

# Module ECUE

# “Machine Learning for Image Processing”

## Data Enhancement

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Morpheme team

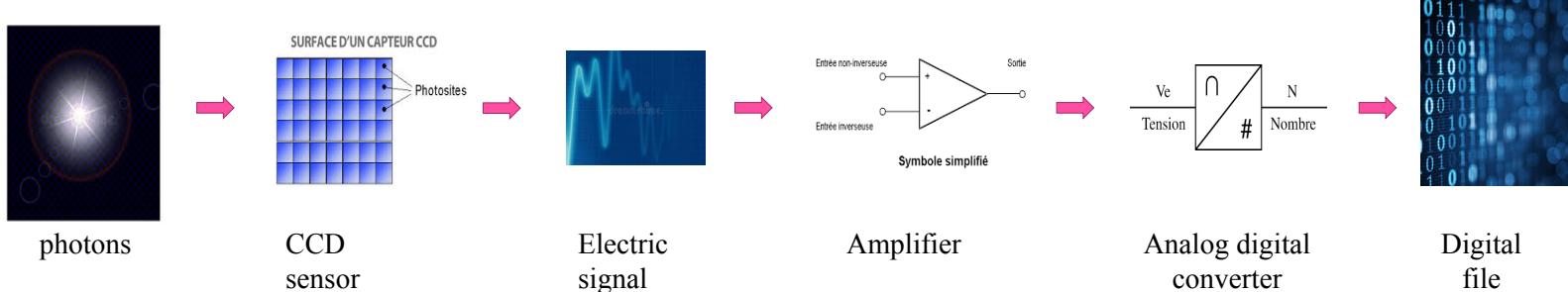
INRIA/I3S/iBV

# Introduction : why data enhancement ?

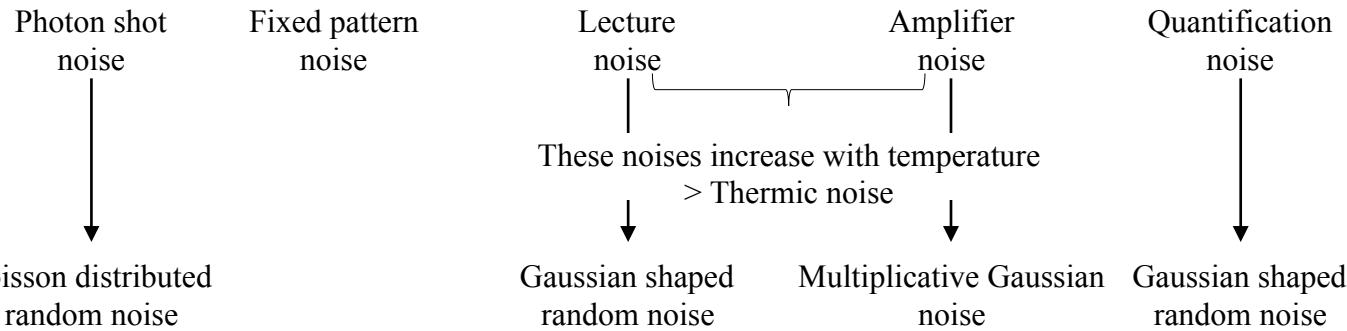
- Data (images in our case ) can be subject to :
  - noise (additive gaussian, pepper and salt,...)
  - poor contrast (backlight, bad camera tuning,...)
  - light heterogeneity (optical effect, shadows,...)
  - Processing artefact
- Goal : improve image quality
  - For visualization
  - As a pre-processing step
- Machine learning
  - Number of approaches are based on features extracted from data (k-means, SVM, random forests,...)
  - Pre-processing improves the quality of features : reduce noise and variability

# Data acquisition : noise sources

Total signal = useful signal + noise



The camera detector collects the photons from the light and transforms them in electrical signal. This signal is amplified before being converted into numerical data (integers). Each step in this pipeline can be a source of noise.



$$\text{SNR} = 10 \times \log (\text{pT})$$

SNR : Signal to Noise Ratio

p = photon density

T = exposure time

# Examples of noise



Original image



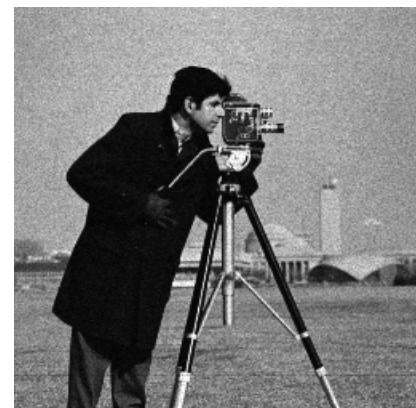
Additive Gaussian



Salt & Pepper



Speckle (multiplicative)



Poisson

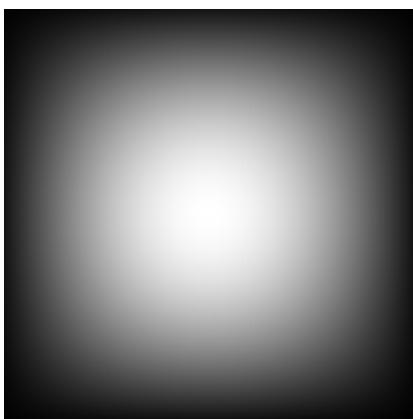
# Examples of light perturbation



Original image



Low contrast



Transfer function

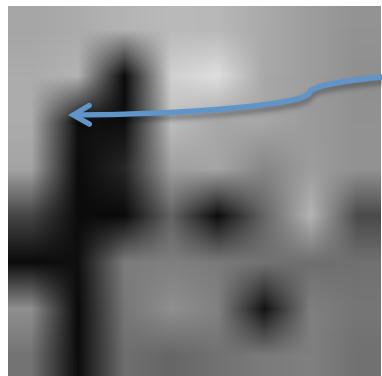


Windowed image

# Three main approaches

- Work on the pixels themselves (in the spatial domain)
- Work in a transformed domain (Fourier transform for example)
- Work on the histogram

# Image: a discrete table

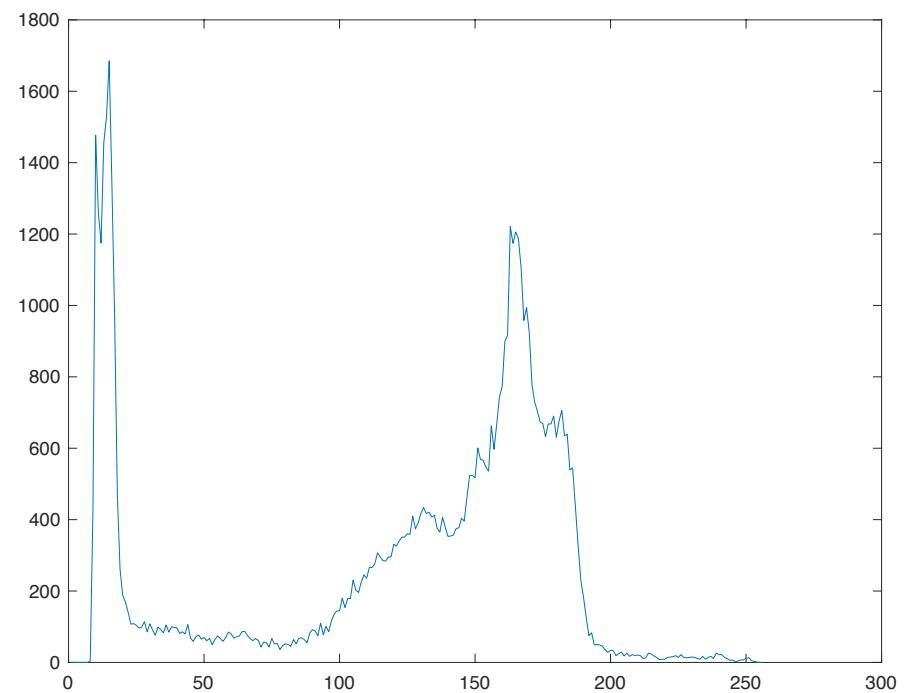


166	172	180	186	184	170	157	147
172	180	11	209	223	169	158	144
172	17	15	191	168	167	155	146
164	11	39	160	166	135	158	146
69	12	10	100	12	102	181	74
11	16	125	128	123	115	111	113
143	10	119	144	130	19	128	118
115	12	111	102	114	123	128	113

# Histogram

$$X \in <1, NG>, h(x) = \frac{\#\{s \in I : i_s = x\}}{\#\{s \in I\}}$$

can be interpreted as a probability



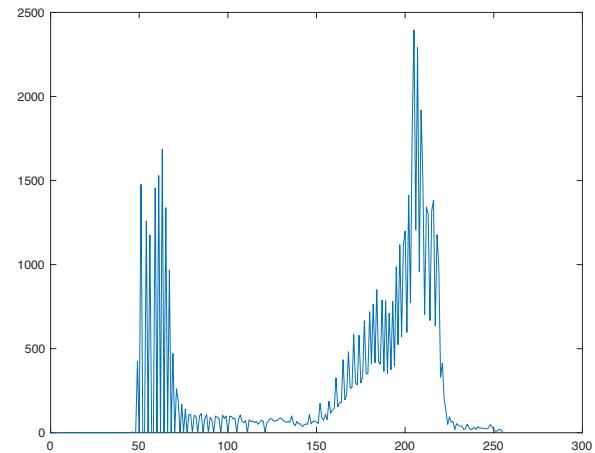
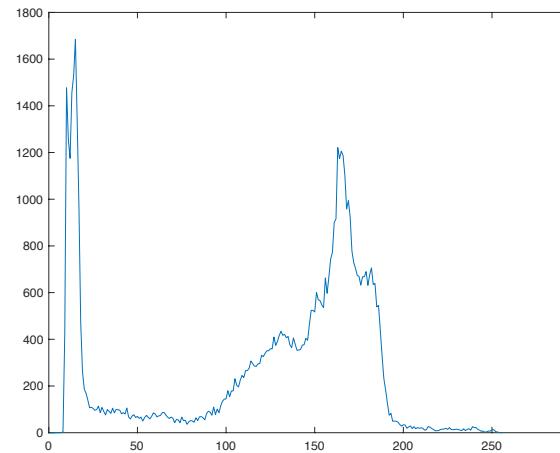
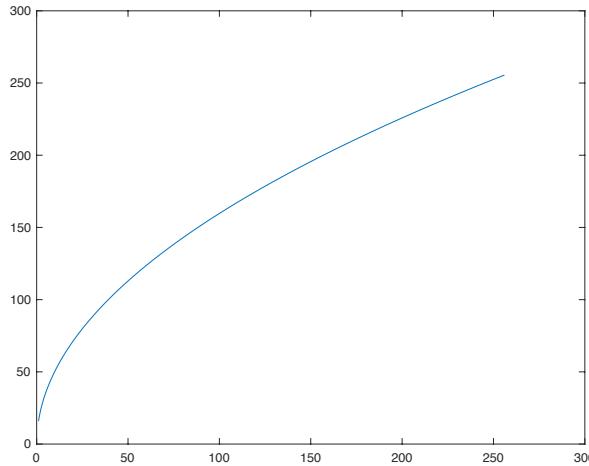
# Histogram transform

$$T : \langle 1, NG \rangle \rightarrow \langle 1, NG \rangle$$
$$x \mapsto T(x)$$

