Title: Using neutral theory to reveal the contribution of dispersal to community assembly in complex landscapes Authors: Dominique Gravel<sup>1,2,\*</sup>, Timothée Poisot<sup>1,2</sup>, Philippe Desjardins-Proulx<sup>1,2</sup> 1: Canada Research Chair on Terrestrial Ecosystems. Département de biologie, chimie et géographique, Université du Québec à Rimouski, 300 Allée des Ursulines, Québec, Canada. G5L 3A1. 2: Québec Centre for Biodiversity Sciences 10 11 Keywords: metacommunity; neutral theory; species sorting; metapopulation; spa-12 tial network; centrality 13 14 Words in the abstract: 15 Words in the main text: 16 Words in the legends: 17 Figures: 4 18 Tables: 2 19 **References:** 20

#### 21 Abstract

The metacommunity perspective appears naturally as the appropriate conceptual frame-22 work to make ecology more predictive, integrating elements of theoretical ecology. 23 The recent development of neutral theory appears as a step back in that direction be-24 cause of the assumption of ecological equivalence and the absence of any effect of the 25 environment on community organization. A remarkable strength of neutral theory is 26 nonetheless to provide a general theory of diversity that accounts for a wide range of 27 empirical observations. In this paper, we argue that neutral theory can be a useful tool 28 to understand the impact of dispersal on community organization in landscapes of var-29 ious complexities. Our main objective is to use neutral theory to stress the importance 30 of complex landscape network structure on the distribution of diversity. We refer to 31 the landscape organization as a "spatial contingency" that could potentially affect the 32 coexistence mechanisms at play. We briefly review the main approaches to describe spatial networks and describe three simple toy models of metacommunity dynamics. We take this opportunity to review their assumptions and main predictions. We then conduct simple simulations of these models to reveal with simple examples the 36 impact of spatial network structure on diversity distribution. The simulation results 37 show that competitive interactions buffer the potential impact of landscape structure. 38 The strongest centrality-species richness relationship was observed for the patch dy-30 namics, a model without any interactions. On the other hand, strong and unequal 40 competitive interactions minimized the effect of centrality. We conclude that the neu-41 tral model is thus a useful tool to understand the joint effects of dispersal and commu-42 nity interactions. Our analysis shows that ecologists must now integrate more realistic landscapes when analyzing community assembly from a metacommunity perspective.

### 45 Introduction

57

60

61

62

63

64

65

66

67

69

Ecology needs to move toward a more predictive approach, integrating elements of theoretical ecology ("A road map for integrating eco-evolutionary processes into bio-47 diversity models"). The metacommunity perspective (Leibold et al. 2004) appears naturally as the appropriate conceptual framework to fill this challenge. The metacom-49 munity concept builds on feedbacks between local scale processes, such as competitive 50 interactions and local adaptation, and regional scale processes such as dispersal, gene 51 flow and speciation. It is particularly relevant to limnology, where exchanges of organ-52 isms and nutrients affect community and ecosystem properties from the local (e.g. ver-53 tical mixing (Ryabov & Blasius 2011)) to the regional (e.g. connection of lakes (Gravel 54 et al. 2010; Leibold & Norberg 2004) scales. It emphasizes the importance of dispersal 55 relative to pairwise interactions in the organization of ecological communities.

At first sight, the development of neutral theory appears as a step back. Neutral theory of biodiversity makes the provocative assumption that species are ecologically equivalent (Bell 2000; Hubbell 2001). Neutral ecological communities are driven only by demographic stochasticity and dispersa and thus, variation in the environment has no impact on demography. Neutral theory sparked an historical debate still lasting after more than a decade (Chave 2004; Clark 2012; Etienne & Rosindell 2011; Rosindell et al. 2012). It was stimulated by the surprising ability of neutral models to fit some well studied empirical observations such as species abundance distributions and distance-decay relationships.

A remarkable strength of the theory is to provide a "formal general theory of abundance and diversity that will account, in a simple and economical fashion, for the many patterns that ecologists have documented" (Bell 2001). Even if new studies rejecting neutral theory are consistently published (e.g. Ricklefs & Renner (2012)), a consensus is forming that neutral theory is a well-developed null hypothesis for niche theory and

could even be used as an adequate approximation of ecological dynamics in some situations. Bell (2001) nicely envisioned two perspectives to neutral theory that are still 72 standing today. Under the weak perspective, neutral theory provides a set of realistic 73 predictions of community organization despite false assumptions. Even if being fun-74 damentally wrong, neutral theory would still useful when used as a null hypothesis (Gotelli & McGill 2006). It is considered as an improvement over traditional null hy-76 potheses based on randomization (Gotelli 2000) because it readily integrates dispersal. On the other had, the strong version posits that neutral theory is a satisfying approximation to community dynamics and an appropriate theory to explain the distribution of biodiversity. It implies that the right mechanisms have been identified and that the 80 consistently observed differences among species do not impact community organiza-81 tion. 82

Neutral theory has also been proposed as a useful tool to understand and predict some aspects of community dynamics. It links to an old philosophical debate between realism and instrumentalism (Wennekes et al. 2012). Because every ecological model is a simplification of reality, scientists have to subjectively decide the level of details they put in, leaving out some elements they consider unimportant. The realism perspective requires that all assumptions of the theory must be true, while the utility of the theory is more important to instrumentalism. The utilitarian value of a theory could either be for understanding or for prediction (another old philosophical debate, see Shmueli (2010)). Obviously neutral theory could only be instrumental. The question then is if such a 'general, large-scale, but vague' theory (Wennekes et al. 2012) is a satisfying approximation.

83

84

85

86

87

88

89

90

91

92

93

94

95

The instrumentalist view of neutral theory raises the question of why it should be a satisfying approximation despite knowing the pieces are wrong? Perhaps stochasticity of various origins blur the deterministic differences among species and promote ecological drift (Gravel et al. 2011). Much has been said the existence of demographic stochasticity (Clark 2012), and we therefore will let this discussion for other papers.

A second answer is that dispersal and historical contingencies might have a much more profound impact on species distribution (Bahn & McGill 2007; Boulangeat et al. 2012) and ecological dynamics. The debate over the equivalence assumption and demographic stochasticity has perhaps overlook the recognition of how much dispersal influence community assembly.

In this paper, we argue that neutral theory can be a useful tool to understand the impact of dispersal on community organization in landscapes of various complexities. Even for purely theoretical analyses, we need a benchmark without niche differences to reveal the role of dispersal in structuring communities and understand how it interacts with niche differentiation. We will explore recent applications of neutral theory, at the crossroad of network theory, to better represent the impact of landscape structure on biodiversity distribution. This analysis will prove particularly relevant to limnology, where most riverine and lacustre habitats are characterized by their discrete nature and spatially complex arrangements (Peterson et al. 2013). We will also explore the relative contribution of ecological interaction and niche differentiation by contrasting predictions of a neutral model to other metacommunity perspectives.

