Convolutional Neural Networks for Sentence Classification 무사무금

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비디오 카메라로 포착한 정보를 컴퓨터로 처리하는 일

Abstract

We report on a series of experiments with convolutional neural networks (CNN) trained on top of pre-trained word vectors for sentence-level classification tasks. We show that a simple CNN with little hyperparameter tuning and static vectors achieves excellent results on multiple benchmarks. Learning task-specific vectors through fine-tuning offers further gains in performance. / We additionally propose a simple modification to the architecture to allow for the use of both task-specific and static vectors. The CNN models discussed herein improve upon the state of the art on 4 out of 7 tasks, which include sentiment analysis and question classification.

1 Introduction

Deep learning models have achieved remarkable results in computer vision (Krizhevsky et al., 2012) and speech recognition (Graves et al., 2013) in recent years. Within natural language processing, much of the work with deep learning methods has involved learning word vector representations through neural language models (Bengio et al., 2003; Yih et al., 2011; Mikolov et al., 2013) and performing composition over the learned word vectors for classification (Collobert et al., 2011). Word vectors, wherein words are projected from a sparse, 1-of-V encoding (here V is the vocabulary size) onto a lower dimensional vector space via a hidden layer, are essentially feature extractors that encode semantic features of words in their dimensions. In such dense representations, semantically close words are likewise close—in euclidean or cosine distance—in the lower dimensional vector

Convolutional neural networks (CNN) utilize layers with convolving filters that are applied to

local features (LeCun et al., 1998). Originally invented for computer vision, CNN models have subsequently been shown to be effective for NLP and have achieved excellent results in semantic parsing (Yih et al., 2014), search query retrieval (Shen et al., 2014), sentence modeling (Kalchbrenner et al., 2014), and other traditional NLP tasks (Collobert et al., 2011).

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In the present work, we train a simple CNN with the layer of convolution on top of word vectors

one layer of convolution on top of word vectors obtained from an unsupervised neural language model. These vectors were trained by Mikolov et al. (2013) on 100 billion words of Google News, and are publicly available. We initially keep the word vectors static and learn only the other parameters of the model. Despite little tuning of hyperparameters, this simple model achieves excellent results on multiple benchmarks, suggesting that the pre-trained vectors are 'universal' feature extractors that can be utilized for various classification tasks. Learning task-specific vectors through fine-tuning results in further improvements. We finally describe a simple modification to the architecture to allow for the use of both pre-trained and task-specific vectors by having multiple channels.

Our work is philosophically similar to Razavian et al. (2014) which showed that for image classification, feature extractors obtained from a pretrained deep learning model perform well on a variety of tasks—including tasks that are very different from the original task for which the feature extractors were trained.

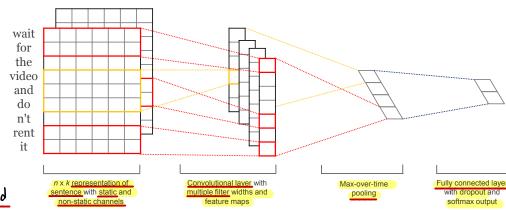
⇒ 다른분아에서도 pre-trained word vectors가 잘먹힘.

2 Model

The model architecture, shown in figure 1, is a slight variant of the CNN architecture of Collobert et al. (2011). Let $\mathbf{x}_i \in \mathbb{R}^k$ be the k-dimensional word vector corresponding to the i-th word in the sentence. A sentence of length n (padded where

¹https://code.google.com/p/word2vec/

भुद्रमा गुरुष्ट्र



* Li ER => K-dimensional word vector + i-th word in the sentence

*filter |WERhk

window of

h words or

: a feature

map

끝에서

적용

Figure 1: Model architecture with two channels for an example sentence.

