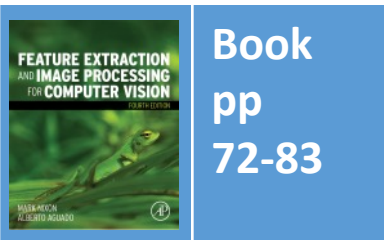


Lecture 4 Point Operators

COMP6223 Computer Vision (MSc)

**How many different operators are there on
image points?**



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Southampton
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and Computer Science

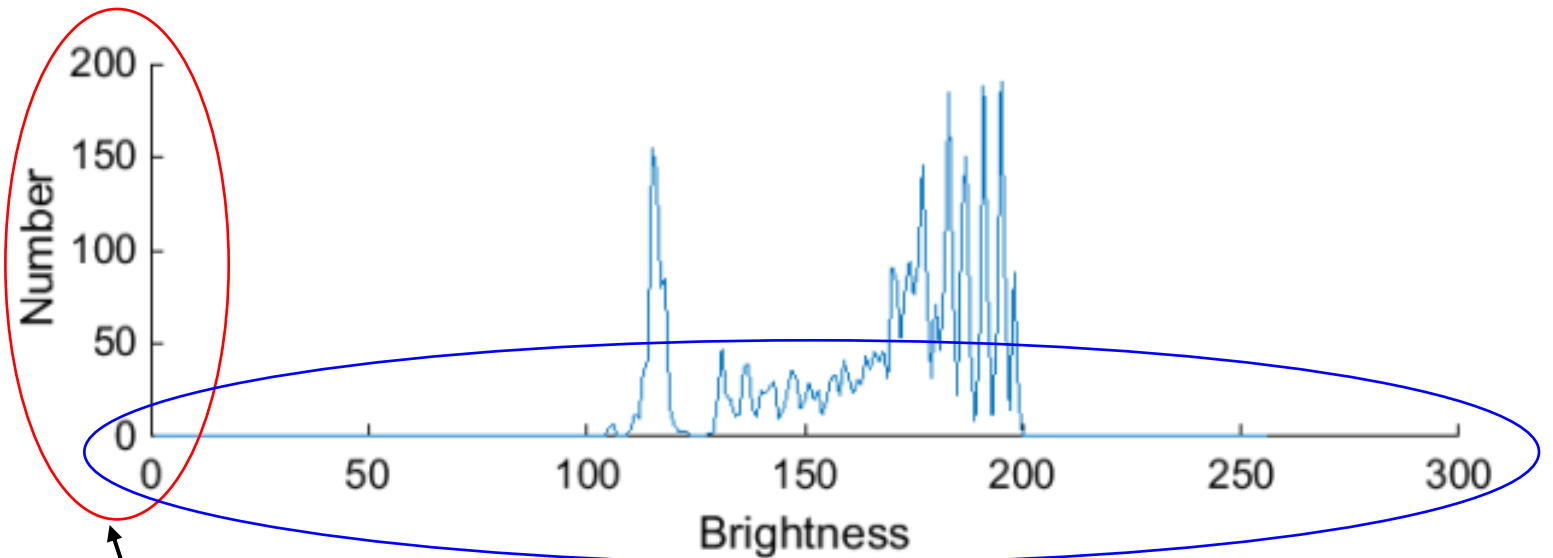
Content

1. How do we best display images?
2. What operators are available; which work solely on image points?

An image and its histogram



(a) image of an eye



(b) histogram of eye image

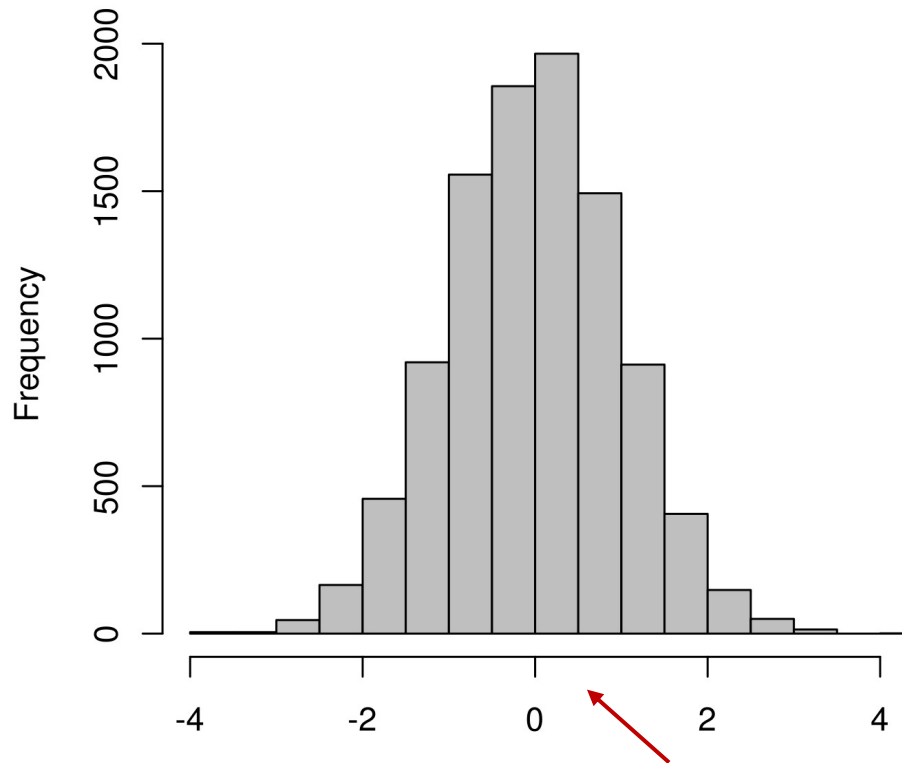
- The histogram plots **the number of pixels** with a particular brightness level
- The histogram shows **contrast** (the range of brightness levels)