Our main objective is to use neutral theory to stress the importance of landscape network structure on the distribution of diversity. We refer to the landscape organization as a *spatial contingency* (Peres-Neto et al. 2012) that could potentially affect the coexistence mechanisms at play. We will therefore move from a perspective where dispersal is either global or spatially explicit (e.g. over a lattice), and spatial constant, to a perspective focusing on the variance of dispersal. A second generation of neutral models (e.g. Desjardins-Proulx & Gravel (2012a,b); Economo (2011); Economo & Keitt (2008)), and even experiments (Carrara et al. 2012), recently introduced more realistic

landscapes and found surprising contributions of spatial contingencies. We start with 123 a short review of the main approaches to describe spatial networks. Then we describe 124 three simple toy models of metacommunity dynamics, using this opportunity to re-125 view their assumptions and main predictions. We provide as Supplementary Material 126 the R scripts for the toy models and all simulations conducted for this paper. We then 127 conduct simple simulations of these models to reveal with simple examples the impact 128 of spatial network structure on diversity distribution. We conclude with a discussion 129 on the operationally of the framework. 130

## Network representation of landscapes

A network is a discrete mathematical object made of two sets: a set of nodes (or ver-132 tices) and a set of edges connecting the nodes (Newman 2010). The term "graph" is 133 often preferred in computer science and mathematics (Gross & Yellen 2006), with 134 graph algorithms being an important and active area of research (Sedgewick 2001). 135 A network is a combinatorial object: it is used to study how discrete entities are con-136 nected and how they combine together to create complex structures. They are used 137 to study molecules, food webs, social networks, or even the relationship between vari-138 ables in statistics (Newman 2010; Wright 1921). We are especially interested in spatial 139 networks, a special kind of network mixing the combinatorial properties of networks 140 with a topological space (Kobayashi 1994). Thus, the vertices in a spatial graph are 141 embedded in some other space, most often the two or three- dimensional Euclidean 142 space. This object brings a rich representation to spatial ecology and is particularly 143 suited for systems of lakes and rivers, which can easily be represented by vertices and 144 edges. There are two notions of distance in spatial networks. Euclidean distance rep-145 resents the geographical distance between the nodes (i, j), i.e.:  $\sqrt{(x_i - x_j)^2 + (y_i - y_j)^2}$ . Geodesic distance is the distance in the graph space, i.e.: the length of the shortest path (Dijkstra 1959). For example, two lakes could be very close on a map (short Euclidean distance) but the geodesic distance could be great if they are not directly linked by a river.

The popularity of network theory stems for its ability to model complex structures while allowing us to extract useful metrics (Table 1). At a very high level, a network can be described by its number of nodes (the order) and edges (the size). Looking more closely, the relationship between nodes is influenced by paths, which are ordered series of nodes. Centrality is a *central* concept in network theory, where it can be seen to as a measure of "importance". The simplest measure of the centrality of a node is its degree, which is the number of nodes directly connected to it. Of course, this is a very rough description of centrality. For example, two lakes can have the same degree, with one being connected to a small isolated cluster, while the other one is part of one of the biggest network of lake. In this case, measures of centrality like eigen-centrality will weight the importance of the connection, so a node connected to well-connected nodes will have higher centrality than a node connected to isolated nodes.

For simulations, spatial networks can easily be generated with the random geometric graph algorithm (Sedgewick 2001). In this algorithm, all nodes are assigned to a position in some two-dimensional space, most often the unit square. Then, all pairs of nodes within some threshold Euclidean distance r are connected with an edge. The resulting networks have the desirable property of locality: if a node A is connected to two vertices B and C are more likely to be connected than two random vertices. Random geometric networks have been extensively studied (Appel et al. 2002; Appel & Russo 1997a,b, 2002; Penrose 2003) and we provide a R function to generate them. The position of nodes is typically random, but we could also imagine alterations where they are either more aggregated or segregated than expected by

173 chance alone.

174

175

176

177

178

179

We also provide the code for a second structure that we call a random geometric tree. The algorithm first builds a random geometric graph, then select a node from which to start the tree. It then calculaes the shortest path tree (Dijkstra 1959) from this node to all other ones. Edges that are not located along this tree are pruned. This random geometric tree does not exactly represent dendritic landscapes but is a convenient model to simulate lake connected by rivers to a series of smaller lakes.

Spatial graphs are increasingly popular in spatial ecology and conservation biology, 180 where patterns of connections can be used to study and influence the flow of organisms 181 (Dale & Fortin 2010; Fall et al. 2007; Garroway et al. 2008; Minor & Urban 2007, 2008; 182 Urban et al. 2009). In the neutral theory, networks were pioneered by Economo and 183 Keitt (Economo & Keitt 2010; Economo & Keitt 2008). They used networks to study 184 how different spatial structures influenced diversity. They were also used to study how 185 the spatial structure influenced nonsympatric speciation (Desjardins-Proulx & Gravel 186 2012a,b). 187

# Model description

In this section we describe three toy models representing different perspectives of metacommunity ecology: patch dynamics, neutral dynamics and species sorting. While the neutral model is interesting in itself, it is by its comparison with a model without any interactions (patch dynamics) and with niche differentiation (species sorting) that we will be able to fully understand the interaction between these processes and land-scape structure. Despite neutral, competitive interactions in neutral models are very strong because of the zero-sum assumption (the community is always at carrying capacity). We will first review the fundamental assumptions of each model with their

description (Table 2 summarizes the parameters and variables that are used), and then briefly discuss their main predictions. Simulation results are presented in the next section, with the corresponding R code provided in the Supplementary Material.

