

To Big 1a7 | 정지/전 주자.

NN Basics

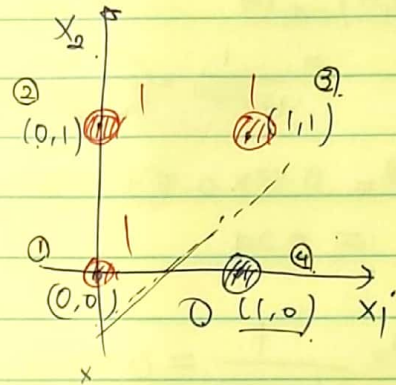
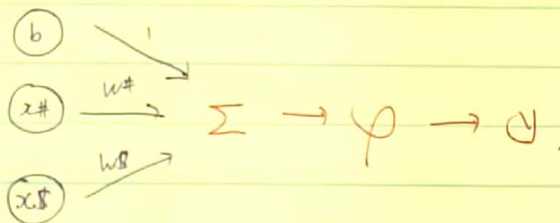
이동

$$1) \sigma(z) = \frac{1}{1 + \exp(-z)} = \frac{1}{1 + e^{-z}}$$

$$\frac{d\sigma(z)}{dz} = \frac{-e^{-z} \cdot (-1)}{(1+e^{-z})^2} = \frac{e^{-z}}{(1+e^{-z})^2} = \frac{1+e^{-z}-1}{(1+e^{-z})^2} = \frac{1}{(1+e^{-z})} - \frac{1}{(1+e^{-z})^2}$$

$$= \sigma(z) - (\sigma(z))^2 = \sigma(z)(1 - \sigma(z))$$

2)



$$1) \sigma(w_1 x_1 + w_2 x_2 + \text{bias}) \begin{cases} 0 & (z < 0) \\ 1 & (z \geq 0) \end{cases}$$

Let $w_1 = -1$, $w_2 = +1$, $\text{bias} = 0.5$.

$$z = -x_1 + x_2 + 0.5. \quad \sigma(1) = 0, \sigma(0.5) = 1, \quad \sigma(3) = \sigma(0.5) = 1$$

$$\sigma(2) = \sigma(1.5) = 1, \quad \sigma(4) = \sigma(-0.5) = 0.$$

→ 분류 잘못됨.

2) Parameter updates.

$$w_1 = 1, w_2 = -1, \text{bias} = 0.5 \rightarrow z = x_1 - x_2 + 0.5$$

$$\sigma(1) = \sigma(0.5) = 1, \quad \sigma(3) = \sigma(0.5) = 1$$

$$\sigma(2) = \sigma(-0.5) = 0, \quad \sigma(4) = \sigma(1.5) = 1 \rightarrow \text{update 3과 4}$$

Let $t = 0.5$.

$$\text{bias} \leftarrow \text{bias} + 0.1(1 - 0) \times 1 \rightarrow \text{bias} = 1.5$$