Different Histograms

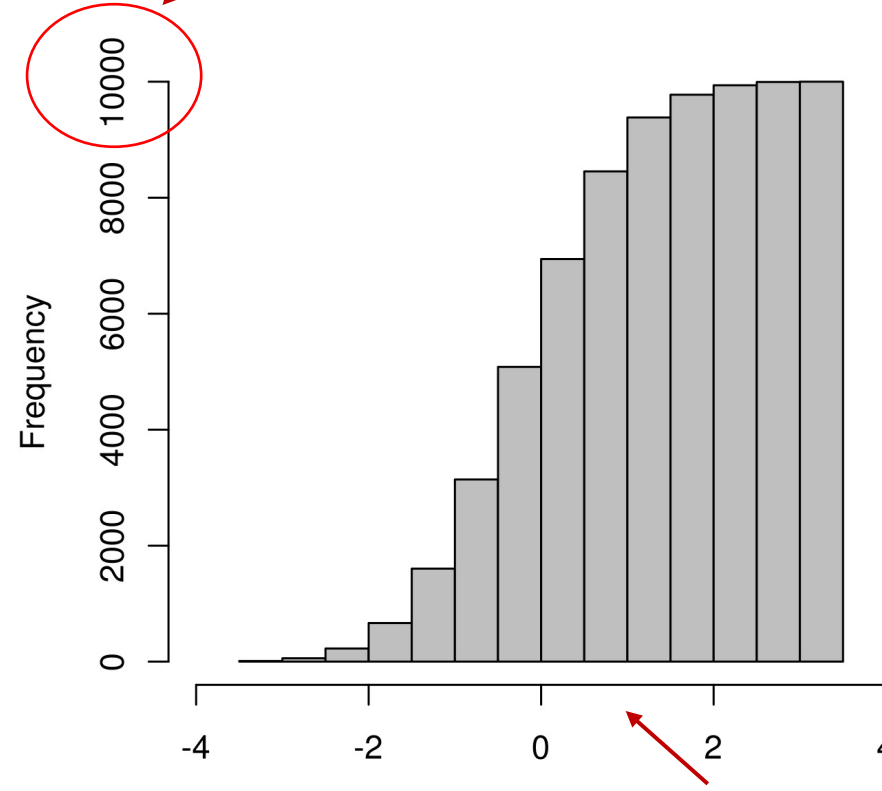
- Example: Histogram of 10000 points in $[-4, 4]$

Ordinary histogram



rnorm(10000) the number of pixels
with a particular value

Cumulative histogram



rnorm(10000) the number of pixels
 \leq a particular value

Can also be scaled so that the highest frequency is **1** by dividing the total number of pixels/points

Modifying Image Intensity

by **choosing** values for k and l

new image

scalar and level

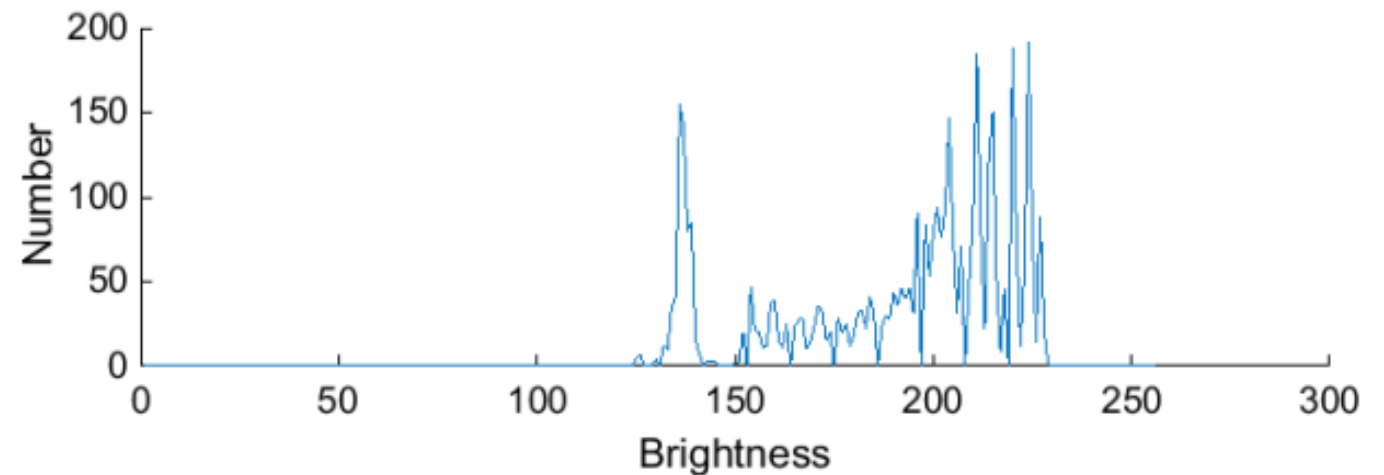
$$\mathbf{N}_{x,y} = k \times \mathbf{O}_{x,y} + l$$

