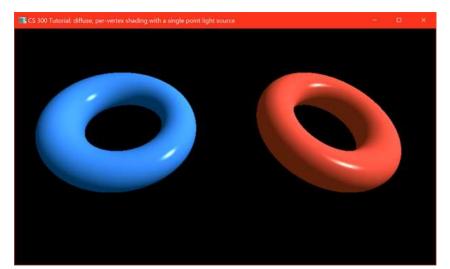
Introduction to Computer Graphics Introduction to Texture Mapping

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Simplified 3D Graphics Pipe Vertex Data Vertex Fetch Frame Buffer **Textures** Vertex Shader Blending **Model-to-World Coordinates Logical Operations** World-to-View Coordinates R Alpha Test View-to-Clip Coordinates Stencil Test Depth Test Clipping **Scissor Test** Per Fragment Projection **Operations** (Clip-to-NDC Coordinates) Compute Color Е **Viewport Transform** Fragment Shader (NDC-to-Window Coordinates)

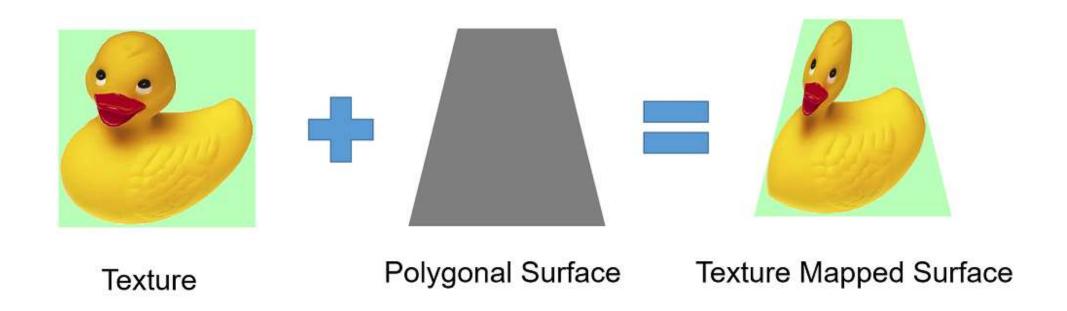
- Images synthesized from polygonal models lack details and richness of real surfaces
 - Imperfections caused by wear and tear
 - Irregular color variations
 - Properties of natural materials such as stone, wood, soil, ...



- Technique for adding detail to surfaces using images, functions, or other data sources
 - This process makes color of surface vary from point to point
 - Detail added without increasing complexity of 3D models

- Technique for adding detail to surfaces using images, functions, or other data sources
- We're concerned with image mapping

 Texture mapping involves mapping an image called texture to simpler surface

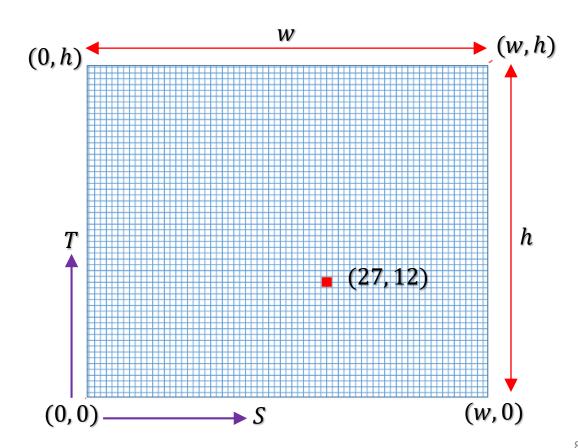


Texture Images and Texels

- Texture image is discrete collection of color samples
 - Each color sample called texel (texture element)
- One-dimensional textures suitable for linear primitives such as lines
- Two-dimensional textures suitable for planar primitives such as triangles – we're only concerned with rectangular textures
- Three-dimensional textures suitable for volumetric objects
- Good idea to have powers-of-two dimensions

Texture Images and Texels (1/2)

- To identify texels, texture images come with their own discrete coordinate system called texel space
- In OpenGL, texel referenced by integral 2-tuple (x, y) with origin at bottom-left corner
 - Reverse of notation for referencing texel's corresponding memory location in C/C++



Texture Images and Texels (2/2)

- In addition to width and height, other consideration is format of data specified at each texel
- Image sample represented in variety of formats:
 - 16 or 24 bit RGB, 32 bit RGBA, various color index methods,

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Texture Coordinates

 Texture coordinates – specified at each vertex – define where texels appear on texture surface

