# Small Test Exact Solution Looped Minimizer

This is the example vignette for function: <a href="mainto:snw\_vfi\_main">snw\_vfi\_main</a> from the PrjOptiSNW Package. This function solves for policy function fully iteratively using matlab minimizer. Small Solution Analysis. This produces the same result as <a href="mainto:snw\_vfi\_main\_bisec\_vec">snw\_vfi\_main\_bisec\_vec</a>, except slower. The purpose of this function is to confirm that the results from <a href="mainto:snw\_vfi\_main\_bisec\_vec">snw\_vfi\_main\_bisec\_vec</a> is correct.

#### Test SNW\_VFI\_MAIN Defaults Small

Call the function with defaults parameters.

```
mp param = snw mp param('default small');
[V VFI,ap VFI,cons VFI,mp valpol more] = snw vfi main(mp param);
SNW_VFI_MAIN: Finished Age Group:18 of 18
SNW VFI MAIN: Finished Age Group:17 of 18
SNW VFI MAIN: Finished Age Group:16 of 18
SNW_VFI_MAIN: Finished Age Group:15 of 18
SNW VFI MAIN: Finished Age Group:14 of 18
SNW_VFI_MAIN: Finished Age Group:13 of 18
SNW VFI MAIN: Finished Age Group:12 of 18
SNW_VFI_MAIN: Finished Age Group:11 of 18
SNW_VFI_MAIN: Finished Age Group:10 of 18
SNW VFI MAIN: Finished Age Group:9 of 18
SNW_VFI_MAIN: Finished Age Group:8 of 18
SNW VFI MAIN: Finished Age Group:7 of 18
SNW_VFI_MAIN: Finished Age Group:6 of 18
SNW_VFI_MAIN: Finished Age Group:5 of 18
SNW_VFI_MAIN: Finished Age Group:4 of 18
SNW_VFI_MAIN: Finished Age Group:3 of 18
SNW_VFI_MAIN: Finished Age Group:2 of 18
SNW_VFI_MAIN: Finished Age Group:1 of 18
Elapsed time is 307.635195 seconds.
Completed SNW_VFI_MAIN;SNW_MP_PARAM=default_small;SNW_MP_CONTROL=default_base
```

### **Small Param Results Define Frames**

Define the matrix dimensions names and dimension vector values. Policy and Value Functions share the same ND dimensional structure.

```
% Grids:
age_grid = [19, 22:5:97, 100];
agrid = mp_param('agrid')';
eta_H_grid = mp_param('eta_H_grid')';
eta_S_grid = mp_param('eta_S_grid')';
ar_st_eta_HS_grid = string(cellstr([num2str(eta_H_grid', 'hz=%3.2f;'), num2str(eta_S_grid', 'wzedu_grid = [0,1];
marry_grid = [0,1];
kids_grid = (1:1:mp_param('n_kidsgrid'))';
% NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
cl_mp_datasetdesc = {};
cl_mp_datasetdesc{1} = containers.Map({'name', 'labval'}, {'age', age_grid});
cl_mp_datasetdesc{2} = containers.Map({'name', 'labval'}, {'savings', agrid});
cl_mp_datasetdesc{3} = containers.Map({'name', 'labval'}, {'eta', 1:length(eta_H_grid)});
cl_mp_datasetdesc{4} = containers.Map({'name', 'labval'}, {'edu', edu_grid});
```

```
cl_mp_datasetdesc{5} = containers.Map({'name', 'labval'}, {'marry', marry_grid});
cl_mp_datasetdesc{6} = containers.Map({'name', 'labval'}, {'kids', kids_grid});
```

## **Analyze Savings and Shocks**

First, analyze Savings Levels and Shocks, Aggregate Over All Others, and do various other calculations.

```
% Generate some Data
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_xtitle') = {'Savings States, a'};
mp_support_graph('st_legend_loc') = 'best';
mp_support_graph('bl_graph_logy') = true; % do not log
```

MEAN(VAL(A,Z)), MEAN(AP(A,Z)), MEAN(C(A,Z))