연명...연等

necessary) is represented as

 \star n : 문장의 길이 \Rightarrow $\mathbf{x}_{1:n} = \mathbf{x}_1 \oplus \mathbf{x}_2 \oplus \ldots \oplus \mathbf{x}_n$,

where \oplus is the concatenation operator. In general, let $\mathbf{x}_{i:i+j}$ refer to the concatenation of words $\mathbf{x}_i, \mathbf{x}_{i+1}, \dots, \mathbf{x}_{i+j}$. A convolution operation involves a *filter*, $\mathbf{w} \in \mathbb{R}^{hk}$, which is applied to a window of h words to produce a new feature. For example, a feature c_i is generated from a window of words/ $\mathbf{x}_{i:i+h-1}$ by

 $c_i = f(\mathbf{w} \cdot \mathbf{x}_{i:i+h-1} + b)$.

: New feature. Here $b \in \mathbb{R}$ is a bias term and f is a non-linear function such as the hyperbolic tangent. This filter 생생하기위해 is applied to each possible window of words in the sentence $\{\mathbf{x}_{1:h}, \mathbf{x}_{2:h+1}, \dots, \mathbf{x}_{n-h+1:n}\}$ to produce a feature map

*ber : bias term
$$\mathbf{c} = [c_1, c_2, \dots, \underline{c_{n-h+1}}],$$
 (3)

with $\mathbf{c} \in \mathbb{R}^{n-h+1}$. We then apply a max-over-*f: nontime pooling operation (Collobert et al., 2011) linear over the feature map and take the maximum value function $\hat{c} = \max\{c\}$ as the <u>feature</u> corresponding to <u>this</u> particular filter. The idea is to capture the most important feature—one with the highest value—for each feature map. This pooling scheme naturally

> deals with variable sentence lengths. (chosen) We have described the process by which <u>one</u> feature is extracted from one filter. The model uses multiple (filters) (with varying window sizes) to obtain multiple features. These features form

the penultimate layer and are passed to a fully connected softmax layer whose output is the probabil-

ity distribution over labels. 두번째의

In one of the model variants, we experiment with having two 'channels' of word vectors—one

결국, 마시막경화장은 Labels of CHit Probability distribution"

미세조생들한 that is kept static throughout training and one that is fine-tuned via backpropagation (section 3.2).² In the multichannel architecture, illustrated in figure 1, each filter is applied to both channels and the results are added/to calculate c_i in equation (2). The model is otherwise equivalent to the single channel architecture.

2.1 Regularization (1 직한, 규칙화)

For <u>regularization</u> we employ dropout on the penultimate layer with a constraint on l_2 -norms of the weight vectors (Hinton et al., 2012). Dropout prevents co-adaptation of hidden units by randomly dropping out—{i.e., setting to zero—a proportion p of the hidden units during fowardbackpropagation. That is, given the penultimate layer $\mathbf{z} = [\hat{c}_1, \dots, \hat{c}_m]$ (note that here we have mfilters), instead of using

for output unit y in forward propagation, dropout uses

 $y = \mathbf{w} \cdot \mathbf{z} + b$

 $y = \mathbf{w} \cdot (\mathbf{z} \circ \mathbf{r}) + b,$ _ element all 적용하여 일이내는 것.

where o is the element-wise multiplication operator and $\mathbf{r} \in \mathbb{R}^m$ is a 'masking' vector of Bernoulli random variables with probability p of being 1. Gradients are backpropagated only through the unmasked units. At test time, the learned weight vectors are scaled by p such that $\hat{\mathbf{w}} = p\mathbf{w}$, and w) is used (without dropout) to score unseen sentences. We additionally constrain l_2 -norms of the weight vectors by rescaling (w) to have $||\mathbf{w}||_2 = s$ whenever $||\mathbf{w}||_2 > s$ after a gradient descent step.

²We employ language from computer vision where a color image has red, green, and blue channels.

> 경사도,변화도 : EZI난 Unit을 닿해서만 역전달됨. * |2-norms of the weight vectors를 <u>wirescaling</u> HM 제한.(IIWII2>5 인패HOLOF |IWII2=S 이각제!!)

2924 filter both channels \downarrow equation(2) 에 대해져서

C; 들계산

(4) ← 이거대신, dropoute

신이얼사용

*re Rm : 'masking' vector with

probability

p) of being

• MPQA: Opinion polarity detection subtask of the MPOA dataset (Wiebe et al., 2005).⁷

3.1 Hyperparameters and Training

For all datasets we use: rectified linear units, filter windows (h) of 3, 4, 5 with 100 feature maps each, dropout rate (p) of 0.5, l_2 constraint (s) of 3, and mini-batch size of 50. These values were chosen via a grid search on the SST-2 dev set.

