# Small Test Exact Solution Vectorized Bisection

This is the example vignette for function: **snw\_vfi\_main\_bisec\_vec** from the **PrjOptiSNW Package.** This function solves for policy function with vectorized bisection. Small Solution Analysis. Small Solution Analysis, husband 5 shocks, wife 1 shocks.

# Test SNW\_VFI\_MAIN Defaults Small

Call the function with defaults parameters.

```
mp_param = snw_mp_param('default_small');
[V VFI,ap VFI,cons VFI,mp valpol more] = snw vfi main bisec vec(mp param);
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:18 of 17, time-this-age:0.019266
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:17 of 17, time-this-age:0.020088
SNW VFI MAIN BISEC VEC: Finished Age Group:16 of 17, time-this-age:0.019484
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:15 of 17, time-this-age:0.020422
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:14 of 17, time-this-age:0.018799
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:13 of 17, time-this-age:0.019274
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:12 of 17, time-this-age:0.019728
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:11 of 17, time-this-age:0.020101
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:10 of 17, time-this-age:0.019674
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:9 of 17, time-this-age:0.019648
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:8 of 17, time-this-age:0.019126
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:7 of 17, time-this-age:0.018838
SNW VFI MAIN BISEC VEC: Finished Age Group:6 of 17, time-this-age:0.01893
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:5 of 17, time-this-age:0.018729
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:4 of 17, time-this-age:0.018653
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:3 of 17, time-this-age:0.018577
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:2 of 17, time-this-age:0.018797
SNW_VFI_MAIN_BISEC_VEC: Finished Age Group:1 of 17, time-this-age:0.019341
Completed SNW_VFI_MAIN_BISEC_VEC; SNW_MP_PARAM=default_small; SNW_MP_CONTROL=default_base; time=0.35835
```

## **Small Param Results Define Frames**

Define the matrix dimensions names and dimension vector values. Policy and Value Functions share the same ND dimensional structure.

```
% Grids:
age_grid = [19, 22:5:97, 100];
agrid = mp_param('agrid')';
eta_H_grid = mp_param('eta_H_grid')';
eta_S_grid = mp_param('eta_S_grid')';
ar_st_eta_HS_grid = string(cellstr([num2str(eta_H_grid', 'hz=%3.2f;'), num2str(eta_S_grid', 'w:
edu_grid = [0,1];
marry_grid = [0,1];
kids_grid = (1:1:mp_param('n_kidsgrid'))';
% NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
cl_mp_datasetdesc = {};
cl_mp_datasetdesc{1} = containers.Map({'name', 'labval'}, {'age', age_grid});
cl_mp_datasetdesc{2} = containers.Map({'name', 'labval'}, {'savings', agrid});
cl_mp_datasetdesc{3} = containers.Map({'name', 'labval'}, {'Hshock', eta_H_grid});
cl_mp_datasetdesc{4} = containers.Map({'name', 'labval'}, {'edu', edu_grid});
cl_mp_datasetdesc{5} = containers.Map({'name', 'labval'}, {'edu', edu_grid});
cl_mp_datasetdesc{6} = containers.Map({'name', 'labval'}, {'marry', marry_grid});
cl_mp_datasetdesc{6} = containers.Map({'name', 'labval'}, {'kids', kids_grid});
```

# **Analyze Savings and Shocks**

First, analyze Savings Levels and Shocks, Aggregate Over All Others, and do various other calculations.

```
% Generate some Data
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
mp_support_graph('cl_st_xtitle') = {'Savings States, a'};
mp_support_graph('st_legend_loc') = 'best';
mp_support_graph('bl_graph_logy') = true; % do not log
```

MEAN(VAL(A,Z)), MEAN(AP(A,Z)), MEAN(C(A,Z))

