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A Parametric Framework to Generate Visual Illusions using Python

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Abstract

Visual illusions are fascinating phenomena that have been used and studied by artists and 13 scientists for centuries, leading to important discoveries about the neurocognitive 14 underpinnings of perception, consciousness, and neuropsychiatric disorders such as 15 schizophrenia or autism. Surprisingly, despite their historical and theoretical importance 16 as psychological stimuli, there is no dedicated software, nor consistent approach, to 17 generate illusions in a systemic fashion. Instead, scientists have to craft them by hand in 18 an idiosyncratic fashion, or use pre-made images not tailored for the specific needs of their 19 studies. This, in turn, hinders the reproducibility of illusion-based research, narrowing possibilities for scientific breakthroughs and their applications. With the aim of addressing 21 this gap, *Pyllusion* is a Python-based open-source software (freely available at https://github.com/RealityBending/Pyllusion), that offers a framework to manipulate and generate illusions in a systematic way, compatible with different output formats such as 24 image files (.png, .jpg, .tiff, etc.) or experimental software stimuli (such as PsychoPy). 25 Keywords: Pyllusion, Visual Illusions, Optical Illusions, Schizophrenia, Python, 26 PsychoPy 27

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Visual illusions have been observed for hundreds of years (Luckiesh, 1965), many of which were described in print by Helmholtz (1856) in 1856 (Helmholtz, 1856). In general terms, 31 a visual illusion can be thought of as the inaccurate perception of a visual stimulus or a 32 given attribute, be it geometrical (size, shape, or angle), or another property such as colour 33 (Adelson, 2000; Delboeuf, 1893; Ebbinghaus, 1902; Howe & Purves, 2005; Muller-Lyer, 1896; Roberts, Harris, & Yates, 2005). Often, an illusory perception resists 'correction' in 35 perception even after an observer has been made aware of the misperception. Novel examples 36 of illusions are still observed and have even cropped up on social media platforms, a famous 37 example being 'The Dress Illusion' (see Fig. 1) as discussed by Schlaffke et al. (2015). 38 See Ninio (2014), Luckiesh (1965), and Robinson (1972) for extensive collections of visual 39 illusions.



Figure 1. The internet-famous 'Dress illusion' image (on the left), which some people perceive as white and yellow vs. black and blue. It is thought to illustrate how perceptual priors (i.e., expectations regarding the lighting conditions) can bias our conscious representation of an object (see visual explanation - from Wikipedia - on the right).

Entertainment value aside, illusions can serve a more practical utility. Visual illusions have helped scientists understand the architecture of the eye and its relationship with processes and structures involved further up stream in the brain, the dynamic interaction of these processes, and visual coding in the brain in general (Carbon, 2014; Clifford, 2002; Forte & Clifford, 2005). Illusions such as the blind-spot or those associated with colour perception, orientation perception, and motion perception, have all been informative of neuronal activity/processes both at the level of the eye and the brain via the measurement of associated illusions (Curran, Clifford, & Benton, 2009; Durgin, Tripathy, & Levi, 1995; Holland, 1965; MacKay, 1957; Webster, 1996; Witkin & Asch, 1948). Visual illusions, and perceptual illusions more generally, are a powerful tool in human perception and brain research, which in turn can inform artificial cognitive systems design considerations (Boyce, Lindsay, Zgonnikov, Rano, & Wong-Lin, 2020; Carbon, 2014).

The use of visual illusions to demonstrate contextual influences on visual perception (Chen, 53 Chen, Gao, Yang, & Yan, 2015; Corbett & Enns, 2006; Roberts, Harris, & Yates, 2005) has underlined its potential relevance in clinical contexts, for instance as markers or tools to investigate typical integration processes in schizophrenia (Clifford, 2014; Palmer, Caruana, Clifford, & Seymour, 2018; Thakkar et al., 2020). Indeed, several studies have demonstrated a diminished susceptibility to visual illusions amongst patients with schizophrenia relative to healthy controls (King, Hodgekins, Chouinard, Chouinard, & Sperandio, 2017; Notredame, Pins, Deneve, & Jardri, 2014). People with schizotypal personality traits perform significantly better at making accurate judgements of contrasts under contextual suppression (Dakin, Carlin, & Hemsley, 2005), are less prone to the perception of illusory motion (Crawford et al., 2010), and are less susceptible to visual size illusions (Uhlhaas, Silverstein, Phillips, & Lovell, 2004). Researchers often contrast this evidence of preserved perceptual performance against a backdrop of poor cognitive abilities (i.e., working memory, object naming, concentration; Liddle, 1987) amongst schizophrenics, contending that the disorder is characterized by a specific processing abnormality rather than a generalized cognitive