We do not otherwise perform any datasetspecific tuning other than early stopping on dev sets. For datasets without a standard dev set we randomly select 10% of the training data(as)the dev set. Training is done through stochastic gradient descent over shuffled mini-batches with the Adadelta update rule (Zeiler, 2012).

3.2 Pre-trained Word Vectors

Initializing word vectors with those obtained from an unsupervised neural language model is a popular method to improve performance in the absence of a large supervised training set (Collobert et al., 2011; Socher et al., 2011; Iyyer et al., 2014). We use the publicly available word2vec vectors that were trained on 100 billion words from Google News. The vectors have dimensionality of 300 and were trained using the continuous bag-of-words architecture (Mikolov et al., 2013). Words not present in the set of pre-trained words are initialized randomly.

3.3 Model Variations

We experiment with several variants of the model.

- CNN-rand: Our baseline model where all words are randomly initialized and then modified during training. ⁽ 칼기호난
- CNN-static: A model with pre-trained vectors from word2vec. All wordsincluding the unknown ones that are randomly initialized—are kept static and only the other parameters of the model are learned.
- CNN-non-static: Same as above but the pretrained vectors are fine-tuned for each task.
- CNN-multichannel: A model with two sets of word vectors. Each set of vectors is treated as a 'channel' and each filter is applied

⁷http://www.cs.pitt.edu/mpqa/

Data	c	l	N	V	$ V_{pre} $	Test
MR	2	20	10662	18765	16448	CV
SST-1	5	18	11855	17836	16262	2210
SST-2	2	19	9613	16185	14838	1821
Subj	2	23	10000	21323	17913	CV
TREC	6	10	5952	9592	9125	500
CR	2	19	3775	5340	5046	CV
MPOA	2	3	10606	6246	6083	CV

Table 1: Summary statistics for the datasets after tokenization. c: Number of target classes. l: Average sentence length. N: Dataset size. |V|: Vocabulary size. $|V_{pre}|$: Number of words present in the set of pre-trained word vectors. Test: Test set size (CV means there was no standard train/test split and thus 10-fold CV was used).

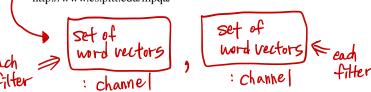
Datasets and Experimental Setup

We test our model on various benchmarks. Summary statistics of the datasets are in table 1.

- MR: Movie reviews with one sentence per review. Classification involves detecting positive/negative reviews (Pang and Lee, 2005).³
- SST-1: Stanford Sentiment Treebank—an extension of MR but with train/dev/test splits provided and fine-grained labels (very positive, positive, neutral, negative, very negative), re-labeled by Socher et al. (2013).⁴
- SST-2: Same as SST-1 but with neutral reviews removed and binary labels. (only +/-)
- Subj: Subjectivity dataset where the task is to classify a sentence as being subjective or objective (Pang and Lee, 2004).
- TREC: TREC question dataset—task involves classifying a question into 6 question types (whether the question is about person, location, numeric information, etc.) (Li and Roth, 2002).⁵
- CR: Customer reviews of various products (cameras, MP3s etc.). Task is to predict positive/negative reviews (Hu and Liu, 2004).6

⁶http://www.cs.uic.edu/~liub/FBS/sentiment-analysis.html





잘 정리된

³https://www.cs.cornell.edu/people/pabo/movie-review-data/ ⁴http://nlp.stanford.edu/sentiment/ Data is actually provided at the phrase-level and hence we train the model on both phrases and sentences but only score on sentences at test time, as in Socher et al. (2013), Kalchbrenner et al. (2014), and Le and Mikolov (2014). Thus the training set is an order of magnitude larger than listed in table 1.

