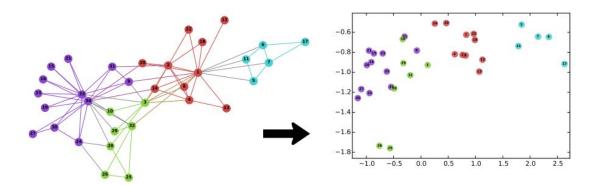
DeepWalk: Online Learning of Social Representations

1. What is DeepWalk?

A method to learn Latent Representations of Vertices in a Network, encoding a *sparse*, *high dimensional* representation (adjacency/weight matrix) into a set of *dense*, *low dimensional* vectors (embeddings)



2. Main Contributions

→ Deep Learning approach to Graph Analysis

B. Perozzi et al. drew inspiration from Natural Language Processing to generate unsupervised features of the nodes.

Generalization Capability

The resulting representations are general and can be combined with any classifier, yielding good performance.

Parallelizability and Scalability

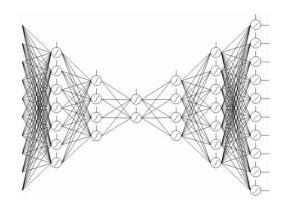
Very efficient algorithm, suitable for analysing real world networks.

→ Extensive Testing and Strong Performance

Evaluation on 3 different datasets shows SOTA results and data efficiency.

3. Latent Representations

- In statistics a **Latent Variable** is a variable that cannot be observed directly but is inferred with a mathematical model from real observations
- Very popular in Machine Learning:
 - **♦** Principal Component Analysis
 - Word Embeddings
 - Autoencoders
 - **♦** .

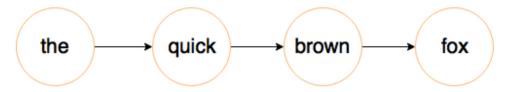


4. Random Walk

- "A Random Walk is a path formed by a sequence of random steps", C. Piccardi It can be seen as an ordered list of nodes where each node is a neighbour of the previous node in the list.
- Interesting properties of short Random Walks:
 - ◆ **Locality**: strong connection to the local structure of a network
 - Parallelizability: several random walkers can explore the network simultaneously
 - ◆ **Generality**: tolerance to small changes in the graph structure

5. From NLP to Graph Analysis

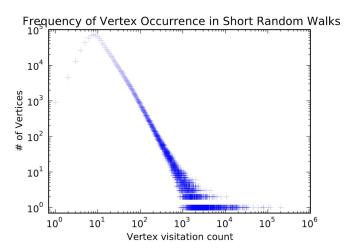
- Sentences can be seen as short Random Walks:
 - ♦ Word → Node
 - ◆ Transition between words → Edge



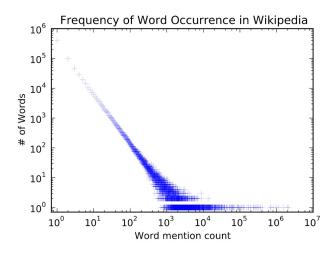
Sentence in a graph representation

5. From NLP to Graph Analysis

Power Law connection:



(a) YouTube Social Graph



(b) Wikipedia Article Text

6. Language Modeling

→ Likelihood estimation of a sequence of words:

$$Pr(w_{n+1}|(w_1, w_2, \dots, w_n))$$

 \rightarrow Equivalently, given a mapping function $\Phi: w \in V \to R^{|V| \times d}$

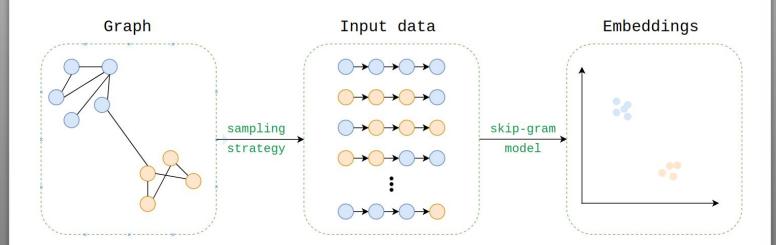
$$Pr(w_{n+1}|(\Phi(w_1),\Phi(w_2),\cdots,\Phi(w_n)))$$