impairment (Dakin, Carlin, & Hemsley, 2005; Tibber et al., 2013). As different illusions could tap on distinct neurocognitive processes, researchers have also been able to further 69 characterize specific perceptual anomalies that occur in schizophrenia. For example, while 70 schizophrenic patients show a heightened resistance to contrast illusions, they are indistin-71 guishable from healthy controls in judging brightness illusions (Tibber et al., 2013), arguing against a broad deficit in low-level perceptual integration since not all illusions are affected. Other studies emphasize the role of high-level perceptual deficits in schizophrenia (e.g., problems in contextual processing that manifest as greater resistance to the Ebbinghaus illusion; Massaro & Anderson, 1971; Uhlhaas, Phillips, Schenkel, & Silverstein, 2006), but the lack of consistency in the tasks' methodologies has posed a significant challenge to advancing our theoretical understanding of schizophrenia (King, Hodgekins, Chouinard, Chouinard, 78 & Sperandio, 2017). Specifically, the finding of an increased perceptual accuracy towards high-level illusions has failed to replicate in several other studies (e.g., Parnas et al., 2001; Spencer & Ghorashi, 2014; Yang et al., 2013), and other kinds of illusions (e.g., the Poggendorff illusion) have simply not been sufficiently tested (Kantrowitz, Butler, Schecter, Silipo, & Javitt, 2009).

Individuals with autistic spectrum disorder (ASD) is another clinical group that demonstrates a similar immunity to perceptual biases, supporting the existence of difficulties in global processing and, conversely, an enhanced preference for idiosyncratic and detailed information (F. G. Happe, 1996). Hence, individuals with ASD appear as protected against the contextual influences of illusions in biasing perception, allowing them to perceive elements accurately in a local fashion (Gori, Molteni, & Facoetti, 2016; referred to as a 'weak central coherence'; Mitchell, Mottron, Soulieres, & Ropar, 2010; Walter, Dassonville, & Bochsler, 2009). Some work has also been successful in delineating the underlying cognitive mechanisms employed by different illusions, revealing that autistic traits in a typical population were related to greater resistance to the Müller-Lyer illusion, but not the Ebbinghaus or Ponzo illusions (Chouinard, Noulty, Sperandio, & Landry, 2013). However, findings of

on schizophrenia, even when the same illusion tasks are used (Hoy, Hatton, & Hare, 2004; Ropar & Mitchell, 1999). These mixed findings are attributed not only to the heterogenous nature of ASD as a clinical population, but also to the large variability in experimental instructions (e.g., asking whether lines "looked the same length" vs. "were the same length," see F. Happe and Frith (2006)) and the subsequent understanding of the task requirements (Chouinard, Noulty, Sperandio, & Landry, 2013).

In summary, these studies suggest that illusions, rather than being mere perceptual arti-102 facts, engage specific neurocognitive processes involved in important higher order functions 103 and neuropsychiatric disorders. A common approach to explain illusory phenomena is us-104 ing the Predictive Coding framework (Friston & Kiebel, 2009), which posits that illusory 105 perception typically arises because of a strong systematic bias for prior beliefs (top-down 106 influence) that are mismatched with actual sensory evidence, causing the generation of an 107 objectively wrong but more plausible percept (i.e., two objectively equivalent-sized circles 108 being interpreted as different sizes because of their surrounding context) (Notredame, Pins, 109 Deneve, & Jardri, 2014). In the case of schizophrenia and also in other states of psychosis, 110 a greater resistance to visual illusions is then interpreted as a product of reduced adaptive top-down influence (Koethe et al., 2009; Schneider et al., 2002) and an over-reliance on 112 sensory evidence (bottom-up processes) in making perceptual judgements (Dima, Dietrich, 113 Dillo, & Emrich, 2010). While evidence from visual illusions research has garnered substan-114 tial support for the predictive coding account, helping to underscore the neurocomputational 115 mechanisms that are fundamental to psychiatric and psychological disorders (Sterzer et al., 116 2018), there are contradictory findings that fail to be integrated within this approach. The 117 lack of consistency and replicability in experimental designs using illusions-based stimuli 118 appear to be one of the main reasons for slowing the progress in the field. 119

Despite the relevance of visual illusions in psychology and neuroscience, the field of illusion research lacks a dedicated software to generate and report the stimuli, in order for them to be

reproduced and re-used by other researchers and studies. As several reviews have highlighted 122 (e.g., Gori, Molteni, & Facoetti, 2016), the lack of a validated paradigm and the improper 123 measurement of visual illusion sensitivity (especially amongst individuals with communica-124 tion problems) may be preventing progress in understanding the distinct mechanisms that 125 underlie psychopathology and other fields alike. This is particularly problematic in the con-126 text of the replicability and reproducibility issues recently outlined in psychological science 127 (Maizey & Tzavella, 2019; Milkowski, Hensel, & Hohol, 2018; Nosek, Cohoon, Kidwell, & 128 Spies, 2015; Topalidou, Leblois, Boraud, & Rougier, 2015). Our software, Pyllusion, aims 129 at addressing this gap by proposing and implementing a parametric framework for illusions 130 generation. 131

A Parametric Framework for Illusion Research

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The core idea of the "parametric" approach proposed here and implemented in *Pyllusion* is 133 to dissociate the parameters of an illusion from its rendered output. For instance, the Ponzo 134 illusion (see Fig. 2) can be described in terms of properties of the "distractor" lines (which 135 create the illusion), such as the angle (related to the illusion strength), the color, width, etc. 136 and properties of the "target" lines (which are affected by the illusion), such as the size of the 137 smallest line, the objective difference of the ratio of their lengths, or their color, width, etc. 138 This set of parameters can then be rendered in different formats with further format-specific 139 characteristics (in the case of images, the image size, ratio, resolution, compression, etc.). 140 This essentially allows researchers to describe, manipulate, process and share their stimuli in 141 a concise yet consistent way. For instance, researchers could report a "linear modulation of the illusion strength between -15 and 15, resulting in a reduced reaction time of...", providing 143 details about the remaining parameters, as well as the Python code used to fully reproduce their stimuli.

