# Project plan

# High-accuracy radiation pressure modeling for LRO

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# Nomenclature

$\alpha$	View angle; angle between surface normals of source and target	rad
λ	Longitude	rad
ν	Shadow function; $\nu=0$ means total eclipse, $\nu=1$ means full radiation	_
Φ	Radiant power	W
$\phi$	Latitude	rad
$\sigma$	Stefan–Boltzmann constant	$\mathrm{W}/(\mathrm{m}^2\mathrm{K}^4)$
$\theta$	Incidence angle; angle between surface normal and incident radiation	rad
n	Normal vector of a surface	_
r	Vector from source to target; depends on context	m
î .	Unit vector from source to target	
A	Area on source that receives radiation	$\mathrm{m}^2$
$C_a$	Absorptivity	
$C_d$	Diffuse reflectivity	
$C_r$	Radiation pressure coefficient	_
$C_s$	Specular reflectivity	_
E	Irradiance/flux density	$ m W/m^2$
$E_s$	Solar irradiance	$ m W/m^2$
m	Mass	kø

#### 1 Introduction

Scientific results obtained from a combination of LRO altimetry, GRAIL gravity field determination and Lunar Laser Ranging can in some cases lead to conflicting results on specific details on lunar geodetic properties (tides, rotation, etc.) Although minor, these discrepancies may not allow the exceptionally accurate data sets that are available to be processed to their inherent accuracy.

For this project, one possible contributor to this issue will be analyzed: errors in non-conservative force modelling of the spacecraft. In particular, this project will investigate the impact of various level of detail of the radiation pressure modelling of the LRO spacecraft, with the aim of contributing to a more robust error budget of the attained orbit determination results. This leads to the research question:

What is the quantitative influence of using high-accuracy radiation pressure models on the attainable orbit precision for the Lunar Reconaissance Orbiter?

The models will be implemented in Tudat, an open-source simulation framework for astrodynamics, developed by TU Delft.

#### 2 Models

On the highest level, we divide radiation pressure models into sources and targets. Sources emit or reflect electromagnetic radiation onto the target, which experiences an acceleration. For sources, we regard direct solar, albedo and thermal radiation. For targets, we regard cannonball and paneled models with and without self-shadowing.

Source models and target models can be developed independently, then mixed and matched. The interface between sources and targets consists of 2 quantities:

- Irradiance, or flux density, E from source at target
- Unit vector **r** from source to target

These can be combined into the directional irradiance  $\mathbf{E} = E\hat{\mathbf{r}}$ . This assumes that all radiation is parallel, i.e. originates from a distant point, which is a good approximation for distant sources (e.g., the Sun at 1 AU distance). Sources for which the spatial extent is relevant (e.g., Earth albedo radiation in LEO) can be discretized into multiple point sources.

We treat all radiation equally as total flux, independently of wavelength. While most optical properties such as reflectivity are physically wavelength-dependent, characterizing their dependence is challenging in practice. This leads us to using the same surface properties across wavelengths, even though albedo radiation is in the visible range while thermal radiation is infrared.

#### 2.1 Sources

The most significant source of radiation pressure in Earth and lunar orbits is direct solar radiation, which follows an inverse square law:

$$E_s = \nu \frac{3.839 \times 10^{26} \,\mathrm{W}}{4\pi \|\mathbf{r}\|^2} \tag{1}$$

This leads to the well-known solar irradiance of  $E_s = 1367 \,\mathrm{W/m^2}$  at  $\|\mathbf{r}\| = 1 \,\mathrm{AU}$ . Note that this irradiance is a time average, and varies [1] as Earth moves between its perihelion and aphelion, but also with changes in the Sun's radiant power itself. Time series for total solar irradiance at Earth exist, but not Sun's radiant power, making a constant value the only feasible option for lunar orbits.

 $\nu \in [0,1]$  is the shadow function, scaling the received irradiance according to the visible portion of the sun, which may be occulted by other bodies. A conical model dividing space into regions of full sunlight, penumbra and umbra due to a single body is the standard [2]. This model could be extended to consider (partial) occultation by two bodies as described by Zhang *et al.* [3].

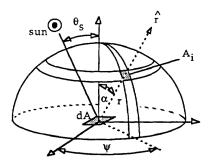


Figure 1: Geometry of albedo radiation. dA is the source element,  $A_i$  is the target.