6. Language Modeling

- Instead of using the context to predict the missing word, use the word to predict the context
- Use context on both left and right side of the word
- Order independence assumption
- > Rewrite as optimization problem on the node embedding:

$$minimize_{\Phi} - log(Pr(\{v_{i-w}, \dots, v_{i-1}, v_{i+1}, \dots, v_{i+w}\} | \Phi(v_i)))$$

7. Algorithm



7. Algorithm

- Random Walk generator:
 - ◆ For each node in the graph start a random walk with length t = 40
 - ◆ Repeat **y** = **30** times (training epochs)
 - Random restarts can be used but it doesn't help
- → Each sequence generated by a short Random Walk is divided into
 subsequences of length 2w + 1, with window size w = 10

7. Algorithm

Compute error

- > Embedding update procedure:
 - ♦ Skip-Gram:

$$J(\Phi) = -\log \Pr(u_k \mid \Phi(v_j))$$

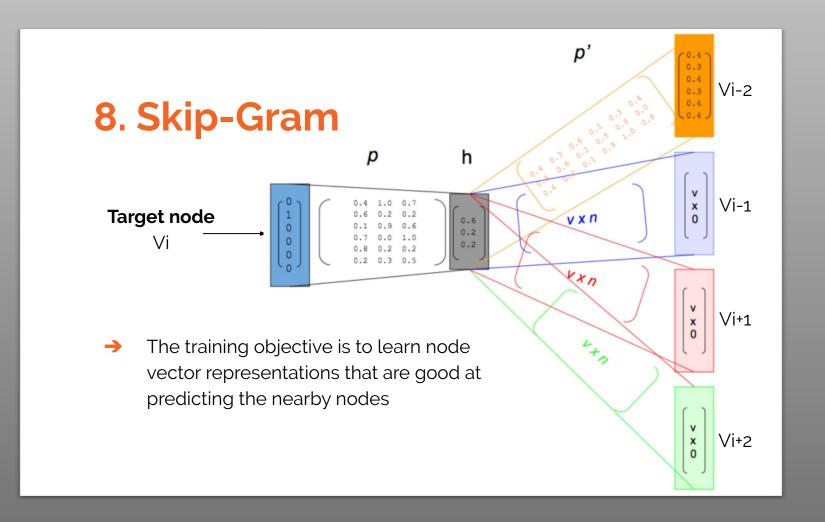
$$\Phi = \Phi - \alpha * \frac{\partial J}{\partial \Phi}$$

The quick brown fox jumps over the lazy dog.

The quick brown fox jumps over the lazy dog.

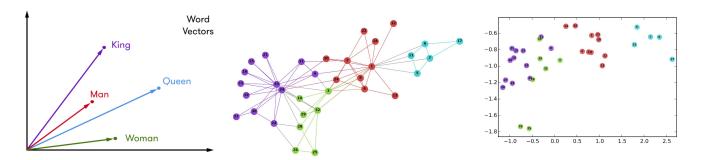
Take the gradient and update

The quick brown fox jumps over the lazy dog.



9. Properties

- Nodes that belong to the **same community** will have **similar embeddings** (i.e. the Euclidean distance will be small)
- The latent representations also capture the relationships between nodes



10. Evaluation

- Now that we have a set of features that encode the relationships among nodes we can test them on **multi-label classification**
- → Against 5 state of the art baselines with Micro/Macro-F1 score
- → On 3 datasets:

Name	BlogCatalog	FLICKR	YouTube
$\overline{ V }$	10,312	80,513	1,138,499
E	$333,\!983$	5,899,882	2,990,443
$ \mathcal{Y} $	39	195	47
Labels	Interests	Groups	Groups