17

18

19

20

21

22

23

24

25

40

47.979

56.953

66.982

78.125

90.439

103.98

118.82

135

3.1102

3.2059

3.2825

3.3443

3.3948

3.4364

3.4709

3.4998

3.5241

Tabulate value and policies along savings and shocks:

```
% Set
% NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
ar_permute = [1,4,5,6,3,2];
% Value Function
tb_az_v = ff_summ_nd_array("MEAN(VAL(A,Z))", V_VFI, true, ["mean"], 4, 1, cl_mp_datasetdesc, ar
xxx MEAN(VAL(A,Z)) xxxxxxxxxxxxxxxxxxxxxxxxxxxxxx
   group
             savings
                         mean_eta_1
                                                                  mean_eta_4
                                                                               mean_eta_5
                                      mean_eta_2
                                                    mean_eta_3
                           -17.393
                                        -9.1596
     1
                    0
                                                      -4.4164
                                                                    -1.5922
                                                                                -0.05106
                           -16.967
     2
            0.0097656
                                         -9.023
                                                      -4.3405
                                                                    -1.5316
                                                                               0.0054259
     3
             0.078125
                           -14.925
                                        -8.2554
                                                      -3.9177
                                                                    -1.2071
                                                                                  0.3028
     4
              0.26367
                          -11.699
                                        -6.8681
                                                                    -0.6913
                                                                                 0.75178
                                                      -3.1808
     5
                          -8.2751
                                         -5.167
                0.625
                                                      -2.2786
                                                                   -0.13883
                                                                                  1.1911
     6
               1.2207
                          -5.3024
                                        -3.4437
                                                      -1.3431
                                                                    0.38361
                                                                                  1.5638
     7
               2.1094
                          -2.9816
                                        -1.9066
                                                     -0.47798
                                                                    0.86412
                                                                                  1.8672
               3.3496
     8
                                       -0.64407
                          -1.2609
                                                      0.28611
                                                                    1.3001
                                                                                  2.1163
     9
                         -0.012545
                                        0.34403
                    5
                                                       0.9369
                                                                     1.6782
                                                                                  2.3266
               7.1191
                                          1.097
    10
                            0.8875
                                                       1.4725
                                                                     1.9981
                                                                                  2.5086
                                                       1.9037
               9.7656
                            1.5392
                                                                                  2.6684
    11
                                          1.665
                                                                     2.2701
    12
               12.998
                            2.0158
                                         2.0932
                                                       2.2465
                                                                     2.5004
                                                                                  2.8071
    13
               16.875
                            2.3684
                                         2.4172
                                                       2.5172
                                                                     2.6933
                                                                                  2.9263
    14
               21.455
                            2.6328
                                         2.6644
                                                       2.7307
                                                                     2.8535
                                                                                  3.0288
    15
               26.797
                            2.8339
                                         2.8549
                                                       2.8997
                                                                      2.986
                                                                                  3.1174
               32.959
                            2.989
    16
                                         3.0032
                                                        3.034
                                                                     3.0954
                                                                                  3.1939
```

```
% Aprime Choice
tb_az_ap = ff_summ_nd_array("MEAN(AP(A,Z))", ap_VFI, true, ["mean"], 4, 1, cl_mp_datasetdesc, a
```

3.1416

3.2282

3.2986

3.3562

3.4036

3.443

3.476

3.5037

3.5272

3.1857

3.2603

3.3222

3.3738

3.4169

3.4532

3.4838

3.5098

3.5319

3.2598

3.3164

3.3649

3.4064

3.4421

3.4728

3.4991

3.5219

3.5416

3.12

3.2128

3.2875

3.348

3.3975

3.4384

3.4724

3.501

3.5251

| 1  | 0         | 2.7521e-05 | 0.0021998 | 0.046507 | 0.23828 | 0.88717 |
|----|-----------|------------|-----------|----------|---------|---------|
| 2  | 0.0097656 | 0.00054716 | 0.0036592 | 0.049526 | 0.24213 | 0.89277 |
| 3  | 0.078125  | 0.021674   | 0.027305  | 0.079508 | 0.27478 | 0.93352 |
| 4  | 0.26367   | 0.13129    | 0.14249   | 0.19452  | 0.38205 | 1.0523  |
| 5  | 0.625     | 0.38716    | 0.40422   | 0.44789  | 0.63888 | 1.3005  |
| 6  | 1.2207    | 0.83381    | 0.85545   | 0.90674  | 1.0839  | 1.735   |
| 7  | 2.1094    | 1.5206     | 1.5442    | 1.6064   | 1.7452  | 2.3859  |
| 8  | 3.3496    | 2.477      | 2.5013    | 2.5629   | 2.6789  | 3.3301  |
| 9  | 5         | 3.7541     | 3.7788    | 3.8405   | 3.9859  | 4.5828  |
| 10 | 7.1191    | 5.416      | 5.4412    | 5.5038   | 5.6835  | 6.1821  |
| 11 | 9.7656    | 7.4668     | 7.4912    | 7.5553   | 7.7413  | 8.177   |
| 12 | 12.998    | 9.9008     | 9.9212    | 9.9832   | 10.174  | 10.619  |
| 13 | 16.875    | 12.918     | 12.94     | 12.995   | 13.186  | 13.709  |
| 14 | 21.455    | 16.519     | 16.538    | 16.594   | 16.772  | 17.365  |
| 15 | 26.797    | 20.59      | 20.608    | 20.657   | 20.825  | 21.451  |
| 16 | 32.959    | 25.295     | 25.313    | 25.358   | 25.513  | 26.139  |
| 17 | 40        | 30.657     | 30.68     | 30.732   | 30.877  | 31.477  |
| 18 | 47.979    | 36.752     | 36.772    | 36.831   | 36.99   | 37.553  |
| 19 | 56.953    | 43.764     | 43.786    | 43.839   | 44.003  | 44.551  |
| 20 | 66.982    | 51.595     | 51.618    | 51.678   | 51.84   | 52.393  |
| 21 | 78.125    | 59.943     | 59.966    | 60.026   | 60.198  | 60.756  |
| 22 | 90.439    | 69.256     | 69.28     | 69.342   | 69.517  | 70.086  |
| 23 | 103.98    | 79.744     | 79.765    | 79.824   | 79.998  | 80.576  |
| 24 | 118.82    | 91.106     | 91.13     | 91.192   | 91.358  | 91.933  |
| 25 | 135       | 103.46     | 103.48    | 103.54   | 103.71  | 104.28  |
|    |           |            |           |          |         |         |

