

# FYP

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## Abstract.

XXPREVIOUSXX A device capable of uniformly concentrating a magnetic fields inside of a free space cavity will increase the efficiency of many magnetic devices and sensors. This project shall look at a proposed design for a magnetic field concentrator informed by the transformation optic technique. A metamaterial shell comprised of high and low permeability sections alternating in the angular direction has been shown to approximate the designed concentrator[?]. The ability of the shell acting as a concentrator will be explored in various regimes with a specific focus on improving efficiency of wireless power transmission.

## 1. Introduction

The manipulation of magnetic fields is critical for many modern technologies [?]. Magnetic devices often have efficiencies dependent on the strength of interaction with an external magnetic field. Examples include energy harvesting from magnetic fields [?] to brain activity scans by locating small magnetic gradients [?]. These devices may have increased efficiency by concentrating the desired magnetic field within the area of sensing or harvesting.

Magnetic field may be described by Maxwell's equations [?] and are guided by materials due to their optical properties, such as permittivity and permeability [?]. XpX Fermat's principle of least time allowed the design of many optical devices using geometrical lenses [?], however, with the maturation of fabrication techniques, many materials may be produced with exotic anisotropic optical properties [?] prompting the development of transformation optics (TO) – a modern approach to optical device design.

Here we describe one such TO designed deviceXpX; The magnetic concentrator, with a paticular focus on its efficacy in wireless power transmission.

XeXCould expand on Wireless power transmission.

### 1.1. Transformation Optics and Metamaterials

TO informed the design of many new devices such as perfect lenses [], magenetic-hoses [], -cloaks [], -rotators [], -blackholes [], and -concentrators []. It can be shown that due to the form invariance of Maxwell's equations, a spatial coordinate transform is equivalent to the insertion of a material with specific permeabilities and permittivities. This is shown conceptually by the three steps of the schematic shown in figure ???. First a ray is considered in free cartesian space in panel 1, which due to Fermat's principle will be perfectly straight. The space is then transformed arbitrarily in panel 2 so that the ray adopts the desired path for the final device. The transformation required to morph the ray now informs the optical properties for the specific inserted material of panel 3, which is once again located in cartesian space.

The form invariance of Faraday's law is described by the equivalent expressions

$$\nabla' \times \mathbf{E}' = -j\omega[\mu_0]\mathbf{H}' \quad \text{and} \quad \nabla \times \mathbf{E} = -j\omega[\mu']\mathbf{H}, \quad (1)$$

where the first is expressed in transformed coordinate space  $x'(x, y, z), y'(x, y, z), z'(x, y, z)$  and free space permeability  $[\mu_0]$ , whilst the second is expressed in untransformed cartesian space  $x, y, z$  but with some space dependent permeability  $[\mu']$ . Similar equivalent expressions exist for the other Maxwell equations but with some non-free permittivity  $[\epsilon']$ .

The required permeability and permittivity is found by,

$$\mu' = \frac{A\mu_0 A^T}{|A|} \quad \text{and} \quad \epsilon' = \frac{A\epsilon_0 A^T}{|A|} \quad (2)$$

where  $A$  is the Jacobian matrix describing the transformation of coordinate systems (e.g. between panel 1 and panel 2 in figure ??).

The resulting calculated optical properties may be anisotropic, have arbitrary magnitude and even be negative. As bulk materials rarely, if ever, show these properties, optical metamaterials are often required [?].

Metamaterials are often comprised of repeating units whose dimensions are much smaller than the wavelength of the interacting radiation [?]. The individual units may have specific geometry, orientation and optical properties to selectively interact with the waves so that the net effect of the material mimics a bulk substance with different optical properties than its substituent parts.