⁵http://cogcomp.cs.illinois.edu/Data/QA/QC/

Model	MR	SST-1	SST-2	Subj	TREC	CR	MPQA
CNN-rand	76.1	45.0	82.7	89.6	91.2	79.8	83.4
CNN-static		45.5	86.8	93.0	92.8	84.7	89.6
CNN-non-static	81.5	48.0	87.2	93.4	93.6	84.3	89.5
CNN-multichannel	81.1	47.4	88.1	93.2	92.2	85.0	89.4
RAE (Socher et al., 2011)	77.7	43.2	82.4	_	_	_	86.4
MV-RNN (Socher et al., 2012)	79.0	44.4	82.9	_	_	_	_
RNTN (Socher et al., 2013)	_	45.7	85.4	_	_	_	_
DCNN (Kalchbrenner et al., 2014)	_	48.5	86.8	_	93.0	_	_
Paragraph-Vec (Le and Mikolov, 2014)	_	48.7	87.8	_	_	_	_
CCAE (Hermann and Blunsom, 2013)	77.8	_		_	_	_	87.2
Sent-Parser (Dong et al., 2014)	79.5	_	_	_	_	_	86.3
NBSVM (Wang and Manning, 2012)	79.4	_	_	93.2	_	81.8	86.3
MNB (Wang and Manning, 2012)	79.0	_	_	93.6	_	80.0	86.3
G-Dropout (Wang and Manning, 2013)	79.0	_	_	93.4	_	82.1	86.1
F-Dropout (Wang and Manning, 2013)	79.1	_	_	93.6	_	81.9	86.3
Tree-CRF (Nakagawa et al., 2010)	77.3	_	_	_	_	81.4	86.1
CRF-PR (Yang and Cardie, 2014)	_	_	_	_	_	82.7	_
SVM_S (Silva et al., 2011)	_	_	_	_	95.0		

Table 2: Results of our CNN models against other methods. RAE: Recursive Autoencoders with pre-trained word vectors from Wikipedia (Socher et al., 2011). MV-RNN: Matrix-Vector Recursive Neural Network with parse trees (Socher et al., 2012). RNTN: Recursive Neural Tensor Network with tensor-based feature function and parse trees (Socher et al., 2013). DCNN: Dynamic Convolutional Neural Network with k-max pooling (Kalchbrenner et al., 2014). Paragraph-Vec: Logistic regression on top of paragraph vectors (Le and Mikolov, 2014). CCAE: Combinatorial Category Autoencoders with combinatorial category grammar operators (Hermann and Blunsom, 2013). Sent-Parser: Sentiment analysis-specific parser (Dong et al., 2014). NBSVM, MNB: Naive Bayes SVM and Multinomial Naive Bayes with uni-bigrams from Wang and Manning (2012). G-Dropout, F-Dropout: Gaussian Dropout and Fast Dropout from Wang and Manning (2013). Tree-CRF: Dependency tree with Conditional Random Fields (Nakagawa et al., 2010). CRF-PR: Conditional Random Fields with Posterior Regularization (Yang and Cardie, 2014). SVMs: SVM with uni-bi-trigrams, wh word, head word, POS, parser, hypernyms, and 60 hand-coded rules as features from Silva et al. (2011).

to both channels, but gradients are back-propagated only through one of the channels. Hence the model is able to fine-tune one set of vectors while keeping the other static. Both channels are initialized with word2vec.

In order to disentangle the effect of the above variations versus other random factors, we eliminate other sources of randomness—CV-fold assignment, initialization of unknown word vectors, initialization of CNN parameters—by keeping them uniform within each dataset.

4 Results and Discussion

Results of our models against other methods are listed in table 2. Our baseline model with all randomly initialized words (CNN-rand) does not perform well on its own. While we had expected performance gains through the use of pre-trained vectors, we were surprised at the magnitude of the gains. Even a simple model with static vectors (CNN-static) performs remarkably well, giving

* overfitting : sample의 size보다 너무 많은 parameters 를 사용하는 모델이 갖는 문제점으로, sample data에는 good fit 하지만, 새로운 data에 대해서는 poor fit한 것. competitive results against the more sophisticated deep learning models that utilize complex pooling schemes (Kalchbrenner et al., 2014) or require parse trees to be computed beforehand (Socher et al., 2013). These results suggest that the pretrained vectors are good, 'universal' feature extractors and can be utilized across datasets. Finetuning the pre-trained vectors for each task gives still further improvements (CNN-non-static).

