例 6.4

$$\theta_1 = \frac{\Sigma}{r-1} (x_7 - \overline{X})/n , \quad \overline{\theta}_2 = \frac{\Sigma}{r-1} (x_7 - \overline{X})^2/(h-1)$$

$$E(\chi_{\ell})=v$$
, $V(\chi_{\ell})=\sigma^2=E(\chi_{\ell}^2)-\mu^2$

$$E(\bar{\chi}) = \mu \cdot V(\bar{\chi}) = \frac{\sigma^2}{n} = E(\bar{\chi}^2) - \mu^2$$

$$E(\bar{\theta}_1) = E(\frac{E_1(\chi_7 - \bar{\chi})^2}{n}) = \frac{1}{n} E(\frac{N}{2} + N\bar{\chi}^2 - N\bar{\chi}^2)$$

$$= \frac{1}{n} (\lambda \sigma^2 + N\bar{\mu}^2 - \sigma^2 - N\bar{\mu}^2) = \frac{h^{-1}}{n} \sigma^2$$

$$E(\hat{\theta}_{2}) = E\left(\frac{\hat{\Sigma}_{1}(X_{7}-\hat{\chi})^{2}}{n-1}\right) = \frac{1}{n-1}E\left(\frac{\hat{\Sigma}_{1}(X_{7}-\hat{\chi}^{2})}{n-1}\right)$$

$$= \frac{1}{n-1}(n\sigma^{2}+n\sigma^{2}-\sigma^{2}-n\sigma^{2}) = \sigma^{2}$$