

Set Operations

- We represent a set by the sorted sequence of its elements
- By specializing the auxiliary methods he generic merge algorithm can be used to perform basic set operations:
 - union
 - intersection
 - subtraction
- The running time of an operation on sets A and B should be at most $O(n_A + n_B)$

- Set union:
 - aIsLess(a, S) S.insertFirst(a)
 - \bullet bIsLess(b, S)
 - S.insertLast(b)
 - bothAreEqual(a, b, S) S. insertLast(a)
- Set intersection:
- - \blacksquare aIsLess(a, S){ do nothing }
 - \bullet bIsLess(b, S)
 - { do nothing }
 - bothAreEqual(a, b, S)

S. insertLast(a)

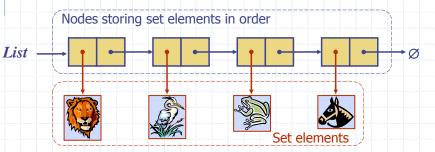
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Storing a Set in a List

- We can implement a set with a list
- Elements are stored sorted according to some canonical ordering
- \bullet The space used is O(n)



Generic Merging

- Generalized merge of two sorted lists A and B
- Template method genericMerge
- Auxiliary methods
 - aIsLess
 - bIsLess
 - bothAreEqual
- Runs in $O(n_A + n_B)$ time provided the auxiliary methods run in O(1) time

```
Algorithm genericMerge(A, B)
S \leftarrow empty sequence
while \neg A.isEmpty() \land \neg B.isEmpty()
    a \leftarrow A.first().element(); b \leftarrow B.first().element()
    if a < b
        alsLess(a, S); A.remove(A.first())
    else if b < a
        blsLess(b, S); B.remove(B.first())
    else \{b = a\}
         bothAreEqual(a, b, S)
        A.remove(A.first()); B.remove(B.first())
while \neg A.isEmpty()
    alsLess(a, S); A.remove(A.first())
 while \neg B.isEmpty()
    blsLess(b, S); B.remove(B.first())
return S
```

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Using Generic Merge for Set Operations



- Any of the set operations can be implemented using a generic merge
- For example:
 - For intersection: only copy elements that are duplicated in both list
 - For union: copy every element from both lists except for the duplicates
- ◆ All methods run in linear time

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