Moreover, this parametric approach is scalable and works well with different kinds of illusions,

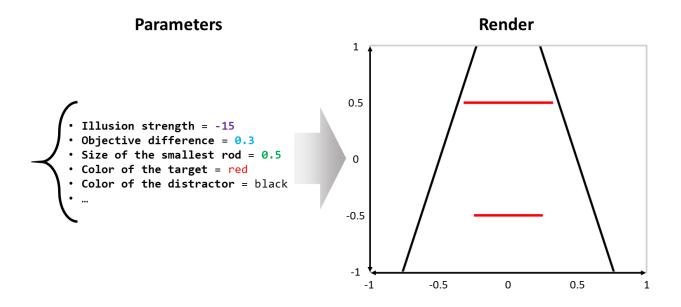


Figure 2. The parametric framework for illusions originally implemented in *Pyllusion* aims at dissociating the *parametric* representation of an illusion (on the left) from its *rendered* representation, in this case as an image of the Ponzo illusion (on the right). In technical terms, an illusion strength of -15 represents a 15 degree tilt of the vertical lines (black distractor lines); an objective difference of 0.3 represents a 30% length difference of the upper and lower horizontal lines (red target lines) where the *size* of the shorter horizontal line is 0.5.

as demonstrated in the software. Indeed, many visual illusions (especially the classical one)
appears to have relatively similar parameters (such as a feature - like the angle or the size
of some shapes - related to the strength of the illusion, or the color of the "target" objects),
which in turn allows for a consistent programming interface (API).

Interestingly, in most of the visual illusions, the strength of the illusion can be dissociated from the actual "difference" (which is impacted by the illusion). For instance, in the Müller-Lyer illusion (see **Fig. 2**), the difference between the two horizontal segments can be modulated orthogonally from the angle of the "distractors" arrows. Allowing researchers to easily manipulate these parameters opens the door for potentially interesting paradigms and experiments. In the following section, we will describe with concrete examples how we

operationalized such a parametric approach in the *Pyllusion* software.

158 Pyllusion

It is not the first time that Python, illusions and cognitive science are brought together.

In his book, "Programming visual illusions for everyone", Bertamini (2017) describes how

to use PsychoPy to generate famous illusions. That said, although being a fantastic tool

and resource for researchers and anybody interested in illusions, it is presented as a fun

introduction to programming and to Python, rather than a dedicated software for illusions

per se.

Pyllusion is an open-source package to programmatically generate illusions written in Python 165 3 (Van Rossum & Drake, 2009), which means that its users benefit from a large number of 166 learning resources and a vibrant community. However, although being a programming-167 based tool, users not familiar with Python or other languages can easily use it as well, as it 168 requires minimal programming skills (one can essentially copy the few necessary lines from 169 the documentation and tweak the explicitly-named parameters). This makes it a very flexible 170 tool; advanced users can incorporate Pyllusion in their scripts or experiments (for instance, 171 to generate illusions "on the fly" based on the input of the user), whereas novice users can 172 simply copy the minimal code to pre-generate and save the illusions as images. 173

The source code is available under the MIT license on GitHub (https://github.com/RealityBending/
Pyllusion/). Its documentation (https://realitybending.github.io/Pyllusion/) is automatically built and rendered from the code and includes guides for installation, a description of
the package's functions, as well as examples of use. Finally, the issue tracker on GitHub
offers a convenient and public forum that allows users to report bugs, get help and gain
insight into the development of the package. Additionally, the repository leverages a comprehensive test suite (using pytest) and continuous integration (using Travis-CI and GitHub
actions) to ensure software stability and quality. The test coverage and build status can

transparently be tracked via the GitHub repository. Thanks to its collaborative and open development, *Pyllusion* can continuously evolve, adapt, and integrate new functionalities to meet the needs of the community.

Pyllusion is available on PyPI, the main repository of software for Python and can thus be installed by running the command pip install Pyllusion. Once the software is installed, it must be loaded in Python scripts with import pyllusion. Once the package is loaded, two steps are further required to generate the illusions, 1) specifying the parameters and 2) rendering the output accordingly.

We will use the Delboeuf illusion in the hands-on example shown below. However, the same workflow applies to other the other illusions supported by *Pyllusion*, including the Ebbinghaus illusion, the Müller-Lyer illusion, the Ponzo illusion, the Zöllner illusion, the Rod and Frame illusion, the Poggendorff illusion and more (see **Fig. 3**, as well as the full list with examples on the **readme**.