1

2

a

0.0097656

2.7511e-05

0.00054711

Tabulate value and policies along savings and shocks:

```
% Set
% NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
ar_permute = [1,4,5,6,3,2];
% Value Function
tb_az_v = ff_summ_nd_array("MEAN(VAL(A,Z))", V_VFI, true, ["mean"], 4, 1, cl_mp_datasetdesc, ar
group
             savings
                        mean_Hshock__1_8395
                                              mean_Hshock__0_91976
                                                                    mean_Hshock_0
                                                                                     mean_Hshock_0_91976
     1
                               -17.393
                                                    -9.1596
                                                                       -4.4164
                                                                                          -1.5921
            0.0097656
                               -16.967
                                                     -9.023
                                                                       -4.3405
     2
                                                                                          -1.5316
     3
             0.078125
                               -14.925
                                                    -8.2554
                                                                       -3.9177
                                                                                          -1.2071
     4
              0.26367
                               -11.699
                                                                       -3.1808
                                                    -6.8681
                                                                                          -0.6913
     5
               0.625
                               -8.2751
                                                    -5.1669
                                                                       -2.2785
                                                                                         -0.13883
     6
               1.2207
                               -5.3024
                                                    -3.4437
                                                                       -1.3431
                                                                                          0.38362
     7
               2.1094
                               -2.9816
                                                    -1.9066
                                                                      -0.47797
                                                                                          0.86412
     8
               3.3496
                                                    -0.64407
                                                                       0.28612
                                                                                           1.3001
                               -1.2609
     9
                             -0.012543
                                                    0.34403
                                                                        0.9369
                                                                                           1.6782
    10
              7.1191
                               0.88751
                                                      1.097
                                                                        1.4725
                                                                                           1.9981
    11
              9.7656
                               1.5392
                                                      1.665
                                                                        1.9037
                                                                                           2.2701
    12
              12.998
                               2.0158
                                                     2.0932
                                                                        2.2465
                                                                                           2.5004
    13
              16.875
                               2.3684
                                                     2.4172
                                                                        2.5172
                                                                                           2.6933
    14
               21.455
                               2.6328
                                                     2.6644
                                                                        2.7307
                                                                                           2.8535
    15
               26.797
                               2.8339
                                                     2.8549
                                                                        2.8997
                                                                                            2.986
               32.959
    16
                                2.989
                                                     3.0032
                                                                         3.034
                                                                                           3.0954
    17
                  40
                               3.1102
                                                       3.12
                                                                        3.1416
                                                                                           3.1857
              47.979
    18
                               3.2059
                                                     3.2128
                                                                        3.2282
                                                                                           3.2603
    19
               56.953
                               3.2825
                                                     3.2875
                                                                        3.2986
                                                                                           3.3222
    20
               66.982
                               3.3443
                                                      3.348
                                                                        3.3562
                                                                                           3.3738
    21
               78.125
                               3.3948
                                                     3.3975
                                                                        3.4036
                                                                                           3.4169
    22
              90.439
                               3.4364
                                                     3.4384
                                                                         3.443
                                                                                           3.4532
    23
              103.98
                               3.4709
                                                     3.4724
                                                                         3.476
                                                                                           3,4838
    24
              118.82
                               3.4998
                                                      3.501
                                                                        3.5037
                                                                                           3.5098
    25
                 135
                               3.5241
                                                     3.5251
                                                                        3.5272
                                                                                           3.5319
% Aprime Choice
tb_az_ap = ff_summ_nd_array("MEAN(AP(A,Z))", ap_VFI, true, ["mean"], 4, 1, cl_mp_datasetdesc, a
savings
                        mean_Hshock__1_8395
                                              mean_Hshock__0_91976
                                                                    mean_Hshock_0
                                                                                     mean_Hshock_0_91976
                                                                                                          mea
   group
```

0.0021997

0.0036547

0.046353

0.049525

0.23828

0.24213

3	0.078125	0.021674	0.027305	0.079481	0.27462
4	0.26367	0.13129	0.14249	0.19451	0.38201
5	0.625	0.38703	0.404	0.44756	0.63879
6	1.2207	0.83381	0.85545	0.90672	1.0839
7	2.1094	1.5206	1.5442	1.6064	1.7452
8	3.3496	2.477	2.5013	2.5629	2.6788
9	5	3.7541	3.7788	3.8405	3.9859
10	7.1191	5.416	5.4412	5.5038	5.6835
11	9.7656	7.4668	7.4912	7.5553	7.7413
12	12.998	9.9008	9.9211	9.9832	10.174
13	16.875	12.918	12.94	12.995	13.186
14	21.455	16.519	16.538	16.594	16.772
15	26.797	20.59	20.608	20.657	20.825
16	32.959	25.295	25.313	25.358	25.513
17	40	30.657	30.68	30.732	30.877
18	47.979	36.751	36.772	36.831	36.99
19	56.953	43.764	43.786	43.839	44.003
20	66.982	51.594	51.617	51.677	51.84
21	78.125	59.942	59.965	60.024	60.197
22	90.439	69.254	69.278	69.34	69.515
23	103.98	79.741	79.762	79.821	79.995
24	118.82	91.103	91.126	91.188	91.354
25	135	103.46	103.48	103.53	103.71