### 1.2. Magnetic Concentrator

As described above, a device capable of magnetic field concentration can increase the efficiency of sensors and energy harvesters. Utilising TO we may design an optimal field concentrator which fulfils the criteria: All magnetic field within a region  $A$  is confined to region  $B$  where  $B$  is free space only. A possible geometry for this device that has cylindrical symmetry is shown in XfXfigure ?. A ray diagram is shown in XfXfigure ? for free space with no inserted material. Two coordinate transforms are now applied: First the region  $\rho < R_2 - \eta$  is radially and linearly compressed to the region  $\rho < R_1$ ; Second, to ensure the continuity of our transformed space, a high ( $k^{th}$ ) order polynomial radial expansion of  $R_2 - \eta < \rho < R_2$  to the region  $R_1 < \rho < R_2$  is made. These transformations are described by the coordinate transformations,

$$\rho' = \frac{R_1}{R_2 - \xi} \rho, \quad \rho' \in [0, R_2 - \xi) \quad \rho' = R_2^{1-k} \rho^k. \quad \rho' \in [R_2 - \xi, R_2) \quad (3)$$

By symmetry we see that  $\theta$  and  $z$  remain unchanged through the two transformations. The corresponding Jacobians may be found for these transformations and using equation 2, the permeabilities of the required inserted material may be found to be

$$\begin{aligned} \mu' &= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & (\frac{R_2 - \xi}{R_1})^2 \end{pmatrix} & \rho' \in [0, R_1) \\ \mu' &= \begin{pmatrix} k & 0 & 0 \\ 0 & 1/k & 0 \\ 0 & 0 & \frac{1}{k} (\frac{\rho'}{R_2})^{2/k-2} \end{pmatrix} & \rho' \in [R_1, R_2) \end{aligned} \quad (4)$$

Taking the limit  $\eta \rightarrow 0$  in order to concentrate all of the field within  $A$  into  $B$ , and matching the boundary conditions at  $R_2 - \eta$  and at  $R_1$ , we find that  $k \rightarrow \infty$ . From this we find that the required permeability within  $B$  is satisfied by free space whilst a material with radial permeability  $\mu_\rho \rightarrow \infty$  and angular permeability  $\mu_\theta \rightarrow 0$  is required for region  $A$ . The  $z$  components of permeability is ignored as we assume it to be invariant if the cyclindrical shell is significantly extended in the  $z$  direction.

To satisfy this highly anisotropic condition, an exploration of metamaterials is required. A possible

**Figure 1.** *a)* The geometry of the described problem. All of magnetic energy in region  $A$  will be concentrated into region  $B$ . *b)* An approximation to the required permeabilities described in equation ?? . MuMetal provides large radial permeability whilst superconducting sheets (SC) restrict angular permeability.

discretized shell construction is proposed [?] where the high radial permeability is provided by ferromagnetic materials whilst the angular permeability is shielded by superconducting material. Materials such as MuMetal, have relative permeabilities of up to  $X \times X$  [?] and ideal superconductors in their Meissner state will exclude all magnetic fields from within their interior giving a relative permeability of 0 [?]. These two materials may be arranged in alternating angular sheets, as seen in figure ??, to approximate the conditions proposed by TO design.

Next discuss where this concentration originates?

In an external static uniform magnetic field, the ideal shell will increase the field within region  $B$  by a factor of  $R_2/R_1$ . Similarly if a dipole with magnetic moment  $m$  is present at the origin and surrounded by the magnetic concentrator shell, then the field outside of the shell will be increased by a factor of  $R_2/R_1$ . Therefore for an observer at  $\rho > R_2$  it will appear that a dipole with magnetic moment  $m \cdot R_2/R_1$  is present at the origin.

Comparison to other conc. techniques: It is known that ferromagnetic materials concentrate magnetic fields within their bulk [?] however, concentration of the field into a free space cavity may be required.

### 1.3. Wireless Power Transfer

Why is WPT useful – what are current techniques.

Strong drop off of power transferred with distance.

### Magnetic Concentrators

#### Coupling — Wireless charging

Wireless power transmission is needed for powering devices which are inconvenient or dangerous to power with wires. Examples include mobile phones and implanted medical devices.

It was suggested ?? that two of the above described shells may be utilised for power transfer due to the ability to increase coupling of two solenoids within the inner radii of the shells. One solenoid is supplied with an alternating current to create an alternating magnetic field. This field is then concentrated by the second shell and a current is induced in the second solenoid.

Two assumptions must be made: first, the metamaterials act appropriately at the required frequency in an AC field and second, that the transformation optic approach is still relevant in non-static fields.