195 Step 1: Parameters

The parameters for each illusion can be generated using the IllusionName_parameters()
function. Many optional arguments are available for modifying, of which the description
and default values can be find in the API documentation (https://realitybending.github.
io/Pyllusion/functions.html). In the example below, we specify the illusion_strength
argument, and the function will compute all of the remaining parameters accordingly.

```
# Load package
import pyllusion as ill

# Create parameters
parameters = ill.(illusion_strength=2)
```

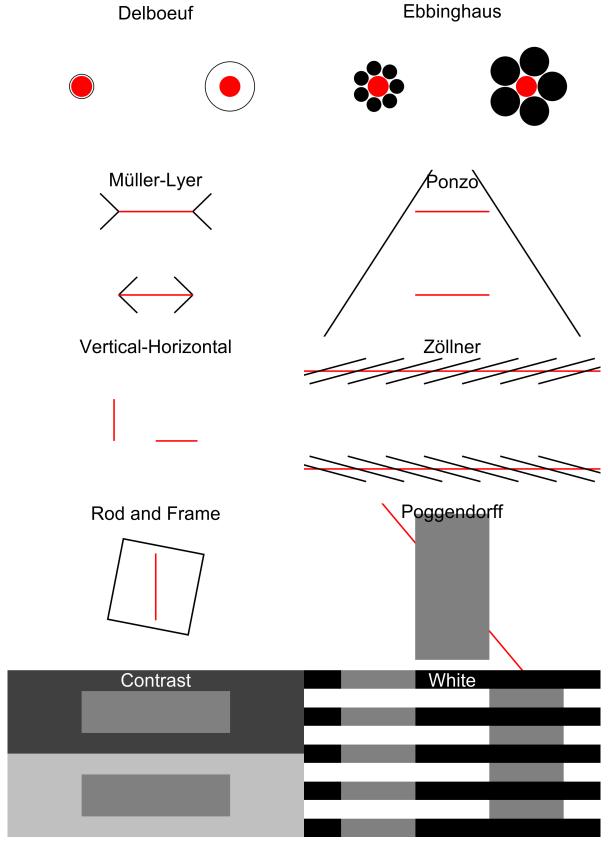


Figure 3. Different historical visual illusions currently supported by *Pyllusion*. These can all be generated using the parametric approach described in this paper, allowing for fully reproducible studies.

```
# Visualize parameters
print(parameters)
```

```
{'Difference': 0,
    'Size_Inner_Left': 0.25,
    'Size_Inner_Right': 0.25,
    'Size_Inner_Difference': 0.0,
    'Illusion_Strength': 2,u
    'Size_Outer_Left': 0.3,
    'Size_Outer_Right': 0.52,
    'Distance_Centers': 1,
    'Distance_Edges_Outer': 0.59,
    'Position_Left': -0.5,
    'Position_Right': 0.5,
    ...}
```

As one can see, the output of this function is a basic Python dictionary (as denoted by the 201 curly brackets), which makes it easy to further process, modify, share, store or investigate. 202 This "container" object stores the values for a large number of parameters, such as the size of 203 each (inner and outer) circles, the distance between the centers and edges of the circles, their position, etc.), and is passed to a "rendering" function which converts this set of parameters into the final output. Note the two main parameters, illusion strength, and difference, have fairly generic names. For instance, in the Ponzo illusion, a less abstract names for these arguments could have been difference_size_outer_circles and difference_size_inner_circles). Indeed, the meaning of these parameters depends on the nature of the illusion. For instance, 210 while illusion strength currently refers to the the area of the outer circles in the Delboeuf 211 illusion, it refers to the angle of the non-horizontal lines in the Ponzo illusion. 212

Conceptually, this term represents the strength of the surrounding context in achieving a 213 biased illusory perception of the relative target features (see Fig. 3). The decision of unifying 214 the "illusion strength" parameter under the same name was further motivated by the aim of 215 having a consistent naming scheme for the API. This means that users can experiment with 216 new illusions by modulating the illusion strength, without the need of learning what is the 217 actual physical parameter (e.g., "angle of the distractor lines") driving the illusion. 218

Step 2: Rendering 219

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This dictionary, containing the parameters of the illusion, can then be passed to a "rendering" function, which actually draws (or displays) the illusion according to the specifications. 221 Render-specific arguments are available at this stage, such as the dimensions of the image. 222 Two output-engines are currently supported, images (in any format thanks to the PIL Python 223 library for image processing; Clark, 2015), or as PsychoPy stimuli (Peirce, 2007), one of the 224 most popular psychological experiments software. 225

Each function is illusion-specific and hence, uniform function names (in the form