Albedo radiation, reflected by planet surfaces, is much smaller but still significant. Albedo requires knowledge of properties of the radiation source (for our intents and purposes, the Sun) and the reflecting body. The solar irradiance  $E_s$  and angle between reflecting surface normal and Sun  $\theta_s$  determine the incident irradiance onto the source surface element dA. The reflected radiation depends on the albedo distribution  $a = a(\lambda, \phi)$  which may vary with longitude  $\lambda$  and latitude  $\phi$ . The received radiation depends on the view angle  $\alpha$ , which is the angle between the surface normals of source and target. This geometry is shown in Figure 1. The irradiance from dA at the target due to albedo is given by [4]:

$$E = a\cos\theta_s E_s \frac{dA\cos\alpha}{\pi \|\mathbf{r}\|^2} \tag{2}$$

where  $a\cos\theta_s E_s$  is the reflected irradiance. Note that albedo radiation only exists if dA receives sunlight. Shadow calculations could also be included but are more involved for albedo models, since both the incoming solar radiation and outgoing albedo radiation could be affected by occultation. Calculations are further complicated since common occultation models assume spherical sources and not flat surface elements.

The simplest choice for the lunar albedo is the average value of a = 0.12 [5]. A more detailed albedo distribution is the 15x15 spherical harmonics model by Floberghagen *et al.* [6]. However, for calculations, paneling of the source is more convenient. Knocke *et al.* [4] introduce a spherical cap centered at the subsatellite point, which is divided into rings of panels of constant albedo, tangent

to the source surface at their center. Equation (2) is then evaluated for each panel dA. We call this  $dynamic\ paneling$ . Alternatively, the whole body could be paneled independently of the satellite position ( $static\ paneling$ )

Similarly, the thermal radiation can be described, scaled by the emissivity e. Additionally, there is a factor of 1/4, which is the ratio between receiving and emitting surface. Then the irradiance from dA at the target due to thermal radiation is given by [4]:

$$E = \frac{eE_s}{4} \frac{dA \cos \alpha}{\pi \|\mathbf{r}\|^2} \tag{3}$$

where  $eE_s/4$  is the emitted exitance. Thermal radiation exists independent of incident sunlight and is therefore constant. The simplest model for lunar emissivity is a constant value of e = 0.95 [5].

Alternatively, a latitude- and local time-dependent temperature distribution of the lunar surface can be assumed [7]. By the Stefan–Boltzmann law, the irradiance at the target due to the thermal radiation is given by:

$$E = e\sigma T^4 \frac{dA\cos\alpha}{\pi \|\mathbf{r}\|^2} \qquad T = \max\left(T_{\max}(\cos\theta_s)^{1/4}, T_{\min}\right)$$
 (4)

where  $T_{\text{max}} = 375 \,\text{K}$  and  $T_{\text{min}} = 100 \,\text{K}$ . Note that the maximum irradiance from Equation (4) is about four times higher than that from Equation (3) since  $\sigma T_{\text{max}}^4 \approx E_s$ , but varies as the dA moves away from the subsolar point ( $\theta_s$  increases) and cools down.

#### 2.2 Targets

The cannonball model is the simplest model for target acceleration due to radiation pressure. The target is modeled as a sphere such that lateral accelerations cancel and there is only an acceleration away from the source along  $\hat{\mathbf{r}}$ . The cross-sectional area A is independent of orientation, and surface properties (reflectance and absorptivity) are captured in the radiation pressure coefficient  $C_r$ . Then the acceleration of a target with mass m is given by [4]:

$$\mathbf{a} = C_r \frac{A}{m} \frac{E}{c} \hat{\mathbf{r}} \tag{5}$$

A more sophisticated paneled target model discretizes the spacecraft into n panels with area A and normal vector  $\mathbf{n}$ . This also means that the incidence angle  $\theta$  differs per panel. Their surface is characterized by the absorptivity  $C_a$ , diffuse reflectivity  $C_d$  and specular reflectivity  $C_s$ , which obey  $C_a + C_d + C_s = 1$ . Then the acceleration of the whole target due to all target panels and a single source is given by [8]:

$$\mathbf{a} = \frac{1}{m} \frac{E}{c} \sum_{j=1}^{n} A \cos \theta \left[ (C_a + C_d) \left( \hat{\mathbf{r}} - \frac{2}{3} \mathbf{n} \right) - 2C_s \cos \theta \mathbf{n} \right]$$
 (6)

where all quantities inside the summation except  $\hat{\mathbf{r}}$  are specific to panel j. For the LRO, these panel properties are given by Smith et~al. [9]. Self-shadowing could also be included here. Mazarico et~al. [10] describe an algorithm to modify the effective area due to self-shadowing and describe the effect on the spacecraft trajectory as significant.