In the case of wireless power transfer there may be a set distance,  $d$ , where no material may exist. Shells take up physical space and so it is worth considering if such shells still offer greater coupling in this regime compared to bringing the dipoles  $d$  apart. As the shell increases the dipoles apparent magnetic moment by  $R_2/R_1$ , the shell at a distance  $d + R_2$  is shown to provide an advantage over bare dipoles when  $\frac{R_2}{R_1} > 1 + \frac{R_2}{d}$ . For a given  $R_2$  this means that  $R_1$  may always be reduced to satisfy this inequality.

## 2. Methods

### 2.1. Construction of shell

0.X mm MuMetal XXX and 0.X mm copper was cut into  $X$  by  $X$  rectangular sheets. A plastic support for holding the MuMetal and Copper sheets was 3D printed using an ultimaker XX to produce

the shells seen in figure ??, with an  $R_2/R_1$  ratio of XXX.

## 2.2. DC Magnetic Fields

Helmholtz coils were powered by a constant DC current to create a uniform magnetic field within their center. A commercially available XXX Hall probe was zeroed by using a MuMetal cannister, and then placed at the center of the Helmholtz coils. A Hall probe relates a measured Hall voltage,  $V_H$ , to a surrounding magnetic field,  $B$  [?] as

$$V_H = \frac{IB}{net}. \quad (5)$$

The probe maintains constant current supply  $I$ , and material parameters  $n$  (charge carrier density),  $e$  (charge of electron) and  $t$  (thickness of probe) meaning a calibrated probe may give accurate readings for magnetic fields.

The magnetic field,  $B$ , produced at the center of Helmholtz coils with radius  $R$ , separated by a distance  $R$  should follow,

$$B = \frac{8}{5\sqrt{5}} \frac{\mu_0 n I}{R}, \quad (6)$$

where  $I$  is the current supplied to the coils and  $n$  is the number of turns of wire. This equation follows directly from the Biot-Savart law [?] and the relative geometry of the coils as seen in figure ?. From equation 6 it can be seen that the magnetic field should increase linearly with supplied current. Using the Hall probe we ensured this was the case and found the relationship of current supplied to magnetic field produced for our particular Helmholtz arrangement.

Now, with the capability to produce known external magnetic fields, the described field concentrating shells may be placed within this field and the Hall probe may be placed within their inner radius to measure concentrated field.

## 2.3. AC characterization

Initially the Helmholtz arrangement was repeated for exploration of the concentrating shells behaviour in alternating magnetic fields. However, instead of a Hall probe, a small solenoid was used to detect the oscillating field. From Faraday's law, a voltage will be induced in a wire loop due to a time dependent magnetic field. A series of loops constituting a small solenoid will respond to a sinusoidal magnetic field,  $B = B_0 \cos \omega t$ , with the relationship,

$$V = -NAB_0\omega \sin \omega t, \quad (7)$$

where  $A$  is the area of one loop and  $N$  is the number of loops,  $\omega$  is the angular frequency of the alternating magnetic field and  $t$  is time.

As  $\omega$  is known and all other parameters except external field are kept constant, the voltage across the solenoid may be measured experimentally to find the relative magnetic field strength.

The solenoid must however be characterized in order to find the absolute magnetic field values. This was done by measurement of the self inductance,  $L$ , of the solenoid as, XXX

$$L = \mu_0 \mu_r N^2 A / l \quad (8)$$

XXX

Due to the induced voltage across the inductor being small and background noise being high, a lock-in amplifier was used to select only the desired signal frequency. This substantially reduced noise in our readings allowing higher frequency and lower magnetic field strength experiments.

Use of solenoid, limitations of Helmholtz and pick up.

## 2.4. Power Transfer

Use of RLC circuitry.

Power transfer experiments measure power dropped across a load resistor in a receiving circuit verses power lost in the transmitting circuit's inductor. The receiving circuit, seen in figure ??, has multiple arrangements to optimise power transfer. The simplest of which is the load resistor in series with the receiving inductor. In this case the optimal load resistance is  $R = \omega * L$ , where  $\omega$  is the angular frequency of the oscillating magnetic field and  $L$  is the circuit inductance.