 They control texture's placement on surface by determining which texels in texture image correspond to which vertices on surface texture coordinates

texture coordinates

texture coordinates

texture coordinates

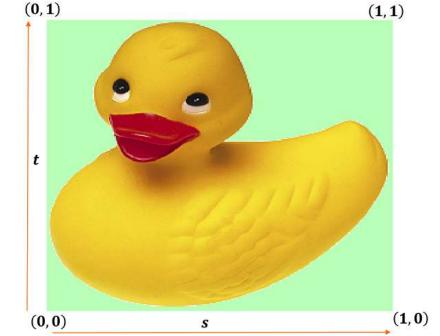
texture coordinates

Texture Space

 Texture coordinates are specified in normalized coordinate system called texture space

 OpenGL uses s for horizontal axis ranging from left to right and t for vertical axis ranging from bottom to top with origin

at bottom-left



Texture Space

- Unit texture space $(s,t) \in [0,1] \times [0,1]$ is mapping of discrete texel space to continuous texture space
- Advantage of using texture space over texel space:
 - More practical and efficient
 - Texture coordinates independent of texture image's width and height and therefore don't need to be recomputed when texture image changes

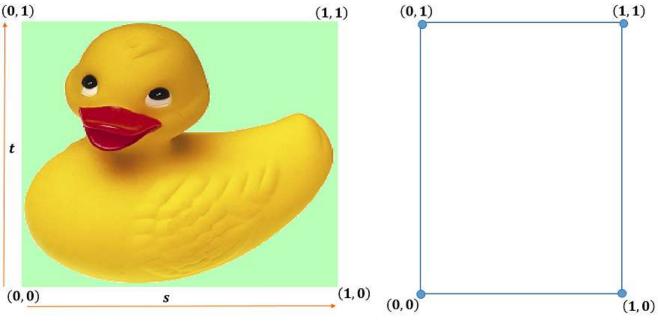
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Understanding Texture Coordinates (1/2)

On left, we've texture image defined in texture space

On right, we've polygon onto which texture image is to

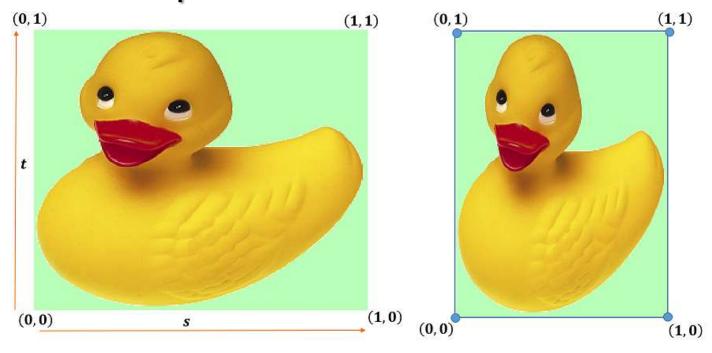
be pasted



Polygon with texture coordinates

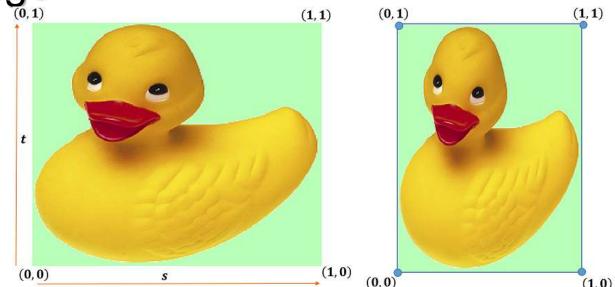
Understanding Texture Coordinates (2/2)

- Image will be "stretched" to fit polygon
 - Rasterizer will interpolate texture coordinates assigned to each vertex to compute texture coordinates for interior points



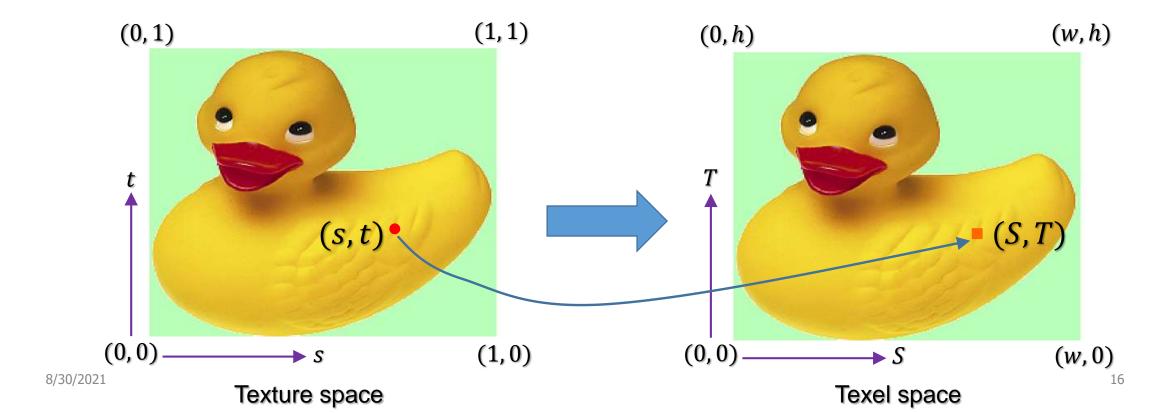
Understanding Texture Coordinates (2/2)