In case of a paneled source, the total acceleration is the vectorial sum of these contributions over all m source panels:

$$\mathbf{a} = \frac{1}{m} \sum_{i=1}^{m} \frac{E}{c} \sum_{j=1}^{n} A \cos \theta \left[ (C_a + C_d) \left( \hat{\mathbf{r}} + \frac{2}{3} \mathbf{n} \right) + 2C_s \cos \theta \mathbf{n} \right]$$
 (7)

where E is the irradiance due to the *i*-th source panel.

### 3 Code design

22

All models presented in Section 2 will be implemented. The following Python-like pseudocode shows the classes and their interactions. The code is not complete but only contains parts relevant for radiation pressure computations.

Design decisions I am uncertain about:

- class RadiationPressureAcceleration bears the main responsibility of combining source and target information, which allows sources and targets to be agnostic of each other. This includes occultation calculations between source and target (occultation calculations for albedo are handled by class PaneledRadiationSourceInterface) Is it too much responsibility for one class?
- Both source geometry and emitted/reflected radiation models are implemented in class PaneledRadiationSourceInterface, even though they are separate concerns and can be applied in various combinations. Multiple source models for albedo and thermal radiation are implemented in the same class, accessible through switches (Lines 112–119). Alternatively, each of Equations (2) to (4) could be implemented in separate classes, which would introduce too much unnecessary complexity in my opinion.

```
1
         ENVIRONMENT
2
  4
     """Models Sun, planets and spacecraft"""
5
     position: Vector3
6
     mass: double
7
8
     # List of all sources originating from this body
9
     # For sun: PointRadiationSourceInterface for direct solar radiation
10
     # For planets: PaneledRadiationSourceInterface for albedo + thermal radiation
     # For spacecraft: -
12
     radiationSourceInterface: RadiationSourceInterface
13
14
     # Target interface (for bodies undergoing radiation pressure acceleration)
15
     # For sun: -
16
     # For planets: -
17
     # For spacecraft: CannonballRadiationPressureTargetInterface or
18
         PaneledRadiationPressureTargetInterface
19
     radiationPressureTargetInterface: RadiationPressureTargetInterface
20
21
```

```
class RadiationPressureAcceleration(AccelerationModel3d):
23
24
      Radiation pressure acceleration from a single source (possibly with multiple source interfaces
25
      for albedo and thermal) onto a single target.
26
27
      source: Body # e.g. Sun
28
      target: Body # e.g. LRO
29
      occultingBodies: list[Body] # e.g. Earth and Moon
30
31
      def updateMembers(currentTime: double) -> void:
32
         """Evaluate radiation pressure acceleration at current time step"""
33
         force = Vector3.Zero()
34
         # Iterate over all source panels and their fluxes
35
         for sourceIrradiance, sourceCenter in source.radiationSourceInterface \
36
                                              .evaluateAtPosition(target.position): # i=1..m
37
            sourceToTargetDirection = (target.position - sourceCenter).normalize()
38
            sourceIrradiance *= calculateShadowFunction(source, occultingBodies, target)
39
            force += target.evaluateRadiationPressureForce(sourceIrradiance,
40
                                                          sourceToTargetDirection)
41
         currentAcceleration = force / target.mass
42
43
44
   def calculateShadowFunction(occultedBody: Body, occultingBodies: list[Body], \
45
                                targetBody: Body) -> double:
46
      # Calculate using Montenbruck 2000 or Zhang 2019 equations
47
      # Compared to current function in Tudat, takes multiple occulting bodies
48
50
   51
   #
           SOURCES
52
   53
54
   abstract class RadiationSourceInterface:
55
      source: Body # The source that this interface belongs to
56
                   # For albedo, this is the reflecting body, not the Sun
57
58
      def evaluateAtPosition(targetPosition: Vector3) -> list[tuple[double, Vector3]]:
59
60
         Calculate irradiance at target position, also return source position. Subclasses
61
         are aware of source geometry. Return a list of tuples of flux and origin to
62
         support multiple fluxes with different origins for paneled sources.
63
         n n n
         pass
65
66
67
   class PointRadiationSourceInterface(RadiationSourceInterface):
68
      """Point source (for Sun)"""
69
      radiantPower: double
70
      def evaluateAtPosition(targetPosition: Vector3) -> list[tuple[double, Vector3]]:
         sourcePosition = source.position
73
         distanceSourceToTarget = (targetPosition - sourcePosition).norm()
74
         irradiance = radiantPower / (4 * PI * distanceSourceToTarget**2) # Eq. 1
75
         return [(irradiance, sourcePosition)]
76
77
```