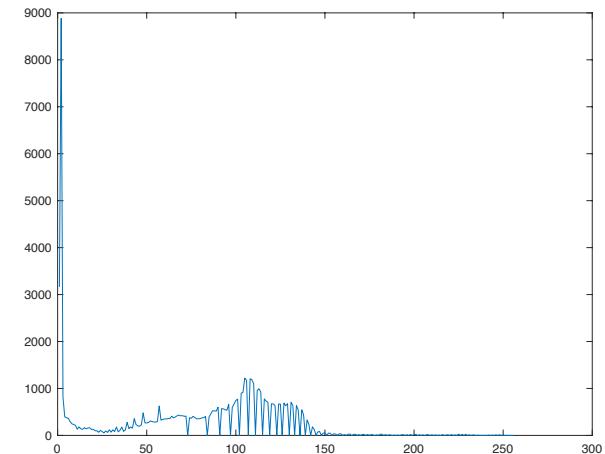
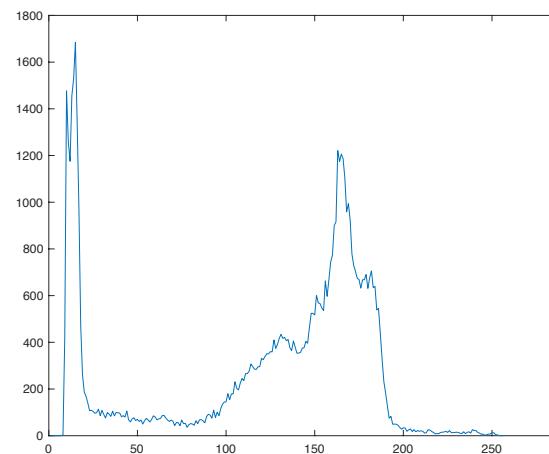
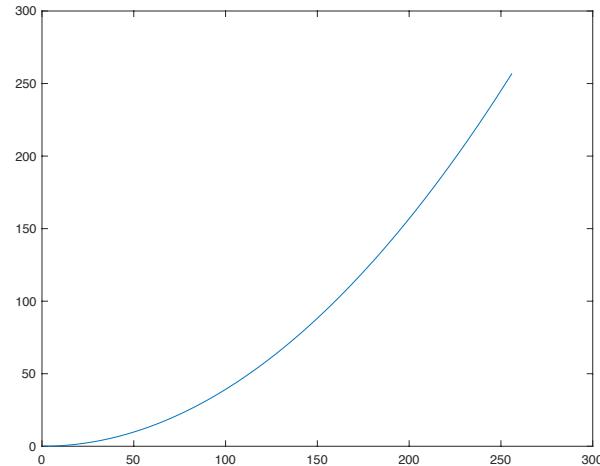
Algorithm :

- Input : image I
- output : image J
- for each pixel s in I :
  - read  $x = I(s)$
  - set  $y(s) = T(x)$

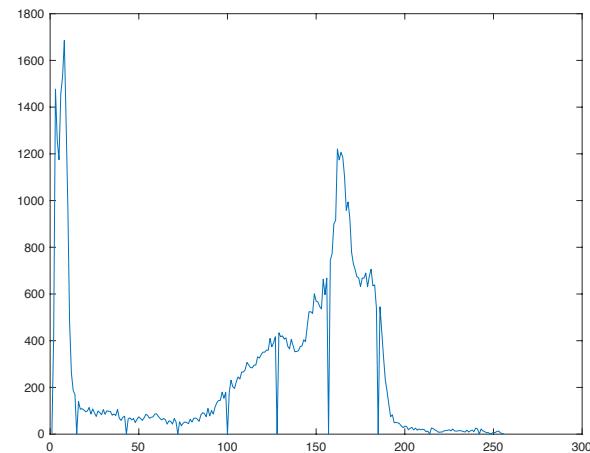
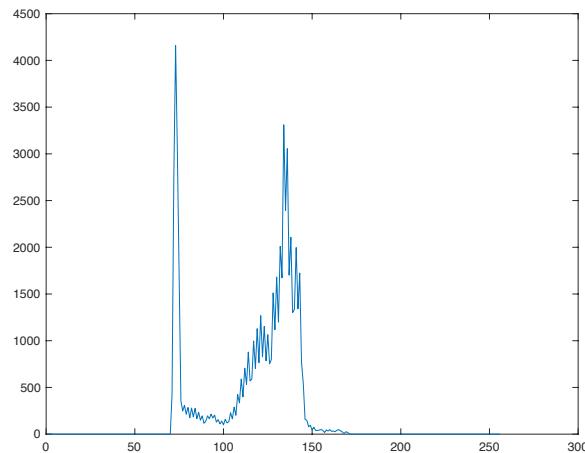
# Transform 1



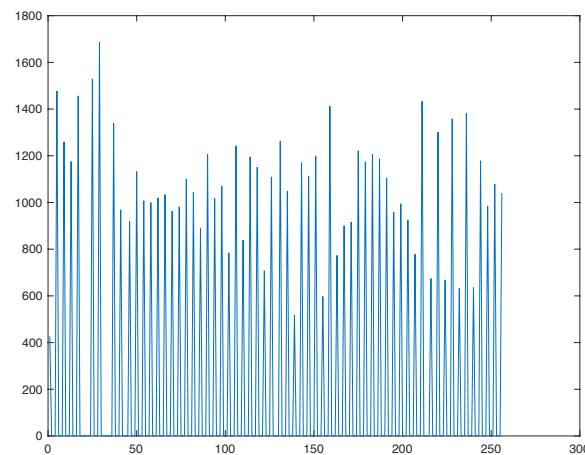
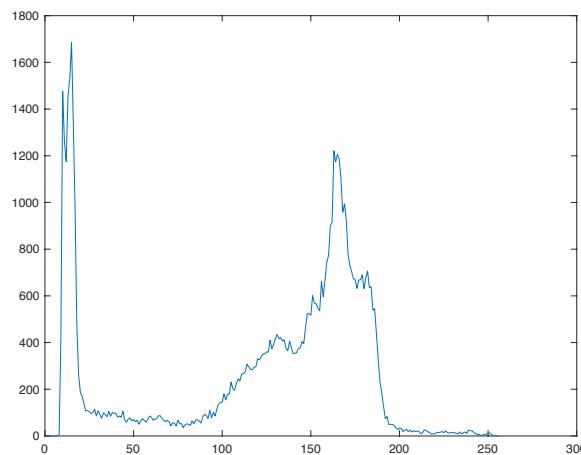
# Transform 2



# Histogram extension

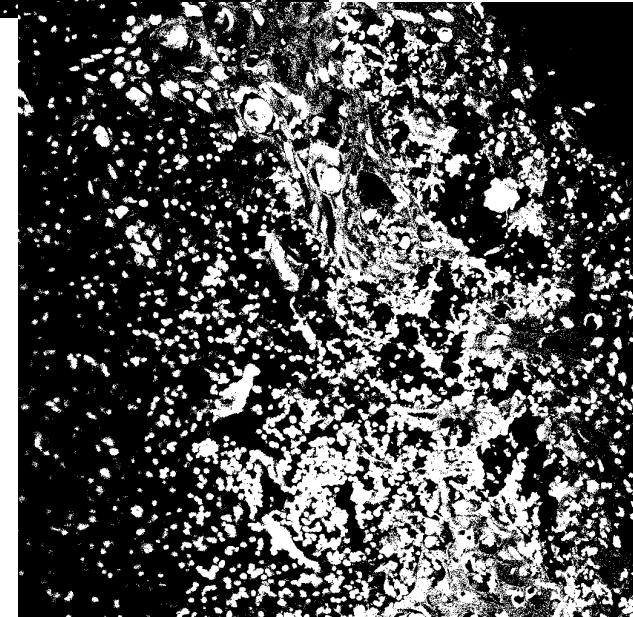
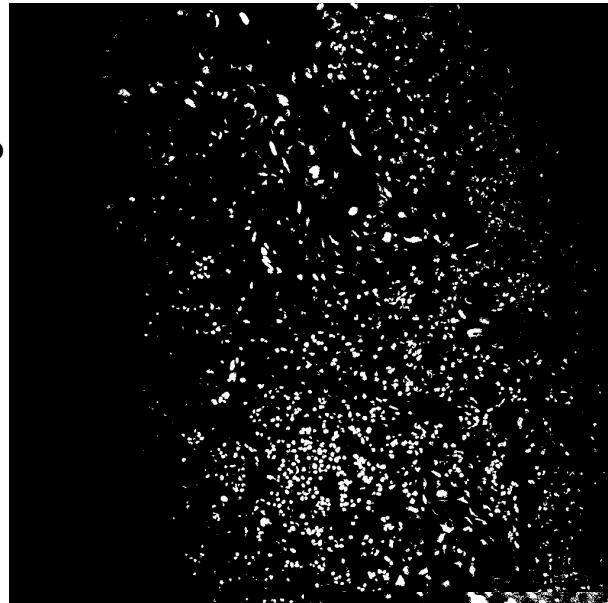
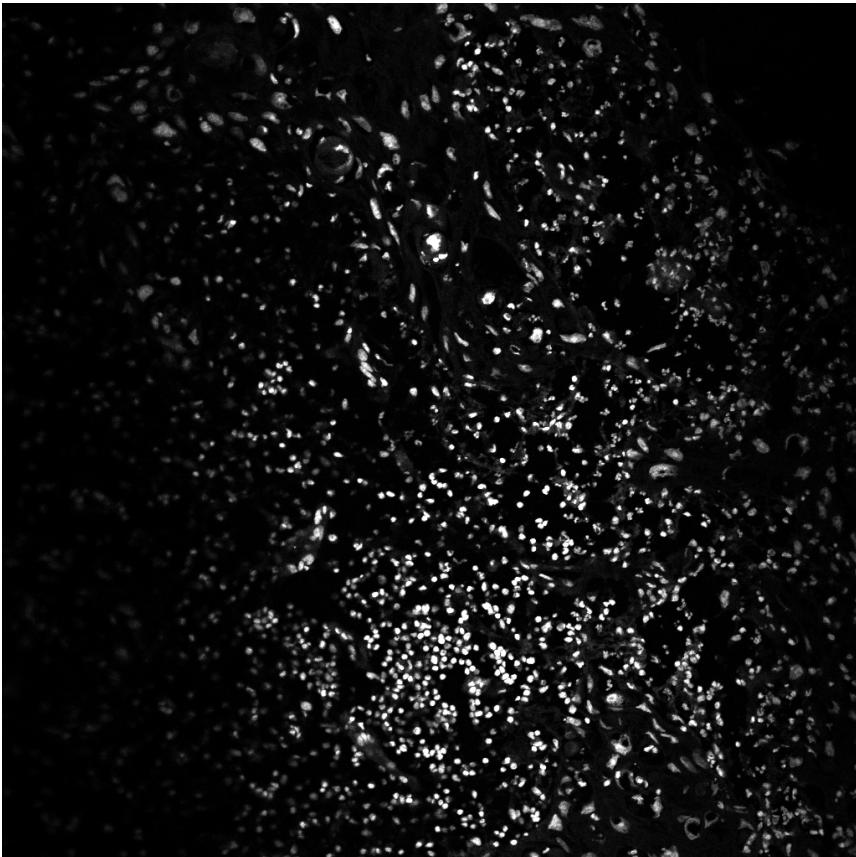


# Histogram equalization



# Local normalization

The intensity may be heterogeneous :  
how to threshold ?