coordinates

old image



(a) image of brighter eye

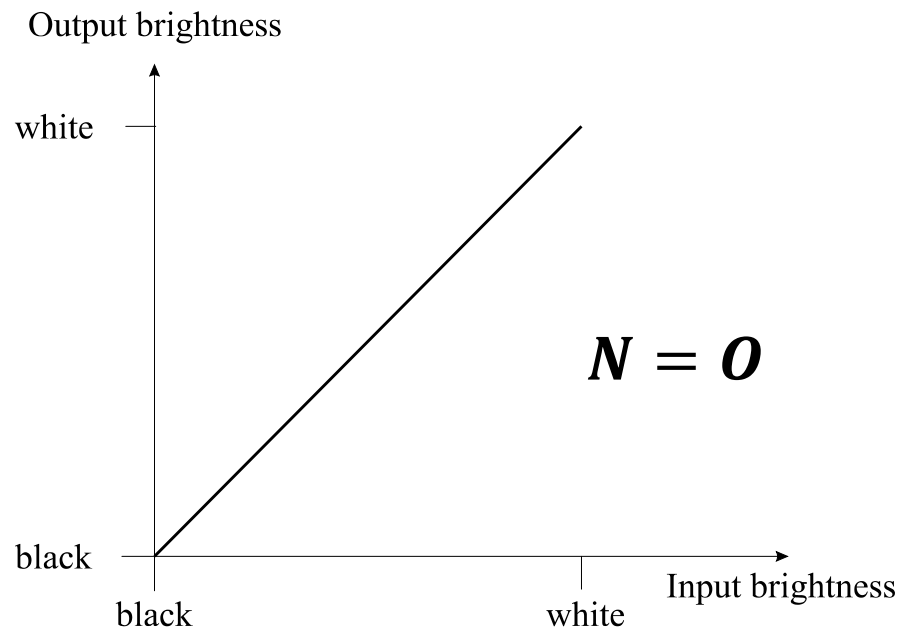


(b) histogram of brighter eye

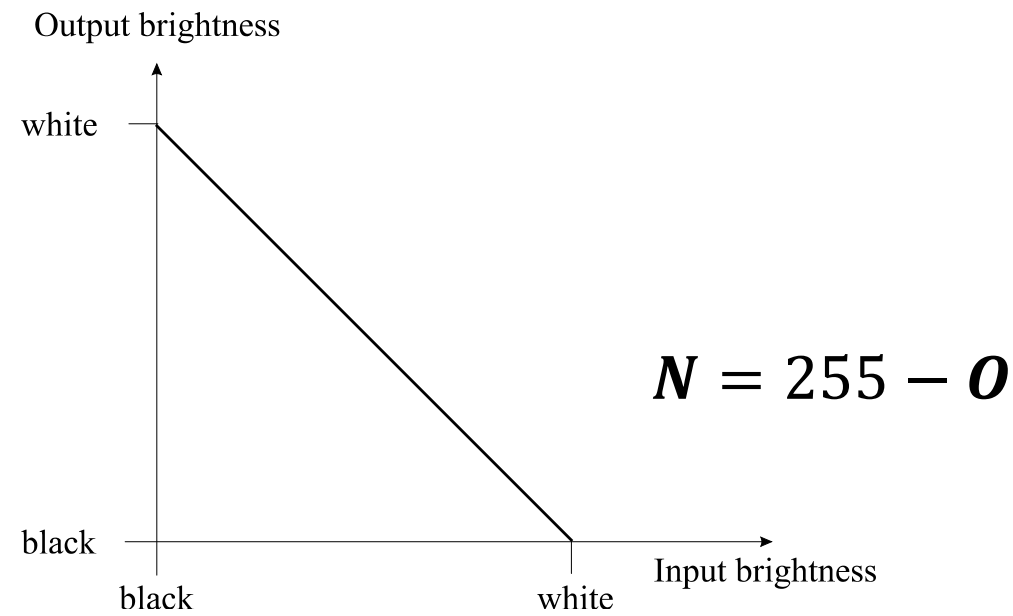
Brightening an Image



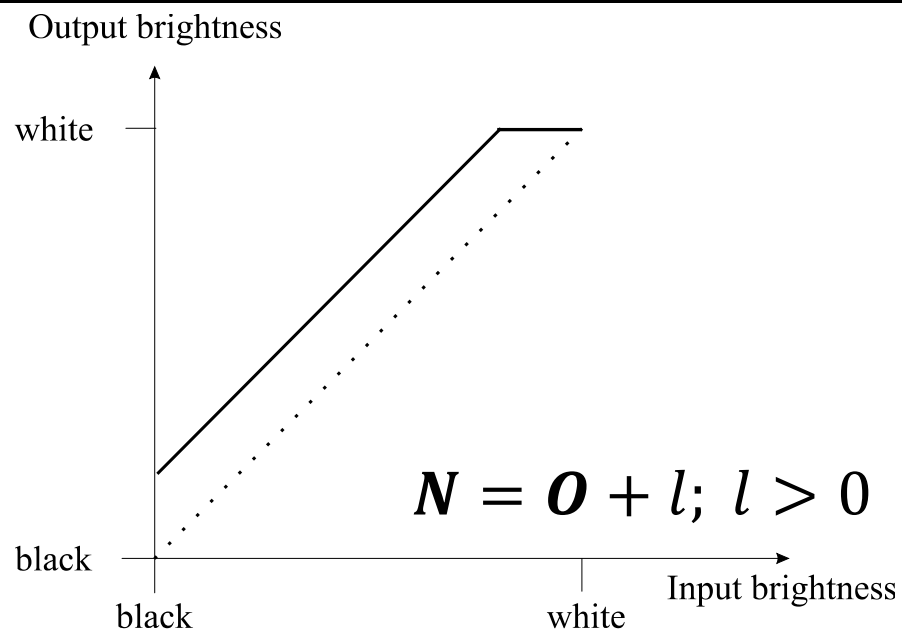
Intensity mappings



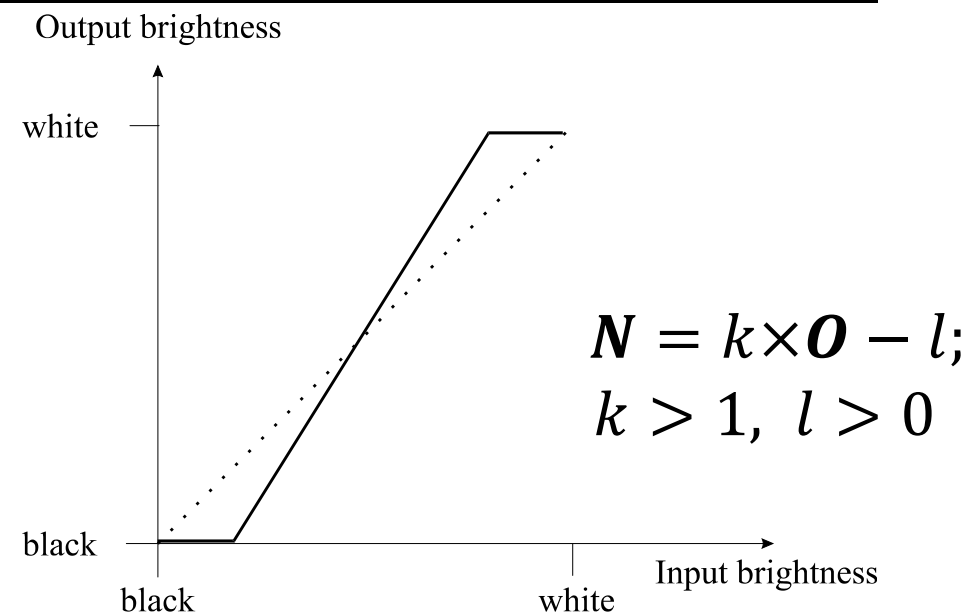
(a) copy



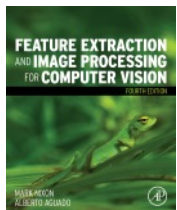
(b) brightness inversion



(c) brightness addition