$$w_1 \leftarrow w_1 + 0.1(1 - 0) \times 0 \rightarrow w_1 = 1$$

$$w_2 \leftarrow w_2 + 0.1(1 - 0) \times 1 \rightarrow w_2 = -0.9$$

$$\Rightarrow z = x_1 - 0.9x_2 + 1.5$$

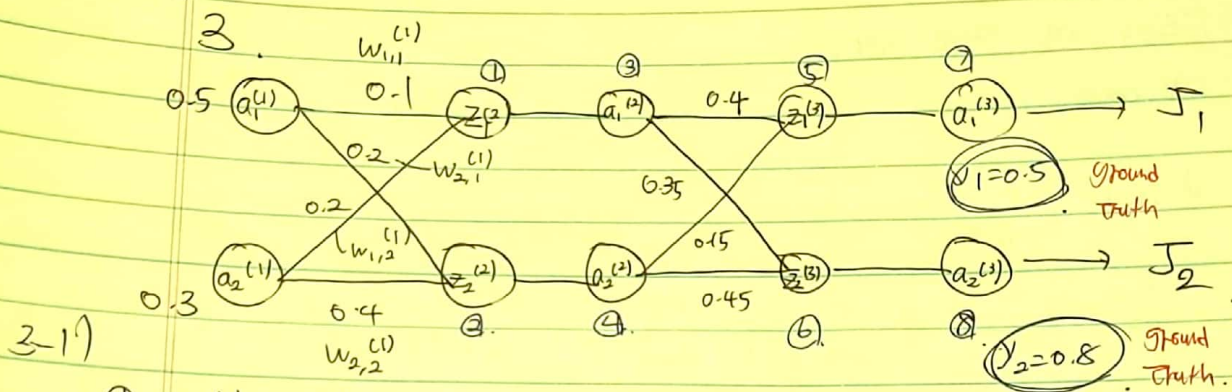
→ update 더 필요함

x_1, x_2 y $0, 1$

1	0	0	1	1
2	0	1	1	0
3	1	1	1	1
4	1	0	0	1

0	0	1	1
0	1	1	1
1	1	1	1
1	0	0	1

✓



$$\begin{aligned} \textcircled{1} \quad z_1^{(2)} &= w_{1,1}^{(1)} \cdot a_1^{(1)} + w_{1,2}^{(1)} \cdot a_2^{(1)} \\ &= 0.1 \times 0.5 + 0.2 \times 0.3 \\ &= 0.11 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad z_2^{(2)} &= w_{2,1}^{(1)} \cdot a_1^{(1)} + w_{2,2}^{(1)} \cdot a_2^{(1)} \\ &= 0.2 \times 0.5 + 0.3 \times 0.4 \\ &= 0.22 \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad \sigma(z_1^{(2)}) &= a_1^{(2)} \\ &= \frac{1}{1 + e^{-0.11}} = 0.53 \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad \sigma(z_2^{(2)}) &= a_2^{(2)} \\ &= \frac{1}{1 + e^{-0.22}} = 0.55 \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad z_1^{(3)} &= 0.53 \times 0.4 + 0.55 \times 0.15 \\ &= 0.29 \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad z_2^{(3)} &= 0.55 \times 0.45 + 0.53 \times 0.35 \\ &= 0.43 \end{aligned}$$

$$\textcircled{7} \quad a_1^{(3)} = \frac{1}{1 + e^{-0.29}} = 0.57$$

$$\textcircled{8} \quad a_2^{(3)} = \frac{1}{1 + e^{-0.43}} = 0.61$$

3-2) let cost function as MSE.

$$\begin{aligned} \textcircled{1} \quad J_1 &= \frac{1}{2} (a_1^{(3)} - y_1)^2 \\ &= \frac{1}{2} (0.57 - 0.5)^2 \\ &= 0.00245 \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad J_2 &= \frac{1}{2} (a_2^{(3)} - y_2)^2 \\ &= \frac{1}{2} (0.61 - 0.8)^2 \\ &= 0.01805 \end{aligned}$$

3-3)

$$\text{Updates) } w_j = w_j - 0.1 \cdot \frac{\delta_{\text{total}}}{\sum w_j} \quad (\text{Learning rate} = 0.1)$$

$$\Rightarrow w_{2,2}^{(2)}, w_{2,1}^{(1)}$$

$$\delta_2^{(3)} = \frac{\partial J}{\partial z_2} = (a_2^{(3)} - y_2) \times a_2^{(3)} \times (1 - a_2^{(3)})$$

$$= (0.61 - 0.8) \times 0.61 \times (1 - 0.61)$$

$$= -0.045$$

$$w_{2,1}^{(2)} = w_{2,1}^{(1)} - \delta_2^{(3)} a_1^{(2)}$$

$$= 0.35 - (-0.045) \times 0.53 = 0.37365$$

$$\approx 0.374$$

$$w_{2,2}^{(2)} = w_{2,2}^{(1)} - \delta_2^{(3)} a_2^{(2)}$$

$$= 0.45 - (-0.045) \times 0.55$$

$$= 0.452475 \approx 0.452$$