78

```
class PaneledRadiationSourceInterface(RadiationSourceInterface):
79
        """Paneled sphere (for planet albedo + thermal radiation)"""
80
        originalSource: Body # Usually the Sun, from where incoming radiation originates
        occultingBodies: list[Body] # For Moon as source, only Earth occults
82
83
        panels: list[SourcePanel]
84
        modelSettings: PaneledRadiationSourceModelSettings # For example, ALBEDO | THERMAL_KNOCKE
85
86
        def _generatePanels():
87
           # Panelize body and evaluate albedo for panels. For static paneling
88
           # (independent of spacecraft position), generate once at start of simulation,
89
           # Query SH albedo model here if available here, or load albedos and
90
           # emissivities from file
91
           panels = ...
92
93
94
        def evaluateAtPosition(targetPosition: Vector3) -> list[tuple[double, Vector3]]:
           # For dynamic paneling (depending on target position, spherical cap centered
95
           # at subsatellite point as in Knocke 1988), could regenerate panels here
96
           # (possibly with caching), or create separate class
           ret = []
98
           for panel in panels: # i=1..m
99
              if not isVisible(panel, targetPosition):
100
                 # Panel hidden at target position
101
                 break
102
103
              sourcePosition = source.position + panel.center
104
              distanceSourceToTarget = (targetPosition - sourcePosition).norm()
105
              # for received radiation at panel
106
              shadowFunction = calculateShadowFunction(originalSource, occultingBodies, panel.center)
107
108
              albedoIrradiance = 0
109
              thermalIrradiance = 0
110
111
              if modelSettings & ALBEDO:
112
113
                 albedoIrradiance = \
                    shadowFunction * panel.albedo * ... # albedo radiation calculation, Eq. 2
114
              if modelSettings & THERMAL_KNOCKE:
115
                 thermalIrradiance = panel.emissivity * ... # thermal radiation calculation, Eq. 3
116
              if modelSettings & THERMAL_LEMOINE:
117
                 temperature = max(...)
118
                 thermalIrradiance = panel.emissivity * ... # thermal radiation calculation, Eq. 4
119
120
              ret.append((albedoIrradiance + thermalIrradiance, sourcePosition))
121
           return ret
122
123
124
     class RadiationSourcePanel:
125
        area: double
126
        center: Vector3 # Panel center relative to source center
127
        normal: Vector3
129
        albedo: Optional[double]
130
        emissivity: Optional[double]
131
132
133
     class PaneledRadiationSourceModelSettings(enum.Flag):
```

134

```
ALBEDO
135
       THERMAL_KNOCKE
136
       THERMAL_LEMOINE
137
138
139
    140
           TARGETS
141
    142
143
    abstract class RadiationPressureTargetInterface:
144
       def evaluateRadiationPressureForce(sourceIrradiance: double,
145
                                       sourceToTargetDirection: Vector3):
146
147
         Calculate radiation pressure force due to a single source panel onto whole target
148
149
150
         pass
151
152
    class CannonballRadiationPressureTargetInterface(RadiationPressureTargetInterface):
153
       area: double
154
       coefficient: double
155
156
       def evaluateRadiationPressureForce(sourceIrradiance: double,
157
                                       sourceToTargetDirection: Vector3):
158
          force = sourceIrradiance * area * coefficient * ...
159
          return force
160
161
162
    class PaneledRadiationPressureTargetInterface(RadiationPressureTargetInterface):
163
       panels: List[TargetPanel]
164
165
       def evaluateRadiationPressureForce(sourceIrradiance: double,
166
                                       sourceToTargetDirection: Vector3):
167
          force = Vector3.Zero()
168
          for panel in panels: # j=1..n
169
            if not isVisible(panel, sourceToTargetDirection):
170
               # Panel pointing away from source
171
               break
172
173
            force += sourceIrradiance * panel.area * ...
174
         return force
175
176
177
    class TargetPanel:
178
       area: double
179
       normal: Vector3
180
181
       absorptivity: double
182
       specularReflectivity: double
183
       diffuseReflectivity: double
184
```

#### 4 Verification & Validation

Verification will check whether the models presented in this document were implemented correctly, based on manual calculations and values from literature. Validation will check whether the mathematical models themselves give sensible results. Both will be implemented as unit tests. Existing radiation pressure unit tests within Tudat will be reused and adapted to avoid regression. However, existing tests include a lot of logic that itself may be flawed. Therefore, the reworked unit tests will be more straightforward, at the cost of duplicate code.