# % Consumption Choices

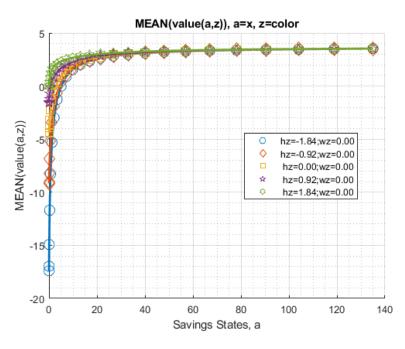
tb\_az\_c = ff\_summ\_nd\_array("MEAN(C(A,Z))", cons\_VFI, true, ["mean"], 4, 1, cl\_mp\_datasetdesc, a

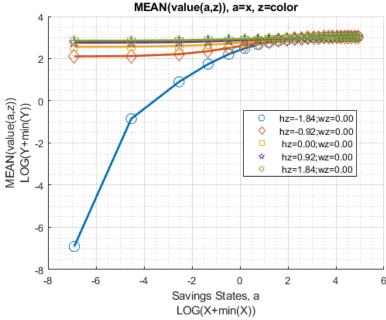
group	C(A,Z)) xxxxx savings	mean_Hshock1_8395	mean_Hshock0_91976	mean_Hshock_0	mean_Hshock_0_91976
1	0	0.3104	0.44	0.69897	1.2297
2	0.0097656	0.3214	0.45001	0.70723	1.2373
3	0.078125	0.3809	0.50664	0.75724	1.2846
4	0.26367	0.48992	0.60921	0.8592	1.3937
5	0.625	0.65917	0.77131	1.0284	1.5584
6	1.2207	0.91141	1.0172	1.2649	1.8076
7	2.1094	1.2649	1.3671	1.6019	2.1815
8	3.3496	1.7572	1.8573	2.0907	2.6915
9	5	2.4045	2.503	2.7347	3.3043
10	7.1191	3.2104	3.3074	3.537	4.0708
11	9.7656	4.2385	4.3358	4.5627	5.0889
12	12.998	5.5627	5.6635	5.8917	6.4121
13	16.875	7.0504	7.1499	7.3847	7.9039
14	21.455	8.7708	8.8721	9.1059	9.6366
15	26.797	10.904	11.007	11.247	11.787
16	32.959	13.355	13.457	13.7	14.254
17	40	16.168	16.266	16.502	17.066
18	47.979	19.337	19.437	19.666	20.215
19	56.953	22.744	22.843	23.078	23.621
20	66.982	26.557	26.654	26.883	27.428
21	78.125	31.145	31.242	31.47	32.006
22	90.439	36.128	36.224	36.451	36.982
23	103.98	41.364	41.464	41.692	42.226
24	118.82	47.222	47.319	47.545	48.086
25	135	53.652	53.751	53.983	54.518

## Graph Mean Values:

```
mp_support_graph('cl_st_graph_title') = {'MEAN(value(a,z)), a=x, z=color'};
```

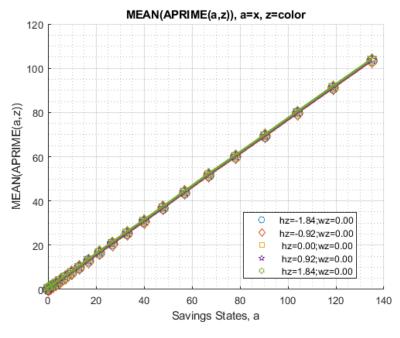
```
mp_support_graph('cl_st_ytitle') = {'MEAN(value(a,z))'};
ff_graph_grid((tb_az_v{1:end, 3:end})', ar_st_eta_HS_grid, agrid, mp_support_graph);
```