#### De Patch dynamics

The simplest metacommunity model is a S species extension of traditional metapopu-201 lation models (()Hanski1999). The standard Levins metapopulation model (()Levins1969) 202 describes the stochastic colonizations and extinctions of a single species over a ho-203 mogenous landscape. The basic unit is the population. The model tracts the dynamics 204 of occupancy (the fraction of the landscape that is occupied) with an ordinary differ-205 ential equation and therefore assumes an infinite landscape. The simulation model 206 we run is more realistic as it simulates a finite number N of discrete patches (or nodes 207 in network terminology). The rules described in the previous section were used to 208 generate connectivity matrices along four scenarios (Fig. 1): global dispersal (con-209 nected graph), a lattice, a random geometric graph and a random tree graph. A patch 210 x shares  $d_x$  links with neighbouring patches (its degree). At each time step (the simulation model is discrete in time), the probability that a colonist coming from an occupied patch y arrives at patch x is  $cd_v^{-1}$ , where c is the probability a colonization event takes 213 place if all connected patches are occupied. The expected probability that a colonist 214 arrives to patch x from patch y is then  $C_{ixy} = cp_{iy}d_v^{-1}$ , where  $p_iy$  is the probability that 215 patch y is occupied by species i. The probability that an extinction occurs in a given 216 patch is e. The Levins model is for a single species, but a basic metacommunity patch 217 dynamics model could be run by aggregating S independent metapopulation models 218 (()Hanski1997). There are no interactions in this simple model, which means there is 219 no limit to local species richness and no carrying capacity. Competitive, mutualistic 220 and predator-prey interactions have been added to this framework (e.g. Gravel et al. 221

(2011); Holt (1996); Klausmeier (1998); Tilman (1994)) but we will keep this model minimal for the sake of comparison with the neutral model.

222

223

Predictions of the patch dynamics metacommunity model are quite straightfor-224 ward. First, a fundamental result of metapopulation ecology is that persistence will 225 occur if colonization probability is larger than extinction probability (c > e). Given 226 that all species are the same, then we should expect the regional diversity  $(\gamma)$  to be S if 227 this condition is satisfied and 0 if not. The situation is however more complex in spa-228 tially explicit landscapes with complex connectivity matrices (Hanski 1998). Spatially 229 explicit dispersal usually reduces the occupancy and thereby the likelihood of per-230 sistence. The second prediction is that, given spatial variation in connectivity, there 231 will be spatial variation in occurrence probability. Given the above formulation of 232 a colonization event to occur, the probability that an empty location is colonized is 233  $I_i x = 1 - \prod d_x (1 - C_{ixy})$ . This equation basically tells us that the colonization probabil-234 ity will increase asymptotically with the degree of a patch (because of the product). It 235 is easy to show from metapopulation theory that the occurrence probability in a patch 236 is then  $p_i x = I_x (I_i x + e)^{-1}$ . The feedback between local and regional dynamics arises 237 because all  $p_i x$  from the landscape are dependent from each other. Simulations are 238 usually conducted to solve the model for a large landscape, but numerical solutions 239 are theoretically possible. The aggregation across the S species of the regional species 240 pool is obtained by taking the summation of occurrence probabilities over all species, 241  $s_x = \sum p_i$ . Because in this model all species are equal, we expect the local species rich-242 ness to be a linear function of the patch degree (number of edges). Multi-species anal-243 ysis of metapopulation models also reveals interesting predictions on other aspects of 244 community organization at various spatial scales such as the species-area relationship 245 (Hanski & Gyllenberg 1997), and proved to be useful in conservation ecology with pre-246 dictions of extinctions following habitat destruction (Rybicki & Hanski 2013; Tilman

250

251

252

253

254

255

256

257

259

260

261

263

264

265

266

267

268

269

270

271

#### **Neutral dynamics**

Neutral theory introduces strong competitive interactions by assuming there is a finite number of individuals that could occupy a patch. There are different ways to simulate this zero-sum rule (Bell 2000; Hubbell 2001), but they all result in the same constraint that the increase in abundance of a species could only occur after an equivalent decrease by another species. One important change in the formulation of most neutral models relative the patch dynamics model presented above is therefore that it is individual-based, not population based. We therefore considered in our toy model of neutral dynamics that each local patch holds  $J_x$  individuals. The model tracts the local abundance of all species  $N_{ix}$  in each local patch. At each time step an individid-258 ual dies with probability k. Recruitment only occurs in vacant sites, similarly to a tree by tree replacement process in a closed canopy forest.

The formulation of the recruitment probability is the central piece of all neutral models, making possible the coupling with the metacommunity and neighbouring patches. We adopt a simple formulation based on (Gravel et al. 2006). The approach is conceptually similar to placing a trap in a canopy gap and picking a seed at random among the ones falling in to determine the identity of the recruited species. The composition of the seed pool in that trap will be a mixture of local dispersal and immigrants from the metacommunity. For simplicity, we consider three spatial scales of dispersal but it would be easy to generalize the approach to a continuous seed dispersal kernel (Gravel et al. 2006). The parameter m is the probability that the recruit is a migrant from neighbouring patches, M is the probability it comes from a larger (and fixed) metacommunity, and consequently, by substraction, 1 - m - M is the probability it comes from local dispersal. The fraction  $N_{ix}J_x^{-1}$  is the local relative abundance and

 $P_i x$  is the relative abundance of species i in the seed pool coming from neighbouring patches x. The relative abundance in the neighborhood is weighted by the degree of 274 the connected nodes because some nodes will spread their seeds across a higher num-275 ber of nodes and thus contribute less to the seed pool. We thus consider  $P_{ix} = \frac{\sum P_{iy} d_y^{-1}}{\sum d_v^{-1}}$ . 276 We assume for simplicity (and without loss of generality, (Bell 2000)) that the relative 277 abundance in the metacommunity is uniform, i.-e. equal to  $S^{-1}$ . This immigration 278 prevents the collapse of the metacommunity to a single species, since otherwise all 279 species except one will face extinction by ecological drift (speciation prevents this 280 phenomenon to occur in Hubbell (2001)). The local recruitment probability is conse-281 quently  $Pr_{ix} = MS^{-1} + mP_{ix} + (1 - m - M)N_{ix}J_x^{-1}$ . 282

283

284

285

286

287

288

289

290

291

292

293

294

295

296

297

The model is neutral because it assumes that the probabilities of local recruitment, immigration and mortality events are all equal across species. Demographic stochasticity is the source of variations in abundance, but larger disturbances could be simulated as well, as long as they hit all species with the same probability, independently of their abundance. The fundamental feature of neutral dynamics is therefore the ecological drift, defined as population changes emerging from neutraly stable population dynamics. It can be measured as the variance between replicated time series of community dynamics (Gravel et al. 2011). Hubbell (2001) provides a very comprehensive analysis of the model, with specific attention to the effect of the different parameters on drift (and consequently variance in abundance) and time to extinction. Despite its simplicity, the neutral model is surprisingly rich in the predictions it makes. Bell (2001) and Hubbell (2001) analyzed the performance of neutral models to predict species abundance distributions, the range-abundance relationship, spatial variation in abundance, the species-area relationship, community turnover (betadiversity) and co-occurrence. Recent trophic neutral models were also found to predict realistic ecological network structures (Canard et al. 2012). Other than the ecological equivalence assumption, one of the most criticized aspect of neutral models is the realism of the speciation process and the required speciation rates to sustain species richness (Etienne et al. 2007; Ricklefs 2003). Recent neutral models with more credible speciation models (Desjardins-Proulx & Gravel 2012b; Rosindell et al. 2010) revealed the difficulty to maintain diversity in neutral models over macro-evolutionary time scales. These models nonetheless proposed interesting predictions on endemic species richness and island biogeography (Desjardins-Proulx & Gravel 2012a; Rosindell & Phillimore 2011).