(d) brightness scaling by multiplication



Applying exponential and logarithmic point operators

Brightness compression

$$\mathbf{N}_{x,y} = \log(\mathbf{O}_{x,y})$$



(a) logarithmic compression

Brightness expansion

$$\mathbf{N}_{x,y} = \exp(\mathbf{O}_{x,y})$$



(b) exponential expansion

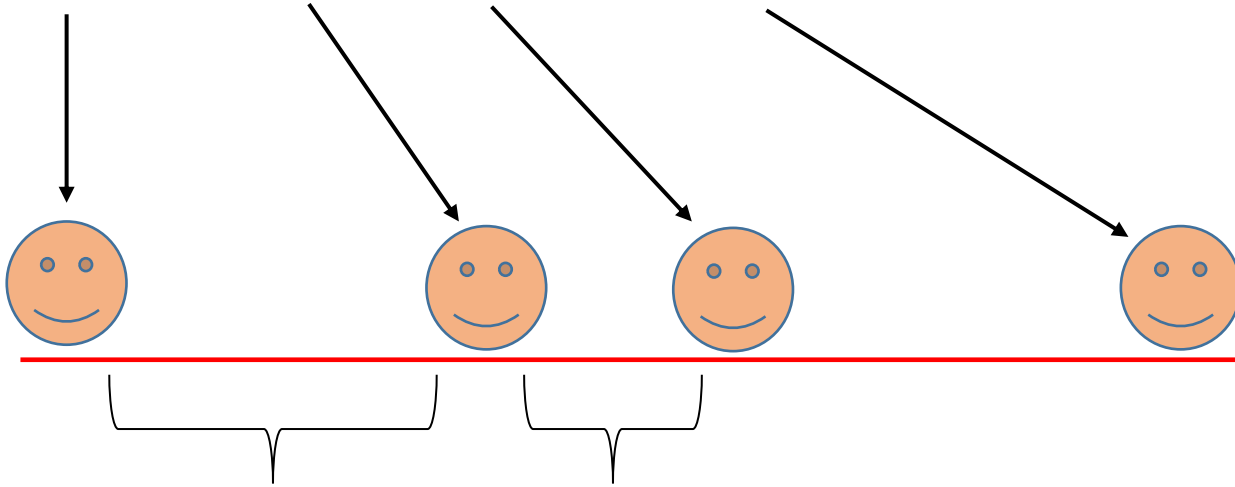
Intensity normalisation

Toy example

Before normalization:



After normalization
(whole range used):