4.1 Multichannel vs. Single Channel Models

We had initially hoped that the multichannel arintecture would prevent overfitting (by ensuring
that the learned vectors do not deviate too far
from the original values) and thus work better than
the single channel model, especially on smaller
datasets. The results, however, are mixed, and further work on regularizing the fine-tuning process
is warranted. For instance, instead of using an
additional channel for the non-static portion, one
could maintain a single channel but employ extra
dimensions that are allowed to be modified during
training.

정단·단당하게 되다. (fine-tuning process 를 regularize하는 작眠이 필요해짐)

*multi-channel일 필없이 약하였고, single channel에다가 <u>training 국제 modified 되는</u> dimensions를 가능면됨.

구분하다.

	Most Similar Words for				
	Static Channel	Non-static Channel			
bad	good	terrible			
	terrible	horrible			
	horrible	lousy			
	lousy	stupid			
good	great	nice $\sqrt{}$			
	bad	decent			
	terrific	solid			
	decent	terrific			
n't	os	not			
	ca	never			
	ireland	nothing			
	wo	neither			
!	2,500	2,500			
	entire	lush			
	jez,	beautiful			
	changer	terrific			
,	decasia	but			
	abysmally	dragon			
	demise	a			
	valiant	and			

Table 3: Top 4 neighboring words—based on cosine similarity—for vectors in the static channel (left) and fine-tuned vectors in the non-static channel (right) from the multichannel model on the SST-2 dataset after training.

4.2 Static vs. Non-static Representations

As is the case with the single channel non-static model, the multichannel model is able to fine-tune the non-static channel to make it more specific to the task-at-hand. For example, good is most similar to bad in word2vec, presumably because they are (almost) syntactically equivalent. But for vectors in the non-static channel that were fine-tuned on the SST-2 dataset, this is no longer the case (table 3). Similarly, good is arguably closer to nice than it is to great for expressing sentiment, and this is indeed reflected in the learned vectors.

For (randomly initialized) tokens not in the set of pre-trained vectors, fine-tuning allows them to learn more meaningful representations: the network learns that exclamation marks are associated with effusive expressions and that commas are conjunctive (table 3).

4.3 Further Observations

We report on some further experiments and observations:

• Kalchbrenner et al. (2014) report much worse results with a CNN that has essentially

the same architecture as our single channel model. For example, their Max-TDNN (Time Delay Neural Network) with randomly initialized words obtains 37.4% on the SST-1 dataset, compared to 45.0% for our model. We attribute such discrepancy to our CNN having much more capacity (multiple filter widths and feature maps).

- Dropout proved to be such a good regularizer that it was fine to use a larger than necessary network and simply let dropout regularize it.
 Dropout consistently added 2%-4% relative performance.
- When randomly initializing words not in word2vec, we obtained slight improvements by sampling each dimension from U[-a,a] where a was chosen such that the randomly initialized vectors have the same variance as the pre-trained ones. It would be interesting to see if employing more sophisticated methods to mirror the distribution of pre-trained vectors in the initialization process gives further improvements.
- We briefly experimented with another set of publicly available word vectors trained by Collobert et al. (2011) on Wikipedia, and found that word2vec gave far superior performance. It is not clear whether this is due to Mikolov et al. (2013) architecture or the 100 billion word Google News dataset.
- Adadelta (Zeiler, 2012) gave similar results to Adagrad (Duchi et al., 2011) but required fewer epochs.

5 Conclusion

In the present work we have described a series of experiments with convolutional neural networks built on top of word2vec. Despite little tuning of hyperparameters, a simple CNN with one layer of convolution performs remarkably well. Our results add to the well-established evidence that unsupervised pre-training of word vectors is an important ingredient in deep learning for NLP.

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나 마산기지 ' 로

구문적으로 동등하기 때문

चेक्ता एउन्स्र

년합#는, 정독사의

⁸http://ronan.collobert.com/senna/

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