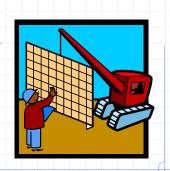
## **Array Lists**



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Array Lists

### The Array List ADT

- The Array List ADT extends the notion of array by storing a sequence of arbitrary objects
- An element can be accessed, inserted or removed by specifying its index (number of elements preceding it)
- An exception is thrown if an incorrect index is given (e.g., a negative index)

- Main methods:
  - get(integer i): returns the element at index i without removing it
  - set(integer i, object o): replace the element at index i with o and return the old element
  - add(integer i, object o): insert a new element o to have index i
  - remove(integer i): removes and returns the element at index i
- Additional methods:
  - size()
  - isEmpty()

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Array Lists

# **Applications of Array Lists**

- Direct applications
  - Sorted collection of objects (elementary database)
- Indirect applications
  - Auxiliary data structure for algorithms
  - Component of other data structures

### **Array-based Implementation**

- $\Box$  Use an array A of size N
- □ A variable *n* keeps track of the size of the array list (number of elements stored)
- $\Box$  Operation get(i) is implemented in O(1) time by returning A[i]
- $\Box$  Operation **set**(i,o) is implemented in O(1) time by performing t = A[i], A[i] = o, and returning t.



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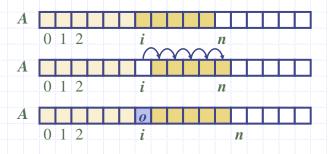
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### Insertion

- □ In operation add(i, o), we need to make room for the new element by shifting forward the n i elements A[i], ..., A[n-1]
- $\Box$  In the worst case (i = 0), this takes O(n) time



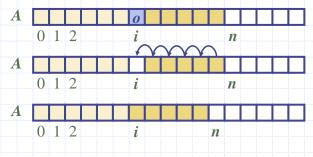
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#### **Element Removal**

- □ In operation remove(i), we need to fill the hole left by the removed element by shifting backward the n i 1 elements A[i + 1], ..., A[n 1]
- □ In the worst case (i = 0), this takes O(n) time



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### Performance

- In the array based implementation of an array list:
  - The space used by the data structure is O(n)
  - size, isEmpty, get and set run in O(1) time
  - add and remove run in O(n) time in worst case
- □ If we use the array in a circular fashion, operations add(0, x) and remove(0, x) run in O(1) time
- In an add operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one

# Growable Array-based Array List

- In an add(o) operation (without an index), we always add at the end
- When the array is full, we replace the array with a larger one
- How large should the new array be?
  - Incremental strategy: increase the size by a constant *c*
  - Doubling strategy: double the size

Algorithm add(o)if t = S.length - 1 then  $A \leftarrow$  new array of size ... for  $i \leftarrow 0$  to n-1 do  $A[i] \leftarrow S[i]$   $S \leftarrow A$   $n \leftarrow n+1$  $S[n-1] \leftarrow o$ 

## Comparison of the Strategies

- We compare the incremental strategy and the doubling strategy by analyzing the total time T(n) needed to perform a series of nadd(o) operations
- We assume that we start with an empty stack represented by an array of size 1
- We call amortized time of an add operation the average time taken by an add over the series of operations, i.e., T(n)/n

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## **Incremental Strategy Analysis**

- $\Box$  We replace the array k = n/c times
- $\Box$  The total time T(n) of a series of n add operations is proportional to

$$n + c + 2c + 3c + 4c + ... + kc =$$
  
 $n + c(1 + 2 + 3 + ... + k) =$   
 $n + ck(k + 1)/2$ 

- $\Box$  Since c is a constant, T(n) is  $O(n + k^2)$ , i.e.,  $O(n^2)$
- $\Box$  The amortized time of an add operation is O(n)

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## **Doubling Strategy Analysis**

- $\square$  We replace the array  $k = \log_2 n$ times
- $\Box$  The total time T(n) of a series of nadd operations is proportional to

$$n+1+2+4+8+...+2^{k} = n+2^{k+1}-1 =$$

3n - 1

- $\Box$  T(n) is O(n)
- □ The amortized time of an add operation is O(1)

geometric series