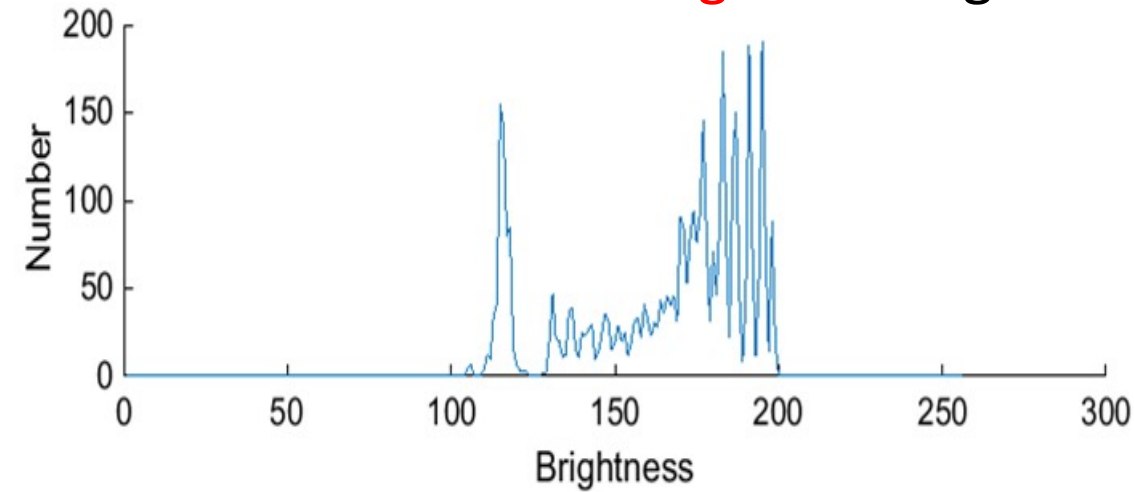


The ratio between the distances
of these smileys is kept

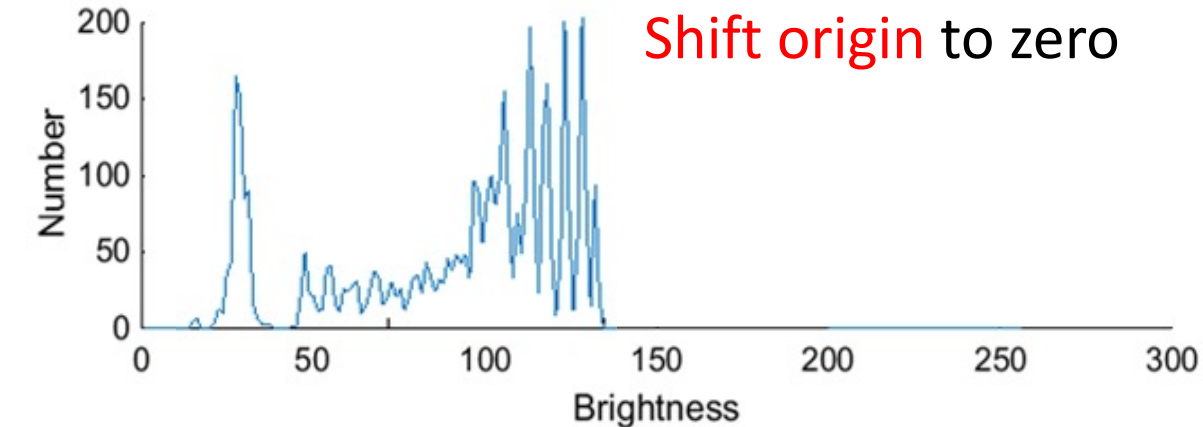
Intensity normalisation

Aim is to use **all** available grey levels for display

Original histogram



Shift origin to zero



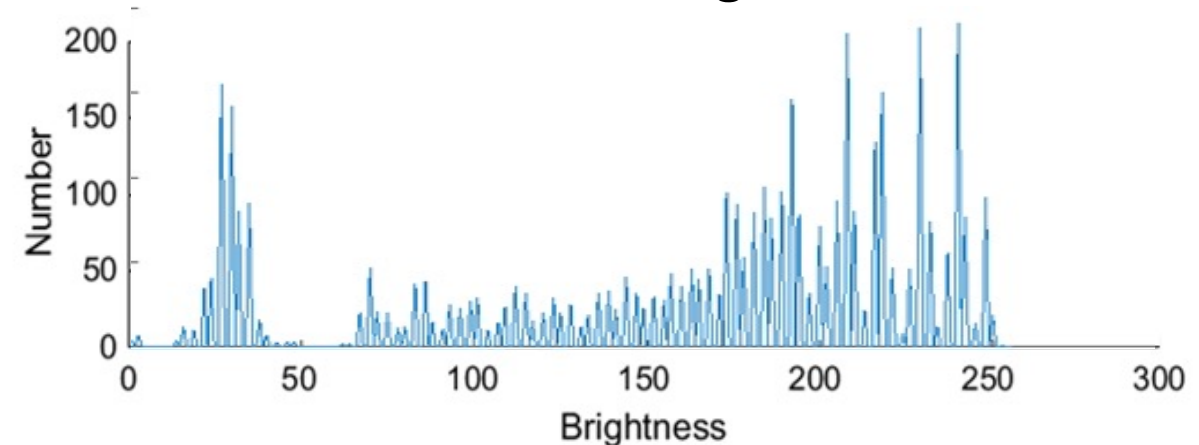
Min and Max of the new image

$$N_{x,y} = \frac{N_{max} - N_{min}}{O_{max} - O_{min}} \times (O_{x,y} - O_{min}) + N_{min}$$