### Species-sorting and mass effect

The species-sorting and the mass effect perspectives build on the notion of species-specific responses to a spatially varying environment (Leibold et al. 2004). There are various ways to simulate such dynamics and we picked the lottery model, in line with tradition (Mouquet & Loreau 2002) and for its proximity to the neutral model described above. Competition for space occurs during recruitment after the death of an adult. The recruitment is a lottery among potential candidates as in the neutral model. The recruitment probability is however biased by species specific responses to local environmental conditions.

The lottery dynamics described above for the neutral model assume there is a very large number of offsprings that are candidate for recruitment but only one will survive and develop to the adult stage. The effect of a differentiation to local environmental conditions could be implemented at this stage with a biased survival probability. The  $J_x$  individuals all experience a unique environmental condition  $E_{nx}$  called a microsite n. We considered a patch average  $\overline{E_x}$ , with a within-patch variance  $\sigma_x$ . The regional average is  $\overline{E_R}$  and the regional variance  $\sigma_R$  (for simplicity we considered normal distributions of environmental conditions, but different distributions will lead to different

regional similarity constraints (Gravel et al. 2006; Mouquet & Loreau 2003; Tilman 2004)). We consider that a fraction  $\lambda_{inx}$  of offsprings reaching the microsite where recruitment occurs will survive. The recruitment probability is therefore biased in favour of the species with highest survival because only some species will be able to cope with the local environmental conditions. We define the relative abundance in the seed rain as  $Z_{ix} = MS^{-1} + mP_{ix} + (1 - m - M)N_{ix}J_x^{-1}$ . The calculation of the relative abun-dance in the seed rain is the same as the neutral model but the recruitment probability differs because only a fraction of offspring survive. It is formulated as  $Pr_{ix} = \frac{\lambda_{inx}Z_{ix}}{\sum \lambda_{jnx}Z_{jx}}$ . The function describing the relationship between a microsite condition and survival could take various forms; we used the traditional gaussian curve describing the niche,  $\lambda_{inx} = \exp{-\frac{(E_{nx}-u_i)^2}{2\Pi b_i^2}}$ , where  $u_i$  is the niche optimum and  $b_i$  is niche breadth. Note that the model will converge to a neutral model when the niche breadth tends to infinity (which is in fact how we simulated neutral dynamics in the Supplementary Material to minimize the complexity of the code). 

Analyses of similar models with a combination of dispersal and species-sorting shown that predictions are extremely variables and depend on the frequency distributions of environmental conditions, niche optimums and breadth. For instance, a well-studied prediction of neutral models is the species abundance distribution. It was shown that niche models can predict similar distributions given appropriate parameters (Gravel et al. 2006; Tilman 2004). The main prediction is nonetheless that stable and predictable (meaning which species will coexist) if species are sufficiently dissimilar, which differs from neutral models. Local species richness will first depend on the joint effects of local heterogeneity and niche breadth because coexistence requires a sufficient dissimilaritya mong species (Schwilk & Ackerly 2005). Local species richness could be increased by a mass effect when dispersal is consistently supplying individuals coming from more favorable locations (refuges). The limiting similarity

required to maintain regional coexistence depends on the amount of dispersal because 350 exchanges among communities homogenizes environmental conditions. This is one of 351 the main result from the species sorting theory and a clever example of local-regional 352 feedbacks: increasing dispersal promotes local coexistence, but on the other hand it 353 diminishes regional coexistence. Only the best average competitors will remain at 354 very high dispersal. We therefore expect a hump-shaped relationship between disper-355 sal and alpha  $(\alpha)$  diversity, with a peak at intermediate dispersal. On the other hand, 356 we expect a monotonic decrease of beta  $(\beta)$  and  $\gamma$  diversity with dispersal (Mouquet 357 & Loreau 2003). This prediction has been validated in some experiments (Logue et al. 358 2011; Venail et al. 2008). 359

#### 50 Results

371

372

In this section we provide simple simulation results to illustrate the impact of saptial 361 contingencies on species distribution and coexistence. We consider four different land-362 scapes, illustrated at Fig. 1. with the outcome of simulations using the neutral model. 363 All of these networks have the same number of nodes (e.g. spatial sampling sites), 364 but both different number of edges (e.g. dispersal routes between sampling sites) and 365 patterns of connectivity between nodes. We ask how these differences in connectivity 366 will shape the emerging properties of the community under the scenarios represented 367 by each metacommunity model. Our analysis is not exhaustive, it is provided sim-368 ply to illustrate the interaction between metacommunity perspectives and landscape 369 structures on  $\alpha$ ,  $\beta$  and  $\gamma$  diversity. 370

 $\alpha$  diversity to facilitate comparison between models. The model parameterization is responsible for differences in both  $\alpha$  and  $\gamma$  diversity, meaning that only the shape of the relationship between centrality and richness ought to be looked at. It appears that both in the geographical and tree graph, the path dynamics model has a much more considerable variation in  $\alpha$  diversity. However, in all cases the  $\alpha$  diversity increases with the node degree centrality, meaning that nodes with more connections also host a more diverse community. Eigen-centrality gave a far less clear-cut result, which can probably be attributed to the fact that our networks are relatively small in size. Eigencentrality reports how well your neighbors are connected, and in graphs with a short diameter (i.e. the two farthest points are not extremely far apart), this measure might hold less information.

Finally, Figs. 3 and 4 present, respectively, the between patch  $\beta$  diversity as a function of the shape of the network, under the three dynamic models. We used Bray-Curtis measure of dissimilarity between patches. In Fig. 3, the distance is expressed as the Euclidean (geographic) distance between two patches. Although this neglects how dispersal connects the different patches, there is already a clear signal of geographic distance on  $\beta$  diversity, indicating the importance of dispersal under the three scenarios. In both the neutral and patch dynamics model, local communities become increasingly dissimilar when the distance between them increases. In other words, two communities which are close to each other will share a large proportion of their species pool, whereas two communities which are afar will share a small proportion. The relationship between distance and dissimilarity is similar for species-sorting. Nonetheless, it forms an enveloppe of points (with most points lying in the upper-left part of the graph). While two distant communities will be dissimilar, there is no telling how dissimilar two close communities will be. Note this relationship for species-sorting varies significantly with the spatial distribution of microsites (not shown). At one extreme,

if all patches hold the same average conditions, then we should expect no relationship 400 between dissimilarity and distance. On the other hand, if the average conditions are 401 highly variable among localities (as in here), then we should expect two communities 402 close to be potentially dissimilar (if conditions are different) or similar (if they are 403 the same). The variance should thus be larger. A distance-dissimilarity relationship 404 arises in the situation where dispersal promotes a mass effect (as in here). Such re-405 sults emphasize the interaction between spatial contingencies (here connectivity and 406 distribution of environmental conditions) and dispersal. 407

To a vast extent, these relationships are preserved when looking at the geodesic distances (Fiig. 4), i.e. along how many edges should one travel to connect two patchs.