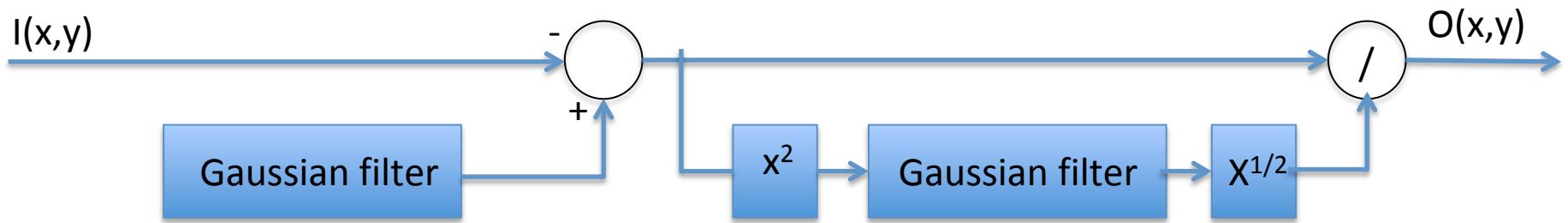


# Local Normalization

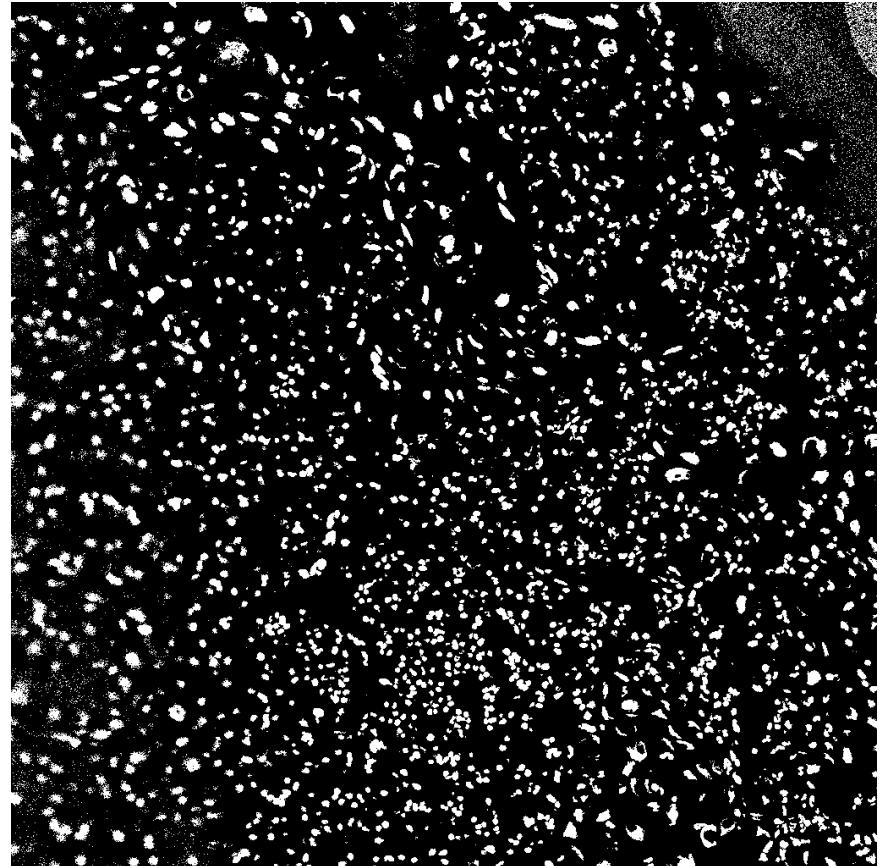
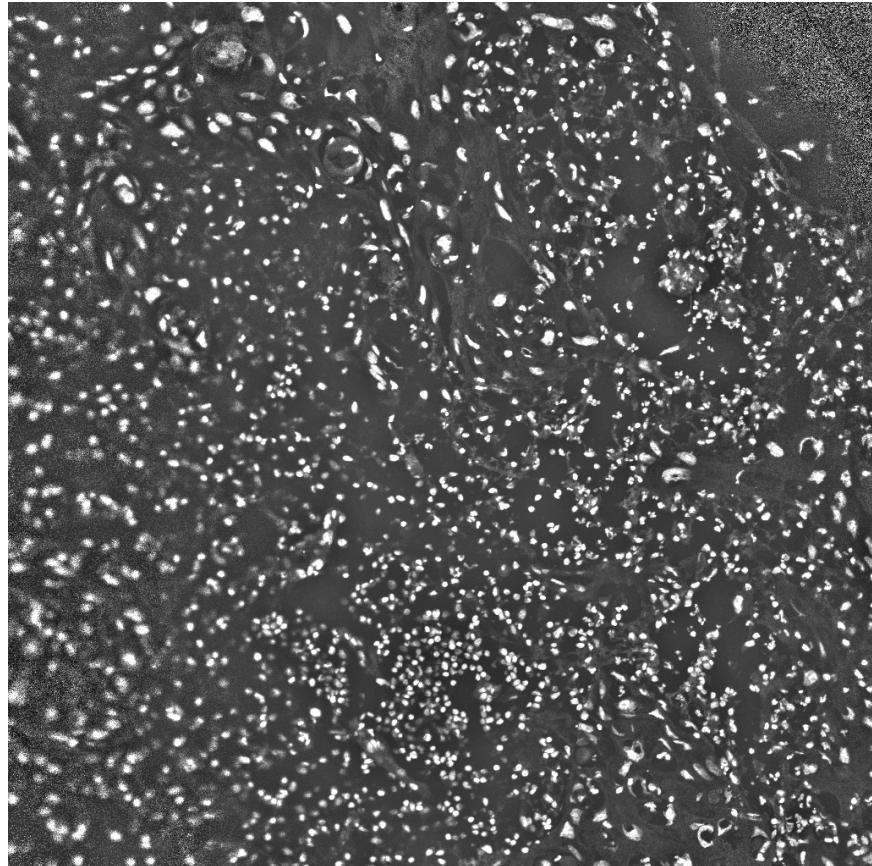
Goal : same mean and same variance everywhere

$$O(x, y) = \frac{I(x, y) - \mu_I(x, y)}{\sigma_I(x, y)}$$

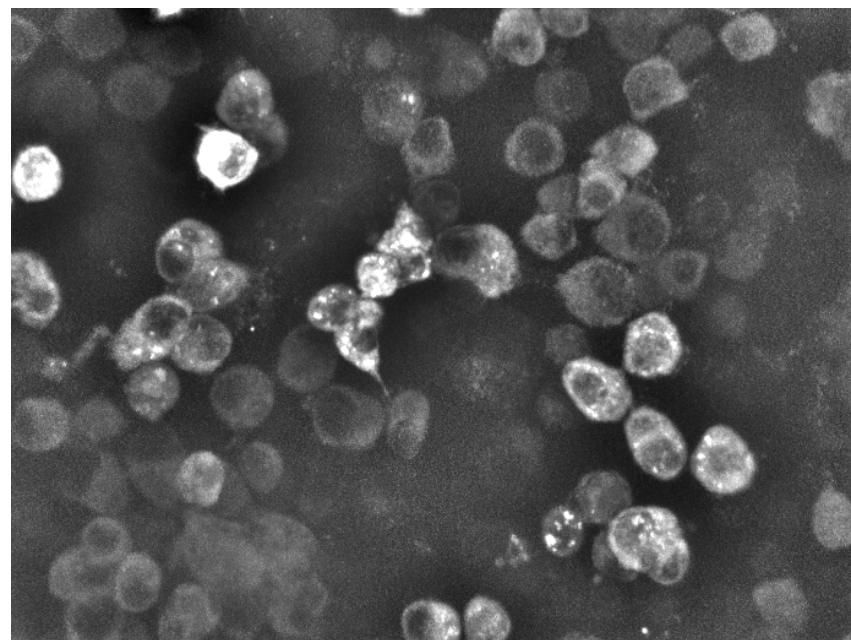
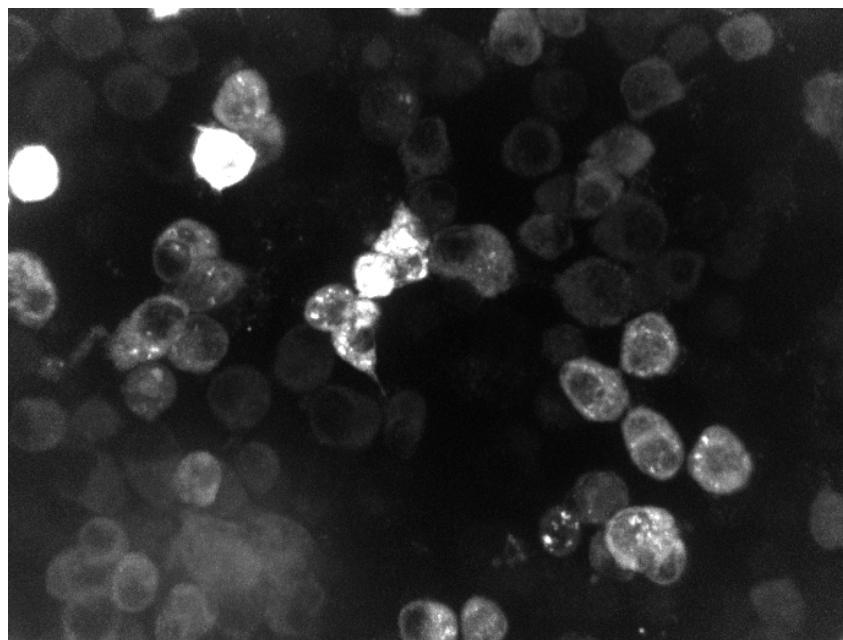
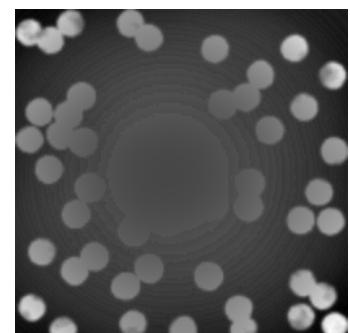
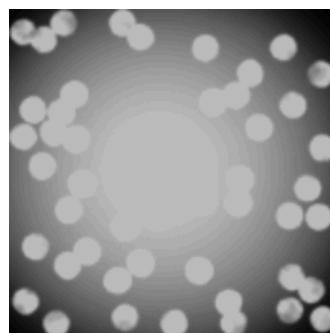
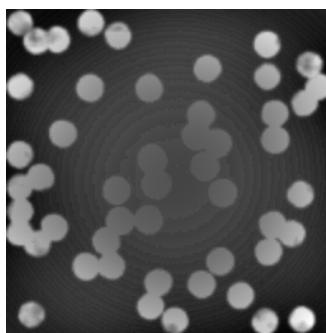
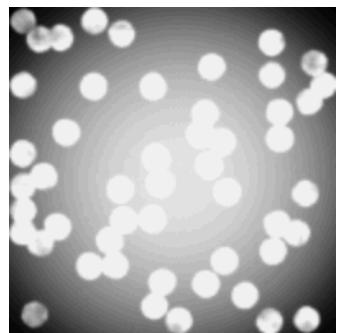
In practice :



# Local normalization



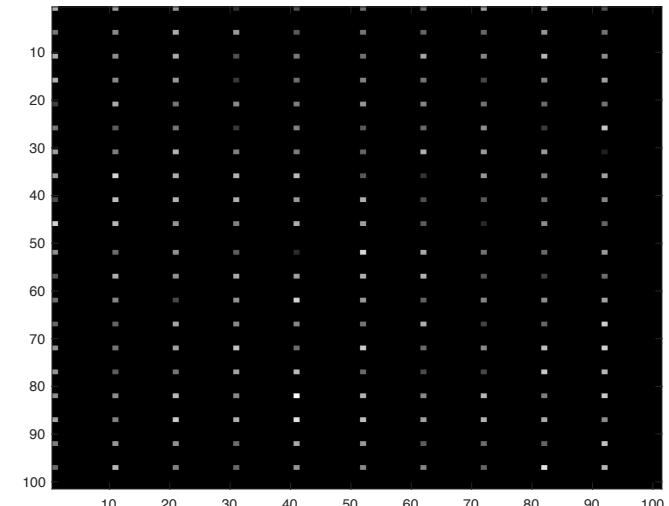
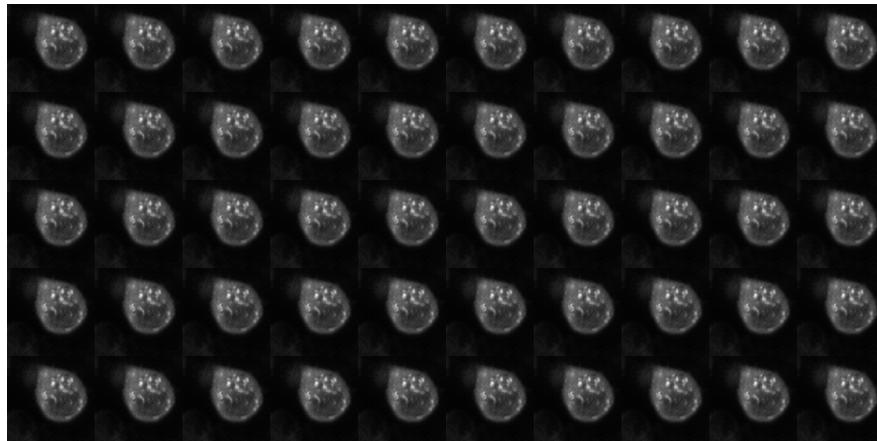
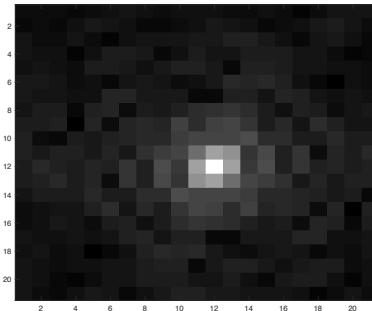
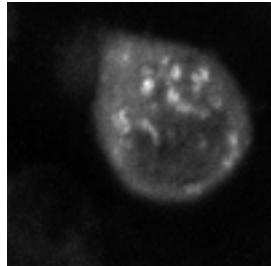
# Spatial normalisation