IllusionName FunctionGoal()) are used in the process of creating the illusion. Parame-227 ters are computed using * parameters() (the asterisk representing the illusion name), and 228 images can be generated via *_image() (or similarly, *_psychopy(), as we will see later). 229 The following Python code shows the full and reproducible code to generate a PNG image 230 with a Delboeuf illusion. However, note that the parameters generation and the rendering have been dissociated for didactic reasons. In practice, the arguments related to the parame-232 ters of the illusion can be passed directly to the rendering function, which will automatically 233 compute the parameters if no dictionary is passed. Similarly, the saving step can be done 234 directly by adding .save() at the end of the the *_image() function, which reduces the 235 amount of Python lines to one.

```
# Load package
import pyllusion as ill

# Create parameters

parameters = ill.delboeuf_parameters(illusion_strength=1, difference=2)

# Generate image from parameters
image = ill.delboeuf_image(parameters, height=600, width=800)

# Save it
image.save("my_illusion.png")
```

Images can be easily post-processed using the PIL library. For instance, with just a few lines, one can loop through different combinations of parameters, generate illusions, add text on them, and collate together in a mosaic, as can be seen in **Fig. 4**.

PsychoPy. As illusions are heavily used in experimental psychology, we designed *Pyllusion* so that it is directly usable within *PsychoPy* (Peirce, 2007) experiments. *PsychoPy* is an open-source, free and Python-based package for experiments creation, recognized for its timing accuracy (Bridges, Pitiot, MacAskill, & Peirce, 2020) and its GUI (the "builder"), thereby allowing users who are not familiar with code to easily build experiments.

The *PsychoPy* "builder" interface allows for code components to be flexibly added, which
makes it convenient to insert the few lines necessary for displaying illusions. However, using
the programming interface of *PsychoPy* (which underlies the graphical interface) reveals how
seamless the integration with *Pyllusion* can be. The following code is a minimal example
demonstrating how to use a Delboeuf illusion within a *PsychoPy* workflow. Running it opens
a new window, displays the illusion in it, and then closes it once an input (a key press) is
detected.

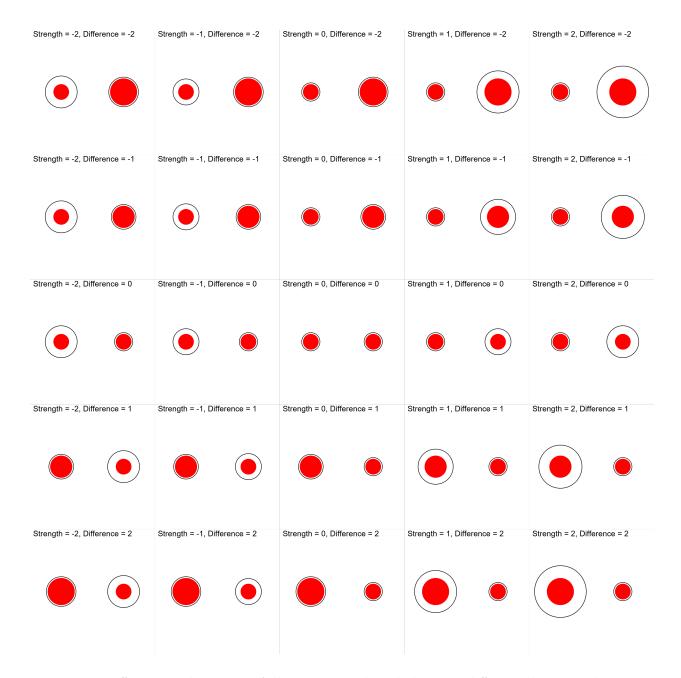


Figure 4. Different combinations of illusion strength and objective difference between the two target stimuli (the area of the red circles) for the Delboeuf illusion. The vertical central column shows different magnitudes of difference in both directions with no illusion, whereas the horizontal central row shows different magnitudes of illusion strength when the targets are of identical sizes. By using negative or positive values for the illusion strength, one can generate congruent or incongruent illusions (that reinforce or attenuate the actual difference respectively).

```
# Load packages
import pyllusion as ill
from psychopy import visual, event

# Create parameters
parameters = ill.delboeuf_parameters(illusion_strength=1, difference=2)

# Initiate Window
window = visual.Window(size=[800, 600], winType='pygame', color='white')

# Display illusion
ill.delboeuf_psychopy(window=window, parameters=parameters)

# Refresh and close window
window.flip()
event.waitKeys() # Press any key to close
window.close()
```

This native integration with PsychoPy could appear as somewhat redundant and unneces-252 sary, as one could pre-generate all the illusions as images, and simply load them in PsychoPy 253 as images, instead of generating them from scratches using PsychoPy's drawing functionali-254 ties. However, this direct integration in experiment building software has multiple benefits, such as avoiding the storage of heavy images (resulting in lighter experiments that can be uploaded and stored online), avoiding issues of image scaling and resolution on different 257 screens, and allowing "on-the-fly" generation of stimuli, which opens the doors for novel 258 adaptive paradigms where the modulation of illusions crucially depends on the participant's 259 input. 260

Future Plans and Developments

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Being an open-source software, *Pyllusion* will continue to grow and evolve based on the community's input. While the direction and state of the package in the long term can be hard to predict, several short term goals can be mentioned.

