LIÈGE université

Academic year 2018-2019

Dynamics of Mechanical Systems

J.C. GOLINVAL

Assignment of Project n°2

Description of the set-up

The system consists of a beam on two supports located at both ends at coordinates P2 and P11 respectively. A steel cylinder of mass M_1 is mounted at location P10 as illustrated in Figure 1.

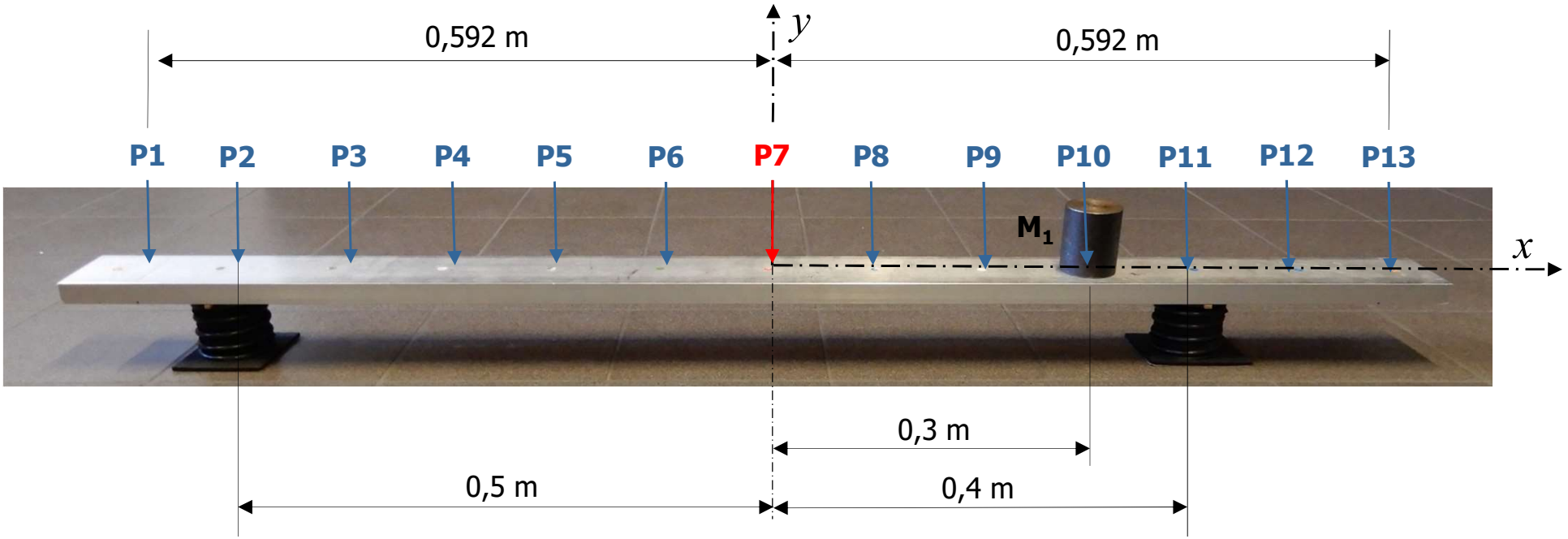


Figure 1.- Beam supporting one mass M_1

Point P7 is located at the centre of the beam, P1 and P13 at a distance of 0,592 m from P7. The distance between two consecutive points (from P2 to P12) is equal to 0,1 m.

Description of the set-up

The beam has a rectangular cross-section and is made of aluminium.