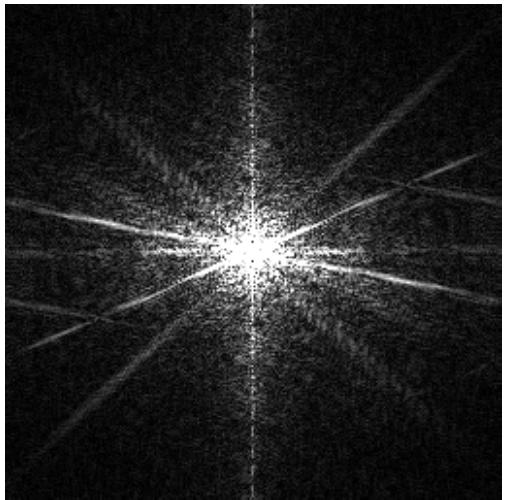
# Fourier transform

$$fftI(p, q) = \sum_{j=0}^{m-1} \sum_{k=0}^{n-1} I(j, k) e^{-2\pi i \frac{jp}{m}} e^{-2\pi i \frac{kq}{n}}$$

Frequency analysis



fft of original image

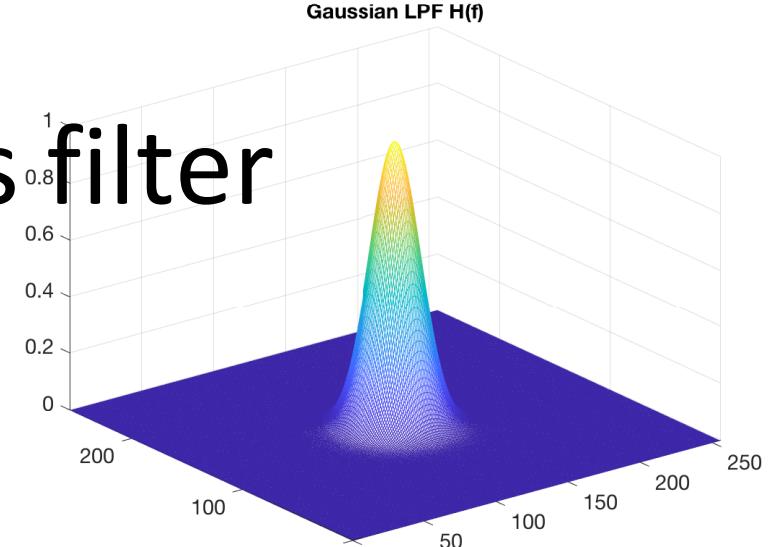


original image

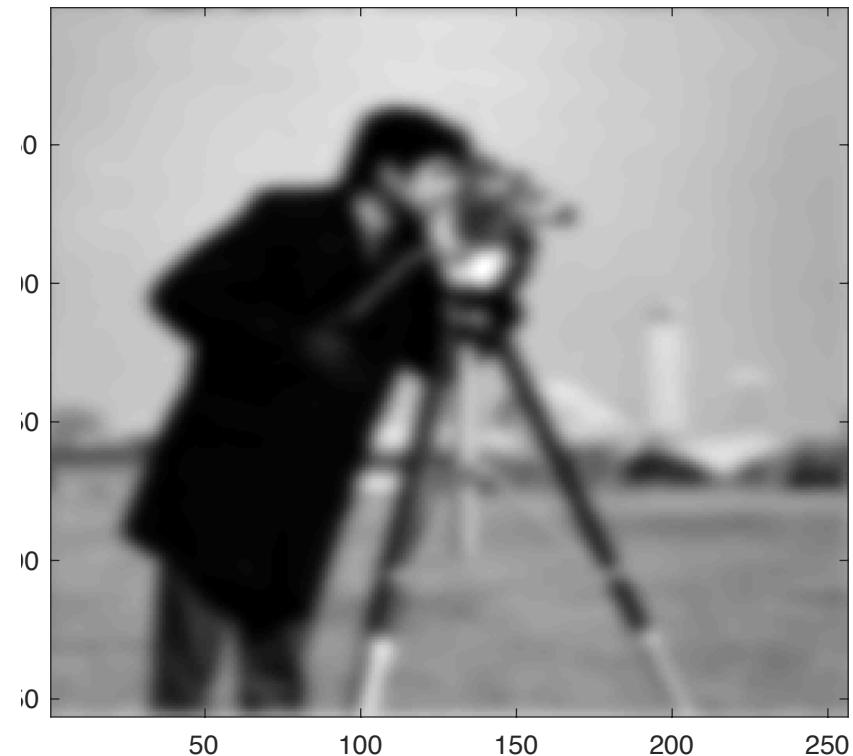


# Lowpass filter

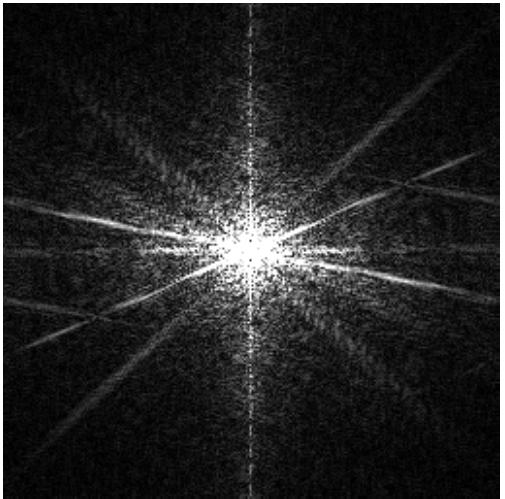
Gaussian LPF  $H(f)$



Cut high frequencies : remove noise (but also edges)



fft of original image

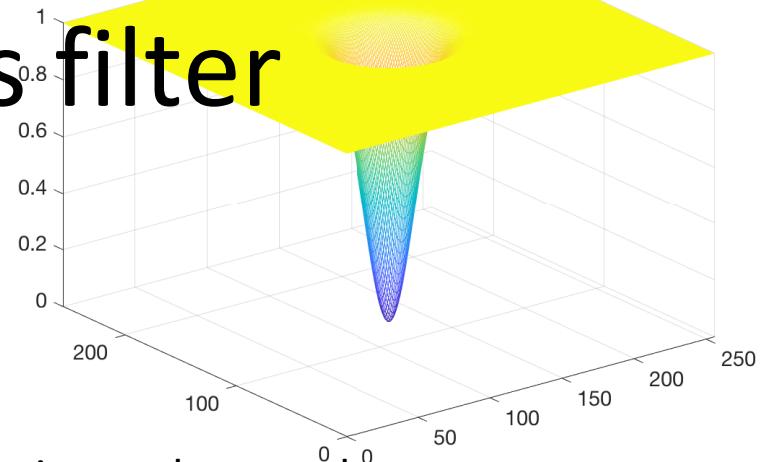


original image



# Highpass filter

Gaussian HPF H(f)



Cut low frequencies : enhance edges



# Spatial filtering : linear

Convolution with a filter : remove noise (example : Gaussian filter)

Lowpass filter : can destroy edges

Adapted to additive noise

$$J = G * I$$



# Spatial filtering : non linear

Mostly median filter

Preserve edges

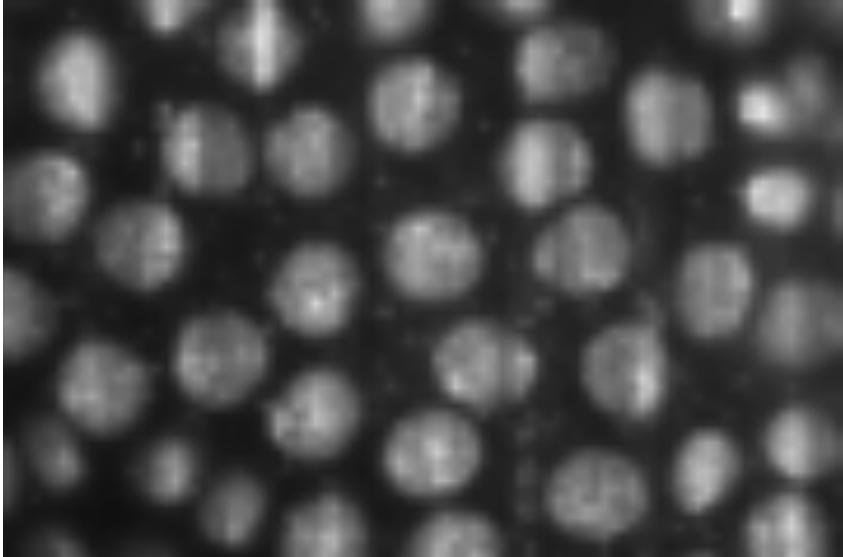
Adapted to salt and pepper noise



# Denoising

- Gaussian Filter :  $O = G * I$

$$G(x, y) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp - \left[ \frac{x^2 + y^2}{2\sigma^2} \right]$$

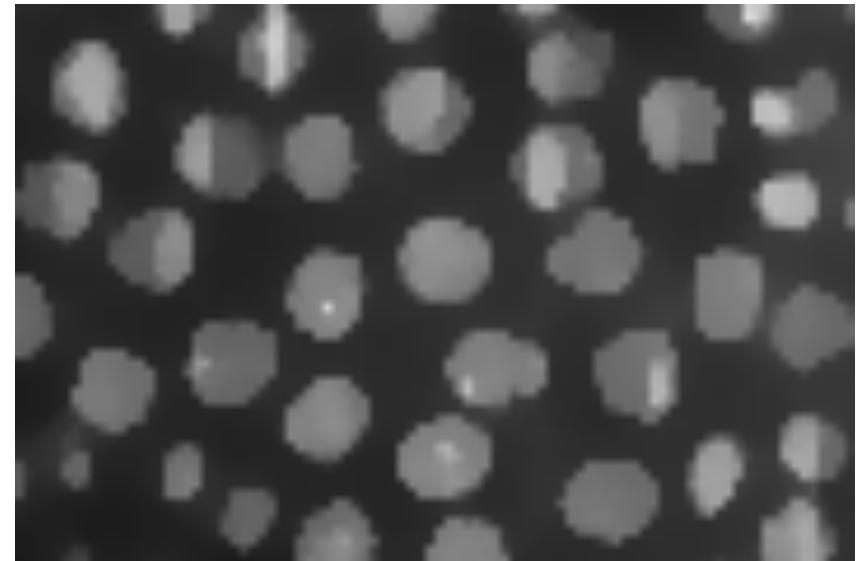
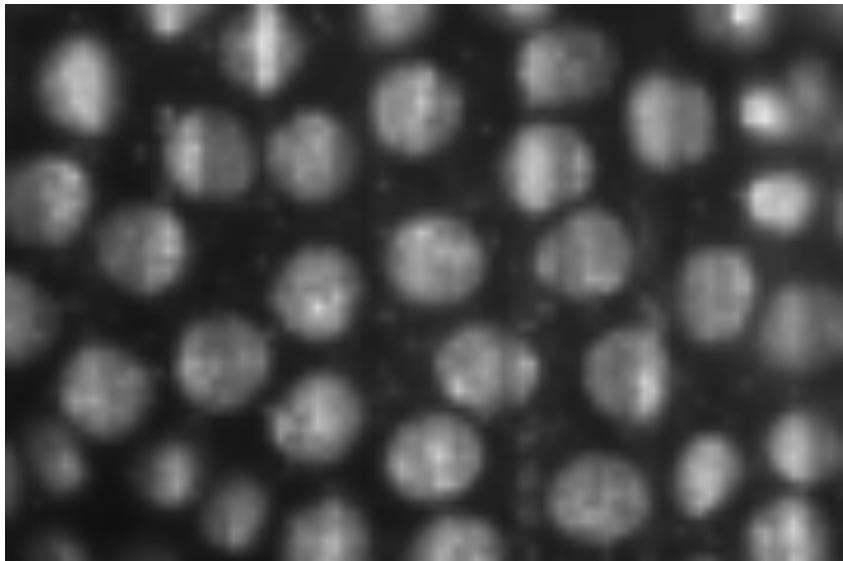


-> Remove noise but blur objects

# Denoising

- Restoration :  $\operatorname{argmin} (||O - I||_{L^n} + \Phi(O))$

Example:  $U = \sum_s \frac{(o_s - i_s)^2}{2\sigma^2} - \beta \sum_{s \sim s'} \frac{1}{1 + \frac{(o_s - o_{s'})^2}{\delta^2}}$



-> Higher algorithmic complexity, embed prior information on the solution (cf Bayesian approach).