The initial release of *Pyllusion* focuses on a set of classical, well-described, visual illusions, 265 as they are the most commonly used (for historical reasons mainly, as well as for their 266 relative simplicity). That said, the number of existing illusions is virtually infinite (and 267 great advances are made to generate new ones using machine learning; Watanabe, Kitaoka, 268 Sakamoto, Yasugi, & Tanaka, 2018). Thus, new illusions, as well as new illusion types (e.g., 269 movement-based using GIF or video formats, or auditory illusions using sounds and music) 270 could be added in the future. Due to the open and collaborative nature of the software, these 271 evolutions will be driven by the needs of the community, ensuring that Pyllusion remains cutting-edge, adaptable and useful to address future issues.

Adding new illusions refers mostly to implementing an algorithm to conceptualise and essentialize them as sets of parameters, which is by design independent from their rendering.

However, more rendering engines could be added down the road. For instance, one of the first milestones could take the form of an integration with other Python-based experiment building software, such as *OpenSesame* (Mathot, Schreij, & Theeuwes, 2012) or *Neuropsydia* (Makowski & Dutriaux, 2017). Additionally, a conversion to other languages could also be an interesting feature, especially *JavaScript*, as this would allow a closer integration with web browser apps (and online experiments software, such as *jsPsych*; Leeuw & Motz, 2016; or *lab.js*; Henninger, Shevchenko, Mertens, Kieslich, & Hilbig, 2020).

Finally, we look forward to the creation of studies that would investigate how, for each illusion, the modulation of the parameters affect behaviour and the conscious perception of neural processing. This would in turn allow for a better understanding of the commonalities and differences between these fascinating stimuli. As such, we hope that our tool contributes

to the development of a strong axis that will unite the community working with illusions to push the field forward.

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291 References

Adelson, E. H. (2000). Lightness perception and lightness illusions. In M. Gazzaniga (Ed.), *The new cognitive neurosciences* (2nd ed., pp. 339–351). MIT Press:

Cambridge MA.

- Bertamini, M. (2017). Programming visual illusions for everyone (Vol. 2). Springer.
- Boyce, W. P., Lindsay, A., Zgonnikov, A., Rano, I., & Wong-Lin, K. (2020). Optimality and limitations of audio-visual integration for cognitive systems. Frontiers

 in Robotics and AI, 7, 94.
- Bridges, D., Pitiot, A., MacAskill, M. R., & Peirce, J. W. (2020). The timing megastudy: Comparing a range of experiment generators, both lab-based and online. PeerJ, 8, e9414.
- Carbon, C.-C. (2014). Understanding human perception by human-made illusions.

 Frontiers in Human Neuroscience, 8, 566.
- Chen, C., Chen, X., Gao, M., Yang, Q., & Yan, H. (2015). Contextual influence on the tilt after-effect in foveal and para-foveal vision. *Neuroscience Bulletin*, 31(3), 307–316.
- Chouinard, P. A., Noulty, W. A., Sperandio, I., & Landry, O. (2013). Global processing during the muller-lyer illusion is distinctively affected by the degree of autistic
 traits in the typical population. Experimental Brain Research, 230(2), 219–231.
- Clark, A. (2015). Pillow (PIL fork) documentation. readthedocs. Retrieved from https://buildmedia.readthedocs.org/media/pdf/pillow/latest/pillow.pdf
- Clifford, C. W. (2002). Perceptual adaptation: Motion parallels orientation. *Trends*in Cognitive Sciences, 6(3), 136–143.
- Clifford, C. W. (2014). The tilt illusion: Phenomenology and functional implications.

 Vision Research, 104, 3–11.

Corbett, J. E., & Enns, J. T. (2006). Observer pitch and roll influence: The rod and frame illusion. *Psychonomic Bulletin & Review*, 13(1), 160–165.

- Crawford, T., Hamm, J., Kean, M., Schmechtig, A., Kumari, V., Anilkumar, A., & Ettinger, U. (2010). The perception of real and illusory motion in schizophrenia.

 Neuropsychologia, 48(10), 3121–3127.
- Curran, W., Clifford, C. W., & Benton, C. P. (2009). The hierarchy of directional interactions in visual motion processing. *Proceedings of the Royal Society B:*Biological Sciences, 276(1655), 263–268.
- Dakin, S., Carlin, P., & Hemsley, D. (2005). Weak suppression of visual context in chronic schizophrenia. *Current Biology*, 15(20), R822–R824.
- Delboeuf, J. (1893). Sur une nouvelle illusion d'optique.
- Dima, D., Dietrich, D. E., Dillo, W., & Emrich, H. M. (2010). Impaired top-down processes in schizophrenia: A DCM study of ERPs. *NeuroImage*, 52(3), 824–832.
- Durgin, F. H., Tripathy, S. P., & Levi, D. M. (1995). On the filling in of the visual blind spot: Some rules of thumb. *Perception*, 24(7), 827–840.
- Ebbinghaus, H. (1902). Grundzuge der psychologie (Vol. I and II). Verlag von Veit & Comp.
- Forte, J. D., & Clifford, C. W. (2005). Inter-ocular transfer of the tilt illusion shows
 that monocular orientation mechanisms are colour selective. *Vision Research*,

 45(20), 2715–2721.
- Friston, K., & Kiebel, S. (2009). Predictive coding under the free-energy principle.