To validate the simulation setup, I will also propagate LRO's orbit and check consistency with ephemerides from SPICE SPKs. While small discrepancies are expected due to differences in other models, the error should be reasonable.

# 5 Result analysis

The question to be answered is What is the quantitative influence of using high-accuracy radiation pressure models on the attainable orbit precision for the Lunar Reconaissance Orbiter? The answer will not include statements about absolute or relative precision improvements, since there is no ground truth. Rather, the answer will give tendencies about how different models and parameters influence orbital elements.

The simulation setup for gathering results will be varied to investigate different levels of accuracy. In the simplest form, the radiation pressure models only contain a direct solar radiation source and a cannonball target (baseline model) In the most complete form (extended model), the setup looks as follows:

- Sun:
  - Ephemeris from DE 421 (used by JPL for LRO ephemeris generation)
  - Gravity field
  - Direct solar radiation source
- Earth:
  - Ephemeris from DE 421
  - Gravity field
  - Occulting body for direct solar and lunar albedo radiation
- Moon:
  - Global origin

- Ephemeris from DE 421
- Gravity field
- Albedo radiation source (paneled Moon with albedo obtained from DLAM-1)
- Thermal radiation source (paneled Moon)
- Occulting body for direct solar radiation

#### • LRO:

- Propagated (translational and rotational) for 226 min, corresponds to about 2 orbital revolutions
- Initial ephemeris from LRO reprocessed spacecraft ephemeris (fdf36\_...) during regular science mission at 50 km altitude, ensure no stationkeeping occured during propagation period and Sun-beta angle is about 45° (so eclipses and no yaw maneuver will occur, cf. [11, Fig. 12])
- Paneled radiation pressure target with areas and coefficients from Smith et al. [9] (assume SA is pointed towards sun, ignore HGA because incorporating CK SPICE kernels for definitive HGA orientation requires too much work)
- No self-shadowing, unless time permits

The result analysis is inspired by Vielberg *et al.* [1] for LEO satellites, but less involved since a lot of details (e.g. observed outgoing fluxes, observed solar irradiance, land coverage) do not exist for or apply to the Moon. The analysis will consider the following aspects:

- Accelerations due to each radiation pressure component (direct solar, albedo, thermal) in radial, cross-track and along-track directions with extended model (cf. [1, Fig. 3])
- Dependence of accelerations on position in orbit and time (cf. [1, Fig. 7]), correlate with relative sun position and albedo map
- Sensitivity analysis for albedo and target reflection/absorption coefficients (since these parametrizations are often inaccurate, investigating influence of their errors is important)
- Effect of different levels of detail of radiation pressure models on accelerations (cf. [1, Fig. 8]) and Keplerian orbit elements (e.g., how does addition of albedo radiation change semi-major axis?), moving from baseline model towards extended model
  - Baseline model: only direct solar radiation source, cannonball target
  - For source, add albedo and thermal radiation (vary paneling resolution, constant and spherical harmonics albedo, constant or varying thermal radiation from Equations (3) and (4), dynamic/static paneling)
  - For target, switch to paneled model with/without self-shadowing

- Compare mean difference and RMS difference w.r.t. baseline in radial, cross-track and along-track directions after propagation arc
- Compare Keplerian orbits w.r.t. baseline after propagation arc
- Measure performance impact of increased level of detail through wall-clock and/or CPU time

## 6 Implementation plan

A minimum viable version will be implemented first, including only a point source and a cannonball target (the baseline model). Once this version works and has been verified, the more complex models can follow. All implementations also include unit tests for verification and validation. The implementation plan is as follows:

- 1. Implement baseline model
  - a) Implement class PointRadiationSourceInterface with abstract base class
  - b) Implement class CannonballRadiationPressureTargetInterface with abstract base class
  - c) Implement class RadiationPressureAcceleration without occultation
  - d) Verify functionality and check if design makes sense
- 2. Implement class PaneledRadiationPressureTargetInterface
- 3. Implement class PaneledRadiationSourceInterface with static paneling (constant albedo until we get access to DLAM-1)
- 4. Implement class OccultationGeometry for single occulting body and include in class RadiationPressureAcceleration
- 5. Implement LRO simulation (baseline model and extended model) as described in Section 5
- 6. Validate complete simulation
- 7. Implement extra items, if time permits
  - a) Implement spherical harmonics lunar albedo model DLAM-1 from Floberghagen et al. [6], if we get access
  - b) Implement occultation by two bodies from Zhang et al. [3]
  - c) Implement class PaneledRadiationSourceInterface with dynamic paneling
  - d) Implement self-shadowing from Mazarico et al. [10]

e) Optimize

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