To maximise power transfer an RLC circuit is constructed on the receiving circuit. Ideally in an RLC circuit the complex impedance of the inductance and capacitance cancel leaving only the load resistance. Our inductance is set by the solenoid we chose to use and so for exploring power transfer at various frequencies, a capacitance can be found to satisfy the resonance condition. If inductance,  $L$ , does not vary then capacitance,  $C$ , is easily found by,

$$C = \frac{1}{\omega^2 L}. \quad (9)$$

However, we need not assume that inductance is constant. A series RLC circuit can be constructed as seen in figure ?? to ensure resonance is met. Resonance occurs in this circuit when  $V_A$  is exactly in phase with  $V_B$ . In this case any imaginary impedances are cancelled and only real resistance remains. For maximal power transfer a parallel RLC circuit is preferable however due to the restraints of the experiment a non-ideal version must be made as seen in figure ?. The resonant condition found by the series RLC is a close approximation to this more complicated parallel circuit.

To maximise power transfer in the series RLC case, a familiar idea of impedance matching occurs, i.e. Power is maximised when the load resistance is equal to any internal resistances of the components [?]. As internal resistances are difficult to measure and may depend on current XXX, this could also be found experimentally by measuring voltage and current over the load resistance whilst varying load resistance.

For the parallel RLC case, a more complicated expression for optimal load resistance was found which depends non trivially on a combination of internal resistances. A model is proposed below, however, experimentally locating the optimal resistances was chosen as measuring internal resistances proved difficult and time consuming.

XXTheory of Rload dependence on power transfer.

## 3. Results

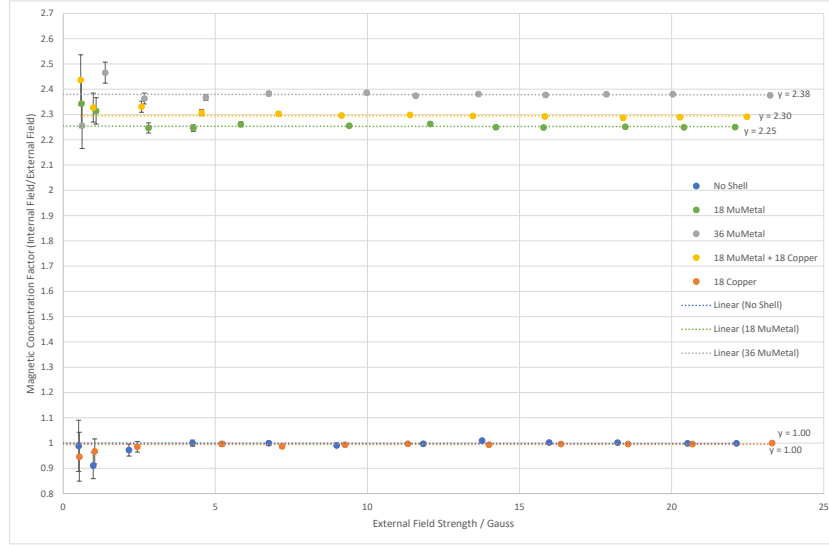
### 3.1. DC Magnetic Fields

Using the DC Helmholtz set up as described in Methods, we observed constant concentration factors for different shell constructions in an external magnetic field ranging from 1 G to 22 G. No shell, 18 MuMetal, 36 MuMetal, 18 Copper and 18 MuMetal + 18 Copper shells were used and their concentration factor with field may be seen in figure 3.1, where concentration factor is defined as (Internal Field)/(External Field).

It was found that the shell construction of 36 MuMetal thin sheets gave the optimum concentration factor of  $C = 2.38$  with minimal error (0.1%) at higher field strengths and a maximum error of 4.0% at an external field of 1.4 G. This increase in error at low magnetic fields is due to limited sensitivity of our Hall probe and current measurements over the Helmholtz coils.

Similar error relationships are observed for the other constructions. It should be noted that we assume the dipole has been placed in the same position and orientation in all experiments and so errors due to placement are excluded here.

It is expected that the copper will have no effect on a static magnetic field and this was confirmed by the 18 copper shell displaying no concentration of internal field. This is due to copper having a relative permeability similar to air,  $\mu_r = 1.0$ , and so negligible field guiding properties. In the



**Figure 2.** How concentration factor depends on frequency for a shell concentrating a static external field into its interior.

oscillating magnetic field regime copper is expected to shield angular fields due to the production of eddy currents. Only air-gaps are used to block the angular component of a static magnetic field within our shells to simplify the experimental set up, however superconducting sheets in a similar shell have been shown to improve the concentration of static fields [?].