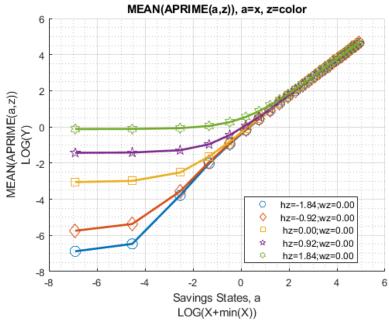




### **Graph Mean Savings Choices:**

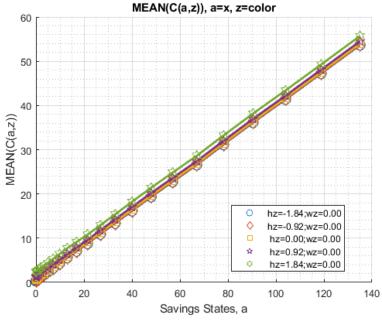
```
mp_support_graph('cl_st_graph_title') = {'MEAN(APRIME(a,z)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(APRIME(a,z))'};
ff_graph_grid((tb_az_ap{1:end, 3:end})', ar_st_eta_HS_grid, agrid, mp_support_graph);
```

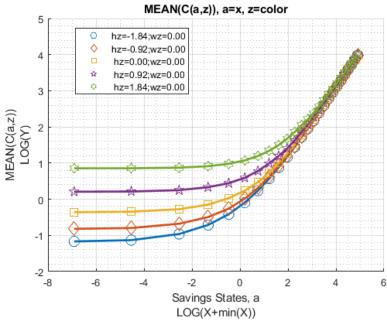




## Graph Mean Consumption:

```
mp_support_graph('cl_st_graph_title') = {'MEAN(C(a,z)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(C(a,z))'};
ff_graph_grid((tb_az_c{1:end, 3:end})', ar_st_eta_HS_grid, agrid, mp_support_graph);
```





# **Analyze Kids and Marriage and Age**

Aggregating over education, savings, and shocks, what are the differential effects of Marriage and Age.

```
% Generate some Data
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
ar_row_grid = ["k0M0", "K1M0", "K2M0", "k0M1", "K1M1", "K2M1"];
mp_support_graph('cl_st_xtitle') = {'Age'};
mp_support_graph('st_legend_loc') = 'best';
mp_support_graph('bl_graph_logy') = true; % do not log
mp_support_graph('st_rounding') = '6.2f'; % format shock legend
mp_support_graph('cl_scatter_shapes') = { 'o', 'd', 's', 'o', 'd', 's'};
mp_support_graph('cl_colors') = {'red', 'red', 'red', 'blue', 'blue', 'blue'};
```

### MEAN(VAL(KM,J)), MEAN(AP(KM,J)), MEAN(C(KM,J))

#### Tabulate value and policies:

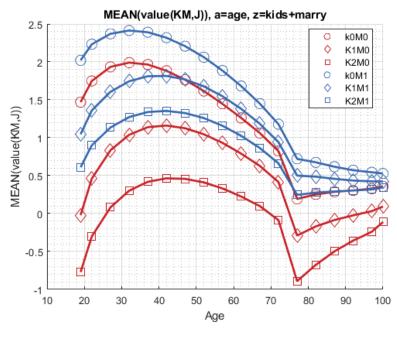
```
% Set
% NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
ar_permute = [2,3,4,1,6,5];
% Value Function
tb_az_v = ff_summ_nd_array("MEAN(VAL(KM,J))", V_VFI, true, ["mean"], 3, 1, cl_mp_datasetdesc, a
group
           kids
                  marry
                          mean_age_19
                                        mean_age_22
                                                     mean_age_27
                                                                   mean_age_32
                                                                                mean_age_37
                                                                                             mean_age_42
                              1.4699
     1
            1
                    0
                                          1.7485
                                                        1.9344
                                                                     1.9907
                                                                                   1.9652
                                                                                                1.8837
     2
            2
                    0
                           -0.020723
                                          0.46111
                                                       0.83504
                                                                     1.0389
                                                                                   1.1397
                                                                                                1.1609
                                         -0.30145
     3
            3
                    0
                            -0.77111
                                                      0.081934
                                                                    0.30157
                                                                                  0.41928
                                                                                               0.46457
     4
            1
                    1
                              2.0205
                                          2.2326
                                                        2.3705
                                                                     2.4138
                                                                                   2.3913
                                                                                                2.3187
     5
            2
                                                                      1.745
                    1
                              1.0463
                                          1.3598
                                                        1.6057
                                                                                   1.8111
                                                                                                1.8148
                             0.61068
                                          0.90045
                                                        1.1354
                                                                     1.2721
                                                                                   1.3395
                                                                                                1.3538
% Aprime Choice
tb_az_ap = ff_summ_nd_array("MEAN(AP(KM,J))", ap_VFI, true, ["mean"], 3, 1, cl_mp_datasetdesc,
mean_age_19
   group
           kids
                                        mean age 22
                                                     mean age 27
                                                                   mean age 32
                                                                                mean age 37
                                                                                             mean age 42
                  marry
                            34.929
                                          34.724
                                                       34.662
                                                                     34.55
                                                                                  34.357
                                                                                               34.071
     1
            1
                    0
     2
            2
                    0
                              34.6
                                          34.331
                                                       34.195
                                                                     33.99
                                                                                  33.687
                                                                                               33.279
                            34.185
                                                                                               33.026
     3
            3
                    0
                                          33.965
                                                       33.873
                                                                      33.7
                                                                                  33.421
     4
            1
                                                       34.562
                                                                                  34.262
                                                                                               33.978
                    1
                            34.819
                                          34.614
                                                                    34.453
     5
            2
                            34.667
                                          34.448
                                                        34.36
                                                                    34.201
                                                                                  33.945
                                                                                               33.586
                    1
     6
            3
                    1
                              34.3
                                         34.115
                                                       34.061
                                                                    33.932
                                                                                    33.7
                                                                                               33.356
    MEVN(C(KW 1))
```