Min and Max of the original/old image

E.g.: $N_{max} = 255$;
 $N_{min} = 0$

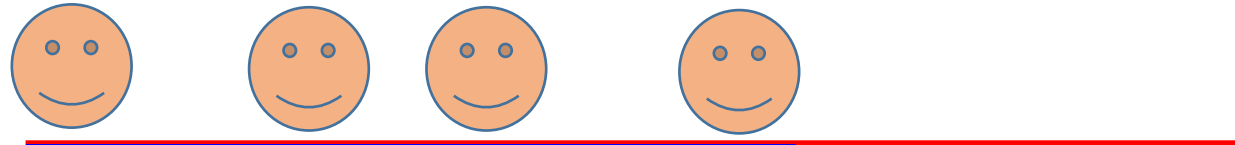
Scale brightness to use
the whole range



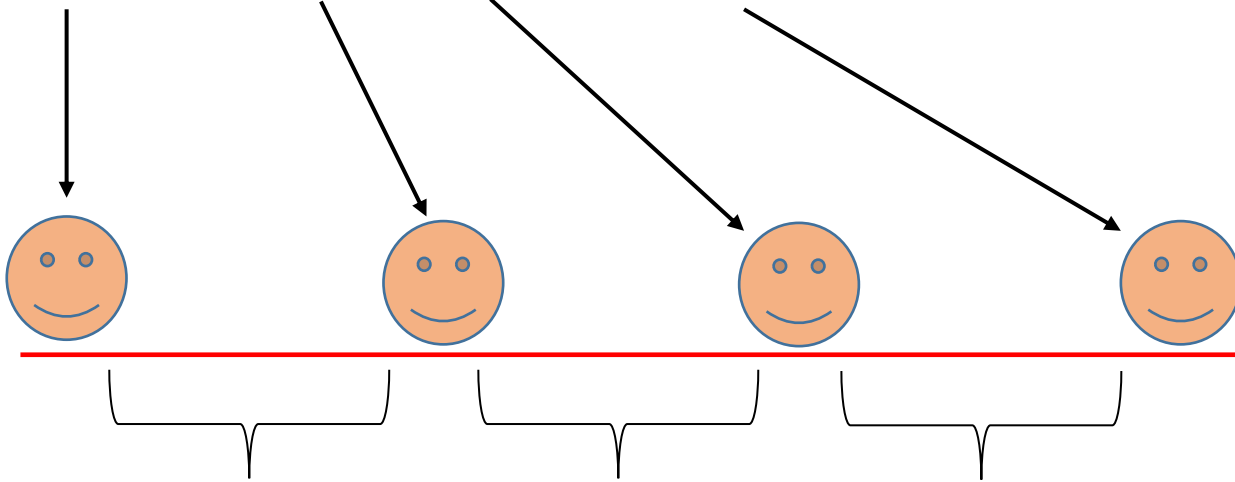
Histogram Equalisation

Toy example

Before normalization:



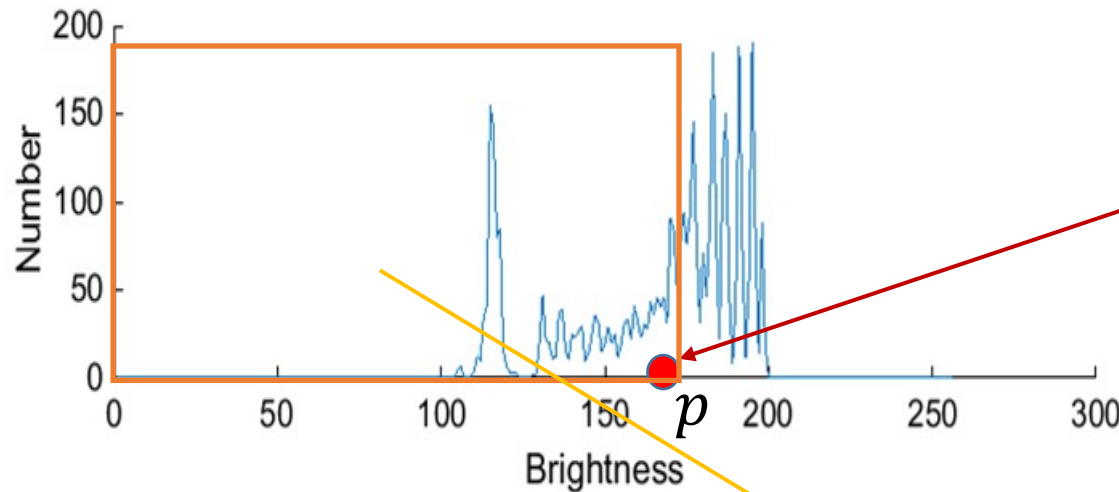
After equalisation
(whole range used):



Same distance between
two adjacent smileys

Histogram Equalisation – aim is a flat histogram

Original histogram



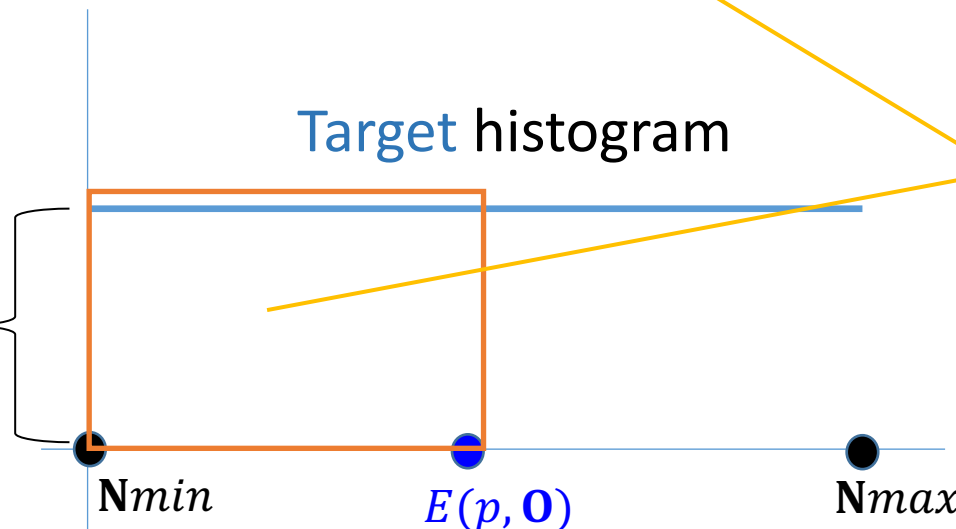
N^2 points in the original and equalised images