Interestingly enough, the distance-dissimilarity relationship for the neutral model is markedly hump-shaped, with sites being at a medium distance having the maximal dissimilarity.

#### Discussion

Our objective in this paper was to review the main assumptions of three metacommu-414 nity models and illustrate how the implementation of more realistic landscapes could 415 reveal the importance of dispersal on community structure. We argued in the intro-416 duction that neutral theory is useful both to understand and predict the impact of 417 dispersal on community organization. The review of the different models shows that 418 the fundamental difference between a neutral model and the patch dynamics model 419 is the effect of competitive interactions on distribution, while the difference between 420 the neutral and the species sorting models is the effect of unequal competitive inter-421 actions. The neutral model is thus a useful tool to understand the joint effects of dis-422 persal and community interactions. Our comparison of the distribution of  $\alpha$  diversity

was particularly meaningful in that respect. The simulation results show that com-424 petitive interactions buffer the potential impact of landscape structure. The strongest 425 centrality-species richness relationship was observed for the patch dynamics, a model 426 without any interactions. On the other hand, strong and unequal competitive inter-427 actions minimized the effect of centrality. Our model analysis greatly illustrates the 428 growing recognition in metacommunity ecology that we must move toward more re-429 alistic landscapes (Gilarranz & Bascompte 2012). For field ecologists, and particularly 430 limnologists, our review emphasizes that we need to go beyond geographic based anal-431 ysis of  $\beta$  diversity (e.g. (Legendre et al. 2005)) to topological based analyses (Peterson 432 et al. 2013). 433

The network approach to the study of spatially explicit landscapes is a major ad-434 vancement in metacommunity ecology. It is a first step to make the concept opera-435 tional because it accounts for more realistic landscape structures and dispersal ker-436 nels. It makes a significant departure to simple island-mainland or global dispersal 437 approaches used previously (e.g. (Hubbell 2001; Mouquet & Loreau 2002; Tilman 438 1994)). But dispersal is also spatially explicit in a lattice model and it does not make 439 the landscape more realistic. We believe the fundamental contribution of this ap-440 proach is the consideration of spatial heterogeneity of dispersal. In agreement with 441 previous theoretical (Desjardins-Proulx & Gravel 2012a; Economo 2011) and exper-442 imemental studies (Carrara et al. 2012), the simulations show that the degree cen-443 trality has a significant impact on  $\alpha$  diversity. Central nodes might also contribute 444 more to maintain  $\gamma$  diversity, as they are essential for species to spread throughout the 445 landscape. The nodes could be potentially quantified as keystone for the metacommu-446 nity (Mouquet et al. 2013). Interestingly, but not surprisingly, this effect is weaker with 447 species sorting dynamics. We could even hypothesize it will vanish in the extreme case 448 of niche differentiation (with low overlap for instance) and low mass effect. In this par-449

ticular case, the neutral versus niche comparison therefore illustrates that very strong unequal competitive interactions could overwhelm the impact of dispersal.

The network approach and the comparison between metacommunity perspectives 452 reveal there could be spatial variation in coexistence mechanisms. If we take the 453 species-sorting perspective for instance, we find that  $\alpha$  diversity is higher in more cen-454 tral nodes. Since the environment is on average the same from one patch to another, 455 it implies that diversity in these communities is maintained by a stronger mass effect. 456 It results in spatial variation in the relative importance of species-sorting, the mass 457 effect and to a certain extent the neutral drift. Because the degree centrality was the 458 best variable explaining diversity, we should expect the degree distribution to strongly 459 impact the relative contribution of these coexistence mechanisms. For a given set of 460 ecological processes and distribution of species traits, we might expect the coexistence 461 mechanisms to differ from one landscape to another. 462

We introduced this article arguing that neutral theory could be used as an instru-463 ment to predict species distribution in spatially heterogeneous landscapes. So far we 464 have treated only theoretical models, but we could also envision to parametrize them 465 and simulate real landscapes. The recruitment probabilities defined above could be 466 used as statistical models (likelihood functions) to fit to empirical data. Prior infor-467 mation could be used to define apriori dispersal kernels and then fit the model as in 468 Gravel et al. (2008). The fit of metapopulation models to spatially explicit landscapes 469 was pioneered by Hanski (1998) and recently extended to species distribution mod-470 els including both species sorting and dispersal limitations (Boulangeat et al. 2012). 471 Given the parametrization, one could run neutral models to generate null hypotheses 472 that could be eventually compared to observed distribution. This would make a sig-473 nificant improvement over traditional null models in ecology (Gotelli & Graves 1996) 474 in which there are no interactions and no dispersal limitations.

The multivariate variance partitioning framework originally proposed by Borcard 476 et al. (1992) and further developed by Borcard & Legendre (2002) has been widely 477 used to quantify the relative importance of species sorting and dispersal limitations in 478 species distribution. This framework was originally proposed to model species dis-479 tribution as a function of environmental variables, taking into account the spatial 480 autocorrelation of species distribution (Borcard et al. 1992; Leduc et al. 1992; Leg-481 endre 1993). This methodology has been widely used over the last decade as a test of 482 the neutral theory, its underlying assumption and a quantification of dispersal limita-483 tions (e.g. Cottenie (2005); Gilbert & Lechowicz (2004); Hardy (2004); Svenning et al. (2004). One problem of this approach is however that it makes a weak test of neu-485 trality (McGill 2003), based on the description of spatial community structure, rather 486 than hypothesis testing. The different models we reviewed in this article could be 487 better employed if used to generate null expectations of species distribution based on 488 different hypotheses and then compare them. But most of all, parametrized spatially 489 explicit neutral models could be more useful if used to predict biodiversity under dif-490 ferent global change scenarios. For instance, neutral models could be used to predict 491 the consequences of habitat destruction, fragmentation or a change in the connectiv-492 ity matrix (Hubbell et al. 2008). The spatially explicit description of the landscape is a 493 major improvement toward that end, providing much flexibility in the scenarios that 494 could be explored. 495

Working with more complex representations on landscapes has several advantages.