% Consumption Choices tb\_az\_c = ff\_summ\_nd\_array("MEAN(C(A,Z))", cons\_VFI, true, ["mean"], 4, 1, cl\_mp\_datasetdesc, a

| group | savings<br> | mean_eta_1 | mean_eta_2 | mean_eta_3 | mean_eta_4 | mean_eta_ |
|-------|-------------|------------|------------|------------|------------|-----------|
| 1     | 0           | 0.3104     | 0.44       | 0.69882    | 1.2297     | 2.3502    |
| 2     | 0.0097656   | 0.3214     | 0.45001    | 0.70723    | 1.2373     | 2.356     |
| 3     | 0.078125    | 0.3809     | 0.50664    | 0.75721    | 1.2844     | 2.3949    |
| 4     | 0.26367     | 0.48992    | 0.60921    | 0.85919    | 1.3936     | 2.4924    |
| 5     | 0.625       | 0.65904    | 0.77109    | 1.0281     | 1.5583     | 2.6654    |
| 6     | 1.2207      | 0.91142    | 1.0172     | 1.2649     | 1.8076     | 2.9247    |
| 7     | 2.1094      | 1.2649     | 1.3671     | 1.6019     | 2.1815     | 3.3081    |
| 8     | 3.3496      | 1.7572     | 1.8573     | 2.0907     | 2.6915     | 3.8066    |
| 9     | 5           | 2.4045     | 2.503      | 2.7347     | 3.3043     | 4.4728    |
| 10    | 7.1191      | 3.2104     | 3.3074     | 3.537      | 4.0708     | 5.3364    |
| 11    | 9.7656      | 4.2385     | 4.3358     | 4.5627     | 5.0889     | 6.4164    |
| 12    | 12.998      | 5.5627     | 5.6635     | 5.8917     | 6.4121     | 7.7296    |
| 13    | 16.875      | 7.0504     | 7.1499     | 7.3847     | 7.904      | 9.1419    |
| 14    | 21.455      | 8.7708     | 8.8721     | 9.1059     | 9.6366     | 10.804    |
| 15    | 26.797      | 10.904     | 11.007     | 11.246     | 11.787     | 12.921    |
| 16    | 32.959      | 13.355     | 13.457     | 13.7       | 14.254     | 15.388    |
| 17    | 40          | 16.168     | 16.266     | 16.502     | 17.066     | 18.225    |
| 18    | 47.979      | 19.337     | 19.437     | 19.666     | 20.215     | 21.411    |
| 19    | 56.953      | 22.744     | 22.843     | 23.078     | 23.621     | 24.831    |
| 20    | 66.982      | 26.557     | 26.654     | 26.882     | 27.427     | 28.632    |
| 21    | 78.125      | 31.144     | 31.241     | 31.469     | 32.005     | 33.205    |
| 22    | 90.439      | 36.126     | 36.222     | 36.449     | 36.981     | 38.169    |
| 23    | 103.98      | 41.361     | 41.46      | 41.689     | 42.223     | 43.402    |
| 24    | 118.82      | 47.219     | 47.315     | 47.541     | 48.083     | 49.265    |
| 25    | 135         | 53.648     | 53.747     | 53.978     | 54.513     | 55.702    |