- Rasterizer will interpolate texture coordinates assigned to each vertex to compute texture coordinates for interior points
- Next, texture coordinates mapped to texel coordinates to retrieve color from image



Mapping Texture Coordinates to Texel Coordinates (1/2)

$$(s*w,t*h) \rightarrow (S,T)$$



Mapping Texture Coordinates to Texel Coordinates (2/2)

- Fragment (x,y) on surface with interpolated texture coordinates (s,t) has floating-point texel coordinates (S,T) = (w*s,h*t)
- Point sampling selects single texel value containing texture coordinate's sample point (S,T)
 - Integer coordinates of selected texel are ([S], [T])

Wrapping Modes (1/2)

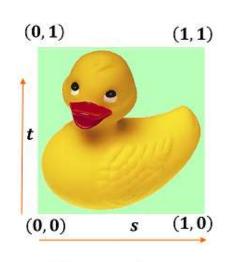
- Values of s and t outside [0, 1] don't map to image, but such values are still valid as texture coordinates
- Why would texture coordinates be outside [0, 1]?
 - When texturing is applied to surfaces whose polygonal geometry is much larger than texture width and height

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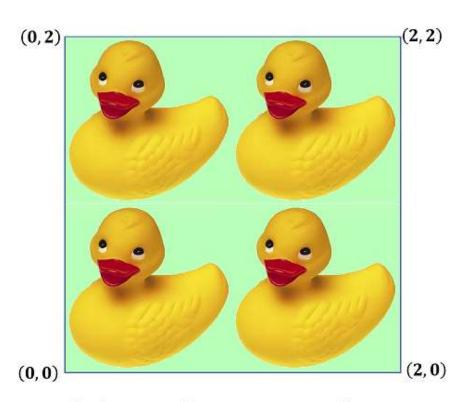
Wrapping Modes (2/2)

- However, texture coordinates must be wrapped so that their mapping to texel coordinates accesses valid texel data
- Two basic wrapping modes:
 - Repeat repeats image by ignoring integer part of texture coordinate and ignoring fractional part
 - Clamp-to-edge projecting texture coordinates to closest texel on edge of texture map

Wrapping with Repeat (1/2)



Texture Image



Polygon with texture coordinates

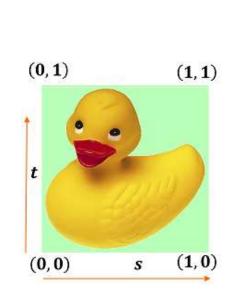
Wrapping with Repeat (2/2)

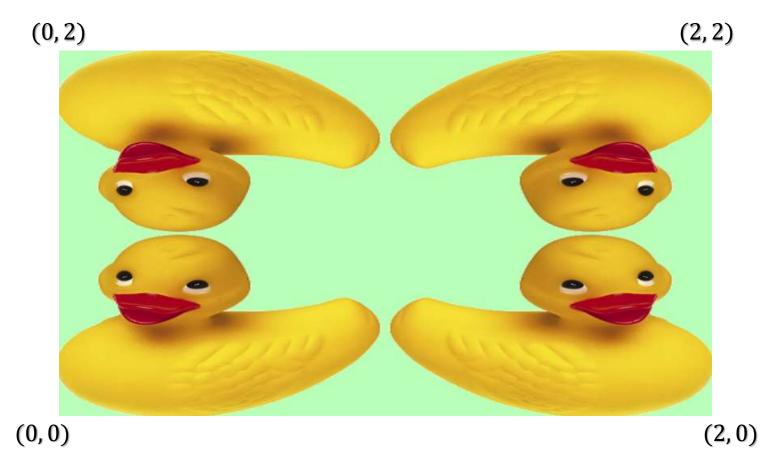
- Texture repeating also known as tiling
- Image repeated across polygon independently in horizontal and vertical directions
- How?
 - Integer part of either s or t, or both s and t is dropped

$$repeat(s) \leftarrow s - \lfloor s \rfloor$$

$$repeat(t) \leftarrow t - \lfloor t \rfloor$$

Wrapping with Mirror (1/2)



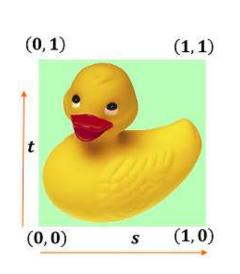


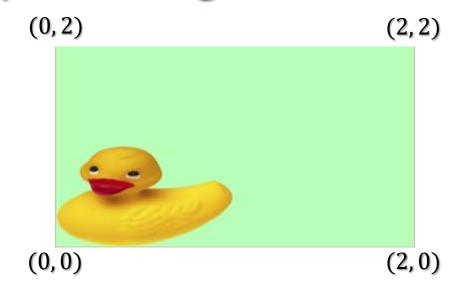
Wrapping with Mirror (2/2)