 Philosophical Transactions of the Royal Society B: Biological Sciences, 364(1521),

 1211–1221.
- Gori, S., Molteni, M., & Facoetti, A. (2016). Visual illusions: An interesting tool to investigate developmental dyslexia and autism spectrum disorder. Frontiers in

- 341 Human Neuroscience, 10, 175.
- Happe, F., & Frith, U. (2006). The weak coherence account: Detail-focused cognitive style in autism spectrum disorders. *Journal of Autism and Developmental Disor*ders, 36(1), 5–25.
- Happe, F. G. (1996). Studying weak central coherence at low levels: Children with
 autism do not succumb to visual illusions. A research note. *Journal of Child*Psychology and Psychiatry, 37(7), 873–877.
- Helmholtz, H. von. (1856). Handbuch der physiologischen optik (2 vols.[vol. 1, 1856; vol. 2, 1867]). Leipzig Germany: L. Voss.
- Henninger, F., Shevchenko, Y., Mertens, U., Kieslich, P. J., & Hilbig, B. E. (2020).

 Lab.js: A free, open, online experiment builder (Version v20.1.1). Zenodo. https:

 //doi.org/10.5281/zenodo.3953072
- Holland, H. C. (1965). Holland 1965 international series of monographs in experimental psychology: II. The spiral after effect. London, Pergamon Press.
- Howe, C. Q., & Purves, D. (2005). The muller-lyer illusion explained by the statistics of image—source relationships. *Proceedings of the National Academy of Sciences*, 102(4), 1234–1239.
- Hoy, J. A., Hatton, C., & Hare, D. (2004). Weak central coherence: A cross-domain phenomenon specific to autism? *Autism*, 8(3), 267–281.
- Kantrowitz, J. T., Butler, P. D., Schecter, I., Silipo, G., & Javitt, D. C. (2009).

 Seeing the world dimly: The impact of early visual deficits on visual experience
 in schizophrenia. *Schizophrenia Bulletin*, 35(6), 1085–1094.
- King, D. J., Hodgekins, J., Chouinard, P. A., Chouinard, V.-A., & Sperandio, I.

 (2017). A review of abnormalities in the perception of visual illusions in schizophrenia. *Psychonomic Bulletin & Review*, 24(3), 734–751.

Koethe, D., Kranaster, L., Hoyer, C., Gross, S., Neatby, M. A., Schultze-Lutter, F.,

Leweke, F. M. (2009). Binocular depth inversion as a paradigm of reduced

visual information processing in prodromal state, antipsychotic-naive and treated

schizophrenia. European Archives of Psychiatry and Clinical Neuroscience, 259(4),

195–202.

- Leeuw, J. R. de, & Motz, B. A. (2016). Psychophysics in a web browser? Comparing response times collected with JavaScript and psychophysics toolbox in a visual search task. Behavior Research Methods, 48(1), 1–12.
- Liddle, P. F. (1987). Schizophrenic syndromes, cognitive performance and neurological dysfunction. *Psychological Medicine*, 17(1), 49–57.
- Luckiesh, M. (1965). Visual illusions: Their causes, characteristics, and applications.

 Dover Publications Inc.
- MacKay, D. M. (1957). Moving visual images produced by regular stationary patterns. *Nature*, 180(4591), 849–850.
- Maizey, L., & Tzavella, L. (2019). Barriers and solutions for early career researchers in tackling the reproducibility crisis in cognitive neuroscience. *Cortex*, 113, 357–359.
- Makowski, D., & Dutriaux, L. (2017). Neuropsydia. Py: A python module for creating experiments, tasks and questionnaires. *Journal of Open Source Software*, 2(19), 259.
- Massaro, D. W., & Anderson, N. H. (1971). Judgmental model of the ebbinghaus illusion. *Journal of Experimental Psychology*, 89(1), 147.
- Mathot, S., Schreij, D., & Theeuwes, J. (2012). OpenSesame: An open-source, graphical experiment builder for the social sciences. *Behavior Research Methods*, 44(2), 314–324.

Milkowski, M., Hensel, W. M., & Hohol, M. (2018). Replicability or reproducibility?

On the replication crisis in computational neuroscience and sharing only relevant

detail. Journal of Computational Neuroscience, 45(3), 163–172.

- Mitchell, P., Mottron, L., Soulieres, I., & Ropar, D. (2010). Susceptibility to the
 shepard illusion in participants with autism: Reduced top-down influences within
 perception? Autism Research, 3(3), 113–119.
- Muller-Lyer, F. (1896). Zur lehre von den optischen tauschungen. Uber Kontrast

 Und Konfiuxion. Zeitschrififir Psychologie Und Physiologie Der Sinnesorgane,

 IX, 1–16.
- Ninio, J. (2014). Geometrical illusions are not always where you think they are: A review of some classical and less classical illusions, and ways to describe them.