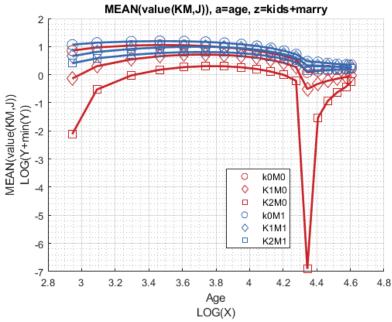
% Consumption Choices						
<pre>tb_az_c = ff_summ_nd_array("MEAN(C(KM,J))",</pre>	cons_VFI,	true,	["mean"],	3,	1,	<pre>cl_mp_datasetdesc,</pre>

XXX	MEAN(C(KM,J))		XXXXXXXX	XXXXXXXXXXXXXXXX	XXXX					
	group	kids 	marry ————	mean_age_19 	mean_age_22 	mean_age_27 	mean_age_32 	mean_age_37 	mean_age_4	
	1	1	0	6.8551	7.1756	7.502	7.8205	8.1483	8.5053	
	2	2	0	7.1843	7.5683	7.9695	8.3802	8.8184	9.2974	
	3	3	0	7.5997	7.934	8.2911	8.6703	9.0841	9.5509	
	4	1	1	7.1871	7.5271	7.8696	8.209	8.5573	8.9343	
	5	2	1	7.3044	7.6564	8.0306	8.4165	8.826	9.2748	
	6	3	1	7.6479	7.9629	8.3009	8.6543	9.0382	9.4691	

#### Graph Mean Values:

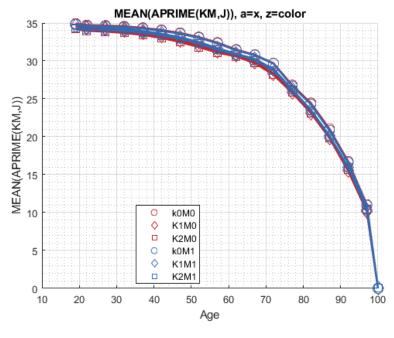
```
mp_support_graph('cl_st_graph_title') = {'MEAN(value(KM,J)), a=age, z=kids+marry'};
mp_support_graph('cl_st_ytitle') = {'MEAN(value(KM,J))'};
ff_graph_grid((tb_az_v{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```

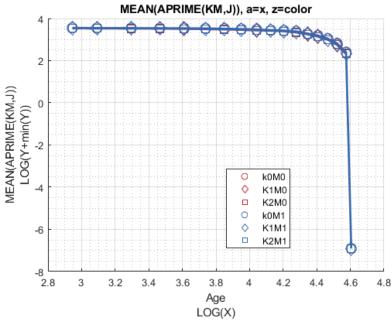




## Graph Mean Savings Choices:

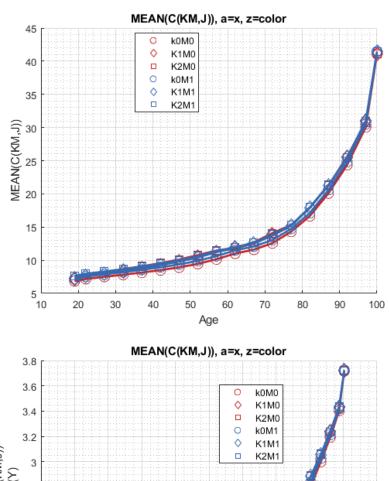
```
mp_support_graph('cl_st_graph_title') = {'MEAN(APRIME(KM,J)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(APRIME(KM,J))'};
ff_graph_grid((tb_az_ap{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```