- Texture repeating also known as tiling
- Image repeated across polygon independently in horizontal and vertical directions but flipped on every other repetition

$$mirror(s) \leftarrow \begin{cases} s - \lfloor s \rfloor & [s] \text{ is even} \\ 1.0 - (s - \lfloor s \rfloor) & [s] \text{ is odd} \end{cases}$$
$$mirror(t) \leftarrow \begin{cases} t - \lfloor t \rfloor & [t] \text{ is even} \\ 1.0 - (t - \lfloor t \rfloor) & [t] \text{ is odd} \end{cases}$$

Wrapping with Clamp-to-Edge





$$clamp(s) \leftarrow max(min(s, 1.0), 0.0)$$

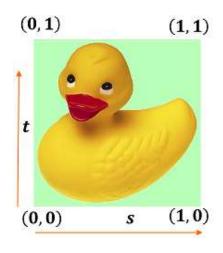
$$clamp(t) \leftarrow max(min(t, 1.0), 0.0)$$

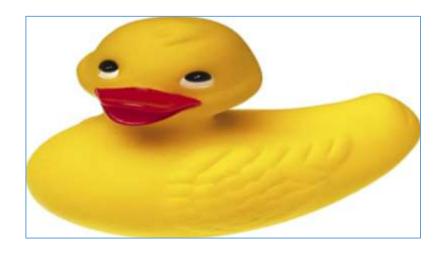
Color Combiner or Texture Blending Modes

- At each fragment, we've color from texturing and say color from lighting (we'll call this color a surface color)
- Texture color can be further transformed with surface color using color combine or textue blending modes
 - Decal
 - Modulate
 - Replace

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Decal Mode (1/2)





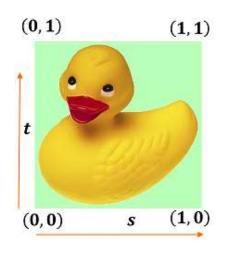
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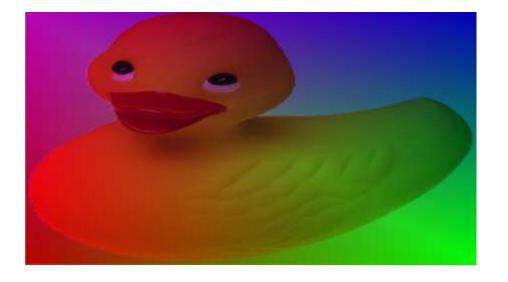
Decal Mode (2/2)

- Texture α value blends between surface and texture colors
- If surface color is $C_s = (r_s, g_s, b_s)$ and texture color is $C_t = (r_t, g_t, b_t, \alpha_t)$, then final color is

$$C = C_S + \alpha_t (C_t - C_S)$$

Modulate Mode (1/2)



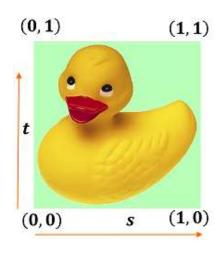


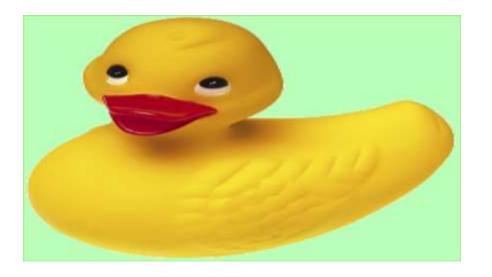
Modulate Mode (2/2)

- Texture color modulated by surface color to give surface shaded appearance
- If surface color is $C_s = (r_s, g_s, b_s)$ and texture color is $C_t = (r_t, g_t, b_t)$, then final color is

$$C = C_S \otimes C_t = (r_S r_t, g_S g_t, b_S b_t)$$

Replace Mode (1/2)





Replace Mode (2/2)

- Texture color replaces/overwrites surface color
- If surface color is $C_s = (r_s, g_s, b_s)$ and texture color is $C_t = (r_t, g_t, b_t)$, then final color is

$$C = C_t = (r_t, g_t, b_t)$$

Texture Mapping in OpenGL

- In order to use texture mapping in OpenGL applications, following steps must be implemented:
 - Create a texture object and load texel data into it
 - Specify sampling parameters such as wrapping, filtering
 - Include texture coordinates as an attribute to vertices
 - Associate a texture sampler with each texture map used in a fragment shader
 - Retrieve texel values through texture sampler in the fragment shader
- Tutorial will be assigned to go thro' above steps

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