$\mathbf{O}(p)$: the histogram at level p
 $\sum_{l=0}^p \mathbf{O}(l)$: the cumulative histogram up to level p

$E(p, \mathbf{O})$: the level after equalisation

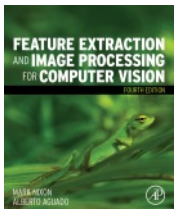
$$\frac{N^2}{N_{max} - N_{min}}$$

Target histogram

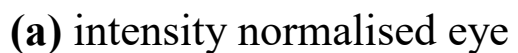


$$\frac{N^2}{N_{max} - N_{min}} (E(p, \mathbf{O}) - N_{min}) = \sum_{l=0}^p \mathbf{O}(l)$$

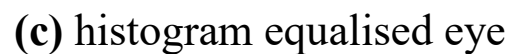
$$E(p, \mathbf{O}) = \frac{N_{max} - N_{min}}{N^2} \sum_{l=0}^p \mathbf{O}(l) + N_{min}$$



Intensity normalisation and histogram equalisation

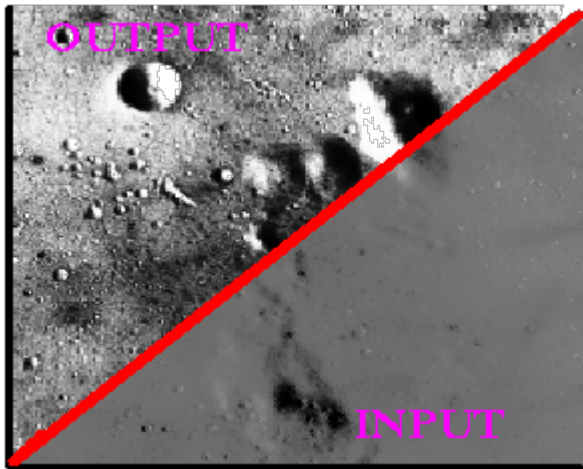


Used in
Matlab's
imagesc



Aimed for
human vision

Applying Histogram Equalisation



<http://homepages.inf.ed.ac.uk/rbf/HIPR2/histeq.htm>

http://docs.opencv.org/doc/tutorials/imgproc/histograms/histogram_equalization/histogram_equalization.html

Thresholding

Thresholding selects points that **exceed** a chosen threshold τ

$$N_{x,y} = \begin{cases} 255, & \text{if } O_{x,y} > \tau \\ 0, & \text{otherwise} \end{cases}$$

coordinates



An eye image



After thresholding



Thresholding: Manual vs Automatic



An eye image



Thresholding: $\tau = 160$



Automatic thresholding
by Otsu: $\tau = 127$

Otsu Thresholding

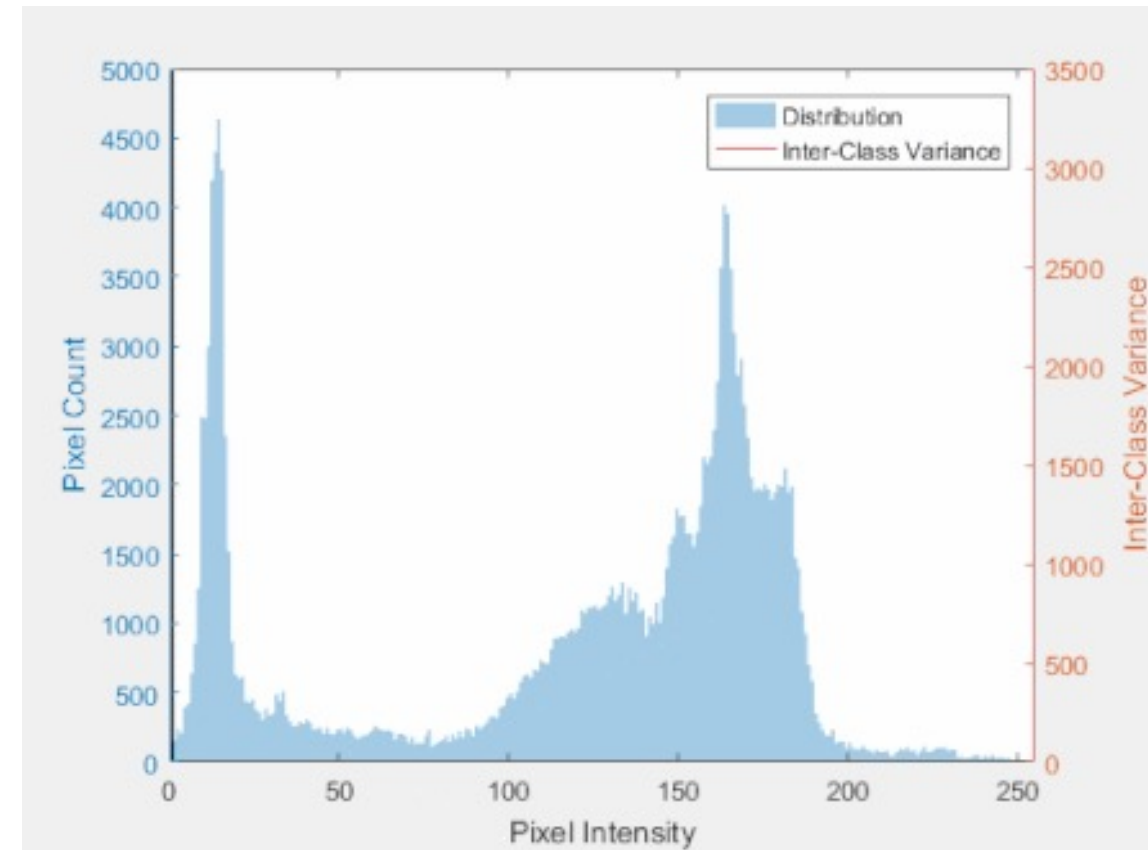
Per cent of the number of pixels in each group (separated by τ) against the total number of pixels

