2nd Persistent cohomology barcodes and 2nd Stiefel-Whitney class of type 4