 Frontiers in Human Neuroscience, 8, 856.
- Nosek, B. A., Cohoon, J., Kidwell, M., & Spies, J. R. (2015). Estimating the reproducibility of psychological science. *Science*, 349(6251), aac4716.
- Notredame, C.-E., Pins, D., Deneve, S., & Jardri, R. (2014). What visual illusions teach us about schizophrenia. Frontiers in Integrative Neuroscience, 8, 63.
- Palmer, C. J., Caruana, N., Clifford, C. W., & Seymour, K. J. (2018). Perceptual integration of head and eye cues to gaze direction in schizophrenia. Royal Society

 Open Science, 5(12), 180885.
- Parnas, J., Vianin, P., Saebye, D., Jansson, L., Volmer Larsen, A., & Bovet, P. (2001).

 Visual binding abilities in the initial and advanced stages of schizophrenia. *Acta Psychiatrica Scandinavica*, 103(3), 171–180.
- Peirce, J. W. (2007). PsychoPy—psychophysics software in python. *Journal of Neu*roscience Methods, 162(1-2), 8–13.

Roberts, B., Harris, M. G., & Yates, T. A. (2005). The roles of inducer size and distance in the ebbinghaus illusion (titchener circles). *Perception*, 34(7), 847–856.

- Robinson, J. (1972). The psychology of visual illusion. Hutchinson University Library.
- Ropar, D., & Mitchell, P. (1999). Are individuals with autism and asperger's syndrome susceptible to visual illusions? *Journal of Child Psychology and Psychiatry*, 40(8), 1283–1293.
- Schlaffke, L., Golisch, A., Haag, L. M., Lenz, M., Heba, S., Lissek, S., ... Tegenthoff,
 M. (2015). The brain's dress code: How the dress allows to decode the neuronal
 pathway of an optical illusion. *Cortex*, 73, 271–275.
- Schneider, U., Borsutzky, M., Seifert, J., Leweke, F., Huber, T., Rollnik, J., & Emrich, H. (2002). Reduced binocular depth inversion in schizophrenic patients.

 Schizophrenia Research, 53(1-2), 101–108.
- Spencer, K. M., & Ghorashi, S. (2014). Oscillatory dynamics of gestalt perception in schizophrenia revisited. Frontiers in Psychology, 5, 68.
- Sterzer, P., Adams, R. A., Fletcher, P., Frith, C., Lawrie, S. M., Muckli, L., ... Corlett,
 P. R. (2018). The predictive coding account of psychosis. *Biological Psychiatry*,
 84(9), 634–643.
- Thakkar, K. N., Ghermezi, L., Silverstein, S., Slate, R., Yao, B., Achtyes, E., & Brascamp, J. (2020). Stronger tilt aftereffects in persons with schizophrenia.
- Tibber, M. S., Anderson, E. J., Bobin, T., Antonova, E., Seabright, A., Wright, B.,

 ... Dakin, S. C. (2013). Visual surround suppression in schizophrenia. Frontiers

 in Psychology, 4, 88.
- Topalidou, M., Leblois, A., Boraud, T., & Rougier, N. P. (2015). A long journey into reproducible computational neuroscience. Frontiers in Computational Neuroscience, 9, 30.

Uhlhaas, P. J., Phillips, W. A., Schenkel, L. S., & Silverstein, S. M. (2006). Theory of mind and perceptual context-processing in schizophrenia. *Cognitive Neuropsy- chiatry*, 11(4), 416–436.

- Uhlhaas, P. J., Silverstein, S. M., Phillips, W. A., & Lovell, P. G. (2004). Evidence for impaired visual context processing in schizotypy with thought disorder.

 Schizophrenia Research, 68(2-3), 249–260.
- Van Rossum, G., & Drake, F. L. (2009). *Python 3 reference manual*. Scotts Valley,
 CA: CreateSpace.
- Walter, E., Dassonville, P., & Bochsler, T. M. (2009). A specific autistic trait that
 modulates visuospatial illusion susceptibility. *Journal of Autism and Develop-*mental Disorders, 39(2), 339–349.
- Watanabe, E., Kitaoka, A., Sakamoto, K., Yasugi, M., & Tanaka, K. (2018). Illusory
 motion reproduced by deep neural networks trained for prediction. Frontiers in

 Psychology, 9, 345.
- Webster, M. A. (1996). Human colour perception and its adaptation. *Network:*Computation in Neural Systems, 7(4), 587–634.
- Witkin, H. A., & Asch, S. E. (1948). Studies in space orientation. IV. Further
 experiments on perception of the upright with displaced visual fields. *Journal of*Experimental Psychology, 38(6), 762.
- Yang, E., Tadin, D., Glasser, D. M., Hong, S. W., Blake, R., & Park, S. (2013).

 Visual context processing in schizophrenia. Clinical Psychological Science, 1(1),

 5–15.