$$\max_{\tau} \omega_0(\tau) \omega_1(\tau) [\mu_0(\tau) - \mu_1(\tau)]^2$$

Inter-class variance

Mean of the two groups separated by τ

Diagram annotations: Two blue arrows point from the text "Per cent of the number of pixels in each group (separated by τ) against the total number of pixels" to $\omega_0(\tau)$ and $\omega_1(\tau)$ in the formula. A bracket above the formula spans from $\mu_0(\tau)$ to $\mu_1(\tau)$ and is labeled "Inter-class variance". Two red arrows point from the text "Mean of the two groups separated by τ " to $\mu_0(\tau)$ and $\mu_1(\tau)$ in the formula.



Thresholding an image of a walking subject



(a) walking subject



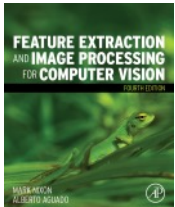
(b) automatic thresholding by Otsu

Many consider that **shape** concerns a **higher** level

Main points so far

1. **point operators** are largely about image display
2. concern **histogram** manipulation
3. **thresholding** used a lot
4. **intensity normalisation** used for display

Need sets of points. That's group operators, coming next.



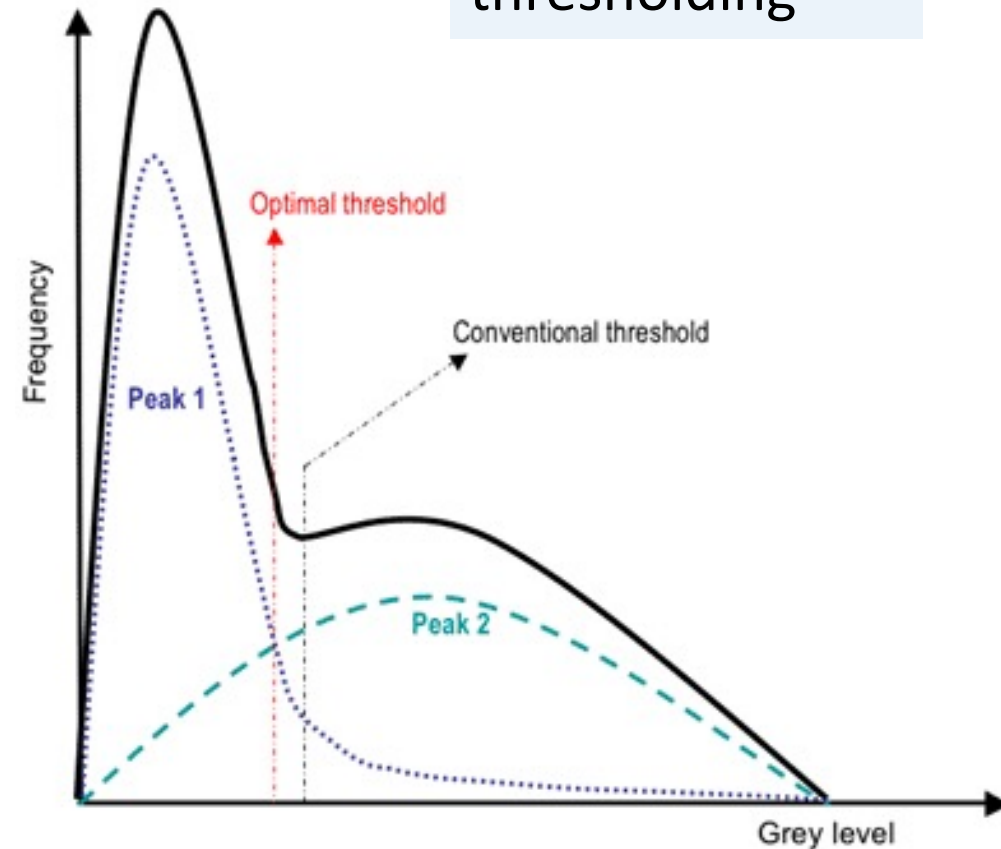
Adaptive Thresholding

Starting with an initialization $\tau^{(0)}$, e.g. the mean of given image, find a proper threshold iteratively by

Mean of the two groups
separated by $\tau^{(i)}$

$$\tau^{(i+1)} = \frac{\mu_0(\tau^{(i)}) + \mu_1(\tau^{(i)})}{2}$$

Other advanced
thresholding



Other thresholding techniques...