# Linear structures enhancement

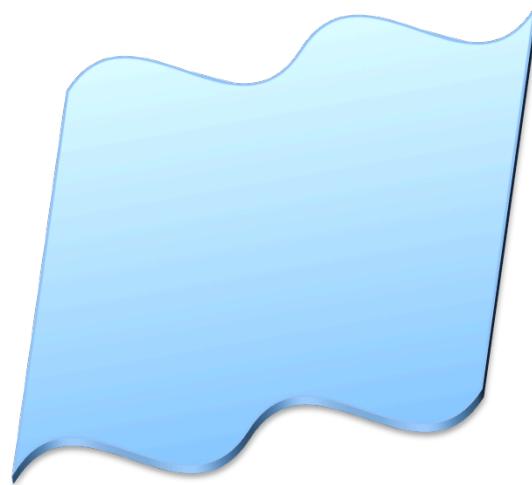
- Before detection (thresholding)
- Numerous applications : road, vessels, axons, filaments, ....
- Define locally a linear structure : homogeneous intensity in the object direction, heterogeneity in the orthogonal direction

# Gabor Filter

Sinusoidal shape weighted by a Gaussian

Parameters :

- Frequency :  $\lambda$
- Orientation :  $\theta$
- Phase :  $\phi$
- Gaussian variance :  $\sigma^2$



$$G_{(x,y)}(u, v | \lambda, \theta, \phi, \sigma) = \exp \left[ -\frac{(u - x)^2 + (v - y)^2}{2\sigma^2} \right] \sin(\lambda(u \cos \theta - v \sin \theta) + \phi)$$

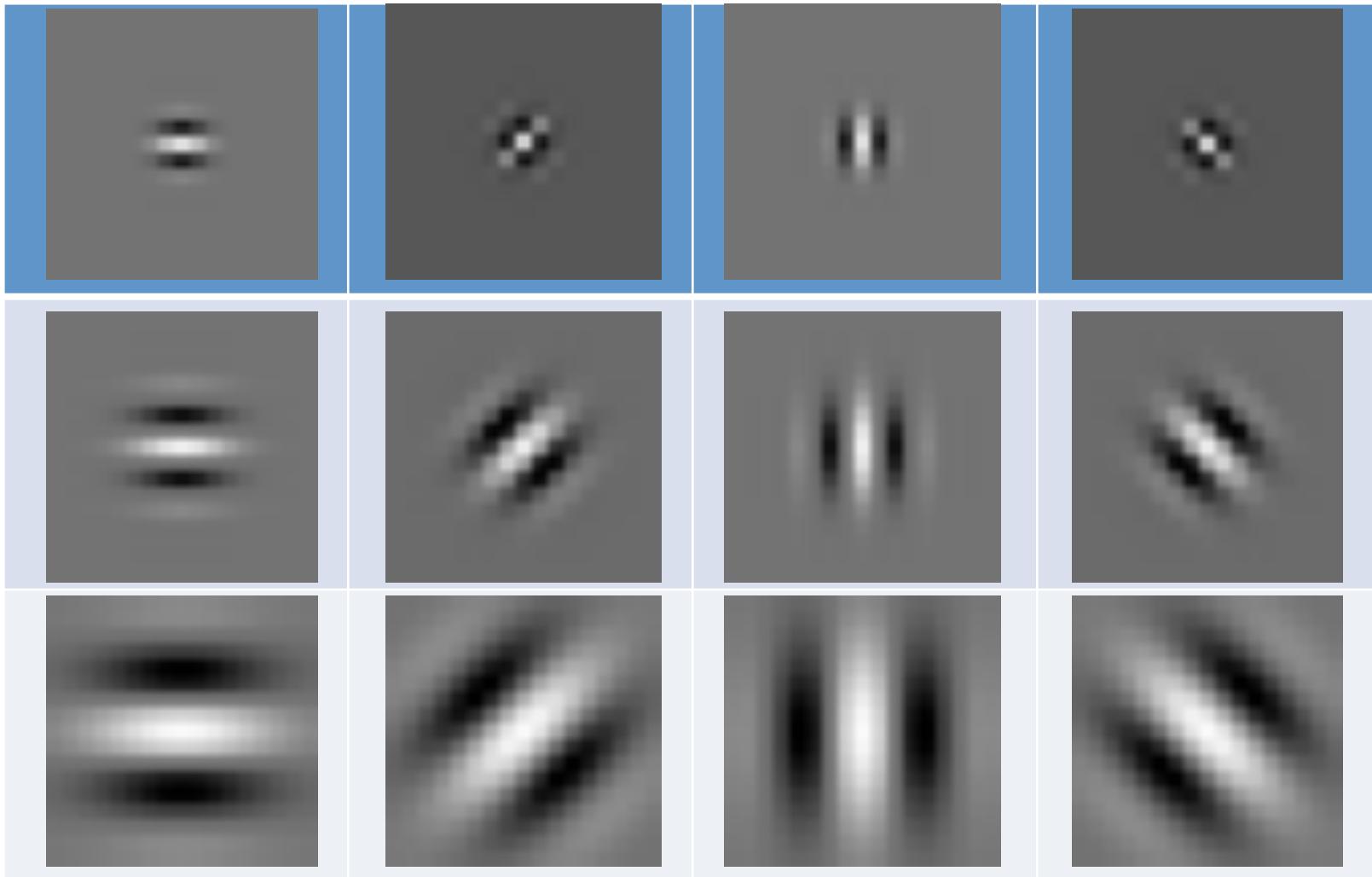
Energy :

$$E(x, y | \lambda, \theta, \sigma) = \left( \sum_{u,v} G_{(x,y)}(u, v | \lambda, \theta, 0, \sigma) I(u, v) \right)^2 + \left( \sum_{u,v} G_{(x,y)}(u, v | \lambda, \theta, \frac{\pi}{2}, \sigma) I(u, v) \right)^2$$

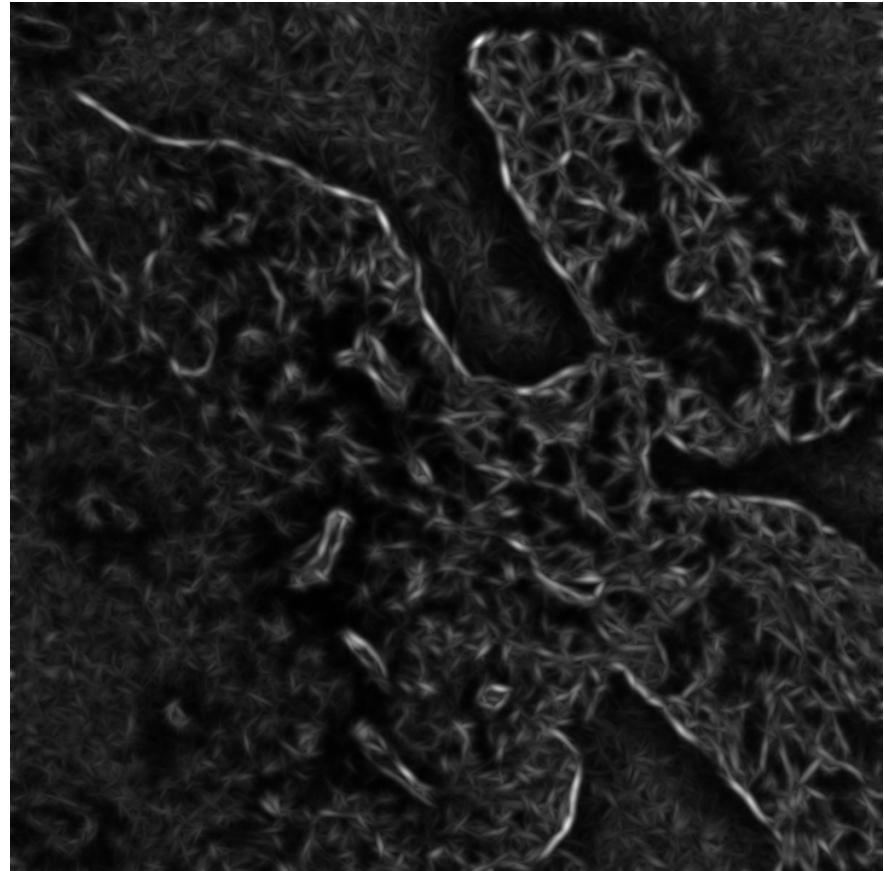
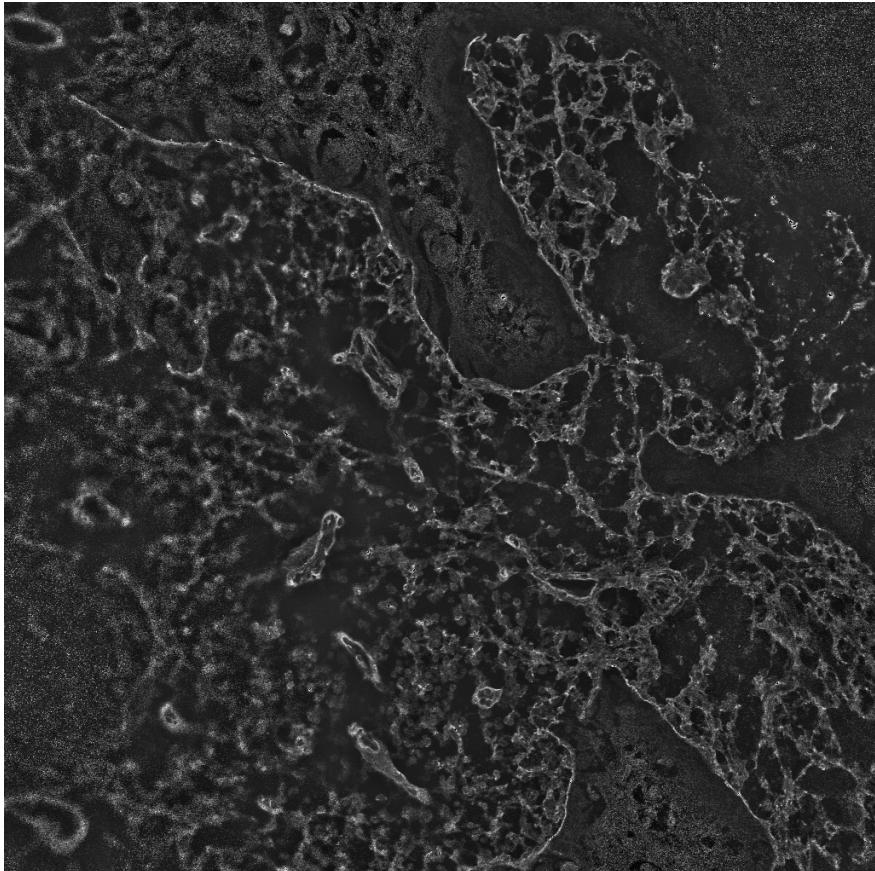
In practice :

$$F(x, y | \lambda, \theta, \sigma) = \max_{\phi} \left( \sum_{u,v} G_{(x,y)}(u, v | \lambda, \theta, \phi, \sigma) I(u, v) \right)^2$$