### 3.2. AC characterization

### 3.3. Helmholtz

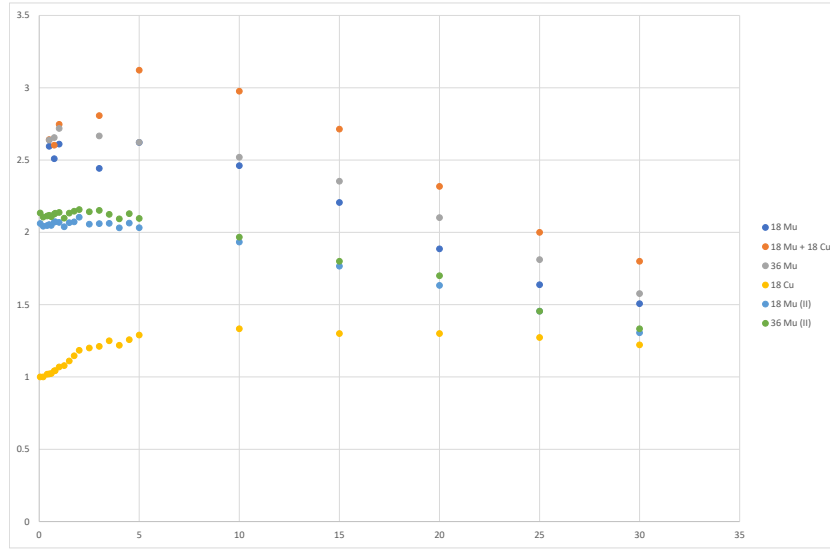
The Helmholtz coils were supplied with an alternating current in order to create an oscillating magnetic field. As described in Methods equation 7, the voltage induced across a solenoid is used to detect the alternating magnetic field strength. The concentration factor for a range of frequencies using various shell arrangements was again explored.

The concentration factors between 0.5 kHz and 30 kHz can be seen in figure 3.2. It was found that a mixed shell of alternating 18 copper and 18 MuMetal sheets had the optimum concentration factor of  $C = 3.12$  XeX at 5 kHz.

Here we can see that the copper sheets have a concentrating effect dependent on frequency. We found that the copper shell increases in efficacy from  $C = 1.0$  at 50 Hz to  $C = 1.3$  (2SF) at 10 kHz and does not increase substantially more as frequency is increased. This behaviour is expected as copper will shield perpendicular alternating magnetic fields by the generation of eddy currents. This effective increase in  $\mu_\theta$  is desired for the optimal TO concentrator. However, it is suprising that this shielding gives a maximum effect at this low frequency. The skin depth of copper at 10 kHz is 0.66 mm which is greater than the 0.3 mm thickness of copper used within the shell.

Supporting work done on COMSOL, seen in figure ??, suggests a similar observed effect where 36 copper sheets increase rapidly in concentration factor from  $C = 1$  at 0 Hz to  $C = 1.5$  (2SF) by 10 kHz and then only a small further increase in efficacy at high frequencies.

The strong linear decay of field concentration after 5 – 10 kHz for all configurations is a suprising result which, although may be partly due to the MuMetal’s permeability frequency response, also



**Figure 3.** How concentration factor depends on frequency for a shell concentrating an oscillating external field into its interior.

appears to occur at too low a frequency.

The COMSOL simulations do not show this relationship which suggests the source may be either not modelled appropriately within COMSOL or be a fault in this experimental design.

Apart from instrument and measurement reading errors which constitute only a small error (XXX%), we observed errors due to stray magnetic fields inducing pick-up within cables connecting the solenoid to the lock-in amplifier. This source of noise is highly frequency dependent and is at the same frequency as our desired signal, so cannot be removed by the use of a lock-in amplifier. To suppress this noise careful cable placement and shielding was installed however, from figure ?? it can be seen that as current was reduced, the measured voltage was still non-zero.

XXX A correction was attempted...

This source of error prompted a decision to focus on two dipole coupling experiments as the field produced by a dipole has a strong distance drop off meaning unwanted pick-up in cables can be greatly reduced.