Real landscapes are not flat geometric objects, they are highly structured and diverse.

This diverse structure has long been recognized as a key component of diversity. In
the 19th century, Moritz Wagner noted that patterns of rivers Coyne & Orr 2004 could
explain how beetles diversified. Yet, to this day, the relationship between spatial structures and biodiversity is not resolved, but networks provide powerful tools to analyze

landscapes and generate testable predictions on the relationship between community assembly and spatial structures. For example, the neutral theory predict less diversity in isolated communities and constant speciation (regardless of isolation) (Economo & Keitt 2008). Adding the effect of gene flow changes the predictions, but the neutral theory do not predict adaptive radiation and might thus face problems for predicting many long-term ecological processes.

Finally, our analyses emphasize the need to expand on the canonial neutral theory. As pointed out by Wootton (2005), most of the unexplained deviation of empirical community from the prediction of accurately calibrated neutral models can be attributed to non-competitive interactions. Canard et al. (2012) proposed that neutral processes can explain the network structure of trophic interactions with a good accuracy. Incorporating reasonable complexity in the mechanisms addressed by neutral models is not a theoreticians' exercise: it will re-enforce the usefulness of the neutral theory as an operational concept, specifically one that can be used to derive baseline predictions about (i) the expected local species richness, and (ii) the expected species pool dissimilarity at the between-site and regional scales. These predictions are the benchmark against which empirical relevés of species richness and community structure ought to be compared, and coming up with realistic parameters to calibrate these models calls for a closer cooperation and dialogue between theoreticians and empiricists.

# 522 Acknowledgements

DG received financial support from NSERC and Canada Research Chair program. TP is supported by a MELS-FQRNT post-doctoral fellowship and PDP by a NSERC fellowship.

# References

- Appel, M. J. B., Najim, C. A. & Russo, R. P. (2002) *Limit laws for the diameter of a random*point set. Advances in Applied Probability, **34**, 1–10.
- Appel, M. J. B. & Russo, R. P. (1997a) The maximum vertex degree of a graph on uniform points in  $[0,1]^d$ . Advances in Applied Probability, **29**, 567–581.
- Appel, M. J. B. & Russo, R. P. (1997b) The minimum vertex degree of a graph on uniform points in  $[0,1]^d$ . Advances in Applied Probability, **29**, 582–594.
- Appel, M. J. B. & Russo, R. P. (2002) The connectivity of a graph on uniform points in  $[0,1]^d$ . Statistics & Probability Letters, **60**, 351–357.
- Bahn, V. & McGill, B. J. (2007) Can niche-based distribution models outperform spatial interpolation? Global Ecology and Biogeography, **16**, 733–742.
- Bell, G (2000) *The Distribution of Abundance in Neutral Communities*. The American Naturalist, **155**, 606–617.
- <sup>539</sup> Bell, G (2001) Neutral macroecology. Science (New York, N.Y.), **293**, 2413–8.
- Borcard, D. & Legendre, P. (2002) *All-scale spatial analysis of ecological data by means of*principal coordinates of neighbour matrices. Ecological Modelling, **153**, 51–68.
- Borcard, D., Legendre, P. & Drapeau, P. (1992) Partialling out the Spatial Component of
  Ecological Variation. EN. Ecology, 73, 1045.
- Boulangeat, I., Gravel, D. & Thuiller, W. (2012) Accounting for dispersal and biotic interactions to disentangle the drivers of species distributions and their abundances. Ecology Letters, **15**, 584–593.
- Canard, E. et al. (2012) *Emergence of Structural Patterns in Neutral Trophic Networks*.

  PLoS ONE, **7**. Ed. by Ravasi, T., e38295.
- Carrara, F. et al. (2012) Dendritic connectivity controls biodiversity patterns in experimental metacommunities. Proceedings of the National Academy of Sciences of the United States of America, **109**, 5761–6.

- <sup>552</sup> Chave, J. (2004) *Neutral theory and community ecology*. Ecology Letters, 7, 241–253.
- <sup>553</sup> Clark, J. S. (2012) The coherence problem with the Unified Neutral Theory of Biodiversity.
- Trends in Ecology & Evolution, 27, 199–203.
- Cottenie, K. (2005) *Integrating environmental and spatial processes in ecological commu*nity dynamics. Ecology Letters, **8**, 1175–1182.
- <sup>557</sup> Coyne, J. A. & Orr, H. A. (2004) Speciation, Sinauer Associates.
- Dale, M. R. T. & Fortin, M.-J. (2010) *From Graphs to Spatial Graphs*. Annual Review of Ecology, Evolution, and Systematics, **41**, 21–38.
- Desjardins-Proulx, P. & Gravel, D. (2012a) *A complex speciation-richness relationship in a simple neutral model.* Ecology and Evolution, 2, 1781–1790.
- Desjardins-Proulx, P. & Gravel, D. (2012b) *How likely is speciation in neutral ecology?*The American Naturalist, **179**, 137–44.
- Dijkstra, E. W. (1959) *A note on two problems in connexion with graphs*. Numer. Math., 1, 269–271.
- Economo, E. P. & Keitt, T. H. (2010) *Network isolation and local diversity in neutral meta*communities. Oikos, **10**, 1–9.
- Economo, E. P. (2011) *Biodiversity conservation in metacommunity networks: linking pat*tern and persistence. The American Naturalist, **177**, E167–80.
- Economo, E. P. & Keitt, T. H. (2008) *Species diversity in neutral metacommunities: a net-work approach*. Ecology Letters, **11**, 52–62.
- Etienne, R. S. & Rosindell, J. (2011) The spatial limitations of current neutral models of biodiversity. PloS one, 6, e14717.
- Etienne, R.S. et al. (2007) Modes of speciation and the neutral theory of biodiversity.

  Oikos, 116, 241–258.
- Fall, A. et al. (2007) Spatial graphs: principles and applications for habitat connectivity.

  Ecosystems, **10**, 448–461.