# Gabor Filters

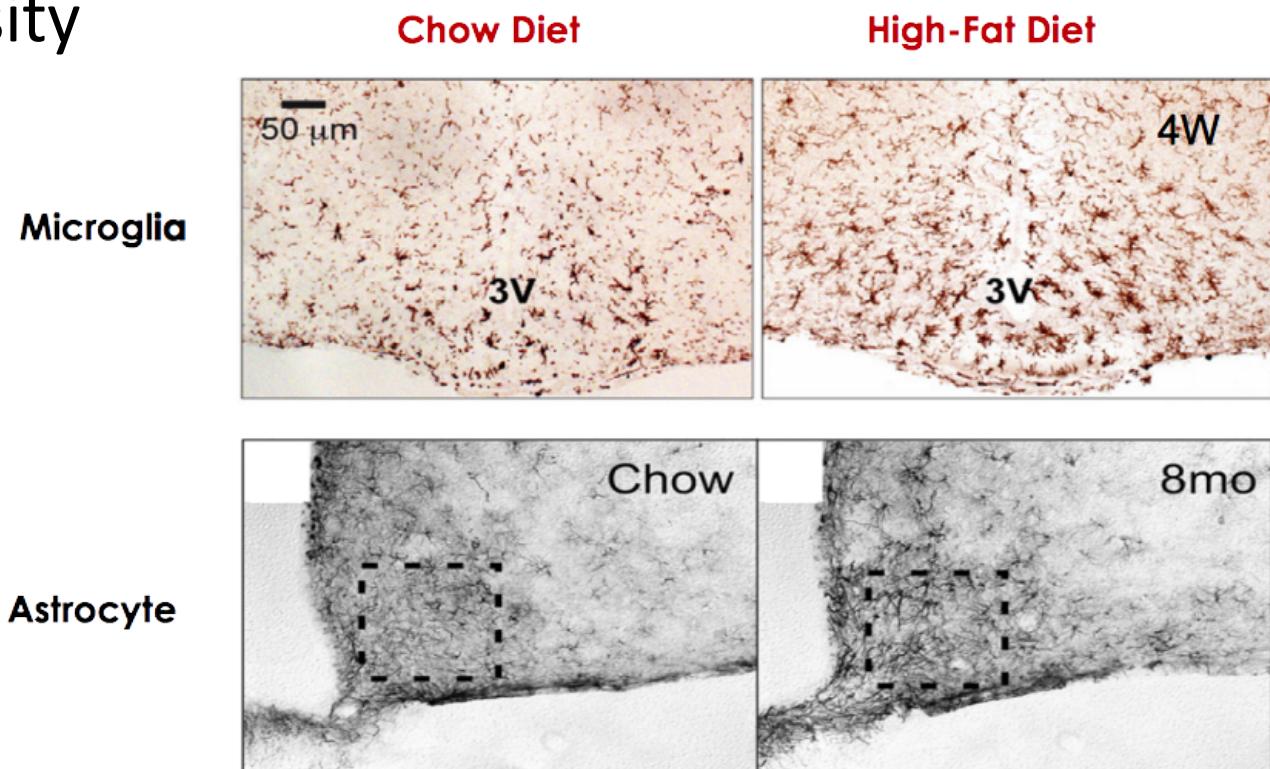


# Gabor filter : example



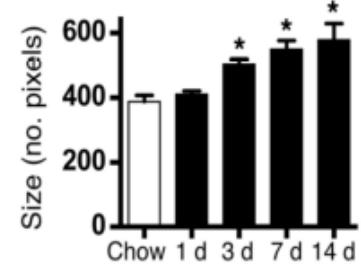
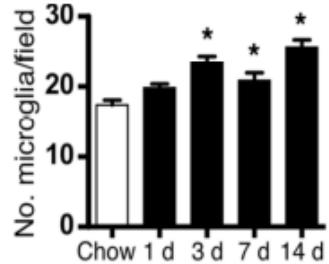
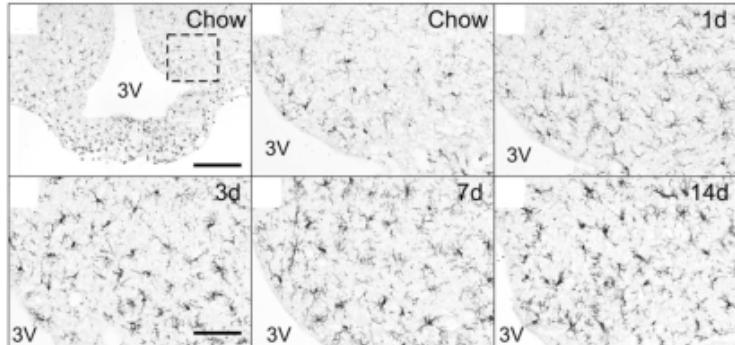
# Case study : Detection and classification of neuronal extensions on fluorescence microscopy images: application to the study of metabolic diseases such as obesity

- Biological context :
  - Glial cells reactivity associated with diet induced obesity

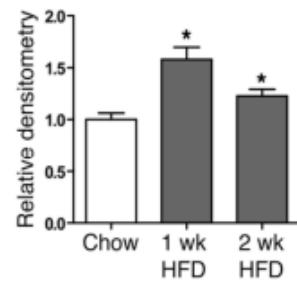
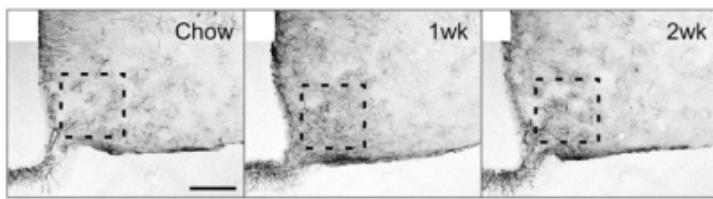


- High fat diet (HFD) induces glial cells reactivity before the onset of obesity

**Microglia**

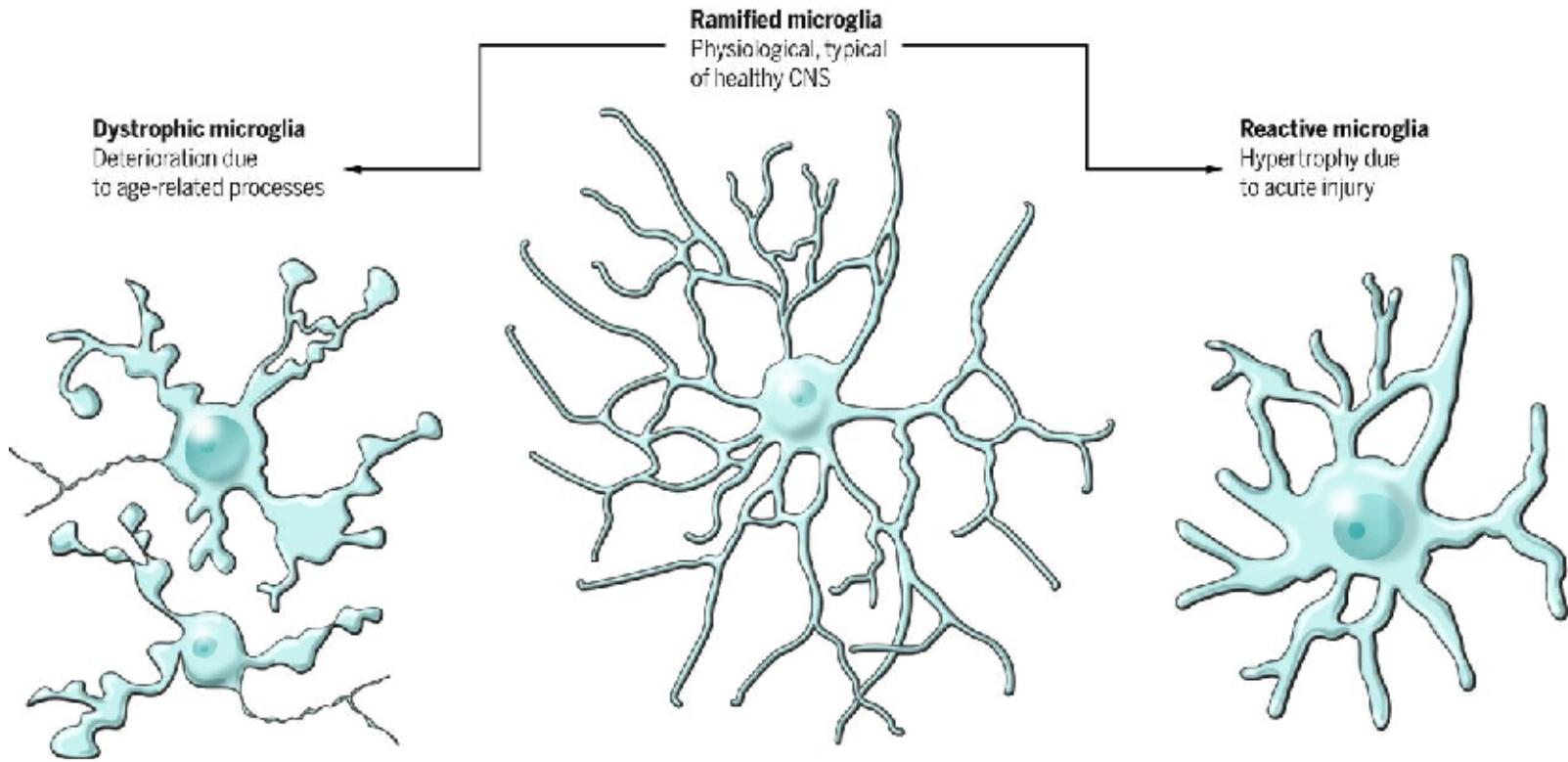


**Astrocyte**



**Does astrocytes and microglia hypothalamic reactivity appear at meal scale in response to HFD?**

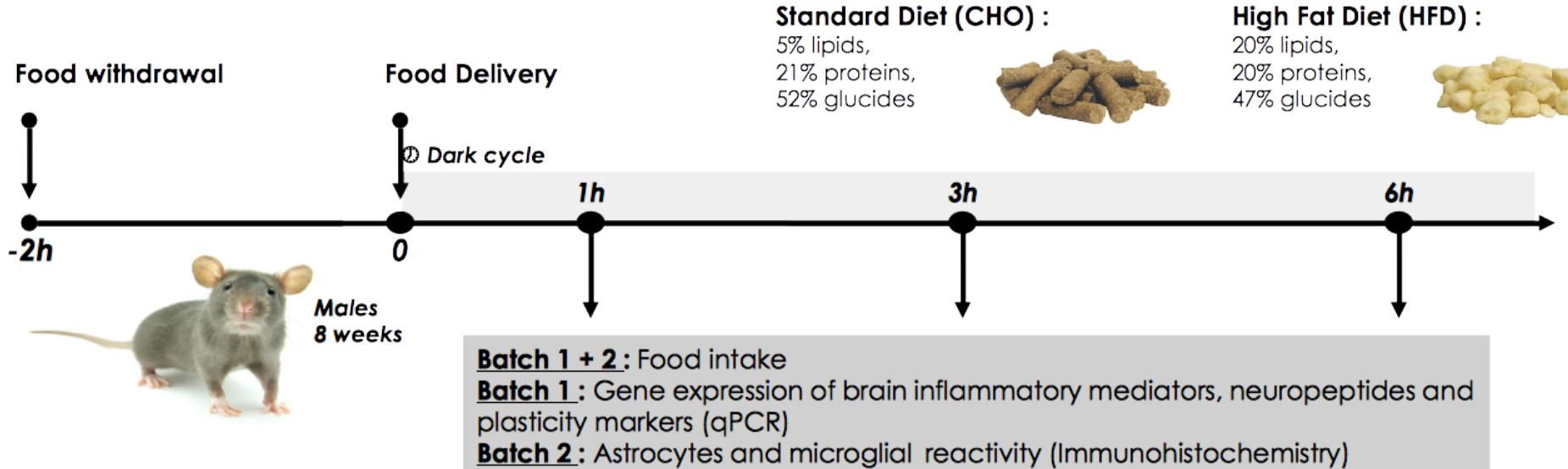
Thaler JP, Yi CX et al. JCI 2012



Morphology of ramified (healthy CNS), reactive, and dystrophic microglia.

***Does astrocytes and microglia hypothalamic reactivity appear at meal scale in response to High fat diet (HFD)?***

# Protocol



# Goal

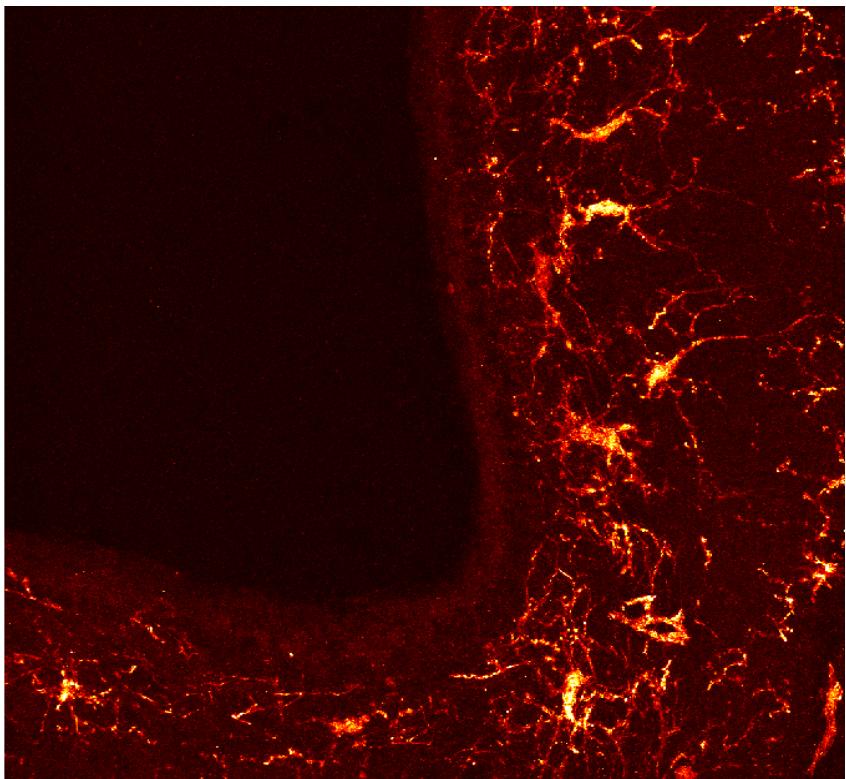
Classify images of neuronal cells into mice fed normally and mice fed with a high-fat diet.