### 3.4. Power transfer

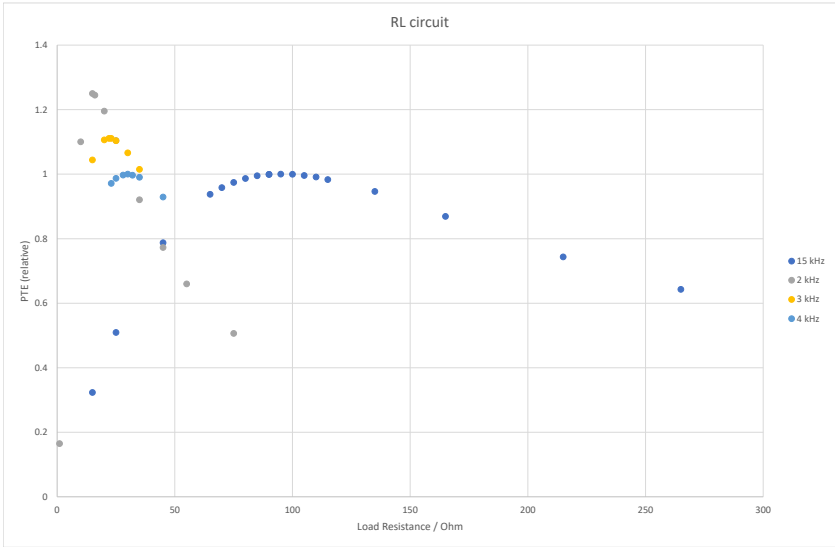
First we show the simplest power transfer experiment where the load resistance is in series with the receiving inductor – an RL circuit. Figure 4 shows the relative PTE versus load resistance for various frequencies. The peaks of these curves confirm the expected optimum load resistance of  $R = \omega L$ .

An Oscillating magnetic field,  $B$ , produced from a solenoid and concentrated by a shell follows,

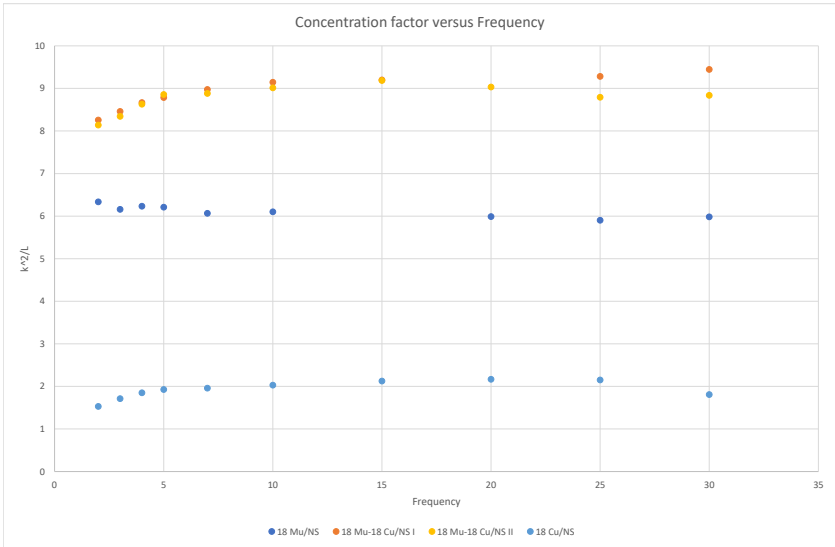
$$B = CI\mu_0 n \cos \omega t,$$

where  $C$  is the concentration factor,  $I$  is the current through the solenoid and  $n$  is the number of turns of the solenoid. If a second solenoid is placed within the field of the first, as shown in figure ??, then voltage will be induced across it according to Faraday's law,

$$V = -NA \frac{dB}{dt},$$



**Figure 4.** How power transfer efficiency depends on load resistance in a coupled inductive circuit for various frequencies.



**Figure 5.** How power transfer efficiency depends on frequency in a coupled inductive circuit.



$$V = C\omega INA\mu_0 n \sin \omega t,$$

where  $N$  is the number of turns of the solenoid and  $A$  is the area of one turn. The power dropped across a resistor with magnitude  $\omega L$  in series with this inductor will then be described by,

$$P = V^2/R$$

$$P = \frac{C^2 w I^2 k}{L} \sin \omega t^2$$

where  $k$  is the collection of constant coefficients that will remain constant between different shells. Max power received in the second circuit is therefore proportional to  $w \cdot \frac{C^2}{L} \cdot I^2$ . Plotting  $\frac{P}{I^2}$  against angular frequency  $w$  therefore gives  $\frac{C^2 k}{L}$  as shown in XX figure 5. Assuming the coefficients in  $k$  remain constant, comparisons of this gradient between a concentrating shell with inductance  $L_s$  and no shell with inductance  $L_0$  and  $C_0 = 1$  yields  $\eta = \frac{C^2 L_0}{L_s}$ , the effective concentration factor for power transfer. Figure XXX 5 shows how  $\eta$  depends on frequency for various shell configurations.