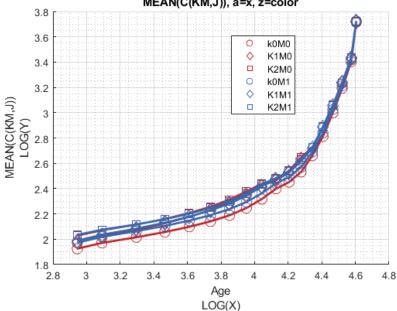




# Graph Mean Consumption:

```
mp_support_graph('cl_st_graph_title') = {'MEAN(C(KM,J)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(C(KM,J))'};
ff_graph_grid((tb_az_c{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```





# **Analyze Education and Marriage and Age**

Aggregating over education, savings, and shocks, what are the differential effects of Marriage and Age.

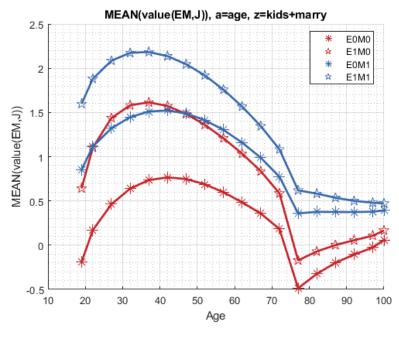
```
% Generate some Data
mp_support_graph = containers.Map('KeyType', 'char', 'ValueType', 'any');
ar_row_grid = ["E0M0", "E1M0", "E0M1", "E1M1"];
mp_support_graph('cl_st_xtitle') = {'Age'};
mp_support_graph('st_legend_loc') = 'best';
mp_support_graph('bl_graph_logy') = true; % do not log
mp_support_graph('st_rounding') = '6.2f'; % format shock legend
mp_support_graph('cl_scatter_shapes') = {'*', 'p', '*', 'p' };
mp_support_graph('cl_colors') = {'red', 'red', 'blue', 'blue'};
```

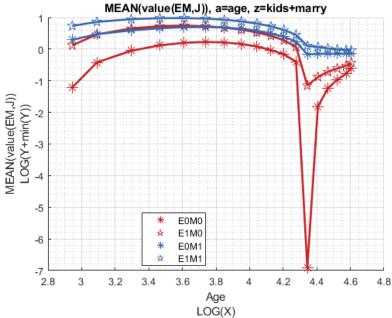
### MEAN(VAL(EKM,J)), MEAN(AP(EKM,J)), MEAN(C(EKM,J))

#### Tabulate value and policies:

```
% Set
 % NaN(n_jgrid,n_agrid,n_etagrid,n_educgrid,n_marriedgrid,n_kidsgrid);
 ar_permute = [2,3,6,1,4,5];
 % Value Function
 tb_az_v = ff_summ_nd_array("MEAN(VAL(EKM,J))", V_VFI, true, ["mean"], 3, 1, cl_mp_datasetdesc,
 group
             edu
                   marry
                           mean_age_19
                                         mean_age_22
                                                       mean_age_27
                                                                    mean_age_32
                                                                                  mean_age_37
                                                                                               mean_age_42
      1
              0
                     0
                            -0.19018
                                           0.16944
                                                        0.46325
                                                                      0.63924
                                                                                   0.73534
                                                                                                 0.76637
       2
              1
                     0
                             0.64221
                                           1.1027
                                                         1.4377
                                                                      1.5815
                                                                                    1.6141
                                                                                                  1.5731
                                                                                    1.5109
       3
                     1
                             0.85396
                                            1.1146
                                                         1.3219
                                                                       1.4469
                                                                                                  1.5218
       4
                              1.5977
                                            1.8806
                                                         2.0859
                                                                       2.1737
                                                                                    2.1837
                                                                                                  2.1364
 % Aprime Choice
 tb az ap = ff summ nd array("MEAN(AP(EKM,J))", ap VFI, true, ["mean"], 3, 1, cl mp datasetdesc
 group
             edu
                   marry
                           mean_age_19
                                         mean_age_22
                                                       mean_age_27
                                                                    mean_age_32
                                                                                  mean_age_37
                                                                                               mean_age_42
       1
              0
                     0
                              34.68
                                           34.441
                                                        34.268
                                                                      34.044
                                                                                   33.748
                                                                                                 33.368
       2
              1
                     0
                             34.463
                                           34.238
                                                        34.218
                                                                      34.116
                                                                                   33.895
                                                                                                 33.549
       3
                             34.723
                                           34.511
                                                                      34.173
                                                                                   33.909
                     1
                                                        34.368
                                                                                                 33.563
                     1
                             34.468
                                           34.274
                                                        34.287
                                                                      34.218
                                                                                   34.029
                                                                                                 33.717
 % Consumption Choices
 tb_az_c = ff_summ_nd_array("MEAN(C(EKM,J))", cons_VFI, true, ["mean"], 3, 1, cl_mp_datasetdesc,
 xxx MEAN(C(EKM,J))
                    XXXXXXXXXXXXXXXXXXXXXXXXXXXXX
     group
             edu
                   marry
                           mean_age_19
                                         mean_age_22
                                                      mean_age_27
                                                                    mean_age_32
                                                                                  mean_age_37
                                                                                               mean_age_42
      1
              0
                     0
                             7.1043
                                           7.4114
                                                        7.7391
                                                                      8.0887
                                                                                   8.4765
                                                                                                 8.9169
      2
              1
                     0
                             7.3218
                                           7.7071
                                                        8.1025
                                                                      8.492
                                                                                   8.8907
                                                                                                 9.3189
      3
                             7.2329
                                                                                   8.5525
                                                                                                 8.9751
              0
                     1
                                           7.5281
                                                        7.8428
                                                                      8.1801
      4
              1
                             7.5267
                                                                      8.6732
                                                                                   9.0619
                                                                                                 9.4769
                     1
                                           7.9028
                                                        8.2913
Graph Mean Values:
 mp support graph('cl st graph title') = {'MEAN(value(EM,J)), a=age, z=kids+marry'};
```

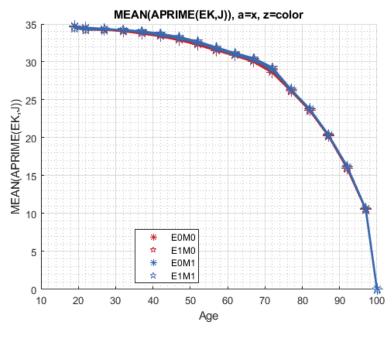
```
mp_support_graph('cl_st_graph_title') = {'MEAN(value(EM,J)), a=age, z=kids+marry'};
mp_support_graph('cl_st_ytitle') = {'MEAN(value(EM,J))'};
ff_graph_grid((tb_az_v{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```

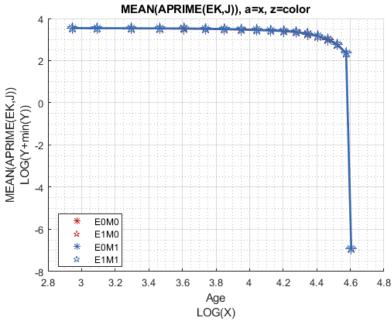




## Graph Mean Savings Choices:

```
mp_support_graph('cl_st_graph_title') = {'MEAN(APRIME(EK,J)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(APRIME(EK,J))'};
ff_graph_grid((tb_az_ap{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```





# Graph Mean Consumption:

```
mp_support_graph('cl_st_graph_title') = {'MEAN(C(EK,J)), a=x, z=color'};
mp_support_graph('cl_st_ytitle') = {'MEAN(C(EK,J))'};
ff_graph_grid((tb_az_c{1:end, 4:end}), ar_row_grid, age_grid, mp_support_graph);
```

