shows the distribution when no links is removed, i.e. seven lines in each figure.

In Figure 4 (a), we can only observe five lines because there are two overlapping lines, which means that when removing links the worst case for the robust routing does not change. Maybe the random traffic matrices is not bad enough, or the removed link really do not affect the MLUR. And from Figure 4, we see that the OPRE is not always be achived for most traffic matrices, the common value is much less than OPRE.

Comparing TMP and ERLU, the conclusion is similar to Figure 3, the latter is always better than the former. Even in some time, ERLU obtains more power saving but with a lower OPRE.

D. Path Stretching

Path stretching must be careful concerned in routing problem. Suppose two vertices connect directly each other in the origin topology, if we remove the connected link then they can connect by another path which is composed by multi links. However we argue path stretching between these situation may be unjust, because path stretching result from the difference of topologies rather than routing selection. So we obtain the shortest path by Dijkstra Algorithm in the final topology, and compare it with robust routings generated by our REAR

algorithm. Futher, we show the difference between two ways of removing link, and see the tendency when margin increased.

In Figure 5, we see every line ends with path stretching ratio of 1, because topology become a tree structure when lose too much links, every path between vertices come to be unique, namely each path is the shortest path. Another conclusion is that, even in the origin topology, our robust routing is 17% longer than the shortest one, it is beacuse our algorithm not only consider the MLUR but also the robust performance. However the Dijkstra just take the path length as metric.

We can observe that, ERLU is always shorter than TMP, although in Geant, the worst case is 36% than the shortest path when margin equal to 1.5. And in the first removed links, the path stretching ratio is near 20%.

VII. CONCLUSION

The conclusion goes here.

REFERENCES

- [1] M.Zhang, C.Yi, B.Liu and B.Zhang, "GreenTE: Power-Aware Traffic Engineering".
- [2] D.Applegate and E.Cohen, "Making Intra-Domain Routing Robust to Changing and Uncertain Traffic Demands: Understanding Fundamental Tradeoffs".
- [3] M.Roughan, A.Greenberg, C.Kalmanek, M.Rumsewicz, J.Yates, and Y.Zhang. Experience in measuring backbone traffic variability: models, metrics, measurements, and meaning. InProceedings of the 2nd Internet Measurement Workshop. ACM, 2002