As observed in the Helmholtz driven field case, we see that the copper sheets increase in concentrating effect rapidly between 0 and 10 kHz. The Copper only shell increases to around  $\eta = 2$  which, if it is assumed that  $L_0 = L_s$ , corresponds to a power transfer increase of 2x or a corresponding field concentration of  $\sqrt{2}$  within the shell's cavity. It can be seen that using only MuMetal sheets gives a power transfer increase of 6x and a concentration of field that is independent of field frequency for the range 0 – 30 kHz. This differs from the previous Helmholtz result where a steady drop off of concentration factor was observed as frequency increased past 10 kHz.

The mixed shell of 18 MuMetal sheets and 18 Copper sheets was found to have the best power transfer increase of 9x after the copper sheet effectively shields the angular field at 10 kHz. This power increase corresponds to a magnetic field concentration of 3 within the shells cavity.

Figure 5 XXX shows the optimal PTE for a range of frequencies with different shell constructions around the receiving inductor. Assuming the inductance value remains constant with different shell configurations (an exploration of this assumption is considered in DiscussionXXX), absolute power transfer can be calculated as described in Methods. Table ?? gives the maximal power transfer for different arrangements of shells.

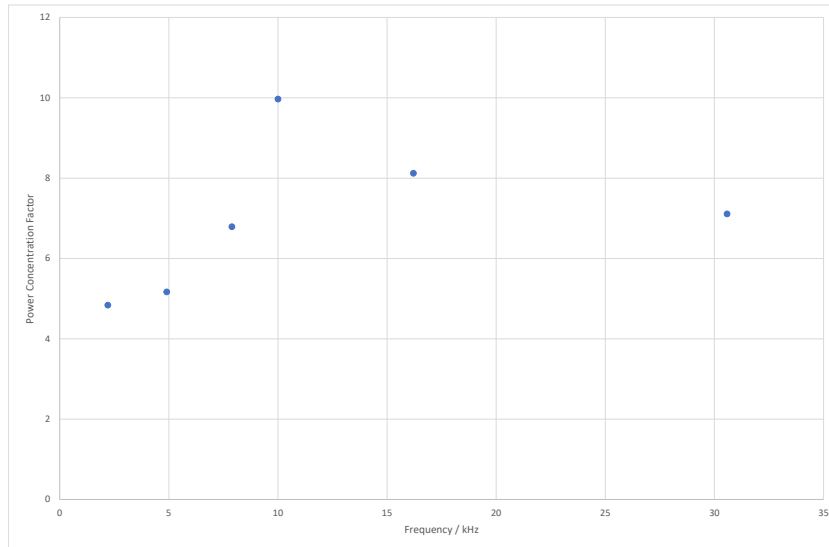
Parallel RLC circuits are more fitting for optimising power transfer [?]. For the arrangement described in figure ??, a shell comprised of 18 MuMetal and 18 Copper sheets was explored. The optimal load resistance was found by taking voltage measurements across a range of load resistance. An example power versus load resistance curve for 30 kHz can be seen in XXX figure ??.

Optimal load resistances were found for a range of frequencies and PTE were calculated as shown in XXX figure ??. Figure XX ?? shows the ratio of shell present versus no shell present for the range of frequencies. It can be seen that the increase of ratio between 0 and 10 Hz is still present, however due to the high error and few data points, other trends are hard to distinguish. In this arrangement, with the coils separated by a distance of XXX mm, maximum observed power transfer is XX 0.05%. To further explore PTE, the distance between the two coils was varied. With a distance of XXX mm and a full shell around the receiving coil, a PTE of XXX% was achieved.

It was expected that a shell around the transmitting coil would further increase the field incident on the receiving coil. Therefore the arrangement described in Methods Figure ?? was constructed and the peak power transfer observed at 30510 kHz was found to be 1.01%.