- Two type of cells
  - **Microglia**
  - **Astrocyte**
- Two different areas of interest of the hypothalamus
  - **Median Eminence (EM)**
  - **Arcuate Nucleus (ARC)**
- 3D images at different times (1, 3 et 6 hours)

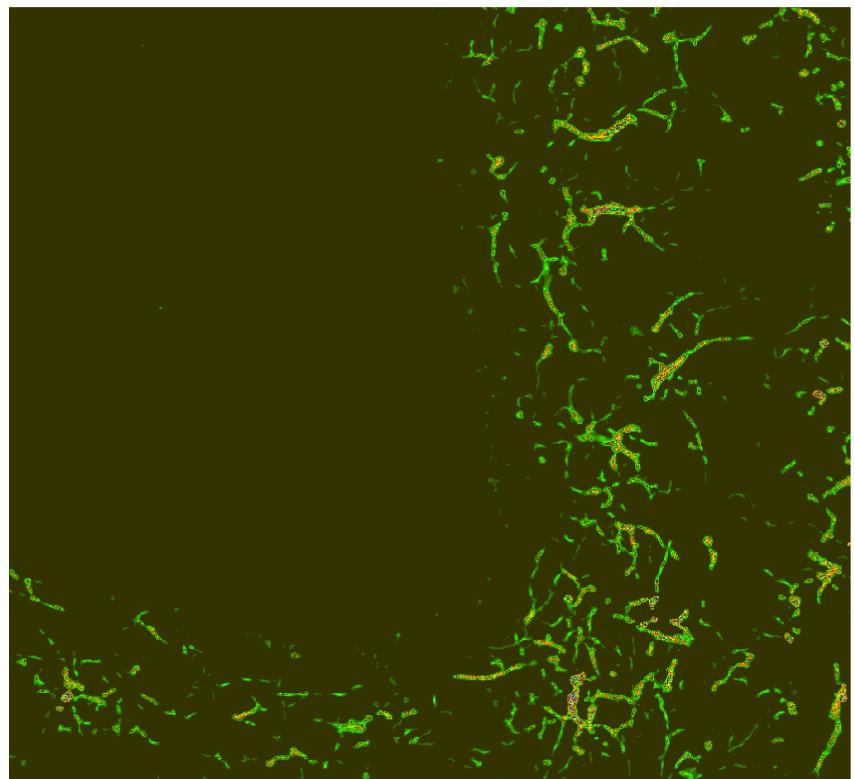
# The four steps

- Extensions detection
- Somas detection
- Connection between filaments/soma and filaments/filaments
- Feature extraction

# Extensions detection : filament enhancement

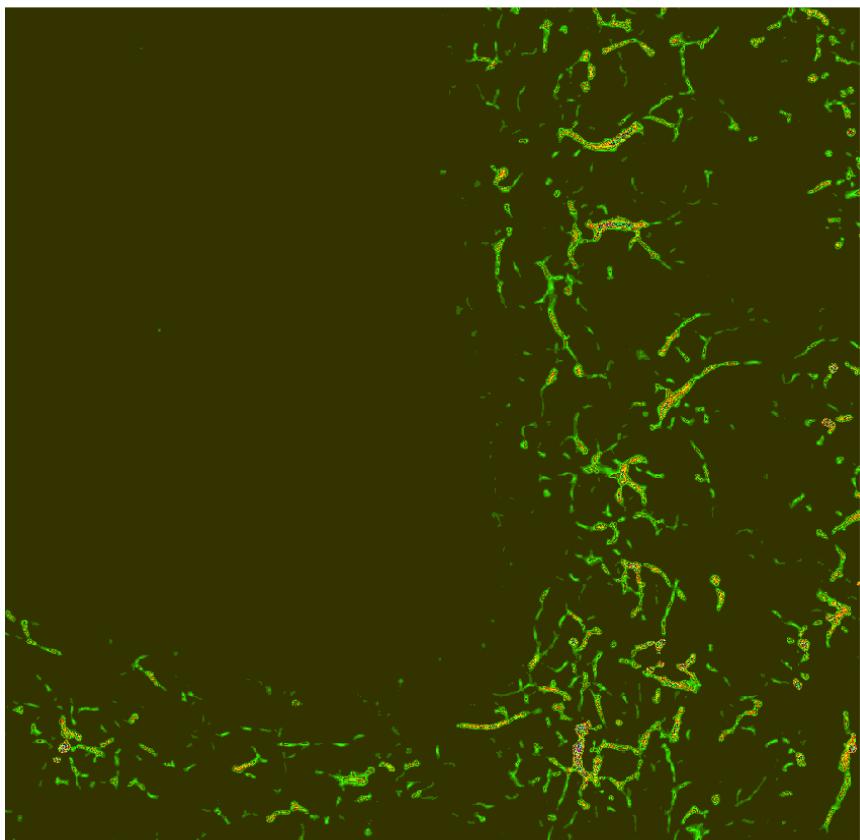


Original MIP (Maximum intensity projection)

