

677-assignment

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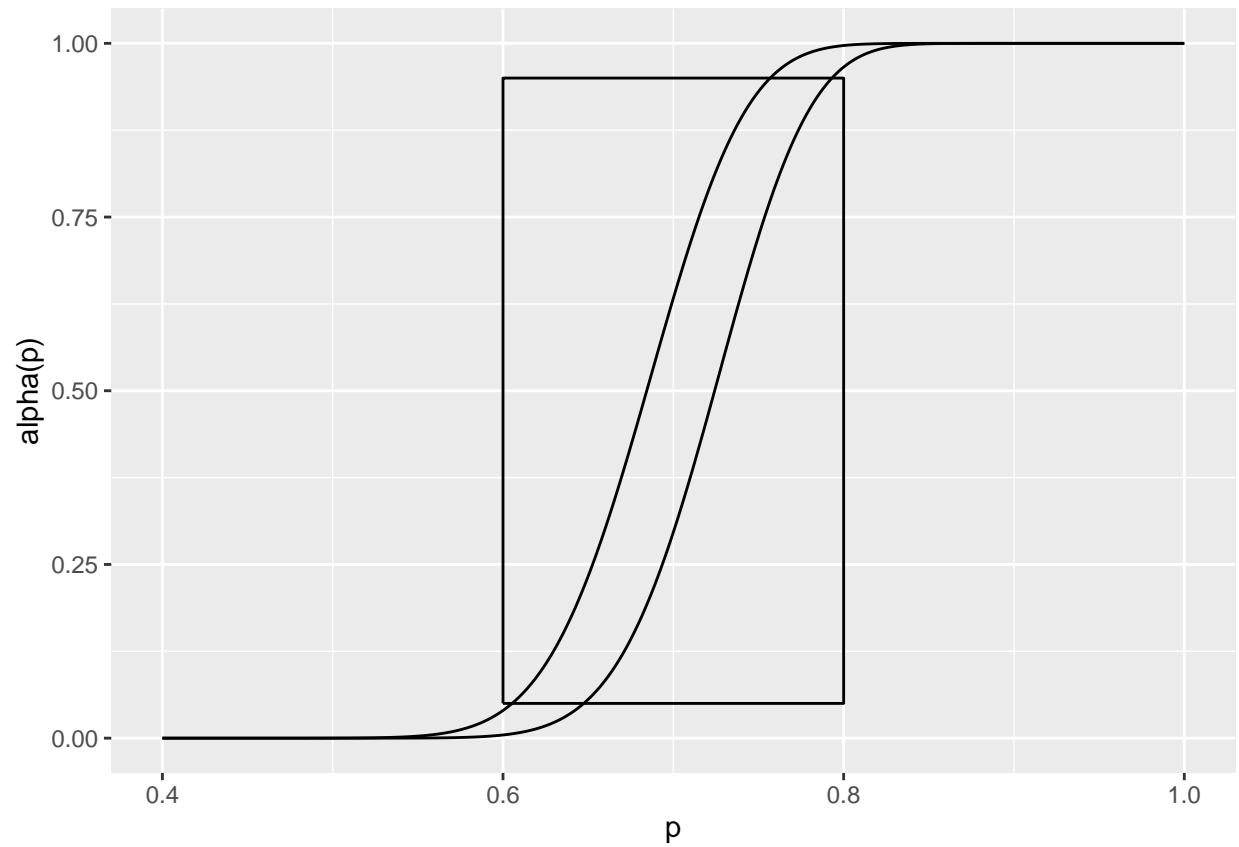
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Creating the function $\alpha(p)$