11. Results (BlogCatalog)

	% Labeled Nodes	10%	20%	30%	40%	50%	60%	70%	80%	90%
	DeepWalk	36.00	38.20	39.60	40.30	41.00	41.30	41.50	41.50	42.00
	SpectralClustering	31.06	34.95	37.27	38.93	39.97	40.99	41.66	42.42	42.62
	EdgeCluster	27.94	30.76	31.85	32.99	34.12	35.00	34.63	35.99	36.29
Micro-F1(%)	Modularity	27.35	30.74	31.77	32.97	34.09	36.13	36.08	37.23	38.18
	wvRN	19.51	24.34	25.62	28.82	30.37	31.81	32.19	33.33	34.28
	Majority	16.51	16.66	16.61	16.70	16.91	16.99	16.92	16.49	17.26
	DeepWalk	21.30	23.80	25.30	26.30	27.30	27.60	27.90	28.20	28.90
Macro-F1(%)	SpectralClustering	19.14	23.57	25.97	27.46	28.31	29.46	30.13	31.38	31.78
	EdgeCluster	16.16	19.16	20.48	22.00	23.00	23.64	23.82	24.61	24.92
	Modularity	17.36	20.00	20.80	21.85	22.65	23.41	23.89	24.20	24.97
	wvRN	6.25	10.13	11.64	14.24	15.86	17.18	17.98	18.86	19.57
	Majority	2.52	2.55	2.52	2.58	2.58	2.63	2.61	2.48	2.62

Table 2: Multi-label classification results in BlogCatalog

11. Results (Flickr)

	% Labeled Nodes	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
	DeepWalk	32.4	34.6	35.9	36.7	37.2	37.7	38.1	38.3	38.5	38.7
	SpectralClustering	27.43	30.11	31.63	32.69	33.31	33.95	34.46	34.81	35.14	35.41
Micro-F1(%)	EdgeCluster	25.75	28.53	29.14	30.31	30.85	31.53	31.75	31.76	32.19	32.84
	Modularity	22.75	25.29	27.3	27.6	28.05	29.33	29.43	28.89	29.17	29.2
	wvRN	17.7	14.43	15.72	20.97	19.83	19.42	19.22	21.25	22.51	22.73
	Majority	16.34	16.31	16.34	16.46	16.65	16.44	16.38	16.62	16.67	16.71
	DeepWalk	14.0	17.3	19.6	21.1	22.1	22.9	23.6	24.1	24.6	25.0
	SpectralClustering	13.84	17.49	19.44	20.75	21.60	22.36	23.01	23.36	23.82	24.05
Macro-F1(%)	EdgeCluster	10.52	14.10	15.91	16.72	18.01	18.54	19.54	20.18	20.78	20.85
	Modularity	10.21	13.37	15.24	15.11	16.14	16.64	17.02	17.1	17.14	17.12
	wvRN	1.53	2.46	2.91	3.47	4.95	5.56	5.82	6.59	8.00	7.26
	Majority	0.45	0.44	0.45	0.46	0.47	0.44	0.45	0.47	0.47	0.47

Table 3: Multi-label classification results in FLICKR

11. Results (YouTube)

	% Labeled Nodes	1%	2%	3%	4%	5%	6%	7%	8%	9%	10%
	DeepWalk	37.95	39.28	40.08	40.78	41.32	41.72	42.12	42.48	42.78	43.05
	SpectralClustering	_	_	_	_	_	_	_	-	_	_
Micro-F1(%)	EdgeCluster	23.90	31.68	35.53	36.76	37.81	38.63	38.94	39.46	39.92	40.07
	Modularity	_		_	_	_	_	_	_	_	_
	wvRN	26.79	29.18	33.1	32.88	35.76	37.38	38.21	37.75	38.68	39.42
	Majority	24.90	24.84	25.25	25.23	25.22	25.33	25.31	25.34	25.38	25.38
	DeepWalk	29.22	31.83	33.06	33.90	34.35	34.66	34.96	35.22	35.42	35.67
	SpectralClustering	-			_	_				_	_
Macro-F1(%)	EdgeCluster	19.48	25.01	28.15	29.17	29.82	30.65	30.75	31.23	31.45	31.54
	Modularity	_		_		_	_		-		_
	wvRN	13.15	15.78	19.66	20.9	23.31	25.43	27.08	26.48	28.33	28.89
	Majority	6.12	5.86	6.21	6.1	6.07	6.19	6.17	6.16	6.18	6.19

Table 4: Multi-label classification results in YouTube

12. BONUS: my implementation

- → Around 80 lines of Python code
- Networkx for the graph
- PyTorch for the neural network
- Tested on **Zachary's karate club** network with 2d embeddings

12. BONUS: my implementation

→ The euclidean distance between central and peripheral nodes seems to be constant

Average distance of nodes 15, 16, 19, 21, 23, 27

from node **34** is **6.23**

 Average distance of nodes 12, 13, 18, 22 from node 1 is 6.52

