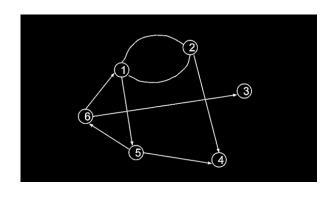
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Course/Year/Section: CpE 2-1

Student Number: 202101628

ACTIVITY: GRAPHS



Graph 9:

$$G_9 = (V_9, E_9)$$

$$V_9 = \{1, 2, 3, 4, 5, 6\}$$

$$E_9 = \{(1,2), (1,5), (2,1)(2,4),$$

Outdegree of node:

2 is 2

3 is 0

4 is 0

5 is 2

6 is 2

Indegree of node:

1 is 2

2 is 1

3 is 1

4 is 2

5 is 1

6 is 1

Vertices adjacent to:

Node 1: $v = \{2,6\}$

Node 2: v = 1

Node 3: v = 6

Node 4: $v = \{2,5\}$

Node 5: v = 1

Node 6: v = 5

Vertices adjacent from:

Node 1: $v = \{2,5\}$

Node 2: $v = \{1,4\}$

Node 3: null

Node 4: null

Node 5: $v = \{4,6\}$

Node 6: $v = \{1,3\}$

Graph 9:

Edges incident to:

Node 1:
$$E = \{(1,2), (1,5), (2,1), (6,1)\}$$

Node 2:
$$E = \{(2,1), (1,2), (2,4), \}$$

Node 3:
$$E = \{(6, 3)\}$$

Node 4:
$$E = \{(2,4), (5,4)\}$$

Node 5:
$$E = \{(1,5), (5,6), (5,4)\}$$

Node 6:
$$E = \{(6,1), (6,3), (5,6)\}$$

Paths with:

Length of 2:
$$v = \{(1,2,4), (1,2,1), (1,5,6), (1,5,4), (2,1,2), (5,6,1), (5,6,3), (6,1,2), (6,1,5)\}$$

Length of 3:
$$v = \{(1.5.6,1), (1.5.6,3), (2.1.5,6), (2,1,5,4), (6,1,5,6), (6,1,2,4), (5,6,1,2), (5,6,1,5), (6,1,5,4)\}$$

Length of 4:
$$v = \{(2,1,5,6,3), (5.6.1.2.4)\}$$

Simple Paths with:

Length of 2:
$$v = \{(1,2,4), (1,5,6), (1,5,4), (5,6,1), (5,6,3), (6,1,2), (6,1,5)\}$$

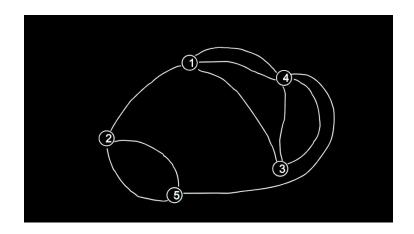
Length of 3:
$$v = \{(1,5,6,3), (2,1,5,4), (2.1.5,6), (5,6,1,2), (6,1,5,4), (6,1,2,4)\}$$

Length of 4:
$$v = \{(2,1,5,6,3), (5,6,1,2,4)\}$$

Simple Cycle with:

Length of 2:
$$v = \{(1,2,1), (2,1,2)\}$$

Length of 3:
$$v = \{(1,5,6,1), (5,6,1,5), (6,1,5,6)\}$$



Graph 10

$$G_{10} = (V_{10}, E_{10})$$

$$V_{10} = \{1, 2, 3, 4, 5, \}$$

$$E_{10} = \{(1,4), (2,1), (2,5)(3,1),$$

Outdegree of node:

1 is 1

2 is 2

Indegree of node:

Vertices adjacent to:

Node 1: $v = \{2,3,4\}$

Node 2:
$$v = 5$$

Node 3:
$$v = 4$$

Node 4:
$$v = \{1,3\}$$

Node 5:
$$v = \{2,4\}$$

Vertices adjacent from:

Node 1:
$$v = 4$$

Node 2:
$$v = \{1,5\}$$

Node 3:
$$v = \{1,4\}$$

Node 5:
$$v = 2$$

Graph 10:

Edges incident to:

Node 1:
$$E = \{(1,4), (2,1), (3,1), (4,1)\}$$

Node 2:
$$E = \{(2,1), (2,5), (5,2), \}$$

Node 3:
$$E = \{(4, 3), (3,4), (3,1)\}$$

Node 4:
$$E = \{(2,4), (5,4)\}$$

Node 5:
$$E = \{(4,1), (4,3), (4,5), (1,4), (3,4)\}$$

Node 6:
$$E = \{(5,2), (2,5), (4,5)\}$$

Paths with:

Length of 2:
$$v = \{(1,4,3), (1,4,1), (1,4,5), (2,1,4), (2,5,2), (3,1,4), (3,4,3), (3,4,1), (3,4,5), (4,1,4), (4,3,1), (4,3,4), (4,5,2), (5,2,5), (5,2,1)\}$$

Length of 3:
$$v = \{(1.4.3,1), (1.4.5,2), (2.1.4,3), (2,1,4,5), (3.4,5,2), (3,1,4,3), (3,1,4,5), (4,3,1,4), (4,5,2,1), (5,2,1,4)\}$$

Length of 4:
$$v = \{(1,4,5,2,1), (2,1,4,5,2), (8.1,4,5,2), (3,4,5,2,1), (4,5,2,1,4), (5,2,1,4,3), (5.2,1,4,5)\}$$

Simple Paths with:

Length of 2:
$$v = \{(1,4,3), (1,4,5), (2,1,4), (3,1,4), (3,4,1), (3,4,5), (4,3,1), (4,5,2), (5,2,1)\}$$

Length of 3:
$$v = (1,4,5,2), (2,1,4,3), (2,1,4,5), (3,4,5,2), (3,1,4,5), (4,5,2,1), (5,2,1,4)$$

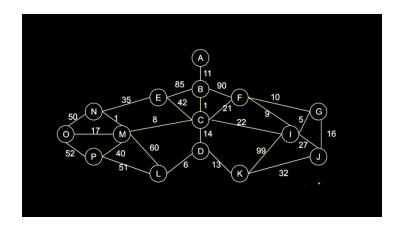
Length of 4:
$$v = \{(3,1,4,5,2), (3,4,5,2,1), (5,2,1,4,3)\}$$

Simple Cycle with:

Length of 2:
$$v = \{(1,4,1), (2.5,2), (3,4,3), (4,1,4), (4,3,4), (5,2,5)\}$$

Length of 3:
$$v = \{(1,4,3,1), (3.1,4,3), (4,3,1,4)\}$$

Length of 4:
$$v = \{(1,4,5,2,1), (2,1,4,5,2), (4,5,2,1,4), (5,2,1,4,5)\}$$



Graph 29:

Minimum Spanning Tree of the graph using Kruskal's algorithm:

BC - 1

NM - 1

GI-5

LD-6

MC - 8

FI-9

AB - 11

DK - 13

DC – 14

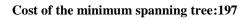
GJ – 16

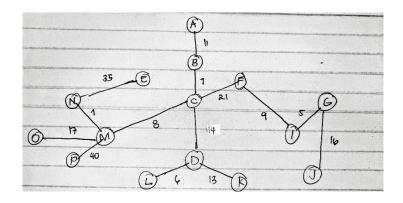
MO - 17

CF-21

NE - 35

MP-40





Minimum Spanning Tree of the graph using Prim's algorithm:

Arbitrary start is @ vertex A.



BC - 1

CM-8

NM - 1

CD - 14

DL-6

DK - 13

OM – 17

CF - 21

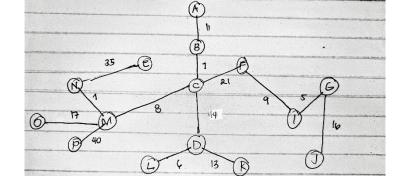
FI-9

GI-5

GJ - 16

NE - 35

MP-40



Cost of the minimum spanning tree: 197