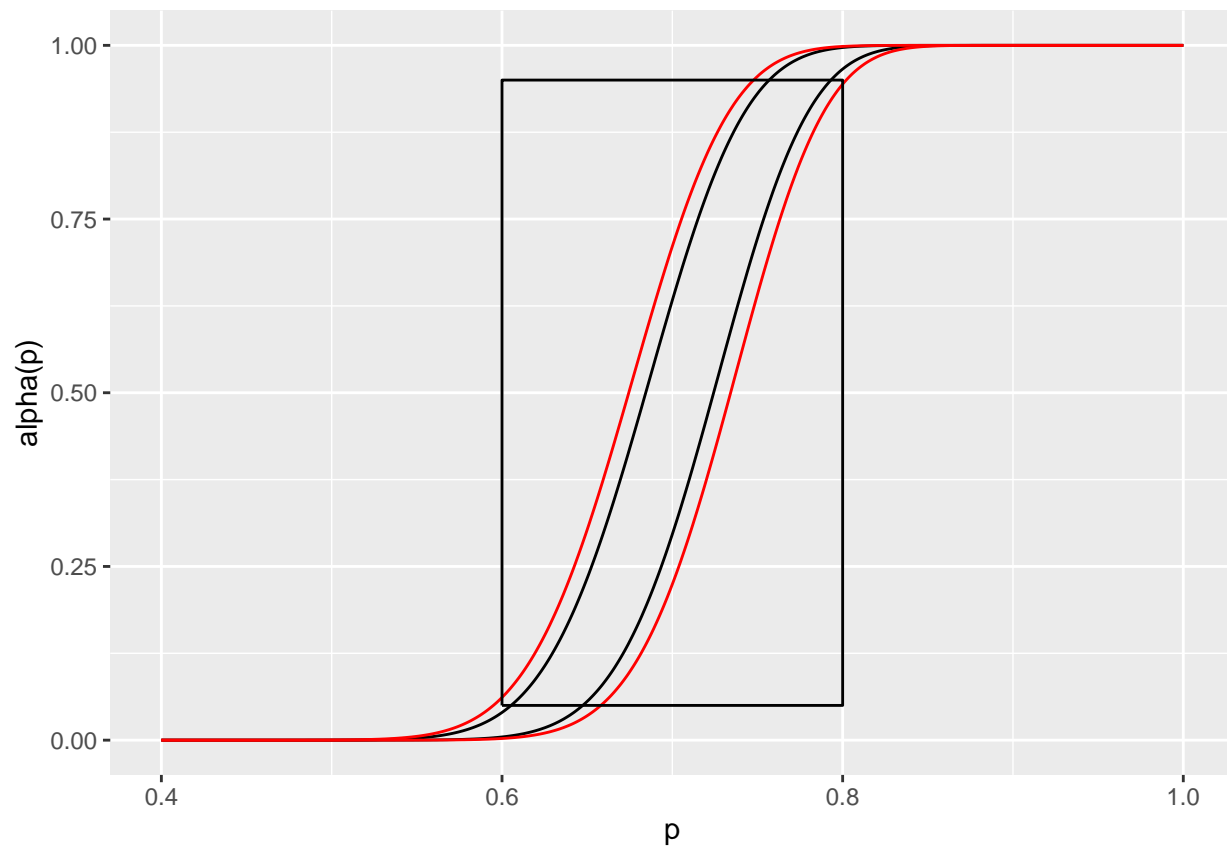
```
alpha_p = function(n,m,p){  
  a= 0  
  for(k in m:n){  
    a = a+dbinom(k, size = n, p)  
  }  
  return(a)  
}
```

Plot

```
n = 100  
x1 = seq(0.4,1,by = 0.001)  
  
y1 = alpha_p(n,69,x1)  
y2 = alpha_p(n,73,x1)  
y3 = alpha_p(n,68,x1)  
y4 = alpha_p(n,74,x1)  
dat = data.frame(x1, y1, y2, y3, y4)  
  
r1 = c(0.6,0.6,0.8,0.8,0.6)  
r2 = c(0.05,0.95,0.95, 0.05, 0.05)  
rec = data.frame(x = r1, y = r2)  
  
ggplot(data =dat) +  
  geom_line(aes(x = x1, y = y1)) +  
  geom_line(aes(x = x1, y = y2))+  
  geom_path(aes(x = r1, y = r2), data = rec) +  
  xlab("p")+ ylab("alpha(p)")
```



```
ggplot(data = dat) +
  geom_line(aes(x = x1, y = y1)) +
  geom_line(aes(x = x1, y = y2)) +
  geom_line(aes(x = x1, y = y3), color = "red") +
  geom_line(aes(x = x1, y = y4), color = "red") +
  geom_path(aes(x = r1, y = r2), data = rec) +
  xlab("p") + ylab("alpha(p)")
```



The two red lines in the second graph represent the function $\alpha(p)$ with the critical value $m = 68$ and $m = 74$ respectively. Both of them are either outside the bottom line or outside the top line. Therefore the critical value should be between 69 and 73.