Geometry of the beam

Length = $1{,}25\ m$

Width = $80\ mm$

Height = $20\ mm$

Material (aluminium)

Density = $2\ 690\ kg/m^3$

Elasticity modulus ~ $6{,}45\ 10^{10}\ N/m^2$

Poisson ratio = $0{,}39$

Steel cylinder

Mass (M_1) = $1\ kg$; height = $61\ mm$; diameter = $51\ mm$

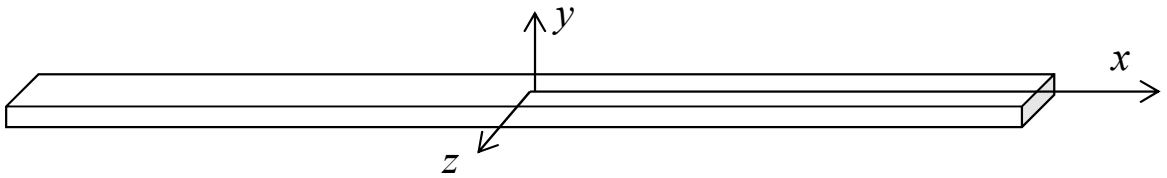
Supports

Each support will be modelled by a single stiffness element with the following characteristic:

$$k_{support} = 10\ 500\ N/m$$

Calculation of inertia

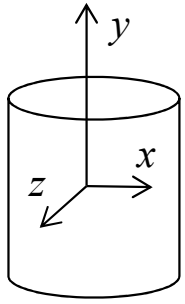
Moment of inertia of a beam about the z-axis passing through its centre of gravity



$$J_{beam} = \frac{M\ L^2}{12}$$

where M and L are the mass and the length of the beam respectively.

Moment of inertia of a cylinder about the z-axis passing through its centre of gravity



$$J_{cylinder} = \frac{M_1\ (3\ R^2 + h^2)}{12}$$

where M_1 is the mass, R the radius and h the height of the cylinder.

Project statement

Project 2 (Part 1)

Build a 2 DOF model of the system with the assumption that the beam is rigid; calculate the natural frequencies and the associated mode-shapes; calculate the coordinate of the nodal node for the second mode.

The results will be summarized on the form provided in the file Project 2_part1_form.pdf to be sent by e-mail at the following address: JC.Golinval@uliege.be. The form will be renamed as follows:

DSM2_part 1_LAST NAME_first name.pdf

The deadline for the submission of the form is fixed to

November 22, 2018.

Project statement

Project 2 (Part 2)

1. Relaxing the assumption of a rigid beam, compute the first 5 natural frequencies and mode-shapes of the system using the Rayleigh-Ritz method; to this purpose, at least 10 polynomial functions will be chosen as approximation functions.
2. The FRF are measured by accelerometers at coordinates P4 and P10. The excitation consists of an impact produced successively every 0,1 m from points P1 to P13 using the so-called «roving hammer technique». The responses are measured in the frequency range from 0 to 400 Hz with a frequency resolution of 0,1 Hz. The results of the experimental modal identification in terms of natural frequencies and mode-shapes are available on MyULg website in the files 'Project_2018_freq.txt' and 'Project_2018_modes.txt' as explained hereafter.
3. Compare the theoretical predictions of the different models with the experimental results in terms of frequencies and mode-shapes.

Project statement

Experimental data available on MyULg

- The file 'Project_2018_freq.txt' contains 5 identified frequencies (1st column) and modal damping factors (2nd column).
- The file 'Project_2018_modes.txt' contains the amplitudes of the corresponding identified mode-shapes (columns 1 to 5) under the format:

Mode 1	Mode 2	Mode 3	Mode 4	Mode 5
…	…	…	…	…
…	…	…	…	…
…	…	…	…	…

13 lines corresponding to locations P1 to P13

Recommendations

1) The report must be concise (max 3 pages according to the template given in the file Project 2_part2_form.pdf).
2) Figures must be clear (legend, readability).
3) The text must be well structured and should be free of spelling and grammatical mistakes.
4) Penalty for late report: -1 point/24h

Submission of the report

A PDF version of the report will be sent by e-mail at the following address: JC.Golinval@uliege.be and will be named as follows:

DSM2_Part 2_LAST NAME_first name.pdf

The deadline for the submission of the report is fixed to

December 13, 2018.