### 3.5. Distance

Experimentally we found that power drops off as  $r^{-5.6}$  which is in close agreement to the theoretical  $r^{-6}$ .



**Figure 6.** How the increase in power transfer efficiency depends on frequency in a coupled parallel RLC circuit.

#### 4. Discussion

For the constructed shells used in these experiments, their  $R_2/R_1$  ratio was  $40 \pm 2$  mm. From the theoretical TO work, it is predicted that the field should be concentrated by the perfect shell by  $R_2/R_1$ . We found a range of concentrations for both static,  $C = 2.25 - 2.38$  XeX and oscillating,  $C = 2 - 3.1$  XeX, external fields whose maximum concentration factors are still well below the expected theoretical concentration factor of  $4.0 \pm 0.2$ . This is likely explained by our approach to approximating the perfect TO designed anisotropic shells with shells comprised of discrete sections of high and low permeability. In both static and oscillating fields, we found that 36 MuMetal sheets performed better than 18 MuMetal sheets which suggests that finer discretization of the proposed shells gives concentrations closer to the theoretical value. In the static field experiments, only air was used to approximate the zero relative angular permeability. Air has a permeability of  $\mu = 1$ , which although is far less than the MuMetal's  $\mu = XXX$ , is likely still a poor approximation. This can be seen by the increase in performance in the oscillating external field experiments where copper sheets are introduced in order to effectively screen out angular field density by the production of Eddy currents. Eddy current screening is proportional to frequency of the oscillating field [?], and therefore, it can be seen that the concentration factor for shells with copper present increase with frequency.

Eddy currents may be modelled as a wire loop perpendicular to an oscillating magnetic field. A current is produced within the loop which is proportional to frequency of the field and, due to Lenz's law, flows in a direction to oppose the change in field density. The induced current in the loop is

$$I = \frac{A}{R} \omega (B - B'),$$

and the field produced by the current is,

$$B' = -I\mu_0 r.$$

Combining these equations give,

$$B' = \frac{\omega B}{1 + \omega},$$

which may be seen plotted with the COMSOL and experimental results for a copper only shell.

XwX Superconducting material has been suggested to effectively screen angular field in the static case [?]....

For many results we have assumed that the inductance of the solenoid was independent of the shell surrounding it. Here we shall reexplore some results without this assumption.

For the resonant condition of a series RLC circuit,  $\omega = 1/LC$ , and so we may use the known capacitance,  $C$  and measured frequency peak,  $\omega$ , to calculate an effective inductance,  $L$ , for the solenoid. Table ?? summarises the observed inductances for the various shell configurations. It should be noted that the inductance of the coils used does have a dependency on current, however for the range of currents used in the series RLC experiment, this change in inductance with current was negligible compared with the observed change in inductances with different surrounding shells. From equation ?? it can be seen that the effective power concentration,  $\eta$ , is dependent on both field concentration and effective inductance of the solenoid.

DC:

- further explanation on error source in placement

Linear decay of coil in non RLC

- Due to pick up that is proportional to  $w^2$ ?
- Expected drop off due to magnetic saturation? or other reasons for MuMetal failure. - COMSOL MU thickness

RLC How L changed with the shell construction.

Power transfer

- Generally low PTE due to high loss of inductor. Could have used laminated AC inductor to reduce eddy currents. Could have not used iron core as hysteresis.
- Discussion of other power transfer techniques and coupled inductor papers. Why a shell is better than no shell with distances.
- Why a shell allows a small radii inductor to be used - efficiency of scale Better coupling for given distance. See p.51 pratt.
- Relationship of PTE with distance  $-r^{-5.6}$ . Effective mutual inductance changed.
- Two shells present.
- Another exploration on error sources and summary of largest sources.

Comparison of RL, series RLC and parallel RLC circuitary:

- models
- expected efficiency

can use a smaller solenoid, plot spider graphs in python

## 5. Conclusions

### EXTENSIONS

0) For further understanding we would need to look at more frequencies and especially at much higher freqs. A selection of different dipoles would also be beneficial to ensure that frequency dependence is

not linked to non-ideal dipole.

0) Perhaps another circuit could be designed that works more similarly to an RLC? Could propose one however experimentation has not been performed.

0) Could a more complicated and directional shell be designed for power transfer?

## **6. References**