- Garroway, C. J. et al. (2008) Applications of graph theory to landscape genetics. Evol.
- Appl., 1, 620–630.
- Gilarranz, L. J. & Bascompte, J. (2012) Spatial network structure and metapopulation per-
- sistence. Journal of theoretical biology, 297, 11–6.
- <sup>582</sup> Gilbert, B. & Lechowicz, M. J. (2004) Neutrality, niches, and dispersal in a temperate forest
- understory. Proceedings of the National Academy of Sciences of the United States
- of America, **101**, 7651–6.
- Gotelli, N. J. & McGill, B. J. (2006) Null Versus Neutral Models: What's The Difference?
- Ecography, 29, 793–800.
- Gotelli, N. J. (2000) Null Model Analysis of Species Co-Occurrence Patterns. Ecology, 81,
- 588 2606.
- Gotelli, N. & Graves, G. (1996) Null models in ecology, Smithsonian Institution Press,
- Washington, D.C.
- <sup>591</sup> Gravel, D., Beaudet, M. & Messier, C. (2008) Partitioning the factors of spatial variation
- in regeneration density of shade-tolerant tree species. Ecology, **89**, 2879–88.
- <sup>593</sup> Gravel, D., Guichard, F. & Hochberg, M. E. (2011) Species coexistence in a variable world.
- Ecology letters, **14**, 828–39.
- <sup>595</sup> Gravel, D. et al. (2006) Reconciling niche and neutrality: the continuum hypothesis. Ecol-
- ogy Letters, **9**, 399–409.
- Gravel, D. et al. (2010) Source and sink dynamics in meta-ecosystems. Ecology, 91, 2172–
- 598 84.
- 599 Gravel, D. et al. (2011) Persistence increases with diversity and connectance in trophic
- *metacommunities*. PloS one, **6**, e19374.
- Gross, J. L. & Yellen, J. (2006) Graph Theory and its Applications. 2nd, Chapman & Hall.
- 602 Hanski, I (1998) Metapopulation dynamics. Nature, **396**, 41–49.

- Hanski, I & Gyllenberg, M (1997) Uniting Two General Patterns in the Distribution of

  Species. Science (New York, N.Y.), 275, 397–400.
- Hardy, O (2004) Spatial pattern analysis of tree species distribution in a tropical rain forest of Cameroon: assessing the role of limited dispersal and niche differentiation. Forest Ecology and Management, **197**, 191–202.
- Holt (1996). Food webs in space: an island biogeographic perspective. *Food webs: contemporary perspectives* (ed. by Polis, G. A. & Winemiller, K. O.), pp. 313–323. Chapman and Hall, London, UK.
- Hubbell, S. (2001) *The Unified Neutral Theory of Biodiversity and Biogeography*, Princeton, NJ.
- Hubbell, S. et al. (2008) *How many tree species are there in the Amazon and how many of*them will go extinct? Proceedings of the National Academy of Sciences, **105**, 11498–
  11504.
- Klausmeier, C. A. (1998) *Models of Habitat Destruction*. The American Naturalist, **152**, 303–310.
- Kobayashi, K. (1994) On the spatial graph. Kodai Mathematical Journal, 17, 511–517.
- Leduc, A. et al. (1992) Study of spatial components of forest cover using partial Mantel tests and path analysis. Journal of Vegetation Science, 3, 69–78.
- Legendre, P. (1993) Spatial autocorrelation: trouble or new paradigm? Ecology, 74, 1659–1673.
- Legendre, P., Borcard, D. & Peres-Neto, P. R. (2005) *Analyzing beta diversity: partitioning*the spatial variation of composition data. EN. Ecological Monographs, **75**, 435–450.
- Leibold, M. & Norberg, J. (2004) *Biodiversity in metacommunities : Plankton as complex adaptive systems ?* Limnology and Oceanography, **49**, 1278–1289.
- Leibold, M. et al. (2004) The metacommunity concept: a framework for multi-scale community ecology. Ecology Letters, 7, 601–613.

- Logue, J. et al. (2011) *Empirical approaches to metacommunities: a review and comparison*with theory. Trends in Ecology & Evolution, **26**, 482–491.
- 631 McGill, B. (2003) Strong and weak tests of macroecological theory. Oikos, 102, 679–685.
- Minor, E. S. & Urban, D. L. (2007) *Graph theory as a proxy for spatially explicit population*models in conservation planning. Ecological Applications, **17**, 1771–1782.
- Minor, E. S. & Urban, D. L. (2008) A graph theory framework for evaluating landscape connectivity and conservation planning. Conservation Biology, 22, 297–307.
- Mouquet, N. & Loreau, M. (2002) Coexistence in Metacommunities: The Regional Similarity Hypothesis. The American Naturalist, **159**, 420–426.
- Mouquet, N. & Loreau, M. (2003) *Community Patterns in Source-Sink Metacommunities*.

  The American Naturalist, **162**, 544–557.
- Mouquet, N. et al. (2013) Extending the concept of keystone species to communities and ecosystems. Ecology Letters, **16**, 1–8.
- Newman, M. (2010) Networks: An Introduction, Oxford University Press.
- Penrose, M. (2003) Random Geometric Graphs, Oxford University Press.
- Peres-Neto, P., Leibold, M. & Dray, S (2012) Assessing the effects of spatial contingency and environmental filtering on metacommunity phylogenetics. Ecology, **93**, 14–30.
- Peterson, E. E. et al. (2013) *Modelling dendritic ecological networks in space: an integrated*network perspective. Ecology letters, **16**, 707–19.
- Ricklefs, R. E. (2003) A comment on Hubbell's zero-sum ecological drift model. Oikos, **100**, 185–192.
- Ricklefs, R. E. & Renner, S. S. (2012) Global correlations in tropical tree species richness and abundance reject neutrality. Science (New York, N.Y.), **335**, 464–7.
- Rosindell, J. & Phillimore, A. B. (2011) *A unified model of island biogeography sheds light*on the zone of radiation. Ecology Letters, **14**, 552–60.

- $_{654}$  Rosindell, J. et al. (2010) Protracted speciation revitalizes the neutral theory of biodiversity.
- 655 Ecology Letters, **13**, 716–27.
- Rosindell, J. et al. (2012) The case for ecological neutral theory. Trends in Ecology &
- Evolution, 27, 204–209.
- Ryabov, A. B. & Blasius, B. (2011) A graphical theory of competition on spatial resource
- *gradients*. Ecology Letters, **14**, 220–8.
- Rybicki, J. & Hanski, I. (2013) Species-area relationships and extinctions caused by habitat
- loss and fragmentation. Ecology Letters, **16**. Ed. by Enquist, B., 27–38.
- 662 Schwilk, D. & Ackerly, D. (2005) Limiting similarity and functional diversity along envi-
- ronmental gradients. Ecology Letters, 272–281.
- Sedgewick, R. (2001) Algorithms in C++ Part 5: Graph Algorithms. 3rd, Addison-Wesley
- Professional.
- 666 Shmueli, G. (2010) To Explain or to Predict? Statistical Science, 25, 289–310.
- 667 Svenning, J.-C. et al. (2004) Ecological determinism in plant community structure across
- *a tropical forest landscape*. EN. Ecology, **85**, 2526–2538.
- Thuiller, W. et al. A road map for integrating eco-evolutionary processes into biodiversity
- 670 *models*. Ecology Letters,
- Tilman, D. (1994) Competition and Biodiversity in Spatially Structured Habitats. Ecology,
- **75,** 2–16.
- Tilman, D. (2004) Niche tradeoffs, neutrality, and community structure: a stochastic the-
- ory of resource competition, invasion, and community assembly. Proceedings of the
- National Academy of Sciences of the United States of America, **101**, 10854–61.
- Tilman, D. et al. (1994) *Habitat destruction and the extinction debt*. Nature, **371**, 65–66.
- Urban, D. L. et al. (2009) *Graph models of habitat mosaics*. Ecology Letters, 12, 260–273.
- Venail, P., MacLean, R. & Bouvier, T (2008) Diversity and productivity peak at interme-
- diate dispersal rate in evolving metacommunities. Nature, 452, 2010–2014.