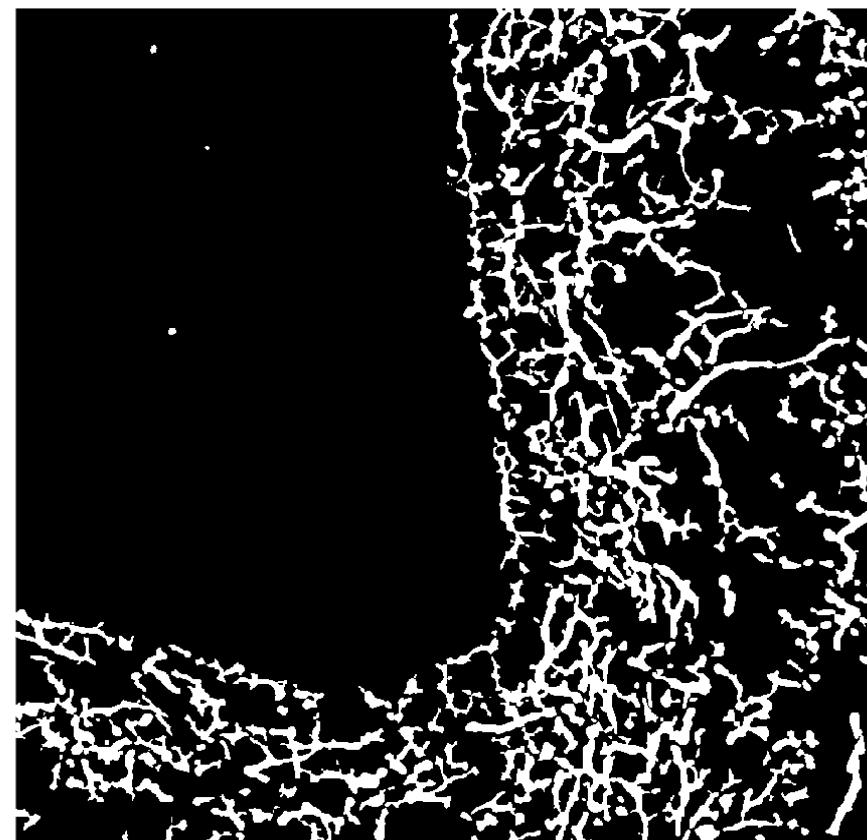


MIP after Frangi filter

# Extensions detection : threshold by hysteresis

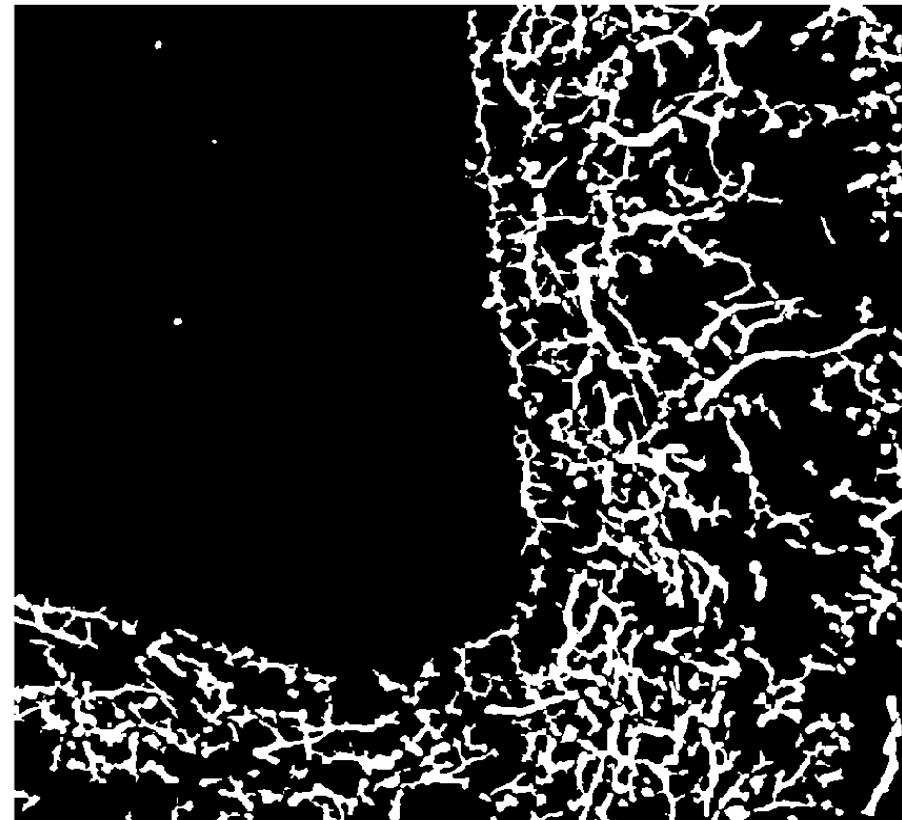


MIP Frangi

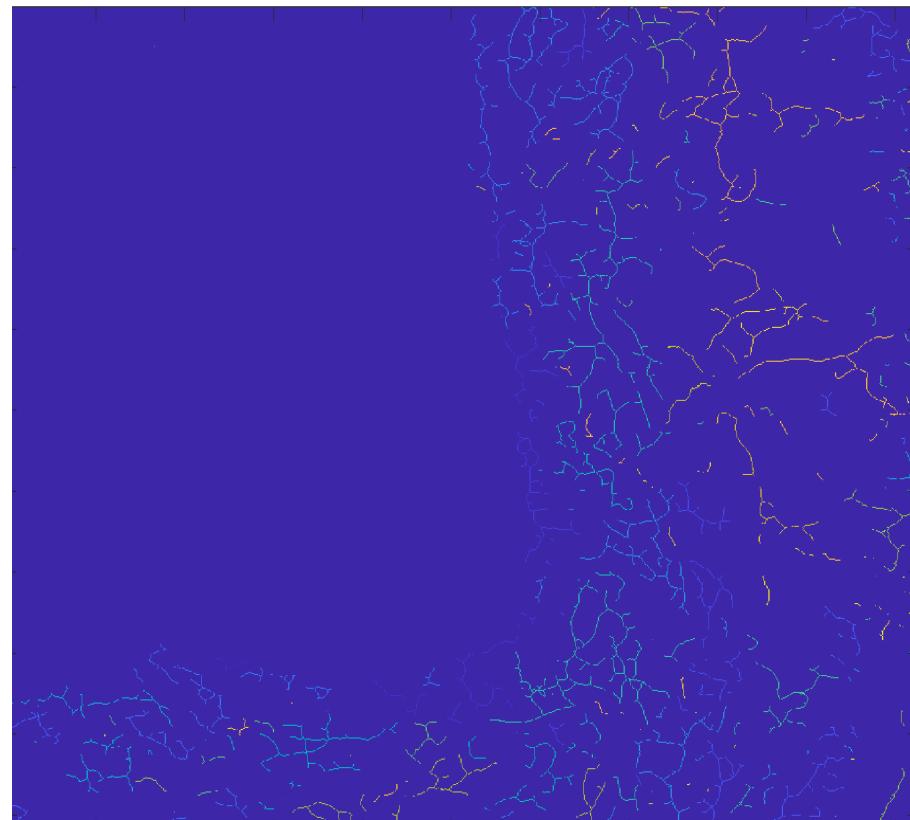


MIP Frangi binarized

# Extensiosn detections : skeletonization and labelling

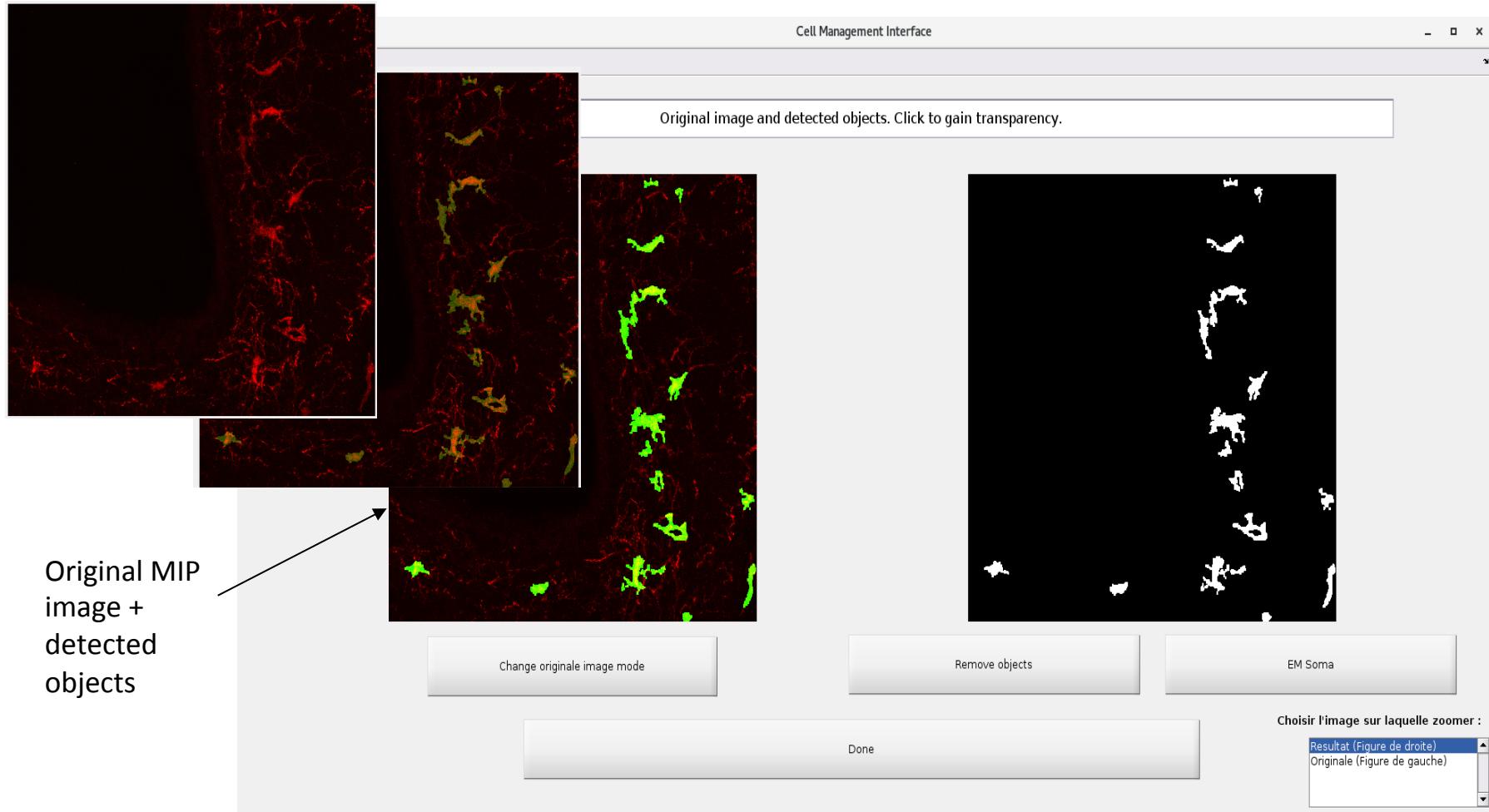


MIP Frangi binarized



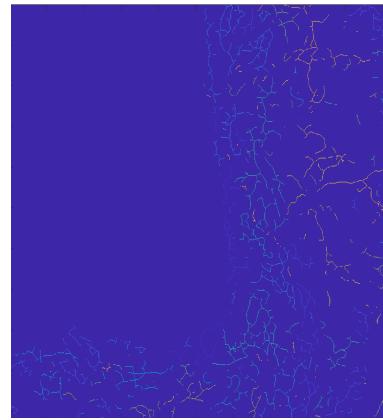
MIP of labeled skeleton

# Somas detection



# Connection between filaments/soma and filaments/filaments

- Closest filaments



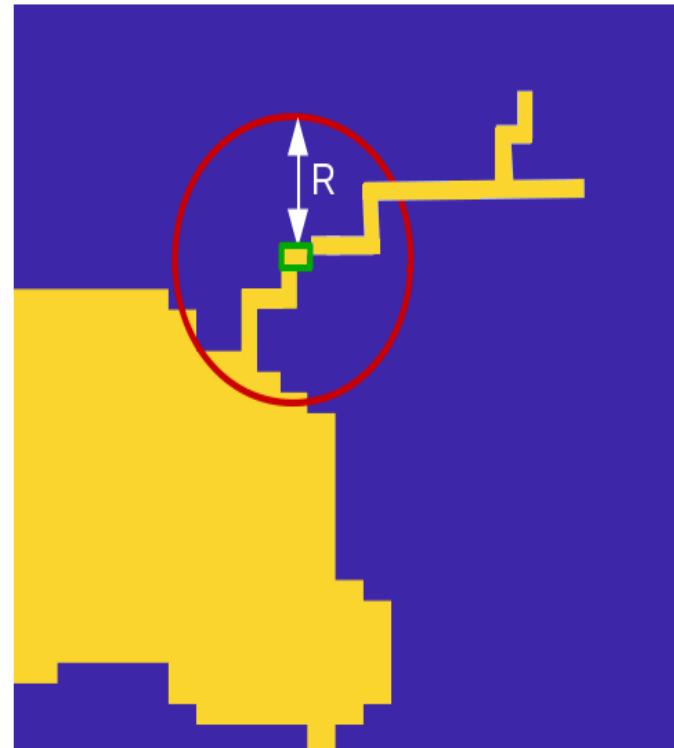
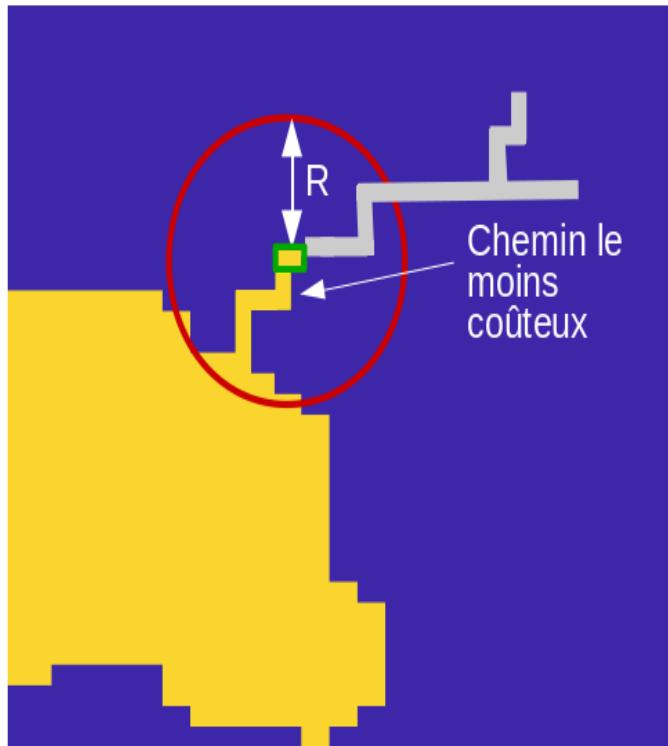
MIP  
extensions



MIP somas

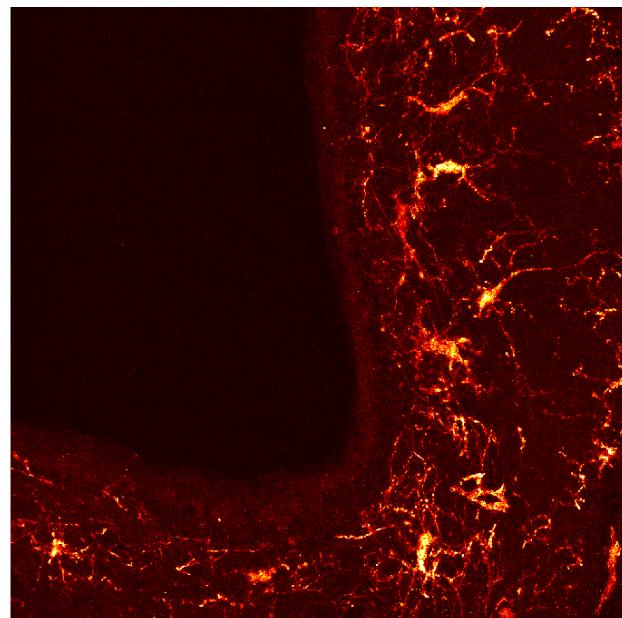
# Connection between filaments/soma and filaments/filaments

- Minimal path : dynamic programming

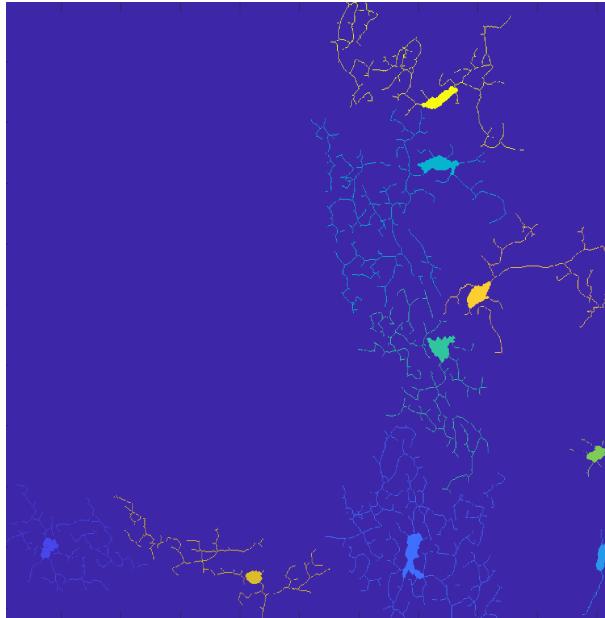


# Connection between filaments/soma and filaments/filaments

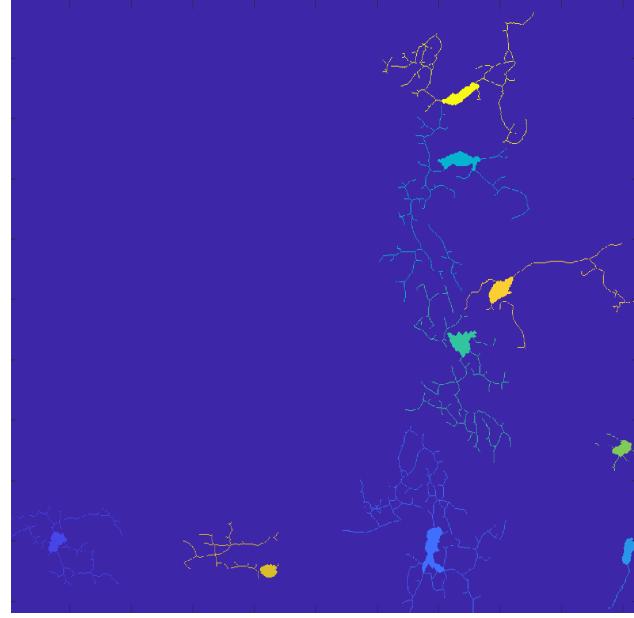
- Threshold on path energy



Original MIP image



Threshold on energy = **Inf**



Threshold on energy = **0.2**

# Features extraction

- **Microglia:**
- **Soma**
  - - Number of main branches
  - - Area, diameter and eccentricity of the soma
  - - Area in which it is located (EM/ARC)
- **Extensions**
  - - Total length
  - - Width (average / median / variance)
- **Main branches**
  - - Median lengths
  - - Average number of branches
- **Branches**
  - - Average length / median / variance