- Wennekes, P. L., Rosindell, J. & Etienne, R. S. (2012) The Neutral -Niche Debate: A philosophical perspective. Acta Biotheoretica, 60, 257–271.
- Wootton, J. T. (2005) Field parameterization and experimental test of the neutral theory of biodiversity. Nature, **433**, 309–312.
- Wright, S. (1921) *Correlation and causation*. Journal of Agricultural Research, **20**, 557–585.

# **Figure legends**

## 687 Figure 1

Illustration of the four simulated landscapes. The color code represents the  $\alpha$  diversity simulated with a neutral model, ranked from the poorest (red) to the richest (blue). Parameters: N=25, r=0.3, S=100, m=0.2, M=0.01, k=0.1,  $J_x=100$ . Simulations run 1000 time steps.

### 692 Figure 2

Relationship between  $\alpha$  diversity and node centrality. The upper two panels are simulation results conducted with the random geometric graph illustrated at Fig. 1 and the lower two panels are runs with the random tree graph. Parameters:S = 100, c = 0.4, e = 0.1,  $J_x = 100$ , m = 0.2, M = 0.01, k = 0.1,  $u \in [0,100]$ , b = 15,  $E_x \in [0,100]$ ,  $\overline{E_R} = 50$ ,  $\sigma E_R = 5$ . Simulations run 1000 time steps

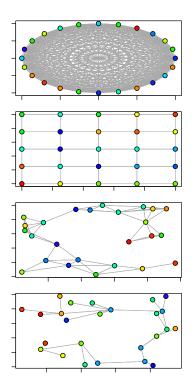
### 698 Figure 3

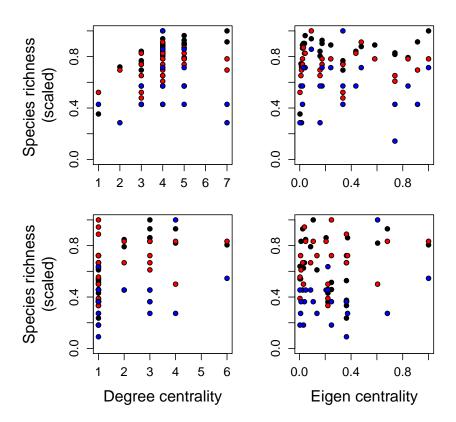
Bray curtis dissimilarity as a function of Euclidean distance. Parameters as in Fig.

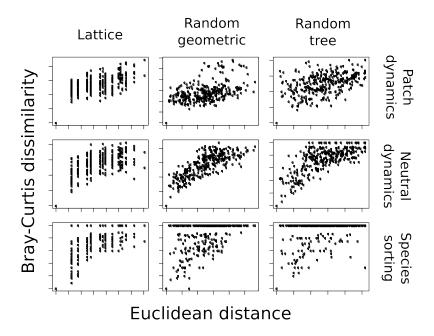
2.

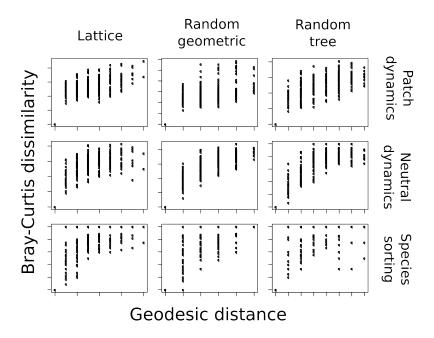
## 701 Figure 4

Bray curtis dissimilarity as a function of geodesic distance. Parameters as in Fig. 2.









Concept	Definition		
Path	A sequence of edges forming a sequence of		
1 4411	nodes		
Connection	Two nodes are connected if there is a path		
	between them		
Euclidean distance	Geographical distance between two nodes		
Geodesic distance	Length of the shortest path between two nodes		
Network-level metrics			
Order	Total number of nodes		
Size	Total number of edges		
Connectivity	A measure of robustness: the minimum		
	number of elements to remove to isolate		
	the nodes		
Components	The number of connected subsets		
Node-level metrics			
Degree	The number of edges of a node		
Closeness centrality	Average geodesic distance between a node		
	and all other vertex		
Eigenvector centrality	A measure of centrality based on the con-		
	cept that connection to highly connected		
	nodes are more important		
Betweenness centrality	The number of shortest paths from all		
	nodes to all others that pass through that		
	note		

Table 1: Main descriptors of spatial networks used in this study.

	Definition	Patch dynamics	Neutral	Species-sorting
Variables				
p	Occupancy	X		
N	Local population size		X	X
Z	Local rel. abund.		X	X
P	Rel. abund. in the neighborhood		X	X
S	Local species richness	X	X	X
d	Node degree	X	X	X
C	Prob. of a colonization event	X		
I	Prob. of a colonization event	X		
Pr	Recruitment prob.		X	X
$\lambda$	Survival prob.			X
Indices				
<i>x</i> , <i>y</i>	Node location	X	X	X
i, j	Species	X	X	X
n	Microsite			X
<b>Parameters</b>				
S	Size of regional species pool	X	X	X
С	Colonization prob.	X		
e	Extinction prob.	X		
J	Local carrying capacity		X	X
m	immigration prob. from neigh.		X	X
M	immigration prob. from metaco.		X	X
k	Death prob.		X	X
и	Niche optimum			X
b	Niche breadth			X
E	Microsite env. conditions			X
$\overline{E}$	Local env. average			X
σ	Local env. variance			X
$\overline{E_R}$	Regioal env. average			X
$\sigma_R$	Regional env. variance			X

Table 2: List of variables, indices and parameters from the three models